

# Towards Energy Efficient Federated Meta-learning in Edge Network

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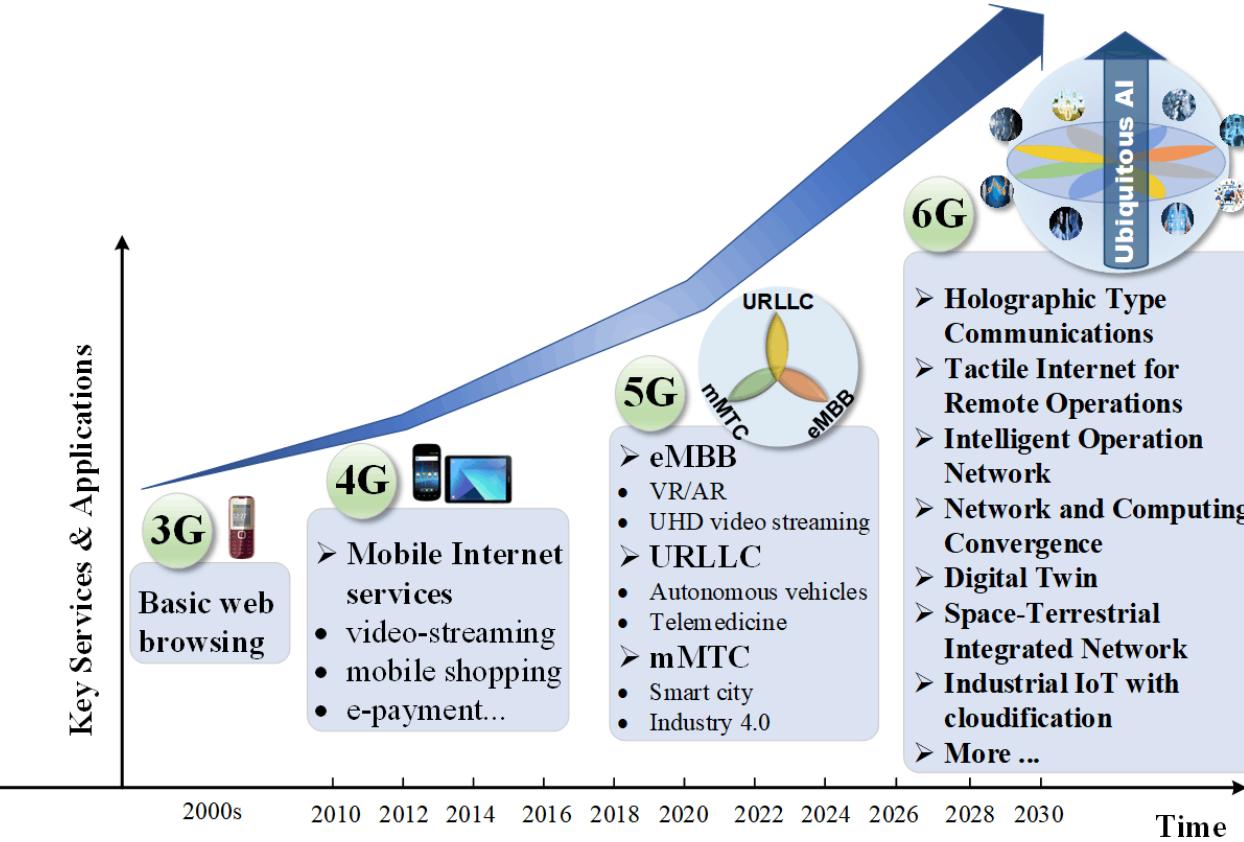


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# Outline

- **Background and Motivation**
- **System Model and Problem Formulation**
- **Analytical Solutions**
- **Experiments and Simulation Results**
- **Conclusions**

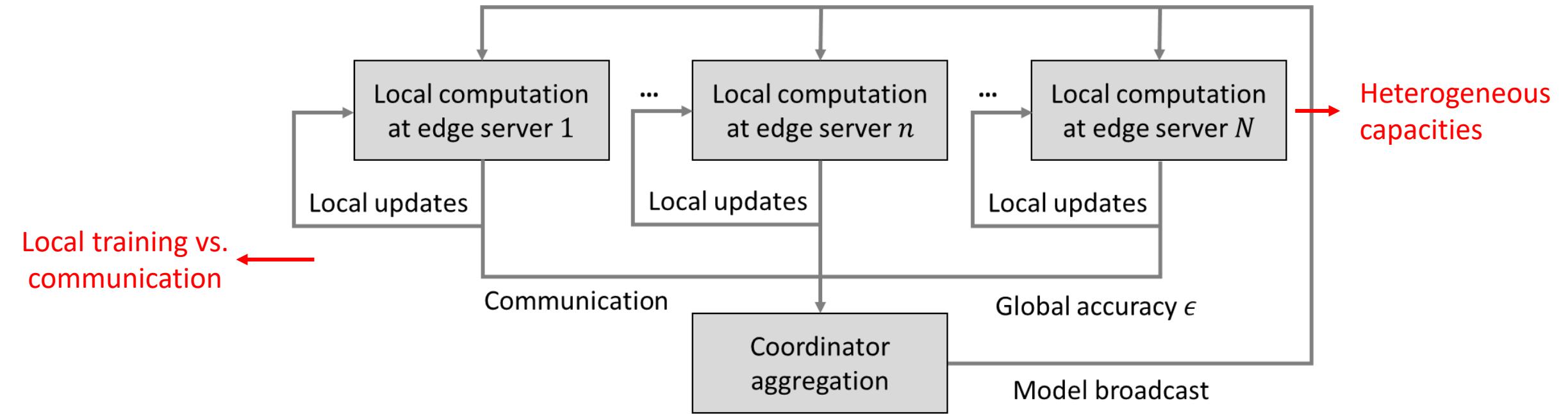
# Background



- More and more network access
- Progressively increasing computing power at the edge of the network
- Growing need for privacy

- 6G takes AI as the core driving force
- Federated Edge Intelligence(FEI) is a candidate technology for network AI in 6G

# Motivation



## Challenges for FEI System

- Heterogeneous storage, communication, and computation capacities
- Multiple rounds of model training and model coordination
- Lack of a simple and comprehensive framework

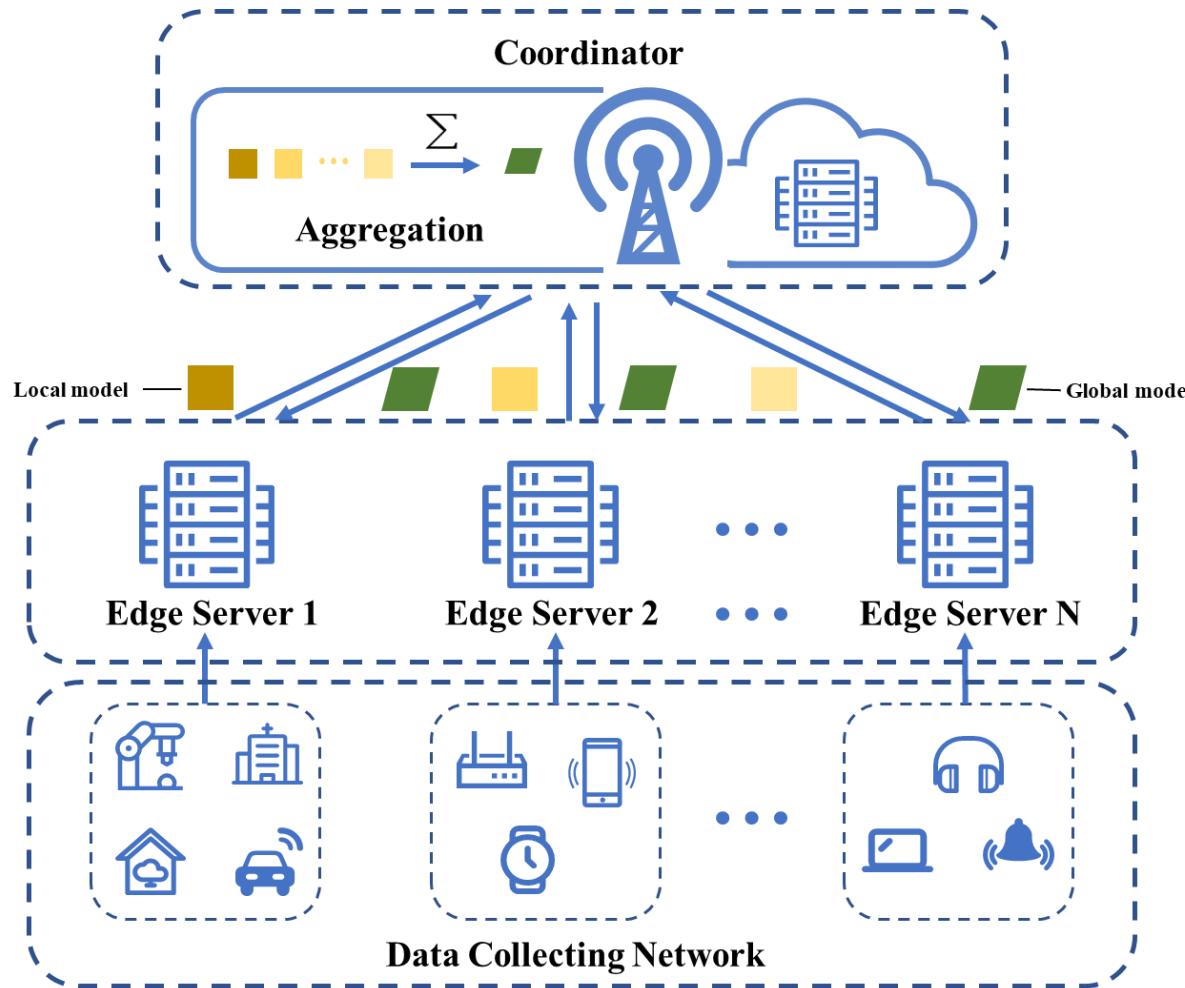
# Key Contributions

- ✓ Propose an energy consumption model
- ✓ Derive the analytical solutions for the energy consumption of FEI networks with two popular distributed algorithms, FedAvg and FedMeta
- ✓ Develop a hardware prototype and conduct extensive measurements on real-world dataset

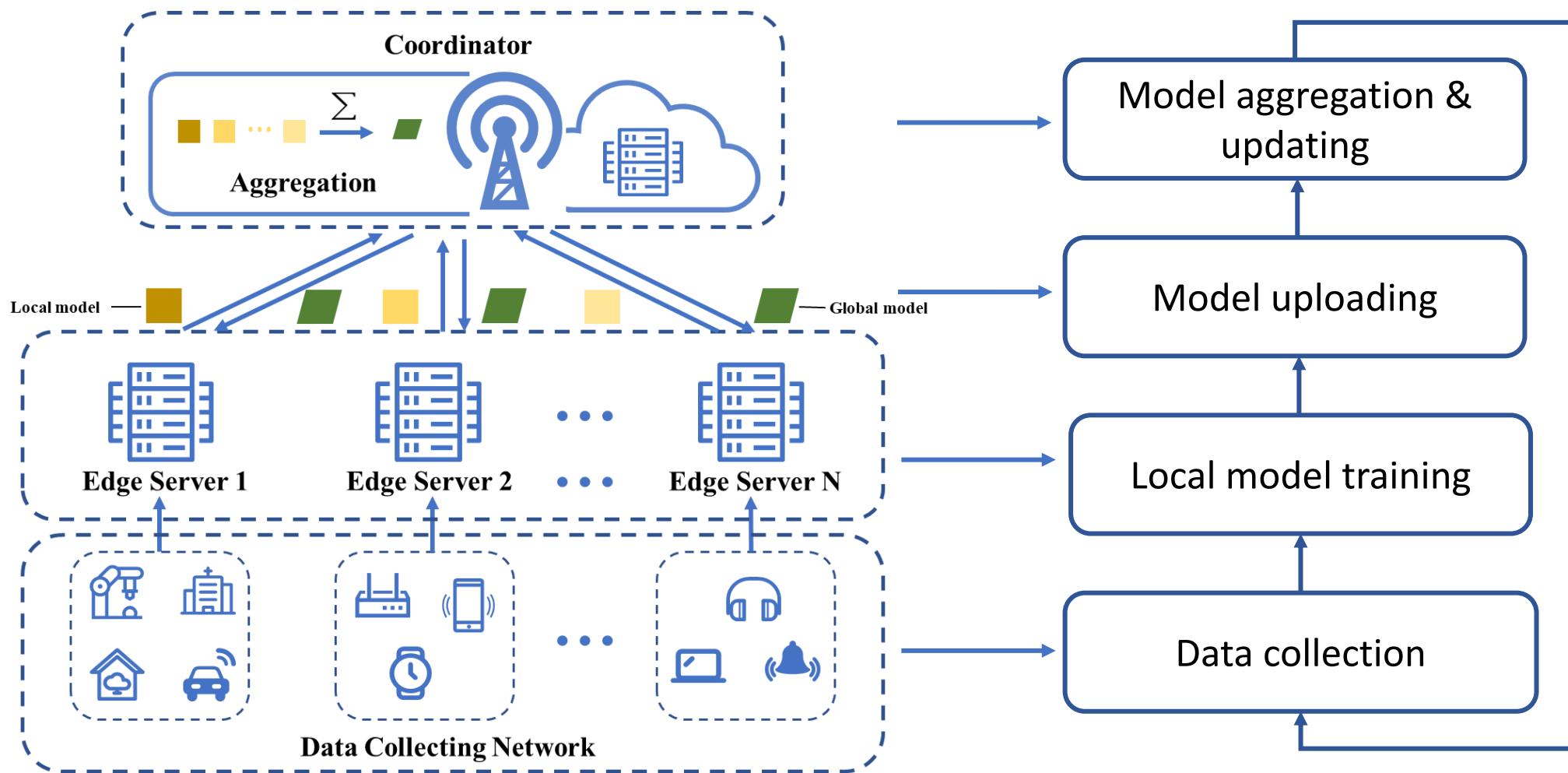
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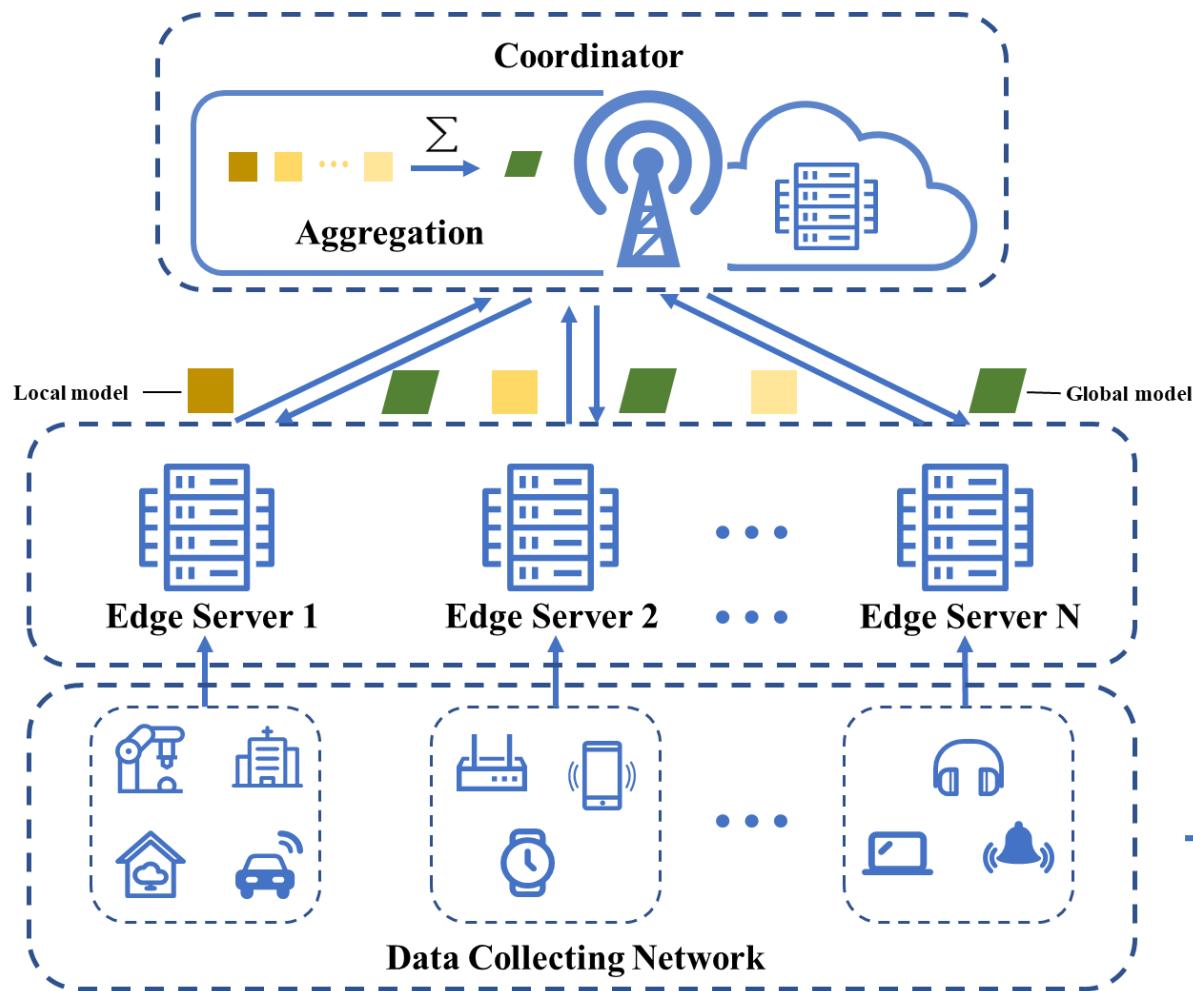
# System Model



# System Model



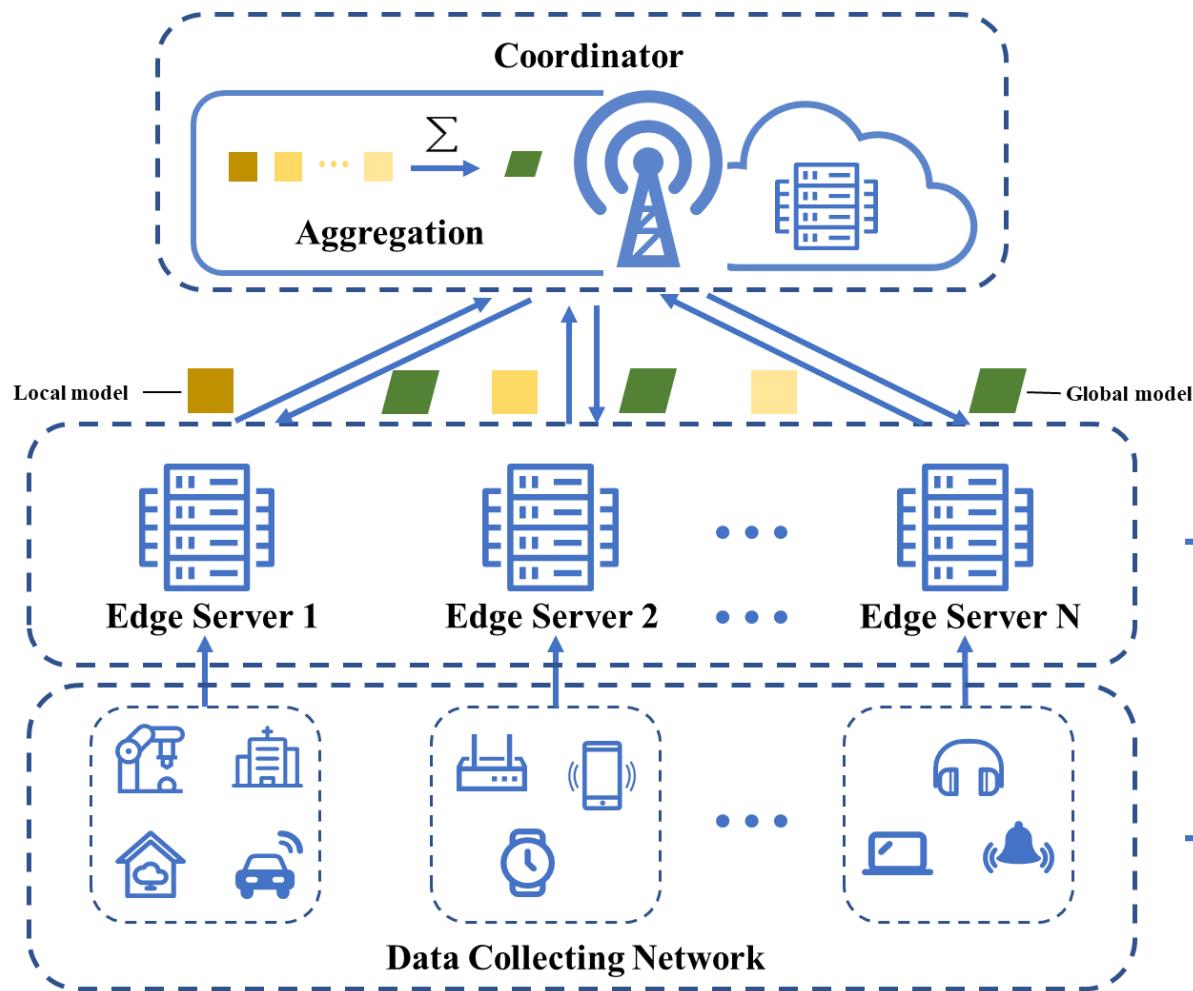
# Problem Formulation



**Energy consumption of data collection:**  
 $E_n^{dc}(K) = \eta K$

*K*: the required number of data samples

# Problem Formulation

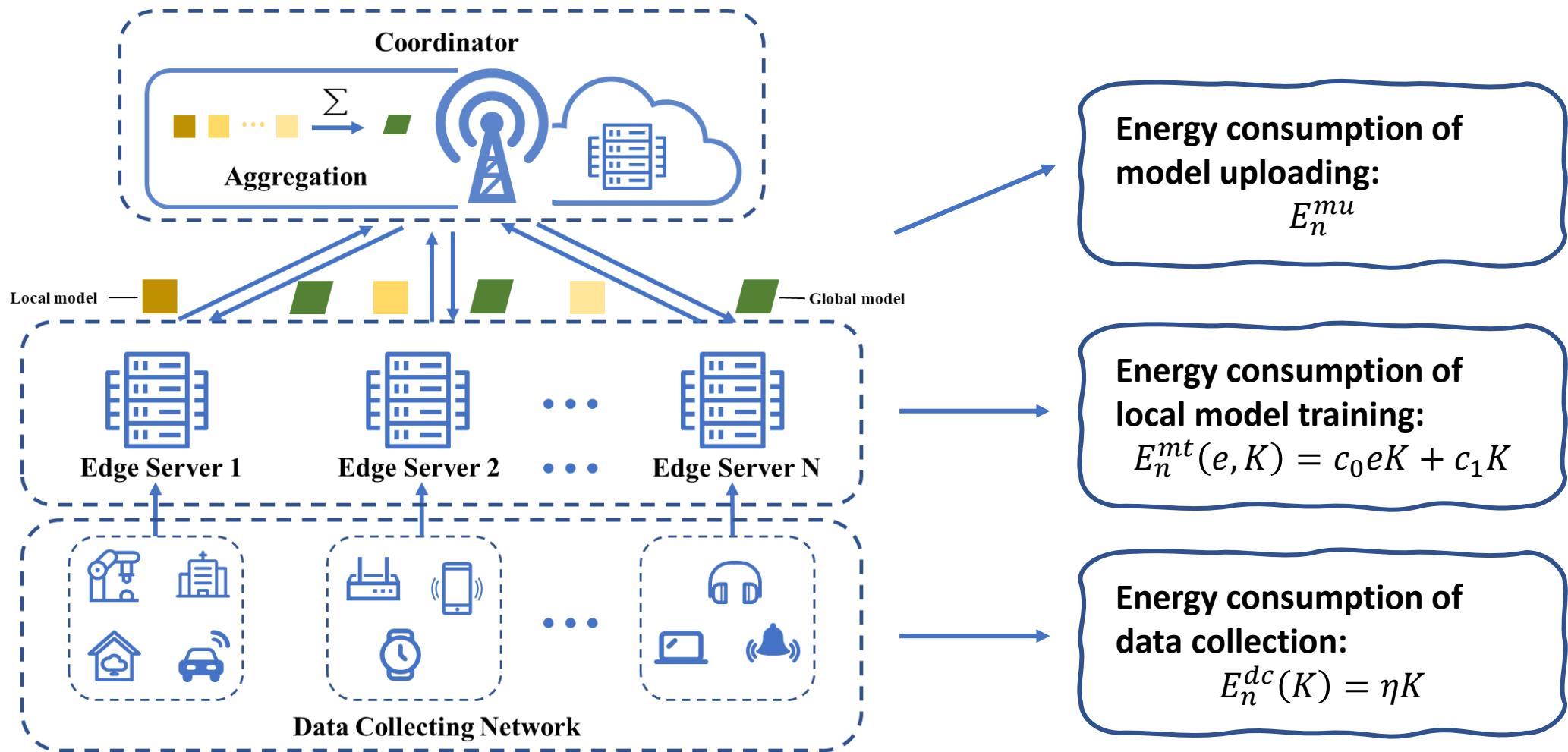


**Energy consumption of local model training:**  
 $E_n^{mt}(e, K) = c_0 e K + c_1 K$

**Energy consumption of data collection:**  
 $E_n^{dc}(K) = \eta K$

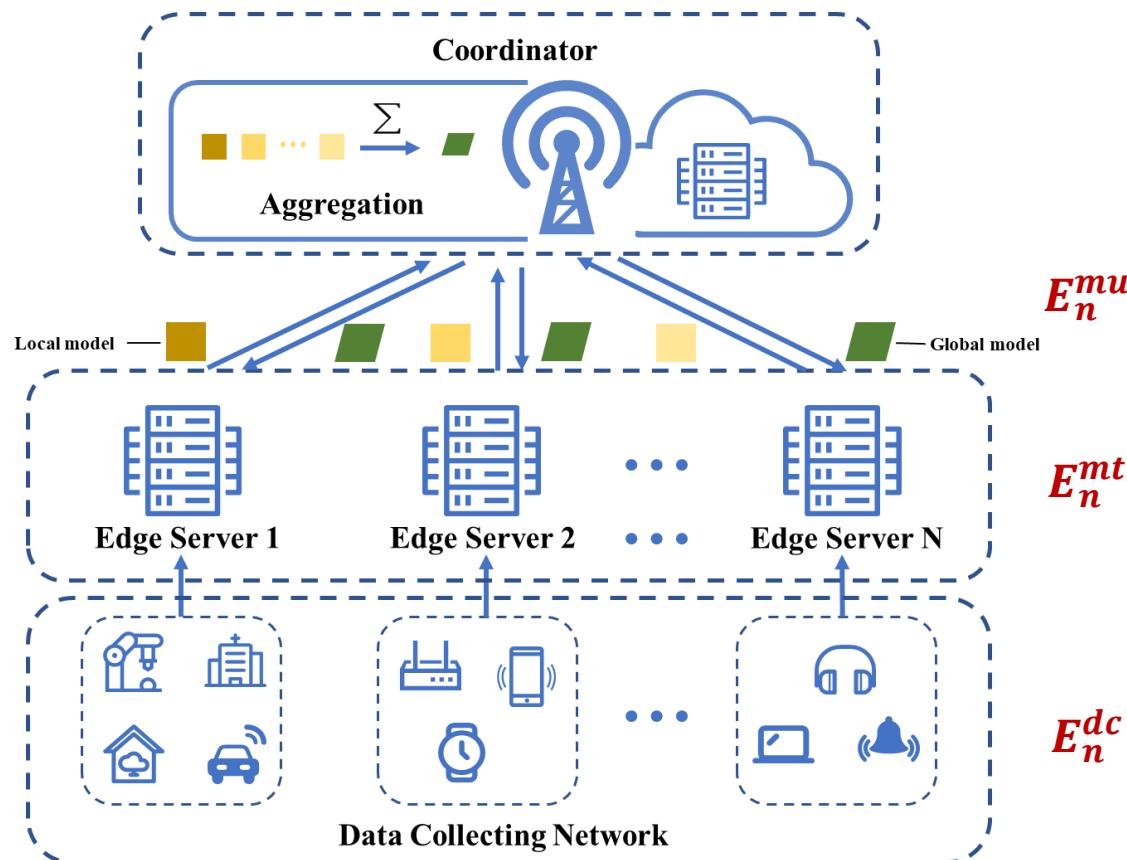
$K$ : the required number of data samples  
 $e$ : the steps of local training

# Problem Formulation



$K$ : the required number of data samples  
 $e$ : the steps of local training

# Problem Formulation



**Overall energy consumption** of FEI system

$$E(K, T) = \sum_{t=1}^T \sum_{n \in \mathcal{N}} (E_n^{dc} + E_n^{mt} + E_n^{mu})$$

**Energy minimization problem** of FEI system

$$\min_{K, T} [E(K, T)]$$

$$\text{s. t. } \frac{1}{eT} \sum_{t=0}^{T-1} \sum_{\tau=0}^{e-1} \mathbb{E}[\|\nabla \mathcal{R}(\bar{w}_{t+1}^\tau)\|^2] \leq \epsilon$$

$$\text{where } \bar{w}_{t+1}^\tau = \frac{1}{N} \sum_{n \in \mathcal{N}} w_{n,t+1}^\tau.$$

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# Training Procedure

- Objective function of FedAvg

$$\mathcal{R}_n(w_t) = f_n(w_t, \mathcal{S}_n)$$

- Objective function of FedMeta

$$\mathcal{R}_n(w_t) = f_n\left(w_t - \alpha \nabla f_n(w_t, \mathcal{S}_n^{in}), \mathcal{S}_n^{out}\right)$$

Step size

$$f_n(w, \mathcal{S}_n) = \frac{1}{|\mathcal{S}_n|} \sum_{x \in \mathcal{S}_n} \ell_n(w; x)$$

[1] M. Brendan, M. Edier, H. Seth, et al, "Communication-efficient learning of deep networks from decentralized data," in AISTATS, Florida, Apr., 2017.

[2] A. Fallah, A. Mokhtari, and A. Ozdaglar, "Personalized federated learning with theoretical guarantees: A model-agnostic meta-learning approach," in NeurIPS, Virtual, Dec. 2020.

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Step size

$$f_n(w, \mathcal{S}_n) = \frac{1}{|\mathcal{S}_n|} \sum_{x \in \mathcal{S}_n} \ell_n(w; x)$$



Local update

$$w_{n,t+1}^\tau = w_{n,t+1}^{\tau-1} - \beta \nabla \mathcal{R}_n(w_{n,t+1}^{\tau-1})$$

Local learning rate

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# Energy Consumption

## FedAvg

Convergence constraint

$$\frac{1}{eT} \sum_{t=0}^{T-1} \sum_{\tau=0}^{e-1} \mathbb{E}[\|\nabla \mathcal{R}(\bar{w}_{t+1}^\tau)\|^2] \leq \frac{A_1}{T} + \frac{A_2}{K} + A_3$$



Under a given accuracy

$$\frac{A_1}{T} + \frac{A_2}{K} + A_3 \leq \epsilon$$



The optimal  $T^*$

$$T_{Avg}^* = \frac{KA_1}{K\epsilon - A_2 - KA_3}$$



The optimal overall energy consumption

$$\mathbb{E}[\hat{E}(K)] = \frac{KA_1}{K\epsilon - A_2 - KA_3} N(B_0 K + B_1)$$

## FedMeta

Convergence constraint

$$\frac{1}{eT} \sum_{t=0}^{T-1} \sum_{\tau=0}^{e-1} \mathbb{E}[\|\nabla \mathcal{R}(\bar{w}_{t+1}^\tau)\|^2] \leq \frac{C_1}{T} + \frac{C_2}{K} + C_3$$



Under a given accuracy

$$\frac{C_1}{T} + \frac{C_2}{K} + C_3 \leq \epsilon$$



The optimal  $T^*$

$$T_{Meta}^* = \frac{KC_1}{K\epsilon - C_2 - KC_3}$$



The optimal overall energy consumption

$$\mathbb{E}[\hat{E}(K)] = \frac{KC_1}{K\epsilon - C_2 - KC_3} N(2B_0 K + B_1)$$

# Energy Consumption

The optimal overall energy consumption

$$\mathbb{E}[\hat{E}(K)] = \frac{KA_1}{K\epsilon - A_2 - KA_3} N(B_0K + B_1)$$

$$B_0 = \mathbb{E}[c_0]e$$
$$B_1 = \mathbb{E}[\eta]K + \mathbb{E}[c_1]e + \mathbb{E}[E_n^{mu}]$$

The optimal overall energy consumption

$$\mathbb{E}[\hat{E}(K)] = \frac{KC_1}{K\epsilon - C_2 - KC_3} N(2B_0K + B_1)$$

➤ **Note1:**

Objective function of FedAvg:

$$\mathcal{R}_n(w_t) = f_n(w_t, \mathcal{S}_n)$$

Objective function of FedMeta:

$$\mathcal{R}_n(w_t) = f_n(w_t - \alpha \nabla f_n(w_t, \mathcal{S}_n^{in}), \mathcal{S}_n^{out})$$

➤ **Remark1:** Within a single communication round,

Energy consumption: **FedMeta > FedAvg**

The number of data samples:

**FedMeta > FedAvg**

To perform the same  
number of local updates

More local computation

# Energy Consumption

The optimal overall energy consumption

$$\mathbb{E}[\hat{E}(K)] = \frac{KA_1}{K\epsilon - A_2 - KA_3} N(B_0K + B_1)$$

$\downarrow$

$$T_{Avg}^* \quad B_0 = \mathbb{E}[c_0]e$$
$$B_1 = \mathbb{E}[\eta]K + \mathbb{E}[c_1]e + \mathbb{E}[E_n^{mu}]$$

The optimal overall energy consumption

$$\mathbb{E}[\hat{E}(K)] = \frac{KC_1}{K\epsilon - C_2 - KC_3} N(2B_0K + B_1)$$

$\downarrow$

$$T_{Meta}^*$$

➤ **Note2:**

By setting the number of local updates as  $e = \mathcal{O}(\epsilon^{-1/2})$ ,  
the number of samples as  $K = \mathcal{O}(\epsilon^{-1})$ ,  
the stepsize as  $\beta = \mathcal{O}(\epsilon)$ .

To achieve an  $\mathcal{O}(\epsilon)$ -  
first-order stationary  
point of  $\mathcal{R}$

FedAvg:  $T = \mathcal{O}(\epsilon^{-4})$  rounds  
FedMeta:  $T = \mathcal{O}(\epsilon^{-2})$  rounds

➤ **Remark1:** Within a single communication round,

Energy consumption: **FedMeta > FedAvg**

➤ **Remark2:** To achieve a satisfactory model,

Communication rounds: **FedMeta < FedAvg**

# Energy Consumption

The optimal overall energy consumption

$$\mathbb{E}[\hat{E}(K)] = \frac{KA_1}{K\epsilon - A_2 - KA_3} N(B_0K + B_1)$$
$$T_{Avg}^* \quad B_0 = \mathbb{E}[c_0]e$$
$$B_1 = \mathbb{E}[\eta]K + \mathbb{E}[c_1]e + \mathbb{E}[E_n^{mu}]$$

The optimal overall energy consumption

$$\mathbb{E}[\hat{E}(K)] = \frac{KC_1}{K\epsilon - C_2 - KC_3} N(2B_0K + B_1)$$
$$T_{Meta}^*$$

➤ **Note2:**

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**the overall energy consumption**

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# Experiment Setup

Monitor



19 Edge Servers + Observation Server Coordinator

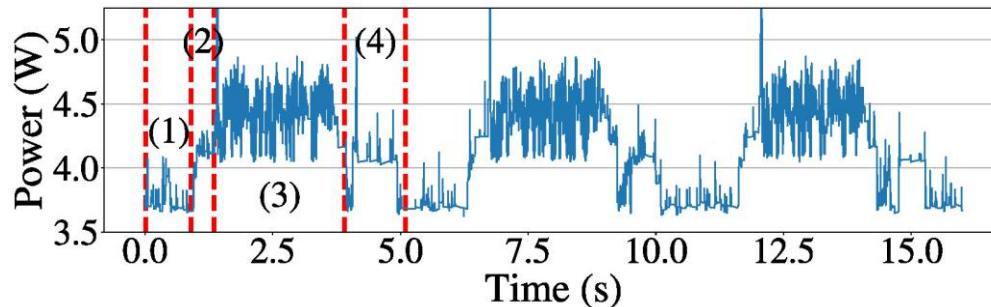
Hardware prototype

| Algorithm                    | FedAvg                | FedMeta                                  |
|------------------------------|-----------------------|--|
| Dataset                      | MNIST                 |  |
| Number of devices            | 20                    |  |
| Number of labels per device  | 2                     |  |
| Number of samples per device | 3000                  |  |
| Learning rate                | 0.005                 | Inner layer: 0.004<br>Outer layer: 0.005 |
| Model architecture           | 2-layer CNN with ReLu |  |
| Communication rounds         | 100                   |  |

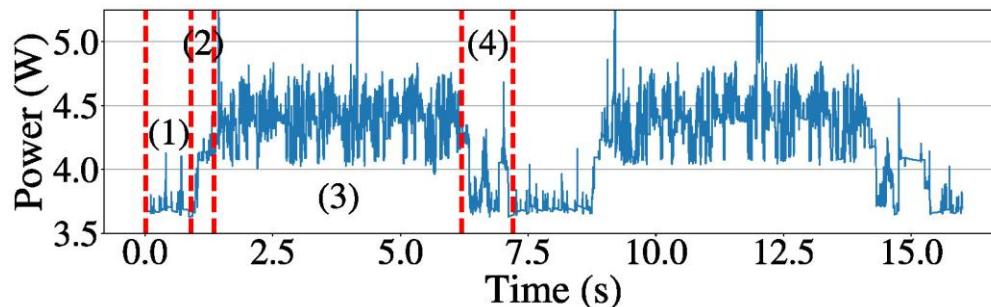
- ❑ Fix a test performance,
- ❑ Compare the energy consumption to achieve it.

# Numerical Results

- FedAvg



- FedMeta



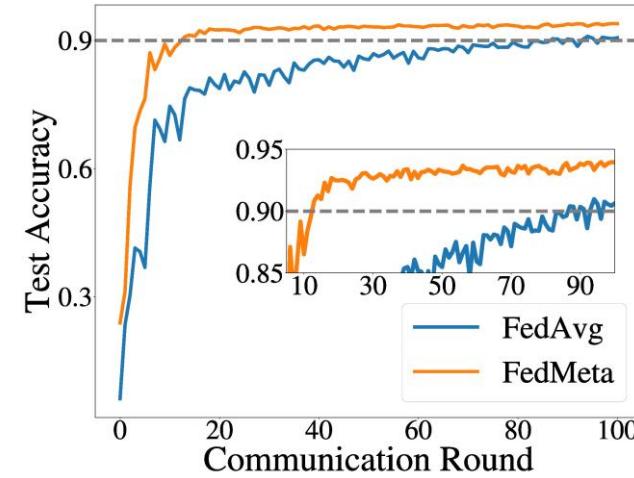
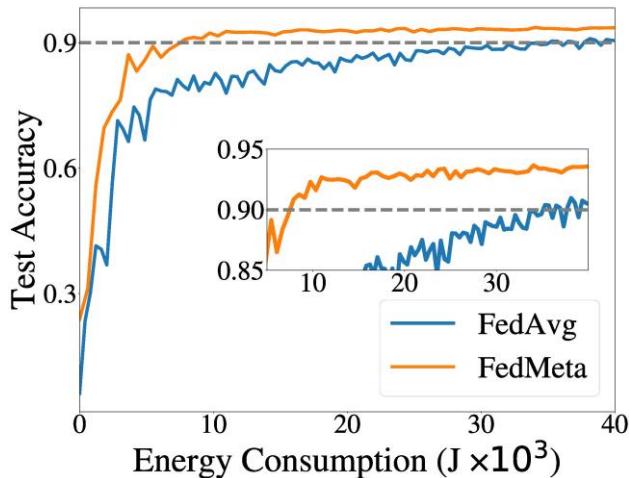
| Stage             | Average power | Energy consumption |
|-------------------|---------------|--------------------|
| Waiting           | 3.7W          | 3.33J              |
| Model downloading | 4.1W          | 1.845J             |
| Local training    | 4.4W          | 11.22J             |
| Model uploading   | 3.9W          | 3.9J               |

| Stage             | Average power | Energy consumption |
|-------------------|---------------|--------------------|
| Waiting           | 3.7W          | 3.33J              |
| Model downloading | 4.1W          | 1.845J             |
| Local training    | 4.4W          | 21.34J             |
| Model uploading   | 3.9W          | 3.9J               |

✓ Within a single communication round, FedMeta requires more energy consumption

# Numerical Results

| Algorithm            | FedAvg         | FedMeta |
|----------------------|----------------|---------|
| Energy consumption   | 36,125J (4.5x) | 7,970J  |
| Communication Rounds | 89 (6.8x)      | 13      |



- ✓ Although within a single round, FedMeta requires more energy consumption
- ✓ For a fixed test accuracy, **FedMeta** requires **fewer communication rounds** and achieves **less energy consumption** than FedAvg.

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# Conclusions

- ✓ Proposed an energy consumption model
- ✓ Derived the analytical solutions for the energy consumption of FEI networks with two popular distributed algorithms, FedAvg and FedMeta
- ✓ Proved that energy consumption is related to many factors, and large energy consumption within a single communication round does not mean large overall energy consumption

# Thank You!

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For more information, please contact:

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