Econ821 Problem Set 1 Result Summaries

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The data analyses for hedonic models were conducted in R. Codes are attached at the end of the file in PDF format. The original R file is uploaded on github.

Question 1

Report means and variances of attributes for each city:

| | | | | | | | | | violent_cri | | |
|----------------------|---------------------|-------------------------------------------------------------------------|-------------------------------------------------------------------|---------------------------------------------------|--------------------------------------------------------------------|----------------------------------------------------|--------------------------------------------------------------------|----------------------------------------------------------------------------------|--------------------------------------------------|----------------------------------------------------------|-----------------------------------------------------------------------------------------------|
| | | | year_built_ | sq_footage_ | bathrooms_ | bedrooms_ | total_rooms | stories_mea | me_rate_ | property_crime_ | year_of_sal |
| city | county | price_mean | mean | mean | mean | mean | _mean | n | mean | rate_mean | e_mean |
| LA | 37 | 311463.9263 | 1952.01876 | 1602.58218 | 1.98569178 | 3.09157726 | 7.93244377 | 1.13457183 | 618.80952 | 1976.515392 | 1999.91664 |
| LA | 59 | 296527.6326 | 1981.45209 | 1541.96509 | 2.15192731 | 2.58722467 | 6.10440529 | 1.59174009 | 314.4707 | 1414.156806 | 1999.93998 |
| LA | 65 | 181315.3171 | 1973.89449 | 1623.62299 | 2.20300657 | 3.12359778 | 6.13233957 | 1.19949469 | 616.38208 | 2436.70124 | 1999.82567 |
| LA | 71 | 188939.8284 | 1979.33519 | 1679.6764 | 2.14879856 | 3.23983488 | 6.5127451 | 1.36482972 | 567.66939 | 2216.85848 | 2000.39754 |
| LA | 111 | 332179.352 | 1978.34596 | 1825.54504 | 2.3424373 | 3.34221863 | 6.64299928 | 1.48824648 | 335.66362 | 1241.452924 | 2000.05462 |
| SF | 1 | 398873.1171 | 1962.17447 | 1672.36158 | 2.0314922 | 3.17236625 | 6.50623577 | 1.43417452 | 441.49934 | 1971.128292 | 2000.34516 |
| SF | 13 | 374582.3608 | 1976.76117 | 1833.1482 | 2.24779821 | 3.30335691 | 8.01458746 | 1.43224894 | 415.78327 | 1898.750281 | 2000.55541 |
| SF | 75 | 501817.0863 | 1945.13257 | 1497.93269 | 1.73122589 | 2.61824094 | 5.86750359 | 1.34167738 | 586.16285 | 2141.653726 | 1999.94978 |
| SF | 81 | 503715.0083 | 1967.16667 | 1587.40496 | 2.04414991 | 2.73966838 | 5.93399993 | 1.35557314 | 349.07914 | 1713.204285 | 2000.26109 |
| SF | 85 | 464683.1897 | 1971.45669 | 1662.78732 | 2.16185856 | 3.21450405 | 6.84787873 | 1.40198467 | 322.55811 | 1358.682926 | 2000.23945 |
| | | | | | | | | | | | |
| | | | year_built_v | sq_footage_ | bathrooms_ | bedrooms_v | total_rooms | | violent_cri me_rate_v | property_crime_ | year_of_sal |
| city | county | price_var | ar | var | var | ar | _var | stories_var | ar | rate_var | e_var |
| LA | 37 | 33942721831 | 240.439066 | 388140.973 | 0.63658388 | 0.69428087 | 4.26628219 | 0.11935241 | 77212.929 | 363360.2422 | 17.6570308 |
| LA | 59 | 30953601267 | 61.1363763 | 582421.099 | 0.45335844 | 0.82331954 | 2.32547899 | 0.26958701 | 18926.972 | 206208.1516 | 15.4169279 |
| LA | | | | | | | 2.020 .7 000 | 0.20000702 | | | |
| | 65 | 11065383445 | 212.658027 | 329746.33 | 0.4548194 | 0.63225427 | 1.86934169 | 0.16273662 | 77673.747 | 681390.2369 | 17.903409 |
| LA | 65 71 | | | 329746.33 389720.428 | | | | 0.16273662 | 77673.747 61450.635 | 681390.2369 368819.3119 | |
| | 71 | | 329.251437 | | 0.38646142 | | 1.86934169 2.65746045 | 0.16273662 0.23528148 | 61450.635 | | 17.3121685 |
| LA | 71 | 12133249510 | 329.251437 261.878758 | 389720.428 | 0.38646142 0.51802005 | 0.70516969 | 1.86934169 2.65746045 2.66677468 | 0.16273662 0.23528148 0.26150082 | 61450.635 23602.373 | 368819.3119 112945.0221 | 17.3121685 17.0726339 |
| LA LA | 71 111 1 | 12133249510 29798698555 | 329.251437 261.878758 697.85835 | 389720.428 563030.2 | 0.38646142 0.51802005 0.57241768 | 0.70516969 0.8037673 0.7728215 | 1.86934169 2.65746045 2.66677468 2.46933555 | 0.16273662 0.23528148 0.26150082 0.26079434 | 61450.635 23602.373 39922.396 | 368819.3119 112945.0221 | 17.3121685 17.0726339 17.7719081 |
| LA LA SF | 71 111 1 | 12133249510 29798698555 41544980702 46561031579 | 329.251437 261.878758 697.85835 379.707879 | 389720.428 563030.2 437987.58 | 0.38646142 0.51802005 0.57241768 0.50037351 | 0.70516969 0.8037673 0.7728215 | 1.86934169 2.65746045 2.66677468 2.46933555 | 0.16273662 0.23528148 0.26150082 0.26079434 0.24541211 | 61450.635 23602.373 39922.396 | 368819.3119 112945.0221 371046.5242 | 17.3121685 17.0726339 17.7719081 17.1362193 |
| LA LA SF SF | 71 111 1 1 | 12133249510 29798698555 41544980702 46561031579 65620319073 | 329.251437 261.878758 697.85835 379.707879 966.905052 | 389720.428 563030.2 437987.58 563350.088 | 0.38646142 0.51802005 0.57241768 0.50037351 0.65790174 | 0.70516969 0.8037673 0.7728215 0.83612014 | 1.86934169 2.65746045 2.66677468 2.46933555 4.26637152 | 0.16273662 0.23528148 0.26150082 0.26079434 0.24541211 0.31268353 | 61450.635 23602.373 39922.396 77245.919 | 368819.3119 112945.0221 371046.5242 359813.9069 | 17.903409 17.3121685 17.0726339 17.7719081 17.1362193 18.3596019 17.8774106 |

points estimates and Bootstrapping results

```
Call:
boot(data = la_data, statistic = bs, R = 500, formula = model)
Bootstrap Statistics:
         original
                         bias
                                  std. error
     1.989657e+06 1.318247e+05 1.498994e+06 Constant
t1*
t2*
     1.864903e+04 3.698016e+01 4.833379e+02 Bathroom
t3*
    -2.493170e+04 1.235183e+00 3.798288e+02 Bedroom
t4* -8.226933e+02 2.001854e+01 5.588499e+02 Stories
t5*
     3.719187e+00 -9.710739e-02 1.439251e+00 PCR
t6*
     4.648937e-04 1.670576e-05 2.359402e-04 PCR^2
t7*
    -8.931034e+02 -1.342622e+02 1.528999e+03 Year_built
t8*
    -2.926118e-02 3.421392e-02 3.899573e-01 Year built^2
t9*
     1.482554e+02 -1.494687e-02 2.396087e+00 Square_footage
t10* -4.293439e-05 -1.033138e-05 5.547963e-04 Square footage^2
t11* -3.354241e+03 -5.874402e+00 7.265847e+02 Total Room
t12* 5.521781e+02 2.813446e-01 4.469041e+01 Total Room^2
t13* -2.022722e+02 -7.585901e-02 3.033704e+00 VCR
t14* 7.382382e-02 6.909663e-05 1.648867e-03 VCR^2
t15* 2.566848e+04 -3.930548e+01 9.007504e+02 year/county dummies
t16* 7.701509e+03 3.342162e+01 1.020723e+03
t17* -6.539264e+03 -2.279894e+00 9.695666e+02
t18* -1.364771e+04 2.527797e+01 8.746022e+02
t19* -1.464752e+04 2.306539e+01 8.820465e+02
t20* -5.470540e+03 -1.388764e+01 7.952660e+02
t21* 1.079181e+04 -1.459507e+01 7.770563e+02
t22* 2.463901e+04 1.320286e+01 7.722553e+02
t23* 4.889535e+04 -1.641579e+01 8.065821e+02
t24* 8.847804e+04 -5.150423e+01 8.735586e+02
t25* 1.498607e+05 -2.011449e+00 9.719851e+02
t26* 2.016449e+05 5.008323e+01 1.015590e+03
t27* 2.211715e+05 -3.594313e+01 1.024624e+03
t28* 2.062445e+05 1.253221e+01 1.304568e+03
t29* 7.796900e+04 2.817227e+01 1.186984e+03
t30* -1.239729e+04 -6.351995e+01 1.166373e+03
t31* -1.064795e+05 -1.513362e+01 8.184827e+02
t32* -1.111114e+05 -1.852039e+01 6.928437e+02
t33* -8.710331e+03 -7.827093e+01 7.906988e+02
```

```
Call:
boot(data = sf_data, statistic = bs, R = 500, formula = model_sf)
Bootstrap Statistics :
                                  std. error
         original
                         bias
t1* -2.107292e+07 2.440171e+03 1.597930e+06 Constant
t2*
     2.168005e+04 2.386806e+01 6.933623e+02 Bathroom
t3* -1.933357e+04 1.014811e+01 4.273925e+02 Bedroom
t4* -2.840383e+04 3.365967e+01 5.910538e+02 Stories
t5*
    -8.203774e+01 3.692447e-02 1.886203e+00 PCR
    9.319009e-03 -1.154506e-06 2.886577e-04 PCR^2
t6*
t7*
    2.308429e+04 -2.259161e+00 1.630007e+03 Year built
t8* -6.270300e+00 5.527835e-04 4.156644e-01 Year_built^2
t9* 2.347345e+02 -8.857729e-02 3.253872e+00 Square_footage
t10* -1.006847e-03 1.494209e-05 7.221151e-04 Square_footage^2
t11* 3.072683e+04 -1.927611e+01 1.138151e+03 Total Room
t12* -1.905501e+03 2.277221e-01 7.789796e+01 Total Room^2
t13* -2.251711e+02 -2.699683e-01 4.004284e+00 VCR
t14* 1.116099e-01 1.321667e-04 2.123464e-03 VCR^2
t15* -4.604047e+04 1.662539e+01 1.048760e+03 year/county dummies
t16* -1.740659e+04 2.982994e+01 1.131023e+03
t17* -3.250213e+04 -1.432047e+01 1.098623e+03
t18* -4.395174e+04 -1.354667e+01 1.058030e+03
t19* -2.290150e+04 -6.975050e+00 1.032970e+03
t20* -6.639792e+03 -1.430323e+01 1.004120e+03
t21* 6.569116e+04 8.390140e+01 1.089710e+03
t22* 8.078236e+04 -4.649580e+01 1.166894e+03
t23* 9.007342e+04 -7.612461e+01 1.141396e+03
t24* 1.083045e+05 -6.126087e+00 1.063366e+03
t25* 1.661588e+05 -1.384953e+01 1.171738e+03
t26* 2.555370e+05 -1.199936e+01 1.172382e+03
t27* 2.605482e+05 -9.132196e+01 1.304497e+03
t28* 2.405591e+05 -8.501107e+01 1.565719e+03
t29* 1.118781e+05 -9.948590e+01 1.795105e+03
t30* -5.835151e+04 -2.622206e+01 6.157978e+02
t31* 1.544596e+05 -7.072409e+01 1.762366e+03
t32* 9.209555e+04 -4.436857e+01 1.103500e+03
t33* 3.594948e+04 -3.365045e+01 5.996326e+02
```

Point estimation by using the actual data:

The first stage: Coefficients of VCR and VCR SQUARE

- LA: -2.022722e+02; 7.382382e-02
- SF: -2.251711e+02 1.116099e-01

The Second Stage:

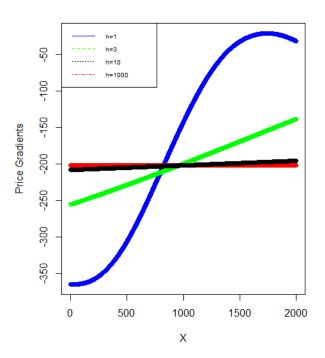
```
Call:
lm(formula = implicit_price ~ violent_crime_rate + buyers_data.3 +
buyers_data.4 + buyers_data.5 + income + LA_indicator, data = buyers_data)
Residuals:
 Min 1Q
-65.336 -4.497
                          Median
0.421
                                          3Q Max 3.734 175.636
Coefficients:
                                 Estimate Std. Error t value Pr(>|t|)
2.033e+02 3.485e-02 -5834.460 < 2e-16
1.690e-01 4.265e-05 3962.643 < 2e-16
3.366e-01 5.840e-02 -5.765 8.19e-09
                               -2.033e+02
1.690e-01
(Intercept)
violent_crime_rate
buyers_data.3
                                -3.366e-01
                                                  3.550e-02
2.943e-02
buyers_data.4
                                                                         5.123 3.01e-07 ***
buyers_data.5
                                 1.507e-01
                                                                                   < 2e-16 ***
< 2e-16 ***
                                                                    -15.925
-415.932
                                    496e-06
                                                  9.392e-08
LA_indicator
                               -9.840e+00 2.366e-02
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 8.639 on 659541 degrees of freedom
Multiple R-squared: 0.9617, Adjusted R-squared: 0.9617
F-statistic: 2.761e+06 on 6 and 659541 DF, p-value: < 2.2e-16
   ########################standard eroors by taking sd of bootstrapped parameters:0.003297735
   secondstage_boot <-read.csv("second_stage_500.csv")
sd(secondstage_boot$violent_crime_rate)
[1] 0.003297735
```

standard errors by taking sd of bootstrapped parameters

```
> secondstage_boot <-read.csv("second_stage_500.csv")
> sd(secondstage_boot$violent_crime_rate)
[1] 0.003297735
> |
```

Analysis: The first stage results tell that housing price is negatively correlated with crime rate for both cities. (sensible) The second stage of Rosen illustrates that people's MWTP for violent(negative) is positively correlated with the violent level. People care less about the crime behaviours in the neighborhood when crime level is higher. They ask for less compensation in terms of housing price (that sounds weird to me) Possible explanation: people who cares less about safety lives in the higher-crime communities. Also, People with higher income care more about the crime. But the difference is tiny.

Hedonic price gradients, non-parametric measurement:



Question 5

MWTP estimates based on Non-parametric gradient

```
> summary(MWTP_estimation)
lm(formula = MWTP ~ income + Asian_pi + black + hispanic, data = la_buyer_data)
Residuals:
   Min
             1Q
                Median
-117.12
        -46.35
                 -22.99
                          22.67
                                 401.42
Coefficients:
              Estimate Std. Error t value Pr(>|t|)
                       4.684e-01 -630.425
                                             <2e-16 ***
(Intercept) -2.953e+02
                        2.438e-06
                                   -13.793
                                             <2e-16 ***
income
            -3.363e-05
Asian_pi
            -7.623e-01
                        8.912e-01
                                              0.392
                                    -0.855
                                             <2e-16 ***
                       1.383e+00
7.029e-01
                                    36.753
black
             5.082e+01
                                             <2e-16 ***
hispanic
                                    30.552
             2.148e+01
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 68.67 on 55493 degrees of freedom
Multiple R-squared: 0.04225, Adjusted R-squared: 0.04218
F-statistic: 612 on 4 and 55493 DF, p-value: < 2.2e-16
```

Point estimation by using the actual data:

```
theta.start = c(-200,0.169, 0,0,0,0)
  names(theta.start) = c("mu1", "mu2", "mu3", "mu4", "mu5", "mu6") theta.mle = optim(par=theta.start, fn=mle, x=buyers_data, method
  theta.mle
$par
         intercept
                          violent crime
                    4.428857e-01
                                        9.380051e+05
                                                                               2.879410e-01
$value
[1] -18826365
$counts
function gradient
145 29
$convergence
[1] 0
$message
NULL
```

Compared to estimation result in Q3, the coefficient of crime rate is higher in the MLE estimation. Coefficient of income seems not that sensible to me.

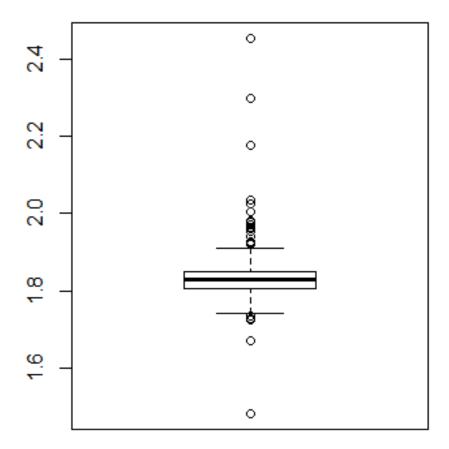
a few thoughts about the MLE method:

- MLE there is very sensitive to the starting point
- the likelihood may turn to be zero sometimes. We have to drop some observations to make the MLE method feasible. The number of drop out will influence the validity and reliability of the result.

Bootstrapping

| > violent_crime |
|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| [1] 1.782217 1.815562 1.827490 1.794456 1.880261 1.925557 1.889934 1.774643 1.858079 1.774413 1.833943 1.792788 1.801808 1.806541 1.824256 1.805515 |
| $\begin{bmatrix} 1.7 \end{bmatrix}$ 1.796021 1.923405 1.838094 1.856386 1.776214 1.804366 1.871373 1.827608 1.828061 1.812526 1.795154 1.851288 1.798909 1.821304 1.796239 1.862773 |
| [33] 1.833526 1.858454 1.899362 1.842968 1.809822 1.841034 1.790144 1.828057 1.814842 1.901679 1.831361 1.844445 1.853300 1.836709 1.818653 1.832467 |
| [49] 1.821470 1.815543 1.777509 1.798629 1.669396 1.798543 1.826587 1.829936 1.723054 1.824571 1.830146 1.852022 1.831964 1.849918 1.789620 1.750084 |
| [65] 1.836406 1.875767 1.835583 1.833205 1.805031 1.826747 1.827572 1.875013 1.786784 1.835285 1.863964 1.824027 1.850505 1.833228 1.830584 1.814005 |
| [81] 1.832528 1.844671 1.754401 1.742563 1.734933 1.857054 1.810795 1.733734 1.773632 1.847787 1.742937 1.801780 1.813951 1.955383 1.819451 1.823219 |
| [97] 1.808826 1.828213 1.801898 1.822880 1.829228 1.868184 2.455006 1.805743 1.858498 1.798693 1.806809 1.844918 1.782432 1.847236 1.804924 1.829262 |
| [113] 1.845973 1.843796 1.830253 1.779808 1.816417 1.823904 1.831860 1.860693 1.841052 1.852699 1.911741 1.823685 1.791700 1.795314 1.842719 1.857360 |
| [129] 1.741861 1.773655 1.829539 1.875210 1.881200 1.807225 1.834390 1.835673 1.835521 1.858576 1.821006 1.939656 1.928155 1.808461 1.847885 1.838589 |
| [145] 1.802460 1.756794 1.831751 1.841636 1.845289 1.865521 1.819513 1.811447 1.856956 1.844261 1.982415 1.884124 1.803105 1.830127 1.817734 1.815931 |
| [161] 1.824232 1.757649 1.838201 1.827747 1.829993 1.776675 1.818443 1.812491 1.810877 1.893814 1.830844 1.798633 1.801474 1.755423 1.875788 1.807063 |
| [177] 1.826129 1.835223 1.981046 1.851005 1.800713 1.857467 1.823567 1.822516 1.792560 1.797511 1.828752 1.811588 1.787637 1.856371 1.814268 1.842550 |
| [193] 1.961541 1.819967 1.867458 1.771259 1.787259 1.831562 1.816855 1.881897 1.832008 1.806375 1.845611 1.814113 1.810295 1.864097 1.828835 1.776685 |
| [209] 1.881765 1.827459 1.895581 1.811705 1.963601 1.807496 1.810979 1.831902 1.870396 1.805486 1.851507 1.864688 1.823412 1.825653 1.809318 1.857794 |
| [225] 1.823519 1.877464 1.860671 1.795439 1.879195 1.821495 1.846106 1.799992 1.813219 1.802394 1.882108 1.782057 1.843765 2.177457 1.823419 1.842632 |
| [241] 1.814171 1.798920 1.866874 1.805572 1.781266 1.811242 1.871169 1.829878 1.856727 1.891387 1.847272 1.837774 1.799051 1.834240 1.847345 1.771250 |
| [257] 1.878384 1.832366 1.820039 1.852922 1.844577 1.778527 1.828818 1.822788 1.848795 1.770491 1.841588 1.857984 1.831653 1.884310 1.750739 1.866524 |
| [273] 1.834363 1.850884 1.822605 1.480867 1.783974 1.787437 1.834372 1.847052 2.034499 1.842540 1.839407 1.851192 1.782973 1.814291 1.771079 1.797482 |
| [289] 1.847628 1.800188 1.981723 1.850050 1.817048 1.782921 1.783625 1.781117 1.782047 1.838412 1.814003 1.845232 1.812335 1.876023 1.840056 1.836015 |
| [305] 1.919997 1.811184 1.919188 1.827879 1.839042 1.982109 1.825886 1.851687 1.792556 1.751103 1.808232 1.813620 1.828643 1.818329 1.818164 1.821381 |
| [321] 1.826291 1.827385 1.976472 1.807699 1.828256 1.745108 1.827543 1.814002 1.825401 1.811616 1.819756 1.853961 1.831233 1.787733 1.819050 1.811777 |
| [337] 1.837244 1.828785 1.851768 1.776763 1.820340 1.857451 1.824107 1.826305 1.849786 1.846581 1.800854 1.830895 1.806507 1.813493 1.870385 1.838442 |
| [353] 1.856770 1.804363 1.876558 1.858419 1.794771 1.971303 1.837848 1.850002 1.760206 1.869202 1.787074 1.811532 1.804852 1.870076 1.759275 1.816105 |
| [369] 1.846268 1.797690 1.886622 1.810495 1.814965 1.838999 1.862691 1.802184 1.843593 1.802868 1.806763 1.864329 1.821768 1.798859 1.848888 1.785530 |
| [385] 1.845353 1.787477 1.799120 1.858385 1.841436 1.797106 1.812691 1.834111 1.802344 1.842712 1.876698 1.778594 1.884942 1.963915 1.832281 1.835261 |
| [401] 1.793340 1.820506 1.854267 1.850917 1.799769 1.825448 1.842333 1.788263 1.802643 1.780569 1.867966 1.784078 1.834533 1.820409 1.836481 1.775132 |
| [417] 1.908003 1.844489 1.815312 2.023438 1.822324 1.851950 1.817398 1.801072 1.919310 1.797241 1.763500 1.768706 1.795012 1.780384 1.875702 1.795257 |
| [433] 1.873304 1.785825 1.804800 1.830827 1.747224 1.843068 1.832453 1.864628 1.782407 1.805847 1.856219 1.843970 1.838836 1.815265 1.804331 1.881960 |
| [449] 2.300400 1.833541 1.786054 1.778829 1.843361 1.788356 1.799483 1.843943 1.827247 1.840947 1.781895 1.894778 1.833538 1.769212 1.845419 1.826205 |
| [465] 1.723023 1.847063 1.803830 1.831288 1.827754 1.804388 1.871295 1.855843 1.853210 1.901544 1.875129 1.862622 1.861755 1.851906 1.726842 1.845828 |
| [481] 1.851554 1.846555 1.795624 1.818731 1.814058 1.803125 1.833952 1.773778 1.850740 1.831377 1.823737 1.816884 1.824068 2.005891 1.813043 1.851244 |
| [497] 1.815051 |
| > mean(violent_crime) |
| [1] 1.831635 |
| s sd(violent_crime) |
| [1] 0.05983717 |
| <u> </u> |

three estimations were removed as outliers before the calculation of mean and standard deviation



boxplot for the coefficient of violent-crime-rate on the "second stage" MLE.

```
setwd("/Volumes/USB30FD/821 ps/hedonic")
library(dplyr)
library(purrr)
library(psych)
la data<- read.table("la data.txt", header = FALSE)</pre>
names(la data) <-</pre>
c("houseid", "price", "county", "year_built", "sq_footage", "bathrooms", "bedrooms", "total_rooms"
"year_of_sale")
la_sta <- la_data %>%
 group by(county) %>%
  summarise(price_mean=mean(price), year_built_mean=mean(year_built),
sq footage mean=mean(sq footage),
bathrooms_mean=mean(bathrooms), bedrooms_mean=mean(bedrooms),
total_rooms_mean=mean(total_rooms), stories_mean=mean(stories),
violent crime rate mean=mean(violent crime rate),
property_crime_rate_mean=mean(property_crime_rate),
year_of_sale_mean=mean(year_of_sale),
            price_var=var(price), year_built_var=var(year_built),
sq_footage_var=var(sq_footage),
bathrooms_var=var(bathrooms), bedrooms_var=var(bedrooms),
total rooms var=var(total rooms), stories var=var(stories),
violent_crime_rate_var=var(violent_crime_rate),
property_crime_rate_var=var(property_crime_rate),
year_of_sale_var=var(year_of_sale))
la_sta$city <- "LA"</pre>
sf data<- read.table("sf data.txt", header = FALSE)</pre>
names(sf data) <-
c("houseid", "price", "county", "year_built", "sq_footage", "bathrooms", "bedrooms", "total_rooms"
"year_of_sale")
sf_sta <-sf_data %>%
  subset(., sf data$county==1|13|75|81|85) %>%
 group_by(county) %>%
  summarise(price_mean=mean(price), year_built_mean=mean(year_built),
sq_footage_mean=mean(sq_footage),
bathrooms_mean=mean(bathrooms), bedrooms_mean=mean(bedrooms),
total_rooms_mean=mean(total_rooms), stories_mean=mean(stories),
violent_crime_rate_mean=mean(violent_crime_rate),
property_crime_rate_mean=mean(property_crime_rate),
year_of_sale_mean=mean(year_of_sale),
            price_var=var(price), year_built_var=var(year_built),
sq_footage_var=var(sq_footage),
bathrooms_var=var(bathrooms), bedrooms_var=var(bedrooms),
total_rooms_var=var(total_rooms), stories_var=var(stories),
violent_crime_rate_var=var(violent_crime_rate),
property_crime_rate_var=var(property_crime_rate),
year_of_sale_var=var(year_of_sale))
sf_sta$city <- "SF"
##combine two stats table
total_sta <- rbind(la_sta, sf_sta)</pre>
write.csv(total_sta, file="Q1_result.csv")
```

```
#Q2
rm(list=ls())
installation needed <- TRUE
loading needed <- TRUE
package_list <- c('foreign', 'xtable', 'plm', 'gmm',</pre>
'AER', 'stargazer', 'readstata13', 'boot')
if(installation_needed){install.packages(package_list, repos='http://
cran.us.r-project.org')}
if(loading_needed){lapply(package_list, require, character.only = TRUE)}
library(boot)
library("dummies")
library(dplyr)
library(purrr)
library(psych)
################################
# data & model LA
la_data<- read.table("la_data.txt", header = FALSE)</pre>
names(la_data) <-</pre>
c("houseid", "price", "county", "year built", "sq footage", "bathrooms", "bedrooms", "total rooms"
"year of sale")
la data <- cbind(la data, dummy(la data$county, sep = "."))</pre>
la_data <- cbind(la_data, dummy(la_data$year_of_sale, sep = "."))</pre>
model_la <- price ~ bathrooms + bedrooms + stories + property_crime_rate +</pre>
I(property_crime_rate^2) + year_built + I(year_built^2) + sq_footage +
I(sq_footage^2) + total_rooms + I(total_rooms^2) + violent_crime_rate +
I(violent_crime_rate^2) + bathrooms + la_data.1993 + la_data.1994 +
la_data.1995 + la_data.1996 + la_data.1997 + la_data.1998 + la_data.2000 +
la_data.2001 + la_data.2002 + la_data.2003 + la_data.2004 + la_data.2005 +
la_data.2006 + la_data.2007 + la_data.2008 + la_data.59 + la_data.65 +
la data.71 + la data.111
# function to obtain regression weights
bs <- function(formula, data, indices) {</pre>
  d <- data[indices,] # allows boot to select sample</pre>
  fit <- lm(formula, data=d)</pre>
  return(coef(fit))
# bootstrapping with 500 replications
results <- boot(data=la_data, statistic=bs,
                R=500, formula=model_la)
results
result bootcef la <- cbind(results$t[,13],results$t[,14])
write.csv(result_bootcef_la, file="result_bootcef_la.csv")
capture.output(results, file = "results boots la.txt", append = TRUE)
###################
# data & model SF
sf data<- read.table("sf data.txt", header = FALSE)</pre>
names(sf data) <-
c("houseid", "price", "county", "year_built", "sq_footage", "bathrooms", "bedrooms", "total_rooms"
"year of sale")
select(sf_data, sf_data$county==1|13|75|81|85)
```

```
sf data <- cbind(sf data, dummy(sf data$county, sep = "."))</pre>
sf_data <- cbind(sf_data, dummy(sf_data$year_of_sale, sep = "."))</pre>
model sf <- price ~ bathrooms + bedrooms + stories + property crime rate +
I(property_crime_rate^2) + year_built + I(year_built^2) + sq_footage +
I(sq_footage^2) + total_rooms + I(total_rooms^2) + violent_crime_rate +
I(violent crime rate^2) + bathrooms + sf data.1993 + sf data.1994 +
sf data.1995 + sf data.1996 + sf data.1997 + sf data.1998 + sf data.2000 +
sf_data.2001 + sf_data.2002 + sf_data.2003 + sf_data.2004 + sf_data.2005 +
sf_data.2006 + sf_data.2007 + sf_data.2008 + sf_data.13 + sf_data.75 +
sf_data.81 + sf_data.85
# bootstrapping with 500 replications
results_boot_sf <- boot(data=sf_data, statistic=bs,
               R=500, formula=model sf)
results boot sf
result bootcef sf <- cbind(results boot sf$t[,13],results$t[,14])
write.csv(result_bootcef_sf, file="result_bootcef_sf.csv")
capture.output(results boot sf, file = "results boots sf.txt", append =
TRUE)
rm(list=ls())
############## data read-in
##buvers
buyers_data<- read.table("buyer_data_sf_la.txt", header = FALSE)</pre>
names(buyers data) <-
c("buyerid", "price", "violent crime rate", "property crime rate", "race",
"income", "LA indicator")
## boostrapped hedonic price gradients from Q2
la_gradients <- read.csv("result_bootcef_la.csv")</pre>
sf_gradients <- read.csv("result_bootcef_sf.csv")</pre>
gradients la sf <- merge(la gradients,sf gradients, by="boot round")</pre>
rm(la_gradients,sf_gradients)
#######################assign implicit price of crime for each individual
*500
for( i in 1:500){
 buyers data[paste("implict price", i, sep= "")] <-</pre>
(buvers data$LA indicator)*gradients la sf[i,2]+ (1-
buyers_data$LA_indicator)*gradients_la_sf[i,4] + 2*gradients_la_sf[i,
3]*(buyers_data$violent_crime_rate)*(buyers_data$LA_indicator) +
2*gradients_la_sf[i,5]*(buyers_data$violent_crime_rate)*(1-
buyers_data$LA_indicator)
######################run second stage regression $ save coefficients *500
##create dummies for race
buyers_data <- cbind(buyers_data, dummy(buyers_data$race, sep = "."))</pre>
##regression
coef1 < -c()
for (j in 1:500){
  test_data <- cbind(buyers_data[, 1:7], buyers_data[, 508:511],
buyers_data[, 7+j])
```

```
colnames(test_data)[12] <- "implicit_price"</pre>
  model <- lm(implicit_price ~ violent_crime_rate + buyers_data.3 +</pre>
buyers_data.4 + buyers_data.5 + income + LA_indicator, data=test_data)
  newcoef1 <- model$coef</pre>
  coef1 <- rbind(coef1,newcoef1)</pre>
}
print(coef1)
#write.csv(coef1, file="second_stage_500.csv")
###################the actural point estimation
##first stage of LA, result: -2.022722e+02; 7.382382e-02
la_data<- read.table("la_data.txt", header = FALSE)</pre>
names(la_data) <-</pre>
c("houseid", "price", "county", "year_built", "sq_footage", "bathrooms", "bedrooms", "total_rooms",
"year_of_sale")
la_data <- cbind(la_data, dummy(la_data$county, sep = "."))</pre>
la_data <- cbind(la_data, dummy(la_data$year_of_sale, sep = "."))</pre>
model_la_actuall <- lm(price ~ bathrooms + bedrooms + stories +</pre>
property_crime_rate + I(property_crime_rate^2) + year_built +
I(year_built^2) + sq_footage + I(sq_footage^2) + total_rooms +
I(total_rooms^2) + violent_crime_rate + I(violent_crime_rate^2) + bathrooms
+ la_data.1993 + la_data.1994 + la_data.1995 + la_data.1996 + la_data.1997
+ la_data.1998 + la_data.2000 + la_data.2001 + la_data.2002 + la_data.2003
+ la_data.2004 + la_data.2005 + la_data.2006 + la_data.2007 + la_data.2008
+ la_data.59 + la_data.65 + la_data.71 + la_data.111, data=la_data)
summary(model_la_actuall)
##first stage of SF, result: -2.251711e+02 1.116099e-01
sf data<- read.table("sf data.txt", header = FALSE)</pre>
names(sf_data) <-</pre>
c("houseid", "price", "county", "year_built", "sq_footage", "bathrooms", "bedrooms", "total_rooms",
"year_of_sale")
select(sf_data, sf_data$county==1|13|75|81|85)
sf_data <- cbind(sf_data, dummy(sf_data$county, sep = "."))</pre>
sf_data <- cbind(sf_data, dummy(sf_data$year_of_sale, sep = "."))</pre>
model_sf_actuall <- lm(price ~ bathrooms + bedrooms + stories +</pre>
property_crime_rate + I(property_crime_rate^2) + year_built +
I(year_built^2) + sq_footage + I(sq_footage^2) + total_rooms +
I(total_rooms^2) + violent_crime_rate + I(violent_crime_rate^2) + bathrooms
+ sf_data.1993 + sf_data.1994 + sf_data.1995 + sf_data.1996 + sf_data.1997
+ sf_data.1998 + sf_data.2000 + sf_data.2001 + sf_data.2002 + sf_data.2003
+ sf_data.2004 + sf_data.2005 + sf_data.2006 + sf_data.2007 + sf_data.2008
+ sf_data.13 + sf_data.75 + sf_data.81 + sf_data.85, data=sf_data)
summary(model_sf_actuall)
##second stage
buyers_data<- read.table("buyer_data_sf_la.txt", header = FALSE)</pre>
names(buyers_data) <-</pre>
c("buyerid", "price", "violent_crime_rate", "property_crime_rate", "race",
"income", "LA_indicator")
```

```
buyers data$implicit price <- (buyers data$LA indicator)*-2.022722e+02+ (1-
buyers_data$LA_indicator)*-2.251711e+02 +
2*7.382382e-02*(buyers data$violent crime rate)*(buyers data$LA indicator)
+ 2*1.116099e-01*(buyers_data$violent_crime_rate)*(1-
buyers data$LA indicator)
buyers data <- cbind(buyers data, dummy(buyers data$race, sep = "."))</pre>
model second stage actuall <- lm(implicit price ~ violent crime rate +
buyers_data.3 + buyers_data.4 + buyers_data.5 + income + LA_indicator,
data=buyers data)
summary(model_second_stage_actuall)
#####################standard eroors by taking sd of bootstrapped
parameters: 0.003297735
secondstage boot <-read.csv("second stage 500.csv")</pre>
sd(secondstage_boot$violent_crime_rate)
#Q4
rm(list=ls())
library(dplyr)
library(purrr)
library(psych)
library(dummies)
##import data of LA
la_data<- read.table("la_data.txt", header = FALSE)</pre>
names(la data) <-
c("houseid", "price", "county", "year built", "sq footage", "bathrooms", "bedrooms", "total rooms"
"year of sale")
##create a function that generates weight vectors (length: # observations)
for each X 1:2000 and h:1:3
la data$weight <- 0
weight <- function(x,h,theta){</pre>
  sigma <- sd(x[, 10])
 x[,13] < (1/(h*sigma))*(1/sqrt(2*pi))*exp(-0.5*(((x[,10]-theta)/
(h*sigma))^2))
 ans <-x[,13]
 return(ans)
}
## for h=1
weight1 <- list()</pre>
for (i in 1:2000){
 weight1[[i]]<- weight(la_data, 1, i)</pre>
## for h=3
weight3 <- list()</pre>
for (i in 1:2000){
 weight3[[i]]<- weight(la_data, 3, i)</pre>
}
## for h=10
weight10 <- list()</pre>
```

```
for (i in 1:2000){
  weight10[[i]]<- weight(la data, 10, i)</pre>
## for h=1000
weight1000 <- list()</pre>
for (i in 1:2000){
  weight1000[[i]]<- weight(la data, 1000, i)</pre>
###########save gradient vector
##model
model <- price ~ violent_crime_rate</pre>
##h1
price_gradient_h1 <- replicate(2000,0)</pre>
for (i in 1:2000){
  estimation <-lm(model, la data, weights=weight1[[i]])</pre>
  price gradient h1[i] <- estimation$coefficients[2]</pre>
save(price_gradient_h1, file = "h1_price_gradients.Rdata")
##h3
price_gradient_h3 <- replicate(2000,0)</pre>
for (i in 1:2000){
  estimation <-lm(model, la_data, weights=weight3[[i]])</pre>
  price gradient h3[i] <- estimation$coefficients[2]</pre>
##h10
price gradient h10 <- replicate(2000,0)</pre>
for (i in 1:2000){
  estimation <-lm(model, la_data, weights=weight10[[i]])</pre>
  price_gradient_h10[i] <- estimation$coefficients[2]</pre>
##h1000
price gradient h1000 <- replicate(2000,0)</pre>
for (i in 1:2000){
  estimation <-lm(model, la_data, weights=weight1000[[i]])</pre>
  price gradient h1000[i] <- estimation$coefficients[2] }</pre>
price gradient h1000
### We eventually get the final result! Let plot it now
x = xis < -c(1:2000)
plot (x_axis, price_gradient_h1, type="b", pch = 19, col="blue",
ylab="Price Gradients", xlab="X")
lines(x_axis, price_gradient_h1000, col="red", type="b")
lines(x_axis, price_gradient_h3, col="green", type="b")
lines(x_axis, price_gradient_h10, col="black", type="b")
legend("topleft", legend=c("h=1", "h=3", "h=10", "h=1000"),
       col=c("blue", "green", "black", "red"), lty=1:4, cex=0.6)
### Q5
rm(list=ls())
```

```
library(dplyr)
library(purrr)
library(psych)
library(dummies)
##import buyer data
la buyer data<- read.table("buyer data la.txt", header = FALSE)</pre>
names(la buyer data) <-</pre>
c("buyer_id","price","violent_crime_rate","property_crime_rate","race","income")
la_buyer_data <- cbind(la_buyer_data, dummy(la_buyer_data$race, sep = "."))</pre>
names(la_buyer_data) <-</pre>
c("buyer id", "price", "violent crime rate", "property crime rate", "race", "income",
                         "Asian_pi", "black", "hispanic", "white")
## import price gradients results
price gradient <- readRDS("h1 price gradients.Rdata")</pre>
##allocate WMTP to each individual
la buyer data$violent crime rate[la buyer data$violent crime rate >= 2000]
<- 2000
la buyer data$MWTP <-</pre>
price_gradient_h1[as.integer(la_buyer_data$violent_crime_rate)]
MWTP estimation <- lm(MWTP~income+Asian pi+black+hispanic,
data=la buyer data)
summary(MWTP estimation)
###06
rm(list=ls())
#First step:boostrap
installation needed <- TRUE
loading needed <- TRUE</pre>
package list <- c('foreign', 'xtable', 'plm', 'gmm',</pre>
'AER', 'stargazer', 'readstata13', 'boot')
if(installation needed){install.packages(package list, repos='http://
cran.us.r-project.org')}
if(loading needed){lapply(package list, require, character.only = TRUE)}
library(boot)
library("dummies")
library(dplyr)
library(purrr)
library(psych)
################################
# data & model LA
la_data<- read.table("la_data.txt", header = FALSE)</pre>
names(la data) <-</pre>
c("houseid", "price", "county", "year built", "sq footage", "bathrooms", "bedrooms", "total rooms"
"vear of_sale")
la data <- cbind(la data, dummy(la data$county, sep = "."))</pre>
la data <- cbind(la data, dummy(la data$year of sale, sep = "."))</pre>
```

```
model la <- price ~ bathrooms + bedrooms + stories + property crime rate +
I(property_crime_rate^2) + year_built + I(year_built^2) + sq_footage +
I(sq_footage^2) + total_rooms + I(total_rooms^2)+ violent_crime_rate +
I(violent_crime_rate^2) + I(violent_crime_rate^3)+ I(violent_crime_rate^4)+
I(violent_crime_rate^5)+ I(violent_crime_rate^6) + bathrooms + la_data.1993
+ la_data.1994 + la_data.1995 + la_data.1996 + la_data.1997 + la_data.1998
+ la_data.2000 + la_data.2001 + la_data.2002 + la_data.2003 + la_data.2004
+ la_data.2005 + la_data.2006 + la_data.2007 + la_data.2008 + la_data.59 +
la data.65 + la data.71 + la data.111
# function to obtain regression weights
bs <- function(formula, data, indices) {</pre>
 d <- data[indices,] # allows boot to select sample</pre>
 fit <- lm(formula, data=d)</pre>
 return(coef(fit))
}
# bootstrapping with 500 replications
results <- boot(data=la_data, statistic=bs,
                R=500, formula=model_la)
results
result_bootcef_la <- cbind(results$t[,13],results$t[,14],results$t[,</pre>
15], results$t[,16], results$t[,17], results$t[,18])
write.csv(result_bootcef_la, file="q6_result_bootcef_la.csv")
capture.output(results, file = "results_boots_la.txt", append = TRUE)
#####################
# data & model_SF
sf_data<- read.table("sf_data.txt", header = FALSE)</pre>
names(sf_data) <-</pre>
c("houseid", "price", "county", "year_built", "sq_footage", "bathrooms", "bedrooms", "total_rooms",
"year_of_sale")
select(sf_data, sf_data$county==1|13|75|81|85)
sf_data <- cbind(sf_data, dummy(sf_data$county, sep = "."))</pre>
sf_data <- cbind(sf_data, dummy(sf_data$year_of_sale, sep = "."))</pre>
model_sf <- price ~ bathrooms + bedrooms + stories + property_crime_rate +</pre>
I(property_crime_rate^2) + year_built + I(year_built^2) + sq_footage +
I(sq_footage^2) + total_rooms + I(total_rooms^2) + violent_crime_rate +
I(violent_crime_rate^2) + I(violent_crime_rate^3)+ I(violent_crime_rate^4)+
I(violent_crime_rate^5)+ I(violent_crime_rate^6) + bathrooms + sf_data.1993
+ sf_data.1994 + sf_data.1995 + sf_data.1996 + sf_data.1997 + sf_data.1998
+ sf_data.2000 + sf_data.2001 + sf_data.2002 + sf_data.2003 + sf_data.2004
+ sf_data.2005 + sf_data.2006 + sf_data.2007 + sf_data.2008 + sf_data.13 +
sf_data.75 + sf_data.81 + sf_data.85
# bootstrapping with 500 replications
results_boot_sf <- boot(data=sf_data, statistic=bs,
                        R=500, formula=model_sf)
results boot sf
result_bootcef_sf <- cbind(results_boot_sf$t[,13],results_boot_sf$t[,</pre>
14],results_boot_sf$t[,15],results_boot_sf$t[,16],results_boot_sf$t[,
17], results boot sf$t[,18])
write.csv(result_bootcef_sf, file="q6_result_bootcef_sf.csv")
capture.output(results_boot_sf, file = "results_boots_sf.txt", append =
TRUE)
```

```
##Bishop Timmins
library(mlogit)
library(dplyr)
library(maxLik)
##buyers data
buyers data<- read.table("buyer data sf la.txt", header = FALSE)</pre>
names(buvers data) <-
c("buyerid", "price", "violent_crime_rate", "property_crime_rate", "race",
"income", "LA_indicator")
## boostrapped hedonic price gradients from Q5
la gradients <- read.csv("q6 result bootcef la.csv")</pre>
sf_gradients <- read.csv("q6_result_bootcef_sf.csv")</pre>
gradients la sf <- merge(la gradients,sf gradients, by="X")</pre>
rm(la_gradients,sf_gradients)
#####point estimation:
point_la <-lm(model_la, data=la data)</pre>
point gradient la <- point la$coefficients[13:18]</pre>
point_sf <- lm(model_sf, data=sf_data)</pre>
point_gradient_sf <- point_sf$coefficients[13:18]</pre>
point_gradient <- cbind(point_gradient_la, point_gradient_sf)</pre>
buyers data$implicit price <- (buyers data$LA indicator)*point gradient[1,1]+ (1-
buyers data$LA indicator)*point gradient[1,2]+
2*point gradient[2,1]*(buyers data$violent crime rate)*(buyers data$LA indicator) +
2*point_gradient[2,2]*(buyers_data$violent_crime_rate)*(1-buyers_data$LA_indicator)
3*point gradient[3,1]*(buyers data$violent crime rate^2)*(buyers data$LA indicator)
+ 3*point gradient[3,2]*(buyers data$violent crime rate^2)*(1-
buyers data$LA indicator)+
4*point gradient[4,1]*(buyers data$violent crime rate^3)*(buyers data$LA indicator)
+ 4*point_gradient[4,2]*(buyers_data$violent_crime_rate^3)*(1-
buyers data$LA indicator)+
5*point gradient[5,1]*(buyers data$violent crime rate^4)*(buyers data$LA indicator)
+ 5*point_gradient[5,2]*(buyers_data$violent_crime_rate^4)*(1-
buyers data$LA indicator)+
6*point_gradient[6,1]*(buyers_data$violent_crime_rate^5)*(buyers_data$LA_indicator)
+ 6*point gradient[6,2]*(buyers data$violent crime rate^5)*(1-
buyers data$LA indicator)
```

```
buyers data$df implict price <- 2*point gradient[2,1]*(buyers data$LA indicator) +
2*point gradient[2,2]*(1-buyers data$LA indicator)+
6*point gradient[3,1]*(buyers data$violent crime rate)*(buyers data$LA indicator) +
6*point_gradient[3,2]*(buyers_data$violent_crime_rate)*(1-buyers_data$LA_indicator)+
12*point gradient[4,1]*(buyers data$violent crime rate^2)*(buyers data$LA indicator)
+ 12*point gradient[4,2]*(buyers data$violent crime rate^2)*(1-
buvers data$LA indicator)+
20*point_gradient[5,1]*(buyers_data$violent_crime_rate^3)*(buyers_data$LA_indicator)
+ 20*point gradient[5,2]*(buyers data$violent crime rate^3)*(1-
buyers data$LA indicator)+
30*point_gradient[6,1]*(buyers_data$violent_crime_rate^4)*(buyers_data$LA_indicator)
+ 30*point gradient[6,2]*(buyers data$violent crime rate^4)*(1-
buyers data$LA indicator)
##create dummies for race
buyers data <- cbind(buyers data, dummy(buyers data$race, sep = "."))</pre>
#generate mle function
mle = function(theta, x) {
   # theta parameter vector; x
   mu1 = theta[1]
   mu2 = theta[2]
   mu3 = theta[3]
   mu4 = theta[4]
   mu5 = theta[5]
   mu6 = theta[6]
   #x[,14]:vij
   x[, 14] < x[, 8] - mu1 - mu2*x[, 3] - mu3*x[, 6] - mu4*x[, 10] - mu5*x[, 11] - mu6*x[, 10] - mu6*x
   sigma <- sd(x[,14])
   x[, 15] < (1/(sigma*sqrt(2*pi)))*exp(-(1/(2*(sigma^2)))*(x[,
14]^2) \times abs((x[,9]-mu2))
   x \leftarrow subset(x, x[,15] > 0) ###We need to drop 0 value!!!!! fairly
important for mle method to work
   ans \leftarrow sum(log(x[,15]))
   return(ans)
#use ols to try the start point
try <- lm(implicit price~ violent crime rate + income + buyers data.2 +
buyers_data.3 + buyers_data.4, data=buyers_data)
theta.start = c(-200, 0.169, 0, 0, 0, 0)
names(theta.start) = c("mu1", "mu2", "mu3", "mu4", "mu5", "mu6")
#theta.mle = maxLik (mle, start=theta.start, x=buyers data, method =
"BFGS") ###the problem here is that mle could be very sensitive about the
start point
theta.mle = optim(par=theta.start, fn=mle, x=buyers_data, method ="BFGS")
######################assign df(implicit price) of crime for each
individual *500
buyers data<- read.table("buyer data sf la.txt", header = FALSE)</pre>
```

```
names(buyers data) <-</pre>
c("buyerid", "price", "violent_crime_rate", "property_crime_rate", "race",
"income", "LA indicator")
for( i in 1:500){
  buyers data[paste("implict price", i, sep= "")] <-</pre>
(buyers data$LA indicator)*gradients la sf[i,2]+ (1-
buyers data$LA indicator)*gradients la sf[i,8]+ 2*gradients la sf[i,
3]*(buyers data$violent crime rate)*(buyers data$LA indicator) +
2*gradients la sf[i,9]*(buyers data$violent crime rate)*(1-
buyers_data$LA_indicator)+ 3*gradients_la_sf[i,
4]*(buyers_data$violent_crime_rate^2)*(buyers_data$LA_indicator) +
3*gradients la sf[i,10]*(buyers data$violent crime rate^2)*(1-
buyers_data$LA_indicator)+ 4*gradients_la_sf[i,
4]*(buyers data$violent crime rate^3)*(buyers data$LA indicator) +
4*gradients_la_sf[i,11]*(buyers_data$violent_crime_rate^3)*(1-
buyers data$LA indicator)+ 5*gradients la sf[i,
6]*(buyers data$violent crime rate^4)*(buyers data$LA indicator) +
5*gradients la sf[i,12]*(buyers data$violent crime rate^4)*(1-
buyers data$LA indicator)+ 6*gradients la sf[i,
7]*(buyers data$violent crime rate^5)*(buyers data$LA indicator) +
6*gradients_la_sf[i,13]*(buyers_data$violent_crime_rate^5)*(1-
buyers_data$LA_indicator)
}
######################assign df(implicit price) of crime for each
individual *500
for( i in 1:500){
  buyers_data[paste("df_implict_price", i, sep= "")] <-</pre>
2*gradients_la_sf[i,3]*(buyers_data$LA_indicator) + 2*gradients_la_sf[i,
9]*(1-buyers data$LA indicator)+ 6*gradients la sf[i,
4]*(buyers data$violent crime rate)*(buyers data$LA indicator) +
6*gradients la sf[i,10]*(buyers data$violent crime rate)*(1-
buyers_data$LA_indicator)+ 12*gradients_la_sf[i,
4]*(buyers_data$violent_crime_rate^2)*(buyers_data$LA_indicator) +
12*gradients la sf[i,11]*(buyers data$violent crime rate^2)*(1-
buyers_data$LA_indicator)+ 20*gradients_la_sf[i,
6]*(buyers data$violent crime rate^3)*(buyers data$LA indicator) +
20*gradients_la_sf[i,12]*(buyers_data$violent_crime_rate^3)*(1-
buyers data$LA indicator)+ 30*gradients la sf[i,
7]*(buyers data$violent crime rate^4)*(buyers data$LA indicator) +
30*gradients la sf[i,13]*(buyers data$violent crime rate^4)*(1-
buyers data$LA indicator)
#####################run second stage regression $ save coefficients *500
##create dummies for race
buyers_data <- cbind(buyers_data, dummy(buyers_data$race, sep = "."))</pre>
theta.start <-c(-1.939636e+02, 4.428857e-01, 9.380051e+05,
9.751060e-01, 2.879410e-01, 1.159335e+00)
names(theta.start) = c("mu1", "mu2", "mu3", "mu4", "mu5", "mu6")
intercept <- c()</pre>
violent crime <- c()</pre>
income <- c()
asian_pi <-c()
black <- c()
```

```
hispanic <- c()
for (i in 1:500){
  sample <- buyers_data[, c(1:7,7+i,507+i,1008:1011)]</pre>
  theta.mle = optim(par=theta.start, fn=mle, x=sample, method ="BFGS")
  intercept[i] <- theta.mle$par[1]</pre>
  violent_crime[i] <- theta.mle$par[2]</pre>
  income[i] <- theta.mle$par[3]</pre>
  asian_pi[i] <- theta.mle$par[4]</pre>
  black[i] <- theta.mle$par[5]</pre>
  hispanic[i] <- theta.mle$par[6]</pre>
}
###drop outlier before summarizing boostrap results
install.packages("outliers")
library(outliers)
boxplot(income)
violent_crime <- rm.outlier(violent_crime)</pre>
violent_crime <- rm.outlier(violent_crime)</pre>
mean(violent_crime)
sd(violent_crime)
```

```
install.packages("mlogit")
install.packages("dplyr")
library(mlogit)
library(dplyr)
setwd("/Volumes/USB30FD/821 ps")
#####data upload and prepare
data <- read.csv("long_data.csv")</pre>
data \leftarrow data[-c(1)]
names(data)[names(data) == "idcase"] <- "id"</pre>
data <- mlogit.data(data, choice = "choice",</pre>
                     shape = "long", alt.levels = (c(1:100)), id ="id")
#Q2.i:try the simple model first
model_1 <- mlogit (choice ~ ramp + restroom + walleye + salmon</pre>
                    + panfish + travelcost | 0, data)
summary(model_1)
#Q2.ii: preference heterogenerity r.t. person specific variables
data$panfish kids <- data$panfish * data$kids
data$restroom kids <- data$restroom * data$kids</pre>
data$ramp_boat <- data$ramp * data$boat</pre>
data$walleye_boat <- data$walleye * data$boat</pre>
#write.csv(data, file="data forloop.csv")
model 2 <- mlogit (choice ~ ramp + restroom + walleye + salmon + panfish
                    + travelcost + panfish_kids + restroom_kids
                    + ramp_boat + walleye_boat | 0, data)
summary(model 2)
#Q2.iii: include an unobserved site attribute
library(mlogit)
library(dplyr)
library(maxLik)
setwd("/Volumes/USB30FD/821 ps")
data <-read.csv("data_forloop.csv")</pre>
data \leftarrow data[-c(1)]
data$alt id <-as.numeric(as.character(data$alt id))</pre>
data$id <-as.numeric(as.character(data$id))</pre>
##small loop
delta = 1e-07 #tolerancel level for first loop to stop
a \leftarrow c(-0.1030564, -0.1632874, 0.3442013, 0.9818902, 0.6961032)
theta_1 <- replicate(100,0)
theta_2 <- replicate(100,0)</pre>
data$theta j = 0
data$choice <- ifelse(data$choice == "FALSE", 0, 1)</pre>
#function that produce the prediction of share S j for all j
maxlikelihood <- c(2000000000)
b < -c(0)
##
repeat{
  data$Prob ij nominator <- exp(0 + a[1]*data$travelcost
+a[2]*data$panfish_kids + a[3]*data$restroom_kids+a[4]*data$ramp_boat +
a[5]*data$walleye_boat)
```

```
data <- data %>%
    group by(id) %>%
    mutate(Prob_ij_denom = sum(Prob_ij_nominator))%>%
    ungroup()
  data$Prob ij <- data$Prob ij nominator / data$Prob ij denom
  data <- data %>%
    group_by(alt_id) %>%
    mutate(share_j = mean(Prob_ij))%>%
    ungroup()
  share <- data$share j[1:100]</pre>
  real share <- data$shares[1:100]</pre>
  for (j in 1:100) {
    theta_2[j] <- theta_1[j] + log(real_share[j]) - log(share[j])</pre>
  theta_diff <- theta_2 - theta_1</pre>
  while (max(abs(theta diff))>delta){
    theta_1 <- theta_2 #update new thetas</pre>
    data$theta_j <- theta_1[data$alt_id]</pre>
    data <- data %>%
      mutate(Prob ij nominator = exp(data$theta j + a[1]*data$travelcost
+a[2]*data$panfish_kids + a[3]*data$restroom_kids+a[4]*data$ramp_boat +
a[5]*data$walleye_boat))%>%
      group by(id) %>%
      mutate(Prob_ij_denom = sum(Prob_ij_nominator))%>%
    data$Prob_ij <- data$Prob_ij_nominator / data$Prob_ij_denom</pre>
    data <- data %>%
      group_by(alt_id) %>%
      mutate(share_j = mean(Prob_ij)) %>%
      ungroup()
    share <- data$share j[1:100]
    for (j in 1:100) {
      theta_2[j] <- theta_1[j] + log(real_share[j]) - log(share[j])</pre>
    theta_diff <- theta_2 - theta_1
    #print(theta 2)
  # theta_2 now is the optimised baseline utility for the specific "a"
parameter set.
  # level normalization: substract the mean
  level norm <- function (x) {</pre>
    scale(x, scale = FALSE)
  }
```

```
baseline util <- level norm(theta 2)</pre>
  ##update the new theta_j to the dataframe
  data$theta_j <- baseline_util[data$alt_id]</pre>
  #x6<- replicate(2404, baseline_util)</pre>
  ## calculate likelihood function based on the baseline utility and
parameter set
  #changed here!!!! be careful
  data <- data %>%
    mutate(Prob ij nominator = exp(data$theta j + a[1]*data$travelcost
+a[2]*data$panfish_kids + a[3]*data$restroom_kids+a[4]*data$ramp_boat +
a[5]*data$walleye boat))%>%
    group_by(id) %>%
    mutate(Prob_ij_denom = sum(Prob_ij_nominator))%>%
    ungroup()
  data$Prob ij <- data$Prob ij nominator / data$Prob ij denom
  data$Prob sitechoice <- log(data$Prob ij^data$choice)</pre>
  LogL_attributes <- data$Prob_sitechoice</pre>
  llmax <- sum(LogL_attributes)</pre>
  maxlikelihood[-llmax < maxlikelihood] <- llmax</pre>
  ## update parameter set by conducting the maximisation loglikelihood
  #compute loglikelood function x1, x2, x3, x4, x5, x6
  ####################################
  loglike = function(theta, x) {
    # theta parameter vector; x
    mu1 = theta[1]
    mu2 = theta[2]
    mu3 = theta[3]
    mu4 = theta[4]
    mu5 = theta[5]
    x[, 20] \leftarrow exp(x[, 19] + mu1*x[, 8] + mu2*x[, 15] + mu3*x[, 16] + mu4*x[, 16]
17] + mu5*x[, 18])
    x1 \leftarrow as.vector(unlist(x[,20]))
    x2 \leftarrow unname(tapply(x1, (seq along(x1)-1) %/% 100, sum))
    x[, 21] \leftarrow cbind(rep(x2, each=100))
    x[, 22] \leftarrow x[, 20] / x[, 21]
    x[, 24] < -x[, 22]^x[, 3]
    ans = sum(log(x[, 24]))
    return(ans)
  }
  theta.start = a
  names(theta.start) = c("mu1", "mu2", "mu3", "mu4", "mu5")
  theta.mle = maxLik (loglike, start=theta.start, x=data, method = "BFGS")
  #theta.mle = optim(par=theta.start, fn=loglike, x=data, method ="BFGS")
  summarv(theta.mle)
  summary(theta.mle$coef)
```

```
# write an additional loop for the first stage to converge
 # print(theta.mle$estimate)
 print(theta.mle$maximum)
 a[theta.mle$maximum > maxlikelihood] <- theta.mle$estimate
 b[round(theta.mle$maximum, 3) == round(maxlikelihood, 3)] <- 1</pre>
 maxlikelihood[round(theta.mle$maximum, 3) > round(maxlikelihood, 3)] <-</pre>
theta.mle$maximum
 print(a)
 if(b > 0){
   break
 }
}
names(a) <- c("travelcost", "panfish_kids", "restroom_kids", "ramp_boat",</pre>
"walleye boat")
print (maxlikelihood)
print(a)
###BLP second stage
BLP2 <- lm(theta j \sim ramp + restroom + walleye + salmon + panfish + 0,
data=data)
summary(BLP2)
#clean the global environment for the new question and upload package and
settings we need
rm(list=ls())
library(mlogit)
library(dplyr)
library(maxLik)
setwd("C:/821 ps")
data <-read.csv("data_forloop.csv")</pre>
data \leftarrow data[-c(1)]
data$alt id <-as.numeric(as.character(data$alt id))</pre>
data$id <-as.numeric(as.character(data$id))</pre>
##small loop
delta = 1e-07 #tolerancel level for first loop to stop
theta_1 <- replicate(100,0)</pre>
theta_2 <- replicate(100,0)
data$theta j = 0
data$choice <- ifelse(data$choice == "FALSE", 0, 1)</pre>
#function that produce the prediction of share S_j for all j
\max likelihood <- c(2000000000)
b < -c(0)
a \leftarrow c(-0.1230331, -0.1408312, 0.5068775, 1.3974301, 0.5928853, 1) ##1
is the initial parameter setting for normal distribution of random
##add a random component in preferences for walleye
```

```
## and we also take the parameter set from Q2.iii for the initial guess.
The initial guess for delta_j is still zero for all j
## generate random value rnorm(2404, mean=0, sd=a[6])
repeat{
  random \leftarrow rnorm(2404, mean=0, sd=a[5])
  data$random <- rep(random, each=100)</pre>
  data$Prob ij nominator <- exp(0 + a[1]*data$travelcost
+a[2]*data$panfish_kids + a[3]*data$restroom_kids+a[4]*data$ramp_boat +
a[5]*data$walleye_boat + data$random*data$walleye)
  data <- data %>%
    group by(id) %>%
    mutate(Prob ij denom = sum(Prob ij nominator))%>%
    ungroup()
  data$Prob ij <- data$Prob ij nominator / data$Prob ij denom
  data <- data %>%
    group by(alt id) %>%
    mutate(share_j = mean(Prob_ij))%>%
    ungroup()
  share <- data$share j[1:100]</pre>
  real share <- data$shares[1:100]</pre>
  for (j in 1:100) {
    theta 2[j] <- theta 1[j] + log(real share[j]) - log(share[j])
  }
  theta_diff <- theta_2 - theta_1
  while (max(abs(theta_diff))>delta){
    theta 1 <- theta 2 #update new thetas
    data$theta_j <- theta_1[data$alt_id]</pre>
    data <- data %>%
      mutate(Prob ij nominator = exp(data$theta j + a[1]*data$travelcost
+a[2]*data$panfish kids + a[3]*data$restroom kids+a[4]*data$ramp boat +
a[5]*data$walleye_boat + data$random*data$walleye))%>%
      group by(id) %>%
      mutate(Prob_ij_denom = sum(Prob_ij_nominator))%>%
      ungroup()
    data$Prob ij <- data$Prob ij nominator / data$Prob ij denom
    data <- data %>%
      group by(alt id) %>%
      mutate(share_j = mean(Prob_ij)) %>%
      ungroup()
    share <- data$share j[1:100]</pre>
    for (j in 1:100) {
      theta_2[j] <- theta_1[j] + log(real_share[j]) - log(share[j])</pre>
    theta_diff <- theta_2 - theta_1</pre>
```

```
print(theta 2)
  # theta_2 now is the optimised baseline utility for the specific "a"
parameter set.
  # level normalization: substract the mean
  level norm <- function (x) {</pre>
    scale(x, scale = FALSE)
  }
  baseline_util <- level_norm(theta_2)</pre>
  ##update the new theta j to the dataframe
  data$theta_j <- baseline_util[data$alt_id]</pre>
  #x6<- replicate(2404, baseline_util)</pre>
  ## calculate likelihood function based on the baseline utility and
parameter set
  data <- data %>%
    mutate(Prob_ij_nominator = exp(data$theta_j + a[1]*data$travelcost
+a[2]*data$panfish_kids + a[3]*data$restroom_kids+a[4]*data$ramp_boat +
a[5]*data$walleye boat + data$random*data$walleye))%>%
    group by(id) %>%
    mutate(Prob_ij_denom = sum(Prob_ij_nominator))%>%
    ungroup()
  data$Prob_ij <- data$Prob_ij_nominator / data$Prob_ij_denom</pre>
  data$Prob sitechoice <- log(data$Prob ij^data$choice)</pre>
  LogL_attributes <- data$Prob_sitechoice</pre>
  llmax <- sum(LogL attributes)</pre>
  maxlikelihood[-llmax < maxlikelihood] <- llmax</pre>
  ## update parameter set by conducting the maximisation loglikelihood
  #compute loglikelood function x1, x2, x3, x4, x5, x6
  ######################################
  loglike = function(theta, x) {
    # theta parameter vector; x
    mu1 = theta[1]
    mu2 = theta[2]
    mu3 = theta[3]
    mu4 = theta[4]
    mu5 = theta[5]
    x[, 21] \leftarrow exp(x[, 19] + mu1*x[, 8] + mu2*x[, 15] + mu3*x[, 16] + mu4*x[, 16]
17] + mu5*x[, 18] + x[,20]*x[,11])
    x1 <- as.vector(unlist(x[,21]))</pre>
    x2 \leftarrow unname(tapply(x1,(seq_along(x1)-1) %/% 100, sum))
    x[, 22] \leftarrow cbind(rep(x2, each=100))
    x[, 23] \leftarrow x[, 21] / x[, 22]
    x[, 25] < -x[, 23]^x[, 3]
    ans = sum(log(x[, 25]))
    return(ans)
```

```
}
  theta.start = a
  names(theta.start) = c("mu1", "mu2", "mu3", "mu4", "mu5", "sigma")
  theta.mle = maxLik (loglike, start=theta.start, x=data, method = "BFGS")
  #theta.mle = optim(par=theta.start, fn=loglike, x=data, method ="BFGS")
  summarv(theta.mle)
  summary(theta.mle$coef)
  # write an additional loop for the first stage to converge
  # print(theta.mle$estimate)
  print(theta.mle$maximum)
  a[theta.mle$maximum > maxlikelihood] <- theta.mle$estimate
  a[6] <- sd(data$random)
  b[round(theta.mle$maximum, 3) == round(maxlikelihood, 3)] <- 1</pre>
  maxlikelihood[theta.mle$maximum > maxlikelihood] <- theta.mle$maximum</pre>
  print(a)
  if(b > 0){}
    break
  }
}
print(a)
print (llmax)
print(theta.mle$estimate)
###BLP second stage
BLP2 <- lm(theta j \sim ramp + restroom + walleye + salmon + panfish + 0,
data=data)
summary(BLP2)
#############Q3
library(mlogit)
library(dplvr)
library(maxLik)
setwd("/Volumes/USB30FD/821 ps")
#####data upload and prepare
data <- read.csv("long_data.csv")</pre>
data <- data[-c(1)]
names(data)[names(data) == "idcase"] <- "id"</pre>
data <- mlogit.data(data, choice = "choice",</pre>
                    shape = "long", alt.levels = (c(1:100)), id ="id")
data$shares <- data$shares*100
names(data)[names(data) == "shares"] <- "shares 100"</pre>
#Q3.1i:try the simple model first
model_1 <- mlogit (choice ~ ramp + restroom + walleye + salmon</pre>
                   + panfish + travelcost + shares_100 | 0, data)
```

```
summary(model 1)
#Q3.1ii: preference heterogenerity r.t. person_specific variables
data$panfish_kids <- data$panfish * data$kids</pre>
data$restroom kids <- data$restroom * data$kids</pre>
data$ramp boat <- data$ramp * data$boat</pre>
data$walleye boat <- data$walleye * data$boat</pre>
model_2 <- mlogit (choice ~ ramp + restroom + walleye + salmon + panfish</pre>
                    + travelcost + panfish_kids + restroom_kids
                    + ramp boat + walleye boat + shares 100 | 0, data)
summary(model 2)
#Q3.1iii: BLP
data$alt id <-as.numeric(as.character(data$alt id))</pre>
data$id <-as.numeric(as.character(data$id))</pre>
##small loop
delta = 1e-07 #tolerancel level for first loop to stop
a \leftarrow c(0, 0, 0, 0, 0)
theta 1 <- replicate(100,0)
theta 2 \leftarrow replicate(100,0)
data$theta j = 0
data$choice <- ifelse(data$choice == "FALSE", 0, 1)</pre>
#function that produce the prediction of share S j for all j
maxlikelihood <- c(2000000000)
b < -c(0)
##
repeat{
  data$Prob_ij_nominator <- exp(0 + a[1]*data$travelcost</pre>
+a[2]*data$panfish kids + a[3]*data$restroom kids+a[4]*data$ramp boat +
a[5]*data$walleye_boat)
  data <- data %>%
    group by(id) %>%
    mutate(Prob ij denom = sum(Prob ij nominator))%>%
    ungroup()
  data$Prob_ij <- data$Prob_ij_nominator / data$Prob_ij_denom</pre>
  data <- data %>%
    group_by(alt_id) %>%
    mutate(share j = mean(Prob ij)*100)%>%
    ungroup()
  share <- data$share_j[1:100]</pre>
  real share <- data$shares 100[1:100]</pre>
  for (j in 1:100) {
    theta_2[j] <- theta_1[j] + log(real_share[j]) - log(share[j])</pre>
```

```
theta_diff <- theta_2 - theta_1</pre>
  while (max(abs(theta diff))>delta){
    theta 1 <- theta 2 #update new thetas
    data$theta_j <- theta_1[data$alt_id]</pre>
    data <- data %>%
      mutate(Prob_ij_nominator = exp(data$theta_j + a[1]*data$travelcost
+a[2]*data$panfish_kids + a[3]*data$restroom_kids+a[4]*data$ramp_boat +
a[5]*data$walleye boat))%>%
      group by(id) %>%
      mutate(Prob ij denom = sum(Prob ij nominator))%>%
      ungroup()
    data$Prob_ij <- data$Prob_ij_nominator / data$Prob_ij_denom</pre>
    data <- data %>%
      group by(alt id) %>%
      mutate(share_j = mean(Prob_ij)*100) %>%
      ungroup()
    share <- data$share_j[1:100]</pre>
    for (j in 1:100) {
      theta_2[j] <- theta_1[j] + log(real_share[j]) - log(share[j])</pre>
    theta diff <- theta 2 - theta 1
    #print(theta_2)
  }
  # theta 2 now is the optimised baseline utility for the specific "a"
parameter set.
  # level normalization: substract the mean
  level norm <- function (x) {</pre>
    scale(x, scale = FALSE)
  }
  baseline util <- level norm(theta 2)</pre>
  ##update the new theta_j to the dataframe
  data$theta_j <- baseline_util[data$alt_id]</pre>
  #x6<- replicate(2404, baseline util)</pre>
  ## calculate likelihood function based on the baseline_utility and
parameter set
  #changed here!!!! be careful
  data <- data %>%
    mutate(Prob ij nominator = exp(data$theta j + a[1]*data$travelcost
+a[2]*data$panfish_kids + a[3]*data$restroom_kids+a[4]*data$ramp_boat +
a[5]*data$walleye boat))%>%
    group by(id) %>%
    mutate(Prob ij denom = sum(Prob ij nominator))%>%
  data$Prob_ij <- data$Prob_ij_nominator / data$Prob_ij_denom
```

```
data$Prob sitechoice <- log(data$Prob ij^data$choice)</pre>
  LogL attributes <- data$Prob sitechoice</pre>
  llmax <- sum(LogL attributes)</pre>
  maxlikelihood[-llmax < maxlikelihood] <- llmax</pre>
  ## update parameter set by conducting the maximisation loglikelihood
  #compute loglikelood function x1, x2, x3, x4, x5, x6
  loglike = function(theta, x) {
    # theta parameter vector; x
    mu1 = theta[1]
    mu2 = theta[2]
    mu3 = theta[3]
    mu4 = theta[4]
    mu5 = theta[5]
    x[, 20] \leftarrow exp(x[, 19] + mu1*x[, 8] + mu2*x[, 15] + mu3*x[, 16] + mu4*x[, 16]
17] + mu5*x[, 18])
    x1 <- as.vector(unlist(x[,20]))</pre>
    x2 \leftarrow unname(tapply(x1,(seq_along(x1)-1) \%/\% 100, sum))
    x[, 21] \leftarrow cbind(rep(x2, each=100))
    x[, 22] \leftarrow x[, 20] / x[, 21]
    x[, 24] < -x[, 22]^x[, 3]
    ans = sum(log(x[, 24]))
    return(ans)
  }
  theta.start = a
  names(theta.start) = c("mu1", "mu2", "mu3", "mu4", "mu5")
  theta.mle = maxLik (loglike, start=theta.start, x=data, method = "BFGS")
  #theta.mle = optim(par=theta.start, fn=loglike, x=data, method ="BFGS")
  summary(theta.mle)
  summary(theta.mle$coef)
  # write an additional loop for the first stage to converge
  # print(theta.mle$estimate)
  print(theta.mle$maximum)
  a[theta.mle$maximum > maxlikelihood] <- theta.mle$estimate</pre>
  b[round(theta.mle$maximum, 3) == round(maxlikelihood, 3)] <- 1</pre>
  maxlikelihood[round(theta.mle$maximum, 3) > round(maxlikelihood, 3)] <-</pre>
theta.mle$maximum
  print(a)
  if(b > 0){
    break
}
names(a) <- c("travelcost", "panfish kids", "restroom kids", "ramp boat",</pre>
"walleye boat")
print(a)
print (maxlikelihood)
print(theta.mle$estimate)
```

```
##> print(a)
##[1] -0.1230306 -0. 1408963 0.5048161 1.3881009 0.5524893
##> print (maxlikelihood)
##[1] -5136.971
##> print(theta.mle$estimate)
                                  mu4
##-0.1230306 -0.1408963 0.5048161 1.3881009 0.5524893
###BLP second stage
##
BLP2 <- lm(theta j ~ ramp + restroom + walleye + salmon + panfish +
shares 100 + 0, data=data)
summary(BLP2)
#Q3.2
library(quantreg)
library(gmm)
###arange data frame
data_iv <- data[1:100 ,]</pre>
data_iv <- subset(data_iv, select=c("ramp", "restroom",</pre>
"walleye", "salmon", "panfish", "shares_100", "theta_j"))
##########generate instruments
###median regression
rqfit <- rq(theta_j ~ ramp + restroom + walleye + salmon + panfish +
shares_100, data=data_iv)
coef <-rqfit$coefficients</pre>
###calculate shares as one of instruments
data$Prob ij nominator <- exp(coef[1] + coef[2]*data$ramp +</pre>
coef[3]*data$restroom + coef[4]*data$walleye + coef[5]*data$salmon +
coef[6]*data$panfish + a[1]*data$travelcost +a[2]*data$panfish_kids +
a[3]*data$restroom_kids+a[4]*data$ramp_boat + a[5]*data$walleye_boat)
data <- data %>%
 group by(id) %>%
 mutate(Prob_ij_denom = sum(Prob_ij_nominator))%>%
 ungroup()
data$Prob ij <- data$Prob ij nominator / data$Prob ij denom
data <- data %>%
 group_by(alt_id) %>%
 mutate(share_j = mean(Prob_ij))%>%
 ungroup()
data_iv <- data[1:100 ,]
data iv <- subset(data iv, select=c("ramp", "restroom",
"walleye", "salmon", "panfish", "shares_100", "theta_j", "share_j"))
data_iv$share_j <- data_iv$share_j*100</pre>
####quantile IV GMM
##generate condition function
g1 \leftarrow function (tet, x){
 #tet <- parameter set
 #x <- data_iv dataframe</pre>
```

```
#Sn <- 0.25, same as the setting of orginal paper
  # intercept from median regression <- -0.1190958
  m1 \leftarrow (pnorm((x[,7] + 0.1190958 - tet[1]*x[,1] - tet[2]*x[,2] -
tet[3]*x[,3] - tet[4]*x[,4] - tet[5]*x[,5] - tet[6]*x[,8])/0.25) - 0.5
  return(m1)
}
####other method: "inverse" quantile estimation
install.packages("remotes")
remotes::install_github("yuchang0321/IVQR")
library(IVQR)
fit <- ivqr(theta_j~ shares_100 | share_j | ramp + restroom + walleye +</pre>
salmon + panfish, 0.5, grid= seq(-4.5, 0, 0.05625), data = data iv)
####Other Method: 2sls
#0LS
ols<- lm(theta j ~ ramp + restroom + walleye + salmon + panfish +
shares 100 + 0, data=data iv)
coef <-ols$coefficients</pre>
#predict shares of visiting as instrument, based on exogenous things only
data$Prob_ij_nominator <- exp( coef[1]*data$ramp + coef[2]*data$restroom +</pre>
coef[3]*data$walleye + coef[4]*data$salmon + coef[5]*data$panfish +
a[1]*data$travelcost +a[2]*data$panfish kids +
a[3]*data$restroom kids+a[4]*data$ramp boat + a[5]*data$walleye boat)
data <- data %>%
  group by(id) %>%
  mutate(Prob ij denom = sum(Prob ij nominator))%>%
  ungroup()
data$Prob_ij <- data$Prob_ij_nominator / data$Prob_ij_denom</pre>
data <- data %>%
  group by(alt id) %>%
  mutate(share_j = mean(Prob_ij))%>%
  ungroup()
data iv <- data[1:100 ,]</pre>
data iv <- subset(data iv, select=c("ramp", "restroom",</pre>
"walleye","salmon","panfish","shares_100","theta_j","share_j"))
data_iv$share_j <- data_iv$share_j*100</pre>
#2SLS
library(ivpack)
twosls <- ivreg(data iv$theta j~ data iv$shares 100 + data iv$ramp +
data iv$restroom +data iv$walleye +data iv$salmon + data iv$panfish |
data iv$share j + data iv$ramp + data iv$restroom +data iv$walleye
+data_iv$salmon + data_iv$panfish
beta <- c(-3.7598, -0.3720, -0.4888, 8.1968, 20.3990, 1.2842) ##from Q3_2
names(beta) <- c("shares_100" , "ramp", "restroom", "walleye", "salmon",</pre>
"panfish")
data_iv$unobserved <- data_iv$theta_j - beta[1]*data_iv$shares_100 -</pre>
beta[2]*data_iv$ramp - beta[3]*data_iv$restroom -beta[4]*data_iv$walleye -
beta[5]*data_iv$salmon - beta[6]*data_iv$panfish
```

```
##data preparation for Q4
unobserved <- data iv$unobserved</pre>
data <- read.csv("long data.csv")</pre>
data \leftarrow data[-c(1)]
names(data)[names(data) == "idcase"] <- "id"</pre>
data <- mlogit.data(data, choice = "choice",</pre>
                     shape = "long", alt.levels = (c(1:100)), id ="id")
data$shares <- data$shares*100
names(data)[names(data) == "shares"] <- "shares 100"</pre>
data$panfish kids <- data$panfish * data$kids</pre>
data$restroom kids <- data$restroom * data$kids</pre>
data$ramp boat <- data$ramp * data$boat</pre>
data$walleye boat <- data$walleye * data$boat</pre>
data$alt id <-as.numeric(as.character(data$alt id))</pre>
data$id <-as.numeric(as.character(data$id))</pre>
data$unobserved <- cbind(rep( unobserved, 2404))
write.csv(data, file = "data_for_welfare_analysis.csv")
###### Welfare Analysis
##data
library(dplyr)
setwd("C:/821 ps")
data <- read.csv("data_for_welfare_analysis.csv")</pre>
data \leftarrow data[-c(1)]
data$id <-as.numeric(as.character(data$id))</pre>
##generate utility calculation function
beta <-c(-3.7598, -0.3720, -0.4888, 8.1968, 20.3990, 1.2842) ##from Q3 2
names(beta) <- c("shares_100" , "ramp", "restroom", "walleye", "salmon",</pre>
"panfish")
alpha <- c(-0.1230306, -0.1408963, 0.5048161, 1.3881009, 0.5524893)
names(alpha) <- c("travelcost", "panfish kids", "restroom kids",</pre>
"ramp_boat", "walleye_boat")
U <- function(beta, alpha, x) {
  ans \leftarrow beta[1]*x[,14] + beta[2]*x[,9] + beta[3]*x[,10]+ beta[4]*x[,11] +
beta[5]*x[,12] + beta[6]*x[,13] + alpha[1]*x[,8] + alpha[2]*x[,15] +
alpha[3]*x[,16] + alpha[4]*x[,17] + alpha[5]*x[,18]+ x[,19]
  return(ans)
############### Partial equilibrium
data$old_utility <- U(beta, alpha, data)</pre>
write.csv(data, file="data welfare.csv")
### scenario A
data$walleye <- data$walleye*1.3
data$walleye_boat <-data$walleye*data$boat</pre>
data$new_utility <- U(beta, alpha, data)</pre>
data$old utility <- exp(data$old utility)</pre>
data$new_utility <- exp(data$new_utility)</pre>
new_utility <- data$new_utility</pre>
```

```
sum new <- unname(tapply(new utility,(seq along(new utility)-1) \%/% 100,
sum))
data$sum new <- cbind(rep(sum new, each =100))</pre>
data$sum_new <- log(data$sum_new)</pre>
old utility <- data$old utility
sum old <- unname(tapply(old utility,(seg along(old utility)-1) %/% 100,
sum))
data$sum_old <- cbind(rep(sum_old, each =100))</pre>
data$sum_old <- log(data$sum_old)</pre>
data$CV <- (1/0.123131)*(data$sum_new-data$sum_old)</pre>
mean(data$CV) ### 5.217842
### scenario B
data <- read.csv("data_welfare.csv")</pre>
data \leftarrow data[-c(1)]
data$change <- ifelse(data$shares 100 >1.5, 1.3, 1)
data$walleye <- data$walleye*data$change
data$walleye boat <-data$walleye*data$boat
data$new_utility <- U(beta, alpha, data)</pre>
data$old_utility <- exp(data$old_utility)</pre>
data$new utility <- exp(data$new utility)</pre>
new utility <- data$new utility
sum new <- unname(tapply(new utility,(seg along(new utility)-1) %/% 100,</pre>
data$sum new <- cbind(rep(sum new, each =100))</pre>
data$sum_new <- log(data$sum_new)</pre>
old_utility <- data$old_utility</pre>
sum old <- unname(tapply(old utility,(seg along(old utility)-1) %/% 100,
sum))
data$sum old <- cbind(rep(sum old, each =100))</pre>
data$sum_old <- log(data$sum_old)</pre>
data$CV \leftarrow (1/0.123131)*(data$sum new-data$sum old)
mean affected <- data$CV[which(data$change == 1.3 & data$choice =="TRUE") ]</pre>
%>% mean() ###5.09357
mean unaffected <- mean(data$CV[which(data$change == 1.0 & data$choice
=="TRUE") ]) %>% mean() ###2.993604
### scenario C
data <- read.csv("data welfare.csv")</pre>
data \leftarrow data[-c(1)]
data <- data[which(data$shares_100 <= 1.5),] ##now we have 82 sites
data$new utility <- U(beta, alpha, data)
data$old_utility <- exp(data$old_utility)</pre>
data$new_utility <- exp(data$new_utility)</pre>
```

```
new utility <- data$new utility</pre>
sum new <- unname(tapply(new utility,(seg along(new utility)-1) %/% 82,
sum))
data$sum_new <- cbind(rep(sum_new, each =82))</pre>
data$sum new <- log(data$sum new)</pre>
old utility <- data$old utility
sum_old <- unname(tapply(old_utility,(seq_along(old_utility)-1) %/% 82,</pre>
sum))
data$sum_old <- cbind(rep(sum_old, each =82))</pre>
data$sum old <- log(data$sum old)</pre>
data$CV \leftarrow (1/0.123131)*(data$sum new-data$sum old)
mean_unaffected_by_removal <- data$CV[which(data$choice =="TRUE") ] %>%
mean() ###9.157485e-17
### scenario D
data <- read.csv("data welfare.csv")</pre>
data \leftarrow data[-c(1)]
data$change <- ifelse(data$shares_100 >1.5, 10, 0)
data$travelcost <- data$travelcost+data$change</pre>
data$new_utility <- U(beta, alpha, data)</pre>
data$old_utility <- exp(data$old_utility)</pre>
data$new_utility <- exp(data$new_utility)</pre>
new utilitv <- data$new utilitv</pre>
sum_new <- unname(tapply(new_utility,(seq_along(new_utility)-1) %/% 100,</pre>
sum))
data$sum_new <- cbind(rep(sum_new, each =100))</pre>
data$sum_new <- log(data$sum_new)</pre>
old utility <- data$old utility
sum old <- unname(tapply(old utility,(seg along(old utility)-1) %/% 100,
sum))
data$sum_old <- cbind(rep(sum_old, each =100))</pre>
data$sum old <- log(data$sum old)</pre>
data$CV \leftarrow (1/0.123131)*(data$sum new-data$sum old)
mean_affected <- data$CV[which(data$change == 10 & data$choice =="TRUE") ]</pre>
%>% mean() ###-4.563843
mean_unaffected <- mean(data$CV[which(data$change == 0 & data$choice
=="TRUE") ]) %>% mean() ###-2.341332
########################### general equilibrium <- resorting
### scenario A
data <- read.csv("data_welfare.csv")</pre>
data \leftarrow data[-c(1)]
data$walleye <- data$walleye*1.3
data$walleye_boat <-data$walleye*data$boat</pre>
```

```
#stimulate new choice set
data$nominator <- exp(U(beta, alpha, data))</pre>
nominator <- data$nominator
denominator <- unname(tapply(nominator,(seq_along(nominator)-1) %/% 100,
data$denomitor <- cbind(rep(denominator, each =100))</pre>
data$pii <- data$nominator/data$denomitor</pre>
data<-arrange(data, data$alt id)</pre>
pij <- data$pij</pre>
pij_mean <- unname(tapply(pij,(seq_along(pij)-1) %/% 2404, sum))</pre>
data$shares_new <- cbind(rep(pij_mean, each =2404))</pre>
data<-arrange(data, data$id)</pre>
##calculate new utility
U GE <- function(beta, alpha, x) {
  ans \leftarrow beta[1]*x[,24] + beta[2]*x[,9] + beta[3]*x[,10]+ beta[4]*x[,11] +
beta[5]*x[,12] + beta[6]*x[,13] + alpha[1]*x[,8] + alpha[2]*x[,15] +
alpha[3]*x[,16] + alpha[4]*x[,17] + alpha[5]*x[,18]+ x[,19]
  return(ans)
data$new_utility <- U_GE(beta, alpha, data)</pre>
data$old_utility <- exp(data$old_utility)</pre>
data$new utility <- exp(data$new utility)</pre>
new utility <- data$new utility
sum_new <- unname(tapply(new_utility,(seq_along(new_utility)-1) %/% 100,</pre>
sum))
data$sum new <- cbind(rep(sum new, each =100))</pre>
data$sum new <- log(data$sum new)</pre>
old utility <- data$old utility
sum_old <- unname(tapply(old_utility,(seq_along(old_utility)-1) %/% 100,</pre>
sum))
data$sum old <- cbind(rep(sum old, each =100))</pre>
data$sum_old <- log(data$sum_old)</pre>
data$CV <- (1/0.123131)*(data$sum_new-data$sum_old)</pre>
mean(data\$CV) ### -147.337
### scenario B
data <- read.csv("data welfare.csv")</pre>
data \leftarrow data[-c(1)]
data$change <- ifelse(data$shares_100 >1.5, 1.3, 1)
data$walleye <- data$walleye*data$change</pre>
data$walleye_boat <-data$walleye*data$boat</pre>
#stimulate new choice set
data$nominator <- exp(U(beta, alpha, data))</pre>
nominator <- data$nominator</pre>
denominator <- unname(tapply(nominator,(seq_along(nominator)-1) %/% 100,
data$denomitor <- cbind(rep(denominator, each =100))</pre>
data$pij <- data$nominator/data$denomitor</pre>
data<-arrange(data, data$alt id)</pre>
pij <- data$pij</pre>
```

```
pij mean <- unname(tapply(pij,(seg along(pij)-1) %/% 2404, sum))</pre>
data$shares_new <- cbind(rep(pij_mean, each =2404))</pre>
data<-arrange(data, data$id)</pre>
##calculate new utility
U_GE <- function(beta, alpha, x) {</pre>
  ans \leftarrow beta[1]*x[,25] + beta[2]*x[,9] + beta[3]*x[,10]+ beta[4]*x[,11] +
beta[5]*x[,12] + beta[6]*x[,13] + alpha[1]*x[,8] + alpha[2]*x[,15] +
alpha[3]*x[,16] + alpha[4]*x[,17] + alpha[5]*x[,18]+ x[,19]
  return(ans)
data$new_utility <- U_GE(beta, alpha, data)</pre>
data$old_utility <- exp(data$old_utility)</pre>
data$new utility <- exp(data$new utility)
new utility <- data$new utility
sum new <- unname(tapply(new utility,(seg along(new utility)-1) %/% 100,
sum))
data$sum_new <- cbind(rep(sum_new, each =100))</pre>
data$sum_new <- log(data$sum_new)</pre>
old_utility <- data$old_utility</pre>
sum old <- unname(tapply(old utility,(seg along(old utility)-1) %/% 100,
sum))
data$sum old <- cbind(rep(sum old, each =100))</pre>
data$sum_old <- log(data$sum_old)</pre>
data$CV \leftarrow (1/0.123131)*(data$sum new-data$sum old)
## update actual choice
data <- arrange(data, id)</pre>
new utility <- c(data$new utility)</pre>
data$new_utility <- new_utility
data<- arrange(data, id, desc(data$new_utility))</pre>
data$new choice = "FALSE"
for (i in 0:2403 ){
  data$new choice[(100*i+1)] <- "TRUE"
}
mean affected <- data$CV[which(data$change == 1.3 & data$new choice
=="TRUE") ] %>% mean() ###NaN, suggesting no person change to the place
when walleye increased in the crowded place.
mean unaffected <- mean(data$CV[which(data$change == 1.0 & data$new choice
=="TRUE") ]) %>% mean() ###-144.6079
###Scenerio C
data <- read.csv("data welfare.csv")</pre>
data \leftarrow data[-c(1)]
data <- data[which(data$shares_100 <= 1.5),] ##now we have 82 sites</pre>
#stimulate new choice set
data$nominator <- exp(U(beta, alpha, data))</pre>
nominator <- data$nominator</pre>
denominator <- unname(tapply(nominator,(seq along(nominator)-1) %/% 82,
sum))
data$denomitor <- cbind(rep(denominator, each =82))</pre>
```

```
data$pij <- data$nominator/data$denomitor</pre>
data<-arrange(data, data$alt id)</pre>
pij <- data$pij
pij_mean <- unname(tapply(pij,(seq_along(pij)-1) %/% 2404, sum))</pre>
data$shares_new <- cbind(rep(pij_mean, each =2404))</pre>
data<-arrange(data, data$id)</pre>
##calculate new utility
U_GE <- function(beta, alpha, x) {</pre>
  ans \leftarrow beta[1]*x[,24] + beta[2]*x[,9] + beta[3]*x[,10]+ beta[4]*x[,11] +
beta[5]*x[,12] + beta[6]*x[,13] + alpha[1]*x[,8] + alpha[2]*x[,15] +
alpha[3]*x[,16] + alpha[4]*x[,17] + alpha[5]*x[,18] + x[,19]
  return(ans)
data$new_utility <- U_GE(beta, alpha, data)</pre>
data$old_utility <- exp(data$old_utility)</pre>
data$new utility <- exp(data$new utility)</pre>
new utility <- data$new utility
sum_new <- unname(tapply(new_utility,(seq_along(new_utility)-1) %/% 82,</pre>
sum))
data$sum_new <- cbind(rep(sum_new, each =82))</pre>
data$sum new <- log(data$sum new)</pre>
old utility <- data$old utility
sum_old <- unname(tapply(old_utility,(seq_along(old_utility)-1) %/% 82,</pre>
sum))
data$sum old <- cbind(rep(sum old, each =82))</pre>
data$sum old <- log(data$sum old)</pre>
 data$CV <- (1/0.123131)*(data\$sum\_new-data\$sum\_old) 
mean unaffected by removal <- data$CV[which(data$choice =="TRUE") ] %>%
mean() ###-350.9764
### scenario D
data <- read.csv("data welfare.csv")</pre>
data \leftarrow data[-c(1)]
data$change <- ifelse(data$shares 100 >1.5, 10, 0)
data$travelcost <- data$travelcost+data$change</pre>
#stimulate new choice set
data$nominator <- exp(U(beta, alpha, data))</pre>
nominator <- data$nominator</pre>
denominator <- unname(tapply(nominator,(seq_along(nominator)-1) %/% 100,
sum))
data$denomitor <- cbind(rep(denominator, each =100))
data$pij <- data$nominator/data$denomitor</pre>
data<-arrange(data, data$alt id)</pre>
pij <- data$pij</pre>
pij_mean <- unname(tapply(pij,(seq_along(pij)-1) %/% 2404, sum))</pre>
data$shares new <- cbind(rep(pij mean, each =2404))</pre>
data<-arrange(data, data$id)</pre>
##calculate new utility
U_GE <- function(beta, alpha, x) {</pre>
```

```
ans \leftarrow beta[1]*x[,25] + beta[2]*x[,9] + beta[3]*x[,10]+ beta[4]*x[,11] +
beta[5]*x[,12] + beta[6]*x[,13] + alpha[1]*x[,8] + alpha[2]*x[,15] +
alpha[3]*x[,16] + alpha[4]*x[,17] + alpha[5]*x[,18]+ x[,19]
  return(ans)
data$new utility <- U GE(beta, alpha, data)</pre>
data$old utility <- exp(data$old utility)</pre>
data$new_utility <- exp(data$new_utility)</pre>
new_utility <- data$new_utility</pre>
sum new <- unname(tapply(new utility,(seg along(new utility)-1) %/% 100,</pre>
sum))
data$sum new <- cbind(rep(sum new, each =100))</pre>
data$sum_new <- log(data$sum_new)</pre>
old utility <- data$old utility
sum old <- unname(tapply(old utility,(seq along(old utility)-1) %/% 100,
sum))
data$sum_old <- cbind(rep(sum_old, each =100))</pre>
data$sum_old <- log(data$sum_old)</pre>
data$CV <- (1/0.123131)*(data$sum_new-data$sum_old)</pre>
## update actual choice
data <- arrange(data, id)</pre>
new utility <- c(data$new utility)</pre>
data$new_utility <- new_utility</pre>
data<- arrange(data, id, desc(data$new_utility))</pre>
data$new choice = "FALSE"
for (i in 0:2403){
  data$new choice[(100*i+1)] <- "TRUE"
mean_affected <- data$CV[which(data$change == 10 & data$new_choice
=="TRUE") ] %>% mean() ###NaN
mean unaffected <- mean(data$CV[which(data$change == 0 & data$new choice
=="TRUE") ]) %>% mean() ###-345.9996
```