Search: Solving a maze

Total Points: 10

The agent has a map of the maze it is in (i.e., the environment is deterministic, discrete, and known). The agent must use the map to plan a path through the maze from the starting location S to the goal location G.

Here is the small example maze:

```
In [68]:
```

```
f = open ("small maze. txt", "r")
maxe str = f.read()
print(maze_str)
XXXXXXXXXXXXXXXXXXXXXXXX
            X X
     XXXXXX X XXXXXXX X
X
XXXXXX
           S X
     X XXXXXX XX XXXXX
X XXXX X
         XXX XXX X X
X
XXXXXXXXX
              XXXXXX X
           XX
XXXXXXXXXXXXXXXXXXXXXXX
```

Notes:

- This is a planing exercise, so you do not need to implement an environment, just use the map to search for a path. Once the plan is made, the agent can just follow the path and does not need percepts. The execution phase is trivial and we do not implement it in this exercise.
- Tree search algorithm implementations that you find online have often a different aim. The algorithms
 assume that you already have a tree and the goal is to traverse all nodes. We are interested in
 dynamically creating a search tree with the aim of finding a good/the best path to the goal state. Ideally,
 we would like to search only a small part of the maze, i.e., create a search tree with as few nodes as
 possible.
- Some mazes may contain cycles and therefore not form proper trees unless cycles are prevented.

Parsing and pretty printing the maze

The maze can also be displayed in color using code in the file maze_helper.py). The code parses the string representing the maze and converts it into a numpy 2d array which you can use in your implementation.

In [69]:

```
%run maze_helper.py

maze = parse_maze(maze_str)

# look at two positions in the maze
print("Position(0,0):", maze[0, 0])

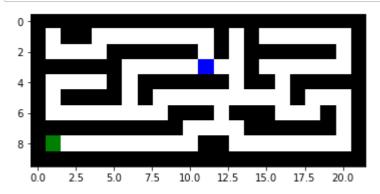
# there is also a helper function called `look(maze, pos)`
print("Position(8,1):", look(maze, [8, 1]))
```

Position (0,0): X Position (8,1): G

Visualize the maze

In [70]:

```
show_maze(maze)
```



Find the position of the start and the goal using the helper function find_pos()

```
In [71]:
```

```
print("Start location:", find_pos(maze, what = "S"))
print("Goal location:", find_pos(maze, what = "G"))
```

Start location: [3, 11] Goal location: [8, 1]

Tree structures

A basic tree implementation in Python is available at https://github.com/yoyzhou/pyTree (found by John Park).

Tasks

Implement the following search algorithms for solving different mazes:

- Breadth-first search (BFS)
- Depth-first search (DFS)
- Iterative deepening search (IDS)
- Greedy best-first search (GBFS)
- A* search

Run each of the above algorithms on the small_maze.txt), medium maze (medium_maze.txt), maze.txt), algorithm, report the following in a table:

- · The solution and its path cost
- · Number of nodes expanded
- · Maximum tree depth searched
- · Maximum size of the frontier.

Display each solution by marking every maze square (or state) visited and the squares on the final path.

Task 1: Defining the search Problem [1 point]

Define the components of the search problem:

- · Initial state
- Actions
- · Transition model
- Goal state
- · Path cost
- 1: Initial State: The start location (S) in the maze
- 2: Actions: Go east/north/south/west until it hits an obstacle.
- 3: Transition model: If we move to points for 1 steps, it will go east/north/south/west with distance 1(1 space length in the txt).
- 4: Goal state: The goal location (G) in the maze
- 5: Path cost: Since we are assuming one step costs 1, the path cost will be equal to the number of steps.

Task 2: Breadth-first, Depth-first and iterative deepening search [4 points]

Implement these search strategies. You can implement a generic tree search following the BFS pseudo-code in your textbook and then just adapt the order in which the frontier is explored.

Breadth First Search:

In [72]:

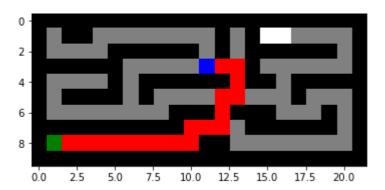
```
import maze helper as helper
from pyTree. Tree import Tree as Tree # It is from https://github.com/yoyzhou/pyTree
from queue import Queue, LifoQueue, PriorityQueue
import math
import copy
def Find Children (maze, Node):
                                                         # A function use to find all the options
for each round of searching
   option = []
    West = [Node[0], Node[1]-1]
   North = [Node[0]-1, Node[1]]
    East = [Node[0], Node[1] + 1]
    South = [Node[0] + 1, Node[1]]
    if (helper. look (maze, West) != 'X'): option.append (West)
    if(helper.look(maze, East) != 'X'): option.append(East)
    if (helper. look (maze, North) != 'X'): option. append (North)
    if (helper. look (maze, South) != 'X'): option. append (South)
   return option
def Find Distance(NodeonTree, Root):
   Total = 0
    while (NodeonTree != Root):
        NodeonTree = NodeonTree.getParent()
        Total = Total + 1
    return Total
def getResult(maze):
                                        # It is a function that find final numbers of path cost
 and area explored
   Result = []
   Cost = 0
   Explored = 0
    for i in range(len(maze)):
        for j in range(len(maze[0])):
            if(maze[i][j] == 'P' or maze[i][j] == 'G'):
                Cost = Cost + 1
                Explored = Explored + 1
            elif(maze[i][j] == '.'):
                Explored = Explored + 1
    Result.append(Cost)
    Result. append (Explored)
    return Result
def BFS Search(maze, vis):
   Start = helper. find pos (maze, what = "S")
    End = helper.find pos(maze, what = "G")
                                                             # Set start point and end point
    Result = []
   MaxFrontier = 1
   MaxDepth = 1
                                                             # If Start is End
    if(Start == End):
        Result.append("Start is End")
        Result.append("Start is End")
        Result. append ("Start is End")
        Result.append("Start is End")
        return Result
    q = Queue (maxsize=(len (maze)*len (maze[0])))
                                                             # It is a FIFO queue
    q. put (Start)
```

```
Root = Tree(Start)
                                                             # Use a tree to store all the paths
  while(q.empty() == False):
       if (q. qsize() > MaxFrontier):
           MaxFrontier = q.qsize()
       Node = q. get()
                                                             # Get a node from queue
       NodeonTree = Root.getNode(Node)
       depth = Find Distance(NodeonTree, Root)
       if (MaxDepth < depth):</pre>
                                                             # Find the depth of the node
           MaxDepth = depth
       children = Find Children(maze, Node)
       if(vis == True):
                                                              # Show paths for each round
           if (Node != Start):
               maze[Node[0]][Node[1]] = 'P'
               helper. show maze (maze)
               maze[Node[0]][Node[1]] = '.'
           else:
               helper. show maze (maze)
       for e in children:
           if (e == End):
               newTreeNode = Tree(e)
               NodeonTree. addChild (newTreeNode)
               tempNode = newTreeNode.getParent()
               while(tempNode != Root):
                   maze[tempNode.data[0]][tempNode.data[1]] = 'P'
                   tempNode = tempNode.getParent()
                                                                     # Rebuild the path based on
the tree
               Result = getResult(maze)
               Result. append (MaxFrontier)
               Result. append (MaxDepth)
               return Result
           if (Root.getNode(e) == None):
               newTreeNode = Tree(e)
               maze[e[0]][e[1]] = '.'
               NodeonTree. addChild(newTreeNode)
                                                                     # Add child to the tree and
to the queue
               q. put (e)
  Result. append ("Path not found")
  Result. append ("Path not found")
                                                                 # If no path founded
  Result. append ("Path not found")
  Result. append ("Path not found")
                                                                 # If no path founded
  return Result
```

In [73]:

```
def BFS SearchRunner(vis):
   mazes = []
   mazes. append ("small_maze. txt")
   mazes. append ("medium_maze. txt")
   mazes. append ("large_maze. txt")
    mazes. append("empty_maze. txt")
   mazes.append("wall_maze.txt")
   mazes. append("loops_maze. txt")
   mazes. append ("open_maze. txt")
    for e in mazes:
        f = open(e, "r")
        maze_str = f.read()
        maze = helper.parse_maze(maze_str)
        print("\n==========
        print("Running BFS with ", e)
        localResult = BFS_Search(maze, vis)
        helper. show maze (maze)
        print("Path cost: ", localResult[0])
        print("Explored squares: ", localResult[1])
        print("Maximum size of the frontier: ", localResult[2])
        print("Maximum tree depth: ", localResult[3])
        print("===========
BFS SearchRunner (False)
```

Running BFS with small_maze.txt

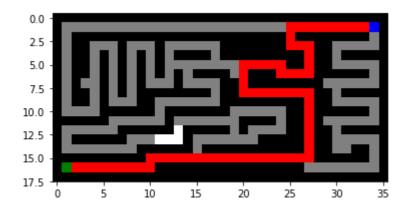


Path cost: 19 Explored squares: 91

Maximum size of the frontier: 8

Maximum tree depth: 18

Running BFS with medium_maze.txt



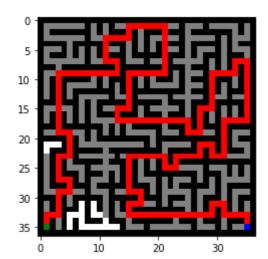
Path cost: 68

Explored squares: 269

Maximum size of the frontier: 8

Maximum tree depth: 67

Running BFS with large_maze.txt



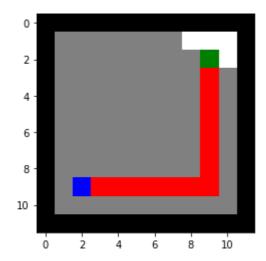
Path cost: 210

Explored squares: 622

Maximum size of the frontier: 8

Maximum tree depth: 209

Running BFS with <code>empty_maze.txt</code>



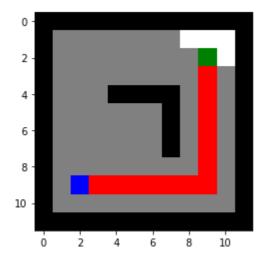
Path cost: 14

Explored squares: 95

Maximum size of the frontier: 12

Maximum tree depth: 13

Running BFS with wall_maze.txt



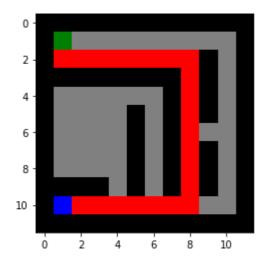
Path cost: 14

Explored squares: 88

Maximum size of the frontier: 11

Maximum tree depth: 13

Running BFS with loops_maze.txt



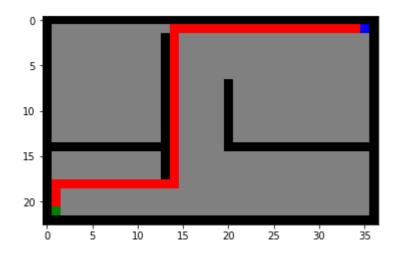
Path cost: 23

Explored squares: 71

Maximum size of the frontier: 7

Maximum tree depth: 22

Running BFS with open_maze.txt



Path cost: 54

Explored squares: 683

Maximum size of the frontier: 23

Maximum tree depth: 53

Breadth First Search Analysis

This Breadth First Search algorithm will loops through top node's neighbours and make branches, after it looked over all the neighbours, it will then go to the next layer.

- Since It will go to all the places it can go eventually, and the layer is finite, it is complete.
- Since it will search based on layers (step = 1), the shortest path(shortest layer) will be found first, so it is optimal.
- Its Time Complexity is O(b^d) because it has d branches and d layers.
- Its Space Complexity is also O(b^d) because of the branches and depth.

Depth First Search

In [74]:

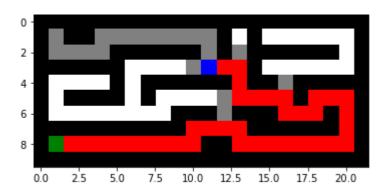
```
def DFS Search(maze, vis):
    Start = helper. find pos (maze, what = "S")
    End = helper. find pos(maze, what = "G")
    Result = []
    MaxFrontier = 1
    MaxDepth = 1
    if (Start == End):
        Result.append("Start is End")
        Result. append ("Start is End")
        Result. append ("Start is End")
        Result.append("Start is End")
        return Result
    q = LifoQueue(maxsize= (len(maze)*len(maze[0])))
                                                                 # It is a LIFO queue, or called
 stack
    q. put (Start)
    Root = Tree(Start)
    while(q.empty() == False):
        if (q. qsize() > MaxFrontier):
            MaxFrontier = q. qsize()
        Node = q. get()
        NodeonTree = Root.getNode(Node)
        depth = Find Distance(NodeonTree, Root)
        if (MaxDepth < depth):</pre>
                                                               # Find the depth of the node
            MaxDepth = depth
        children = Find Children (maze, Node)
        if(vis == True):
            if (Node != Start):
                maze[Node[0]][Node[1]] = 'P'
                helper. show maze (maze)
                maze[Node[0]][Node[1]] = '.'
            else:
                helper. show maze (maze)
        for e in children:
            if (e == End):
                newTreeNode = Tree(e)
                NodeonTree. addChild(newTreeNode)
                tempNode = newTreeNode.getParent()
                while(tempNode != Root):
                    maze[tempNode.data[0]][tempNode.data[1]] = 'P'
                     tempNode = tempNode.getParent()
                                                                      # Rebuild the path based on
 the tree
                Result = getResult(maze)
                Result. append (MaxFrontier)
                Result. append (MaxDepth)
                return Result
            if (Root.getNode(e) == None):
                newTreeNode = Tree(e)
                maze[e[0]][e[1]] = '.'
                NodeonTree. addChild (newTreeNode)
                                                                       # Add child to the tree and
 to the queue
                q. put (e)
```

```
Result.append("Path not found")
Result.append("Path not found")
Result.append("Path not found")
Result.append("Path not found")
return Result
```

In [75]:

```
def DFS SearchRunner(vis):
   mazes = []
   mazes. append ("small_maze. txt")
   mazes. append ("medium_maze. txt")
   mazes. append ("large_maze. txt")
    mazes. append("empty_maze. txt")
   mazes.append("wall_maze.txt")
   mazes. append("loops_maze. txt")
   mazes. append ("open_maze. txt")
    for e in mazes:
        f = open(e, "r")
        maze_str = f.read()
        maze = helper.parse_maze(maze_str)
        print("\n===========
        print("Running DFS with ", e)
        localResult = DFS_Search(maze, vis)
        helper. show maze (maze)
        print("Path cost: ", localResult[0])
        print("Explored squares: ", localResult[1])
        print("Maximum size of the frontier: ", localResult[2])
        print("Maximum tree depth: ", localResult[3])
        print("=========
DFS SearchRunner (False)
```

Running DFS with small_maze.txt

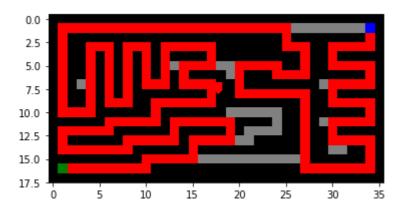


Path cost: 37 Explored squares: 56

Maximum size of the frontier: 6

Maximum tree depth: 36

Running DFS with $medium_maze.txt$



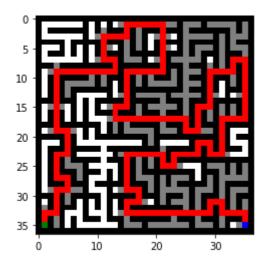
Path cost: 232

Explored squares: 273

Maximum size of the frontier: 11

Maximum tree depth: 231

Running DFS with $large_maze.txt$

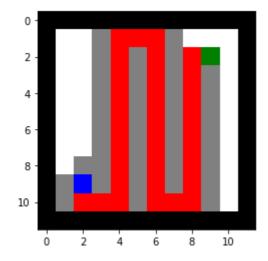


Path cost: 210 Explored squares: 461

Maximum size of the frontier: 32

Maximum tree depth: 209

Running DFS with <code>empty_maze.txt</code>



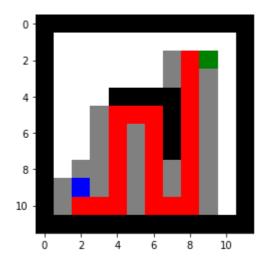
Path cost: 34

Explored squares: 72

Maximum size of the frontier: 39

Maximum tree depth: 33

Running DFS with $wall_{maze.txt}$

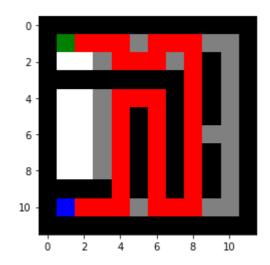


Path cost: 26 Explored squares: 51

Maximum size of the frontier: 25

Maximum tree depth: 25

Running DFS with loops_maze.txt

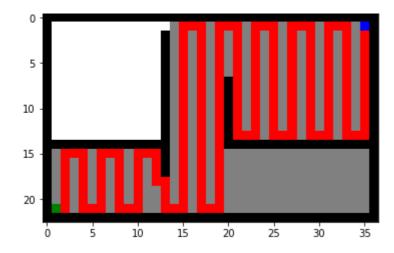


Path cost: 37 Explored squares: 59

Maximum size of the frontier: 12

Maximum tree depth: 39

Running DFS with open_maze.txt



Path cost: 226

Explored squares: 526

Maximum size of the frontier: 194

Maximum tree depth: 225

Depth First Search Analysis

This Depth First Search algorithm will loops through node's neighbours and make branches, for each neighbour, it will keep digging until there is no more child.

- Although many of mazes are infinite-depth spaces, the program will record all the places it visited, so it is complete.
- Since it will always keep digging (ex. from left to right), so it may not be able to find the shortest path(if the path is close to right); it is not optimal.
- Its Time Complexity is O(b^m) and m is the maximum depth because DFS will always dig to the deepest place where no more child.
- Its Space Complexity is O(bm) because it explores one path at a time.

Iterative Deepening Search

In [76]:

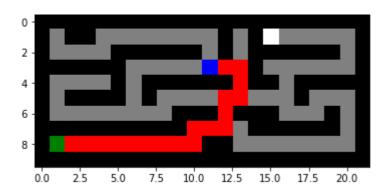
```
def Get layer(TreeNode, Root):
    layer = 0
    while(TreeNode != Root):
        laver = laver + 1
        TreeNode = TreeNode.getParent()
    return layer
def Find_DLS_Children(maze, Node, NodeonTree, Root):
    option = []
    West = [Node[0], Node[1]-1]
    North = [Node[0]-1, Node[1]]
    East = [Node[0], Node[1] + 1]
    South = [Node[0] + 1, Node[1]]
    tempNodeW = Root.getNode(West)
    tempNodeE = Root.getNode(East)
    tempNodeN = Root.getNode(North)
    tempNodeS = Root.getNode(South)
    OldDistance = Find Distance (NodeonTree, Root) + 1
    if (helper. look (maze, West) != 'X'):
        if (tempNodeW != None):
             if (Find Distance(tempNodeW, Root) > OldDistance):
                                                                          # If the node is on the
 tree but with higher distance
                Root. delNode (West)
                option. append (West)
        else:
            option. append (West)
    if (helper. look (maze, East) != 'X'):
        if(tempNodeE != None):
             if (Find Distance(tempNodeE, Root) > OldDistance):
                Root. delNode (East)
                option.append(East)
        else:
            option. append (East)
    if (helper. look (maze, North) != 'X'):
        if (tempNodeN != None):
             if (Find Distance(tempNodeN, Root) > OldDistance):
                Root. delNode (North)
                option. append (North)
        else:
            option. append (North)
    if (helper. look (maze, South) != 'X'):
        if (tempNodeS != None):
             if (Find Distance (tempNodeS, Root) > OldDistance):
                 Root. delNode (South)
                option. append (South)
        else:
            option. append (South)
    return option
def DLS_Search(maze, vis, depth):
    Start = helper. find pos(maze, what = "S")
    End = helper. find pos(maze, what = "G")
    Result = []
    MaxFrontier = 1
    MaxDepth = 1
                                                      # The maximum number will always show with 1
ongest distance
```

```
if(Start == End):
        Result. append ("Start is End")
        Result.append("Start is End")
        Result.append("Start is End")
        Result. append ("Start is End")
        return Result
    q = LifoQueue(maxsize= (len(maze)*len(maze[0])))
                                                                       # It is a LIFO queue like DF
S
    Root = Tree(Start)
    q. put (Root)
    1ayer = 0
    while(q.empty() == False):
        if (q. qsize() > MaxFrontier):
            MaxFrontier = q.qsize()
        NodeonTree = q. get()
        Node = NodeonTree.data
        layer = Get layer(NodeonTree, Root)
        if (layer > MaxDepth):
            MaxDepth = layer
        if (layer < depth):</pre>
            children = Find DLS Children(maze, Node, NodeonTree, Root)
            if(vis == True):
                if (Node != Start):
                    maze[Node[0]][Node[1]] = 'P'
                    helper. show maze (maze)
                    maze[Node[0]][Node[1]] = '.'
                   helper. show maze (maze)
            for e in children:
                if (e == End):
                    newTreeNode = Tree(e)
                    NodeonTree. addChild (newTreeNode)
                    tempNode = newTreeNode.getParent()
                    while(tempNode != Root):
                         maze[tempNode.data[0]][tempNode.data[1]] = 'P'
                         tempNode = tempNode.getParent()
                                                                           # Rebuild the path based
on the tree
                    Result = getResult(maze)
                    Result. append (MaxFrontier)
                    Result. append (MaxDepth)
                    return Result
                newTreeNode = Tree(e)
                maze[e[0]][e[1]] = '.'
                                                                       # Add child to the tree and
                NodeonTree. addChild (newTreeNode)
 to the queue
                q. put (newTreeNode)
    Result. append ("Path not found")
    Result.append("Path not found")
    Result.append("Path not found")
    Result.append("Path not found")
    return Result
def IDS Search(maze, vis):
    result = []
```

In [77]:

```
def IDS SearchRunner(vis):
   mazes = []
   mazes. append ("small_maze. txt")
   mazes. append ("medium_maze. txt")
   mazes. append ("large_maze. txt")
    mazes. append("empty_maze. txt")
   mazes.append("wall_maze.txt")
   mazes. append("loops_maze. txt")
   mazes. append ("open_maze. txt")
    for e in mazes:
        f = open(e, "r")
        maze_str = f.read()
        maze = helper.parse_maze(maze_str)
        print("\n==========
        print("Running IDS with ", e)
        localResult = IDS_Search(maze, vis)
        helper. show maze (maze)
        print("Path cost: ", localResult[0])
        print("Explored squares: ", localResult[1])
        print("Maximum size of the frontier: ", localResult[2])
        print("Maximum tree depth: ", localResult[3])
        print("=========
IDS SearchRunner (False)
```

Running IDS with small_maze.txt

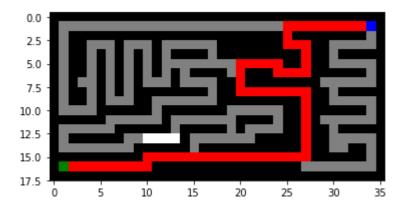


Path cost: 19 Explored squares: 92

Maximum size of the frontier: 5

Maximum tree depth: 19

Running IDS with $medium_maze.txt$



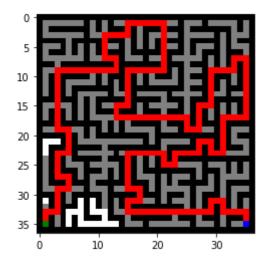
Path cost: 68

Explored squares: 269

Maximum size of the frontier: 7

Maximum tree depth: 68

Running IDS with $large_maze.txt$



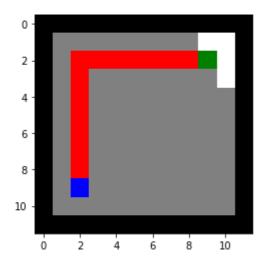
Path cost: 210

Explored squares: 619

Maximum size of the frontier: 32

Maximum tree depth: 209

Running IDS with empty_maze.txt



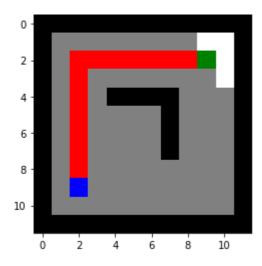
Path cost: 14

Explored squares: 95

Maximum size of the frontier: 22

Maximum tree depth: 14

Running IDS with $wall_{maze.txt}$

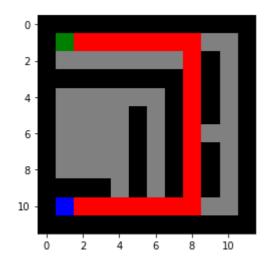


Path cost: 14 Explored squares: 88

Maximum size of the frontier: 20

Maximum tree depth: 14

Running IDS with loops_maze.txt



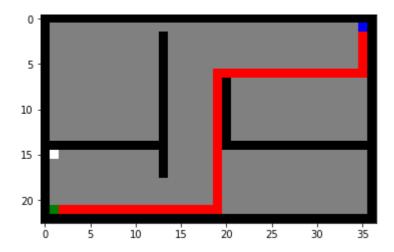
Path cost: 23

Explored squares: 71

Maximum size of the frontier: 10

Maximum tree depth: 23

Running IDS with $open_maze.txt$



Path cost: 54

Explored squares: 682

Maximum size of the frontier: 49

Maximum tree depth: 54

Iterative Deepening Search Analysis

This Iterative Deepening Search algorithm is similar to DFS, but it is restricted by layers. There is a for-loop to go through each lay, and for each round it will do Depth-First Search.

- It will check visited path to avoid loop, so it is complete
- It will implement DFS based on layers, so it will always find the shortest path like BFS; it is optimal
- Its Time Complexity is O(b^d) because it searchs like BFS.
- Its Space Complexity is O(bd) because it will not go to the deepest layer.

Task 3: Greedy best-first search [2 points]

You can use the map to estimate the distance from your current position to the goal using the Manhattan distance (see https://en.wikipedia.org/wiki/Taxicab_geometry) as a heuristic function.

In [79]:

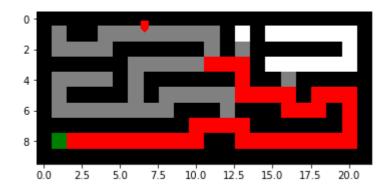
```
def Find Child (maze, Node, End, Dtype, Visited):
    West = [Node[0], Node[1]-1]
    North = [Node[0]-1, Node[1]]
    East = [Node[0], Node[1] + 1]
    South = [Node[0] + 1, Node[1]]
    BestNode = \begin{bmatrix} -1, -1 \end{bmatrix}
    BestDistance = 0
    if(helper.look(maze, West) != 'X' and West not in Visited):
                                                                           # Find Children with be
st h(n)
        if(West == End):
            return West
        else:
            maze[West[0]][West[1]] = '.'
            Distance = 0
            if (Dtype == "MA"):
                Distance = abs(West[0] - End[0]) + abs(West[1] - End[1])
            elif(Dtype == "EU"):
                Distance = math.sqrt((abs(West[0] - End[0]))**2 + (abs(West[1] - End[1]))**2)
            if (Distance <= BestDistance or BestDistance == 0):</pre>
                BestNode = West
                BestDistance = Distance
    if (helper.look (maze, East) != 'X' and East not in Visited):
        if(East == End):
            return East
        else:
            maze[East[0]][East[1]] = '.'
            Distance = 0
            if (Dtype == "MA"):
                Distance = abs(East[0] - End[0]) + abs(East[1] - End[1])
            elif(Dtype == "EU"):
                Distance = math.sqrt((abs(East[0] - End[0]))**2 + (abs(East[1] - End[1]))**2)
            if (Distance <= BestDistance or BestDistance == 0):</pre>
                BestNode = East
                BestDistance = Distance
    if (helper. look (maze, North) != 'X' and North not in Visited):
        if (North == End):
            return North
        else:
            maze[North[0]][North[1]] = '.'
            Distance = 0
            if (Dtype == "MA"):
                Distance = abs(North[0] - End[0]) + abs(North[1] - End[1])
            elif(Dtype == "EU"):
                Distance = math.sqrt((abs(North[0] - End[0]))**2 + (abs(North[1] - End[1]))**2)
            if (Distance <= BestDistance or BestDistance == 0):</pre>
                BestNode = North
                BestDistance = Distance
    if (helper. look (maze, South) != 'X' and South not in Visited):
        if(South == End):
            return South
        else:
            maze[South[0]][South[1]] = '.'
            Distance = 0
            if (Dtype == "MA"):
                Distance = abs(South[0] - End[0]) + abs(South[1] - End[1])
            elif(Dtype == "EU"):
                Distance = math. sqrt((abs(South[0] - End[0]))**2 + (abs(South[1] - End[1]))**2)
            if (Distance <= BestDistance or BestDistance == 0):</pre>
                BestNode = South
```

```
BestDistance = Distance
                                                 # Best Node is a list with the best child nearby
 and the number of area explored
    return BestNode
def GBFS_Search(maze, vis, Dtype):
    Start = helper. find pos(maze, what = "S")
    End = helper. find pos(maze, what = "G")
    Result = []
    Visited = []
    PathCost = 0
    AreaExplored = 0
    MaxFrontier = 1
    MaxDepth = 1
    if(Start == End):
        Result.append("Start is End")
        Result. append ("Start is End")
        Result. append ("Start is End")
        Result. append ("Start is End")
        return Result
    Path = LifoQueue(maxsize= (len(maze)*len(maze[0])))
    Path. put (Start)
    Visited. append (Start)
    while (Path. empty != False):
        if (Path. qsize() > MaxFrontier):
            MaxFrontier = Path. qsize()
        Node = Path. get()
        NewNode = Find Child (maze, Node, End, Dtype, Visited)
        if(NewNode[0] != -1):
            if (NewNode == End):
                Result = getResult(maze)
                Result. append (MaxFrontier)
                Result. append (Result[0])
                return Result
            else:
                Visited. append (NewNode)
                Path. put (Node)
                Path. put (NewNode)
                maze[NewNode[0]][NewNode[1]] = 'P'
                if(vis == True):
                     helper. show maze (maze)
        else:
            maze[Node[0]][Node[1]] = '.'
            Node = Path. get()
            maze[Node[0]][Node[1]] = 'P'
            Path. put (Node)
            if(vis == True):
                helper.show_maze(maze)
    Result. append ("Path not found")
    Result.append("Path not found")
    Result. append ("Path not found")
    Result.append("Path not found")
    return Result
```

In [80]:

```
def GBFS AM SearchRunner(vis):
   mazes = []
   mazes.append("small maze.txt")
   mazes. append ("medium maze. txt")
   mazes. append ("large maze. txt")
   mazes. append ("empty maze. txt")
   mazes. append ("wall maze. txt")
   mazes. append ("loops maze. txt")
   mazes. append ("open_maze. txt")
   for e in mazes:
       f = open(e, "r")
       maze str = f.read()
       maze = helper.parse maze(maze str)
       print("Running GBFS with Manhattan Distance and", e)
       localResult = GBFS Search(maze, vis, "AM")
       helper. show maze (maze)
       print("Path cost: ", localResult[0])
       print("Explored squares: ", localResult[1])
       print("Maximum size of the frontier: ", localResult[2])
       print("Maximum tree depth: ", localResult[3])
       def GBFS EU SearchRunner(vis):
   mazes = []
   mazes.append("small maze.txt")
   mazes. append ("medium maze. txt")
   mazes. append ("large maze. txt")
   mazes. append ("empty maze. txt")
   mazes. append ("wall_maze. txt")
   mazes. append ("loops_maze. txt")
   mazes. append ("open maze. txt")
    for e in mazes:
       f = open(e, "r")
       maze str = f.read()
       maze = helper.parse maze(maze str)
       print("\n=====
       print ("Running GBFS with Euclidean Distance and", e)
       localResult = GBFS Search(maze, vis, "EU")
       helper. show maze (maze)
       print("Path cost: ", localResult[0])
       print("Explored squares: ", localResult[1])
       print("Maximum size of the frontier: ", localResult[2])
       print("Maximum tree depth: ", localResult[3])
       print("======\n")
GBFS AM SearchRunner (False)
GBFS EU SearchRunner (False)
```

Running GBFS with Manhattan Distance and small_maze.txt



-1

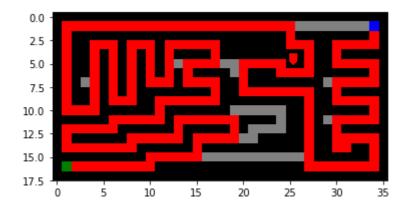
Path cost: 38

Explored squares: 80

Maximum size of the frontier: 45

Maximum tree depth: 38

Running GBFS with Manhattan Distance and medium_maze.txt



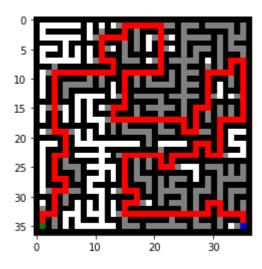
Path cost: 234

Explored squares: 273

Maximum size of the frontier: 234

Maximum tree depth: 234

Running GBFS with Manhattan Distance and large_maze.txt



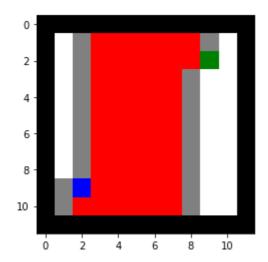
Path cost: 210

Explored squares: 461

Maximum size of the frontier: 210

Maximum tree depth: 210

Running GBFS with Manhattan Distance and empty_maze.txt



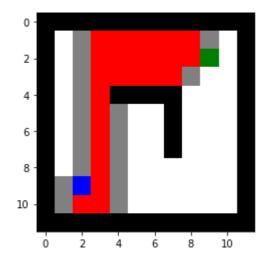
Path cost: 54

Explored squares: 73

Maximum size of the frontier: 54

Maximum tree depth: 54

Running GBFS with Manhattan Distance and wall_maze.txt

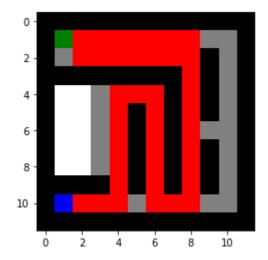


Path cost: 26 Explored squares: 44

Maximum size of the frontier: 26

Maximum tree depth: 26

Running GBFS with Manhattan Distance and loops_maze.txt



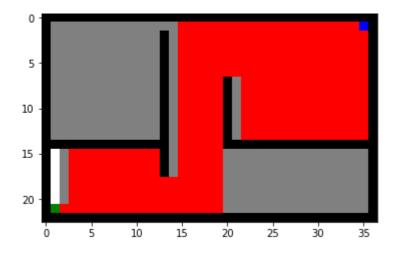
Path cost: 41 Explored squares: 61

M : C 1 C 1

Maximum size of the frontier: 41

Maximum tree depth: 41

Running GBFS with Manhattan Distance and open maze.txt

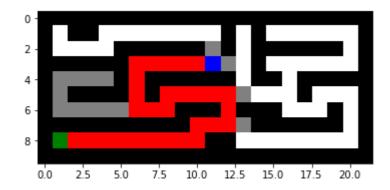


Path cost: 378 Explored squares: 677

Maximum size of the frontier: 477

Maximum tree depth: 378

Running GBFS with Euclidean Distance and small_maze.txt

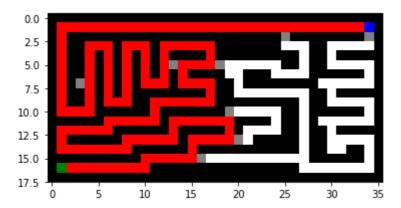


Path cost: 29 Explored squares: 43

Maximum size of the frontier: 29

Maximum tree depth: 29

Running GBFS with Euclidean Distance and $medium_maze.txt$



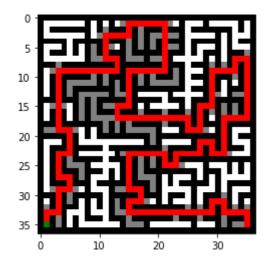
Path cost: 162

Explored squares: 170

Maximum size of the frontier: 162

Maximum tree depth: 162

Running GBFS with Euclidean Distance and large_maze.txt

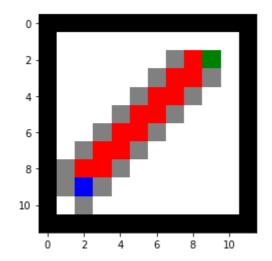


Path cost: 211 Explored squares: 367

Maximum size of the frontier: 210

Maximum tree depth: 211

Running GBFS with Euclidean Distance and empty_maze.txt



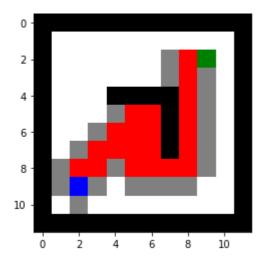
Path cost: 14

Explored squares: 30

Maximum size of the frontier: 14

Maximum tree depth: 14

Running GBFS with Euclidean Distance and wall maze.txt



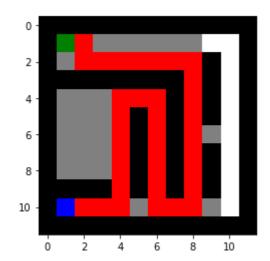
Path cost: 22

Explored squares: 42

Maximum size of the frontier: 22

Maximum tree depth: 22

Running GBFS with Euclidean Distance and loops_maze.txt

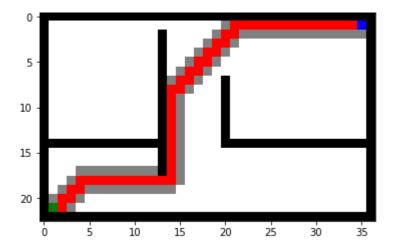


Path cost: 35 Explored squares: 60

Maximum size of the frontier: 35

Maximum tree depth: 35

Running GBFS with Euclidean Distance and open_maze.txt



Path cost: 54

Explored squares: 115

Maximum size of the frontier: 54

Maximum tree depth: 54

Greedy Best-First Search Analysis

The Greedy Best-First Search algorithm will find the shortest neighbour based on the distance between the goal and the current (There are two type of distances I used). It will always to the next node with shortest h(n).

- Since the code will check visited place and do back-tracking, so it is complete in this case.
- The shortest h(n) doesn't always equal to the shortest path, so it is not optimal.
- The Time Complexity is from O(bd) to O(b^m) depends on how the heuristic works.
- The Space Complexity is O(b^m).

Task 4: A* Search [3 points]

Use again the Manhattan heuristic function.

In [82]:

```
def Find F Distance(maze, Node, Root, NodeonTree, End, Dtype):
                                                                                 # A function for
 f(n)
   Total = 0
    while (NodeonTree != Root):
        NodeonTree = NodeonTree.getParent()
        Total = Total + 1
    if (Dtype == "MA"):
        Total = Total + abs(Node[0] - End[0]) + abs(Node[1] - End[1])
    elif(Dtype == "EU"):
        Total = Total + math. sqrt((abs(Node[0] - End[0]))**2 + (abs(Node[1] - End[1]))**2)
   return Total
def Find_A_Star_Children(maze, Node, Root, NodeonTree, End, Dtype):
   Children = []
    NewPath = []
    Visited = 0
    while (NodeonTree != Root):
        NewPath. append (NodeonTree. data)
        NodeonTree = NodeonTree.getParent()
        Visited = Visited + 1
    NewPath. append (NodeonTree. data)
    Visited = Visited + 1
                                             # Rebuild the path based on the node on tree
    West = [Node[0], Node[1]-1]
    if (helper. look (maze, West) != 'X' and West not in NewPath):
        Children. append (West)
   North = [Node[0]-1, Node[1]]
    if (helper.look (maze, North) != 'X' and North not in NewPath):
        Children. append (North)
    East = [Node[0], Node[1] + 1]
    if (helper. look (maze, East) != 'X' and East not in NewPath):
        Children. append (East)
    South = [Node[0] + 1, Node[1]]
    if (helper. look (maze, South) != 'X' and South not in NewPath):
        Children. append (South)
    return Children
                                                  # Return a list of options that it can go
def UpdateMaze(maze, NodeonTree, vis):
    for i in range(len(maze)):
        for j in range(len(maze[0])):
            if(maze[i][j] = 'P'):
                maze[i][j] = '.'
                                           # The original path becomes explored
    path = []
    while (NodeonTree. isRoot() == False):
        path. append (NodeonTree. data)
        NodeonTree = NodeonTree.getParent() # Get the new path
    for e in path:
        maze[e[0]][e[1]] = 'P'
                                            # Put new path to red
    if(len(path) != 0):
```

2020/10/4 Mazo

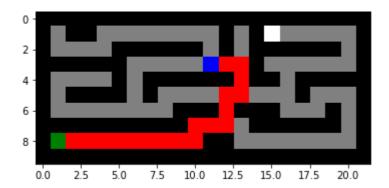
```
maze[path[0][0]][path[0][1]] = '.' # The head is still under exploration
    if(vis == True):
        helper. show maze (maze)
    return path
def A_Star_Search(maze, vis, Dtype):
    Start = helper.find_pos(maze, what = "S")
    End = helper.find_pos(maze, what = "G")
    Result = []
   MaxFrontier = 1
   MaxDepth = 1
    counter = 0
                                    # a counter to identify paths with same distance
    if(Start == End):
        Result. append ("Start is End")
        return Result
    q = []
                                     # It's a sorted list with nodes (can be built as a path by t
ree) from shortest f(n) to largest f(n), like priority queue
    Root = Tree(Start)
    q. append([Find F Distance(maze, Start, Root, Root, End, Dtype), Root, counter])
    while (len(q) != 0):
        if (len(q) > MaxFrontier):
            MaxFrontier = len(q)
        tNode = q[0].copy() # Pull out the node with smallest f(n)
        q. pop(0)
        NodeonTree = tNode[1]
        Node = NodeonTree.data
        depth = Find Distance(NodeonTree, Root)
        if (MaxDepth < depth):</pre>
                                                             # Find the depth of the node
            MaxDepth = depth
        UpdateMaze (maze, NodeonTree, vis)
                                                    # Update maze with each new path
        if(Node == End):
            newTreeNode = Tree(Node)
            NodeonTree. addChild(newTreeNode)
            tempNode = newTreeNode.getParent()
            while(tempNode != Root):
                maze[tempNode.data[0]][tempNode.data[1]] = 'P'
                tempNode = tempNode.getParent()
            maze[End[0]][End[1]] = 'G'
                                                   # Remark Path and Destination's colors
            Result = getResult(maze)
            Result. append (MaxFrontier)
            Result. append (MaxDepth)
            return Result
        children = Find A Star Children (maze, Node, Root, NodeonTree, End, Dtype)
                                                                                              # Ge
t the children of the current path
        for e in children:
           counter = counter + 1
                                                         # Update counter to make diffferent iden
tification for the node
            newchild = Tree(e)
            NodeonTree. addChild (newchild)
            newchildDistance = Find Distance(NodeonTree, Root)
```

```
UpdateMaze(maze, newchild, vis)
            newDistance = Find_F_Distance (maze, e, Root, newchild, End, Dtype) # Find the f(n) f
or that node
            find = False
                                                                   # insert the new node into the
 sorted list
            index = -1
            has = False
            for a in range (len(q)):
                                                                 # Find where the node is already
                if(e = q[a][1]. data):
 in the container
                    if (newDistance \langle q[a][0]\rangle:
                         q[a] = [newDistance, newchild, counter]
                    has = True
                                                                   # Insert it into the container
            if(has == False):
                for b in range(len(q)):
                    if (newDistance < q[a][0]):</pre>
                         q.insert(a , [newDistance, newchild, counter])
                         find = True
                        break
                    elif(newDistance == q[a][0]):
                         if(counter >= q[a][2]):
                             q. insert(a , [newDistance, newchild, counter])
                             find = True
                             break:
                if(find == False):
                    q.append([newDistance, newchild, counter])
    Result. append ("Path not found")
    Result.append("Path not found")
    Result. append ("Path not found")
    Result.append("Path not found")
    return Result
```

In [83]:

```
def A Star AM SearchRunner(vis):
   mazes = []
   mazes.append("small maze.txt")
   mazes. append ("medium maze. txt")
   mazes. append ("large maze. txt")
   mazes. append ("empty maze. txt")
   mazes. append ("wall maze. txt")
   mazes. append ("loops maze. txt")
   mazes. append ("open_maze. txt")
   for e in mazes:
       f = open(e, "r")
       maze str = f.read()
       maze = helper.parse maze(maze str)
       print("Running A_Star Search with Manhattan Distance and", e)
       localResult = A Star Search(maze, vis, "AM")
       helper. show maze (maze)
       print("Path cost: ", localResult[0])
       print("Explored squares: ", localResult[1])
       print("Maximum size of the frontier: ", localResult[2])
       print("Maximum tree depth: ", localResult[3])
       def A Star EU SearchRunner(vis):
   mazes = []
   mazes.append("small maze.txt")
   mazes. append ("medium maze. txt")
   mazes. append ("large maze. txt")
   mazes. append ("empty maze. txt")
   mazes. append ("wall_maze. txt")
   mazes. append ("loops_maze. txt")
   mazes. append ("open_maze. txt")
    for e in mazes:
       f = open(e, "r")
       maze str = f.read()
       maze = helper.parse maze(maze str)
       print ("\n======
       print ("Running A Star Search with Euclidean Distance and", e)
       localResult = A Star Search(maze, vis, "EU")
       helper. show maze (maze)
       print("Path cost: ", localResult[0])
       print("Explored squares: ", localResult[1])
       print("Maximum size of the frontier: ", localResult[2])
       print("Maximum tree depth: ", localResult[3])
       print("======\n")
A Star AM SearchRunner(False)
A Star EU SearchRunner (False)
```

Running A_Star Search with Manhattan Distance and small_maze.txt



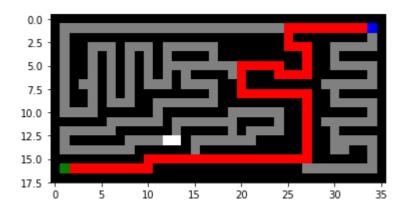
Path cost: 19

Explored squares: 92

Maximum size of the frontier: 9

Maximum tree depth: 19

Running A_Star Search with Manhattan Distance and medium_maze.txt



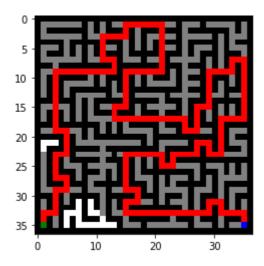
Path cost: 68

Explored squares: 271

Maximum size of the frontier: 12

Maximum tree depth: 68

Running A_Star Search with Manhattan Distance and large_maze.txt



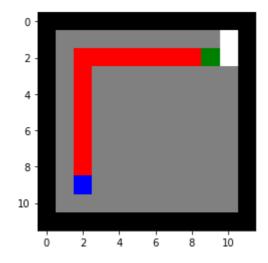
Path cost: 210

Explored squares: 622

Maximum size of the frontier: 8

Maximum tree depth: 210

Running A_Star Search with Manhattan Distance and empty_maze.txt



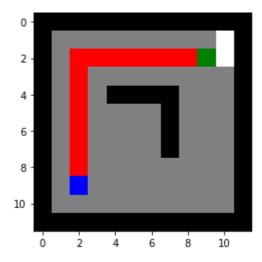
Path cost: 14

Explored squares: 97

Maximum size of the frontier: 52

Maximum tree depth: 14

Running A_Star Search with Manhattan Distance and wall_maze.txt

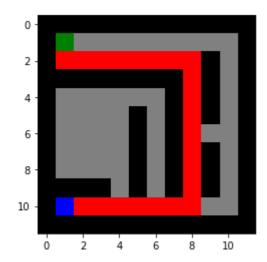


Path cost: 14 Explored squares: 90

Maximum size of the frontier: 49

Maximum tree depth: 14

Running A_Star Search with Manhattan Distance and loops_maze.txt



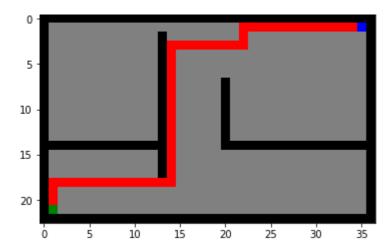
Path cost: 23

Explored squares: 71

Maximum size of the frontier: 18

Maximum tree depth: 23

Running A_Star Search with Manhattan Distance and open_maze.txt



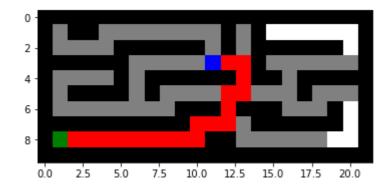
Path cost: 54

Explored squares: 683

Maximum size of the frontier: 333

Maximum tree depth: 54

Running A_Star Search with Euclidean Distance and small_maze.txt



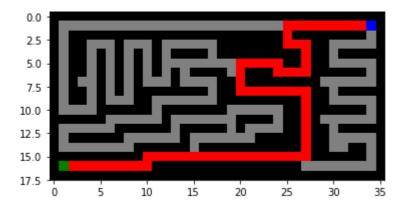
Path cost: 19

Explored squares: 82

Maximum size of the frontier: 7

Maximum tree depth: 19

Running A_Star Search with Euclidean Distance and medium_maze.txt



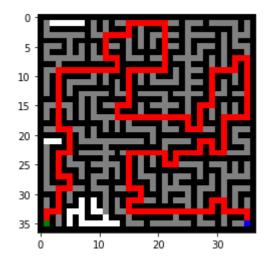
Path cost: 68

Explored squares: 273

Maximum size of the frontier: 13

Maximum tree depth: 76

Running A_Star Search with Euclidean Distance and large_maze.txt



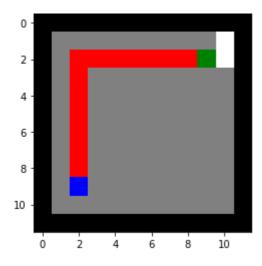
Path cost: 210

Explored squares: 617

Maximum size of the frontier: 10

Maximum tree depth: 210

Running A_Star Search with Euclidean Distance and empty_maze.txt

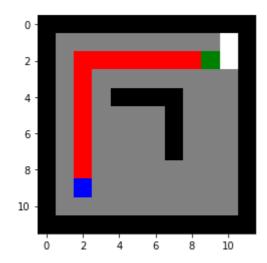


Path cost: 14 Explored squares: 97

Maximum size of the frontier: 50

Maximum tree depth: 14

Running A_Star Search with Euclidean Distance and wall_maze.txt



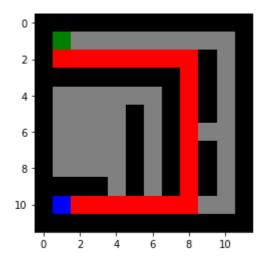
Path cost: 14

Explored squares: 90

Maximum size of the frontier: 47

Maximum tree depth: 14

Running A_Star Search with Euclidean Distance and loops_maze.txt

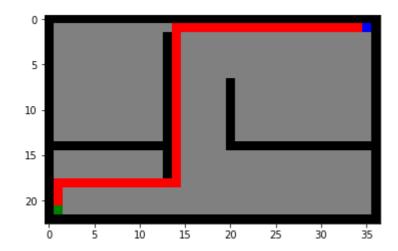


Path cost: 23 Explored squares: 71

Maximum size of the frontier: 20

Maximum tree depth: 25

Running A_Star Search with Euclidean Distance and open_maze.txt



Path cost: 54

Explored squares: 683

Maximum size of the frontier: 310

Maximum tree depth: 54

A* Search Analysis

It is similar to GBFS, but it will find the shortest node based on f(n). It uses a container to store all the options (sorted based on f(n)), and it will always pick the first path.

- It is complete because it will record visited place to avoid infinity loop.
- It is optimal because it will always use the path with best f(n)
- Its Time Complexity may be less that exponential because the container will always store the shortest path from A to B (If it finds A to C to B it will remove it)
- · Its Space Complexity may also be less that exponential.

Don't forget to add a table that compares the following for the algorithms on the different mazes:

- · The solution and its path cost
- · Number of nodes expanded
- · Maximum tree depth searched
- · Maximum size of the frontier.

Analysis

Since I'm not a good python table maker, I put all the data into excel and make the tables.

Path Cost:

Path Cost	Small Maze	Medium Maze	Large Maze	Empty Maze	Wall Maze	Loops Maze	Open Maze
BFS_Search	19	68	210	14	14	23	54
DFS_Search	37	232	210	34	26	37	226
IDS_Search	19	68	210	14	14	23	54
GBFS_Search (MA)	38	234	210	54	26	41	378
GBFS_Search (EU)	29	162	211	14	22	35	54
A*_Search (MA)	19	68	210	14	14	23	54
A*_Search (EU)	19	68	210	14	14	23	54

From the table we can find out that BFS,IDS,and A* will always find the shortest path.

Explored Squares

Explored squares	Small Maze	Medium Maze	Large Maze	Empty Maze	Wall Maze	Loops Maze	Open Maze
BFS_Search	91	269	622	95	88	71	683
DFS_Search	56	273	461	72	51	59	526
IDS_Search	92	269	619	95	88	71	682
GBFS_Search (MA)	80	273	461	73	44	61	677
GBFS_Search (EU)	43	170	367	30	42	60	115
A*_Search (MA)	92	271	622	97	90	71	683
A*_Search (EU)	82	273	617	97	90	71	683

The table shows that the algorithms that can find shortest path need to explore a huge amount of space, nor alogorithms like DFS and GBFS.

Maximum size of the frontier

Maximum size of the frontier	Small Maze	Medium Maze	Large Maze	Empty Maze	Wall Maze	Loops Maze	Open Maze
BFS_Search	8	8	8	12	11	7	23
DFS_Search	6	11	32	39	25	12	194
IDS_Search	5	7	32	22	20	10	49
GBFS_Search (MA)	45	234	210	54	26	41	477
GBFS_Search (EU)	29	162	210	14	22	35	54
A*_Search (MA)	9	12	8	52	49	18	333
A*_Search (EU)	7	13	10	50	47	20	310

I used Queue for BFS, Stack for DFS, IDS, and GBFS. I used a Sorted List (like a priority queue) to store the nodes for A*

Maximum tree depth

Maximum tree depth	Small Maze	Medium Maze	Large Maze	Empty Maze	Wall Maze	Loops Maze	Open Maze
BFS_Search	18	67	209	13	13	22	53
DFS_Search	36	231	209	33	25	39	225
IDS_Search	19	68	209	14	14	23	54
GBFS_Search (MA)	38	234	210	54	26	41	378
GBFS_Search (EU)	29	162	211	14	22	35	54
A*_Search (MA)	19	68	210	14	14	23	54
A*_Search (EU)	19	76	210	14	14	25	54

Algorithms like DFS(or GBFS) will go to the deep layer and find a long path, so the tree, used to store paths, is high.

Bonus Tasks [+1 point]

Instead of defining each square as a state (which you probably did), use only intersections as states. Now the storage requirement is reduced, but the path length between two intersections can be different. If we use total path length in number of squares as path cost, how can we make sure that BFS and iterative deepening search is optimal? Change the code to do so.

Although I didn't write code for this question (not sure how to make only intersections as states), I'm thinking that a state can also be the distance with obstacles. By monitoring the distances between obstacles(North, South, East, and West), we can implement BFS and IDS as what we did before, but instead of looping with depth, we can loop through the distance with obstacles.

Modify your A* search to add weights (see text book) and explore how different weights influence the result.

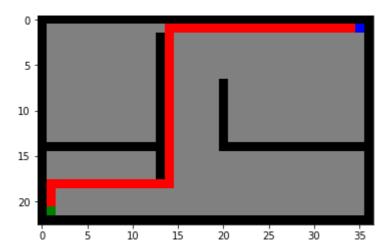
In [88]:

```
def Find Weightd F Distance (maze, Node, Root, NodeonTree, End, Dtype, Weight):
A function for f(n)
   Total = 0
    while (NodeonTree != Root):
        NodeonTree = NodeonTree.getParent()
        Total = Total + 1
    if(Dtype == "MA"):
        Total = Total + Weight * (abs(Node[0] - End[0]) + abs(Node[1] - End[1])) # Here it
 becomes Weight * h(n)
    elif(Dtype == "EU"):
        Total = Total + Weight * ( math.sqrt((abs(Node[0] - End[0]))**2 + (abs(Node[1] - End[1
]))**2))
   return Total
def Weighted A Star Search (maze, vis, Dtype, Weight):
    Start = helper.find_pos(maze, what = "S")
    End = helper. find pos (maze, what = "G")
    Result = []
   MaxFrontier = 1
   MaxDepth = 1
    counter = 0
                                    # a counter to identify paths with same distance
    if(Start == End):
        Result. append ("Start is End")
        return Result
    q = []
                                     # It's a sorted list with nodes (can be built as a path by t
ree) from shortest f(n) to largest f(n), like priority queue
    Root = Tree(Start)
    q. append([Find Weightd F Distance(maze, Start, Root, Root, End, Dtype, Weight), Root, counter])
    while (1en(q) != 0):
        if (len(q) > MaxFrontier):
            MaxFrontier = len(q)
        tNode = q[0].copy()
                                  # Pull out the node with smallest f(n)
        q. pop(0)
        NodeonTree = tNode[1]
        Node = NodeonTree.data
        depth = Find Distance(NodeonTree, Root)
        if (MaxDepth < depth):</pre>
                                                              # Find the depth of the node
            MaxDepth = depth
        UpdateMaze(maze, NodeonTree, vis)
                                                     # Update maze with each new path
        if(Node == End):
            newTreeNode = Tree(Node)
            NodeonTree. addChild(newTreeNode)
            tempNode = newTreeNode.getParent()
            while(tempNode != Root):
                maze[tempNode.data[0]][tempNode.data[1]] = 'P'
                tempNode = tempNode.getParent()
            maze[End[0]][End[1]] = 'G'
                                                     # Remark Path and Destination's colors
```

```
Result = getResult(maze)
            Result. append (MaxFrontier)
            Result. append (MaxDepth)
            return Result
        children = Find_A_Star_Children(maze, Node, Root, NodeonTree, End, Dtype)
                                                                                               # Ge
t the children of the current path
        for e in children:
            counter = counter + 1
                                                          # Update counter to make diffferent iden
tification for the node
            newchild = Tree(e)
            NodeonTree. addChild(newchild)
            newchildDistance = Find_Distance(NodeonTree, Root)
            UpdateMaze(maze, newchild, vis)
            newDistance = Find_Weightd_F_Distance(maze, e, Root, newchild, End, Dtype, Weight)
Find the f(n) for that node
            find = False
                                                                   # insert the new node into the
 sorted list
            index = -1
            has = False
            for a in range (len(q)):
                if(e = q[a][1]. data):
                                                                # Find where the node is already
 in the container
                    if (newDistance < q[a][0]):</pre>
                         q[a] = [newDistance, newchild, counter]
                    has = True
            if(has == False):
                                                                   # Insert it into the container
                for b in range (len(q)):
                    if (newDistance \langle q[a][0]\rangle:
                         q.insert(a ,[newDistance, newchild, counter])
                         find = True
                        break
                    elif(newDistance == q[a][0]):
                         if (counter \geq q[a][2]):
                             q. insert(a , [newDistance, newchild, counter])
                             find = True
                             break:
                if(find == False):
                    q.append([newDistance, newchild, counter])
    Result. append ("Path not found")
    Result.append("Path not found")
    Result.append("Path not found")
    Result. append ("Path not found")
    return Result
```

In [97]:

Running Weighted A_Star Search with Euclidean Distance and open_maze.txt



Path cost: 54

Explored squares: 683

Maximum size of the frontier: 298

Maximum tree depth: 54

Weighted A* Analysis

I add another parameter as the weight and use it to time with h(n). Although the result is the same (may be because the maze is still very small), but adding weight do make the program faster (around half a second on my local machine). However, I've found out that if the weight is too big, it will not be that efficient.

What happens if the agent does not know the layout of the maze in advance (i.e., faces an unkown, only partially observable environment)? How does the environment look then (PEAS description)? How would you implement a rational agent to solve the maze? What if the agent still has a GPS device to tell the distance to the goal?

1: If the environment is partially observable, then the agent will not know where are the obstacles and where are the goals; it doesn't even know where it is.

- 2: Then the PEAS description will be
 - Performance measure: Find the goal, or it may also be required to find the shortest one.
 - Environment: maze with obstacles (If it is a empty maze it does not have any obstacles), a sqaure
 as the goal.
 - Actuators: If can go North, South, East, and West if the node is available(not an obstacle)
 - Sensors: In the partially observable environment, it will only idenity squares nearby.
- 3: If the environment is partially observable, GBFS and A* will not work becuase the agent cannot find where the goal is. Therefore, it will depend on the performance measure; if the measure also includes shortest path, then IDS and BFS are good choice for the agent. If it doesn't, then the agent can also be implement with DFS.
- 4: If the agent has a GPS to tell it where the goal is, it can use A* or GBFS to find the goal (depends on measure).