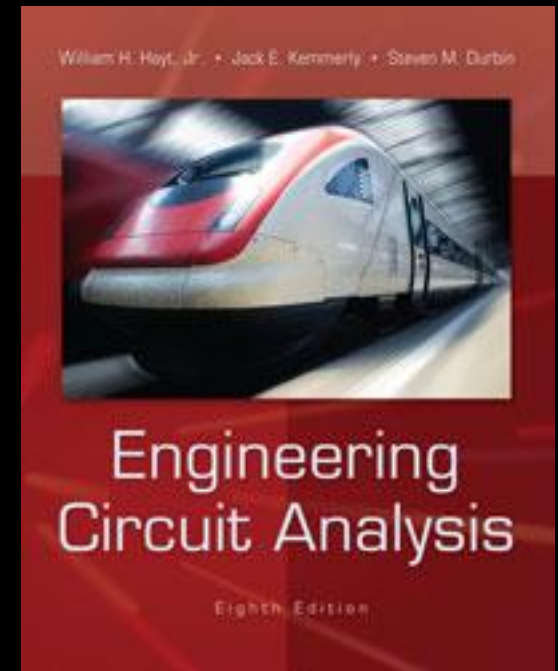


# Chapter 7

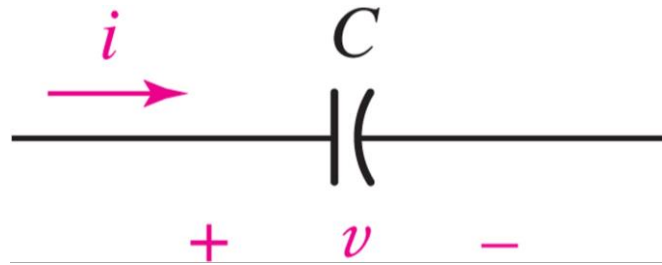
# Capacitors and

# Inductors



# The Capacitor

- the ideal capacitor is a passive element with circuit symbol



- the current-voltage relation is

$$i = C \frac{dv}{dt}$$

- the capacitance  $C$  is measured in farads (F)

# Some Capacitors

- capacitors can be bulky and typical values range from pF to  $\mu\text{F}$



(a)



(b)



(c)

# Capacitors Store Energy

Since

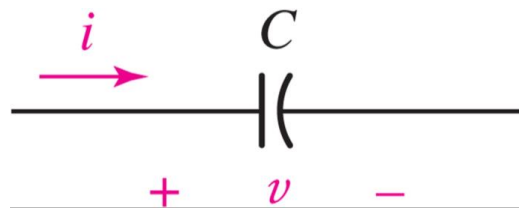
$$p(t) = i(t)v(t) = \left( C \frac{dv}{dt} \right) v = \frac{dw}{dt}$$

then the energy stored in a capacitor is

$$w = \frac{1}{2} C v^2$$

# Key Capacitor Behaviors

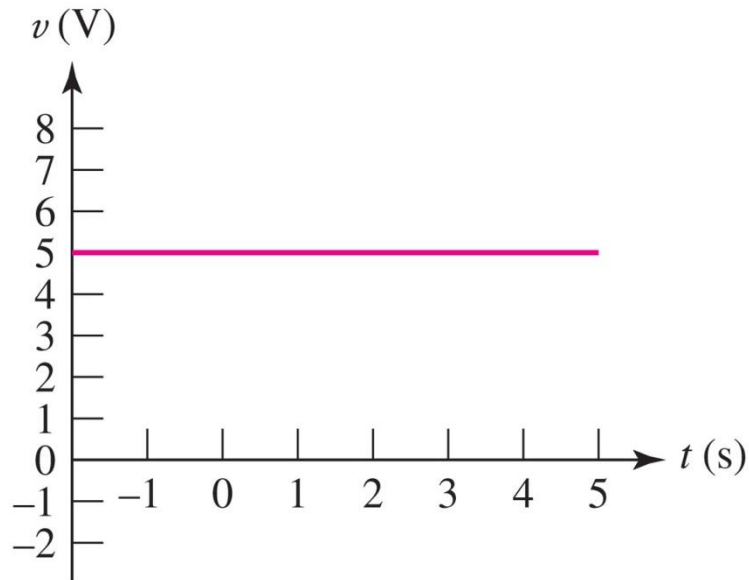
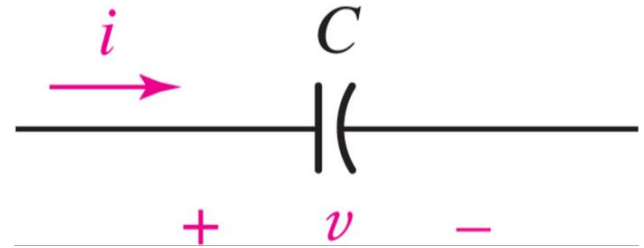
- capacitors are open circuits to dc voltages
- the voltage on a capacitor *cannot* jump
- capacitors store energy ( $iv > 0$ ) or deliver energy ( $iv < 0$ )



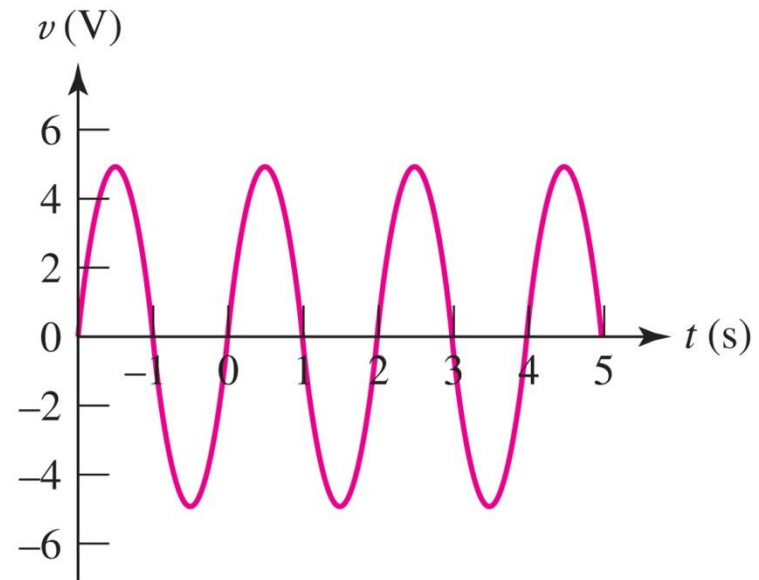
$$i = C \frac{dv}{dt}$$

# Example: i-v Curves (part 1 of 2)

Find  $i(t)$  for the voltages shown, if  $C=2$  F.



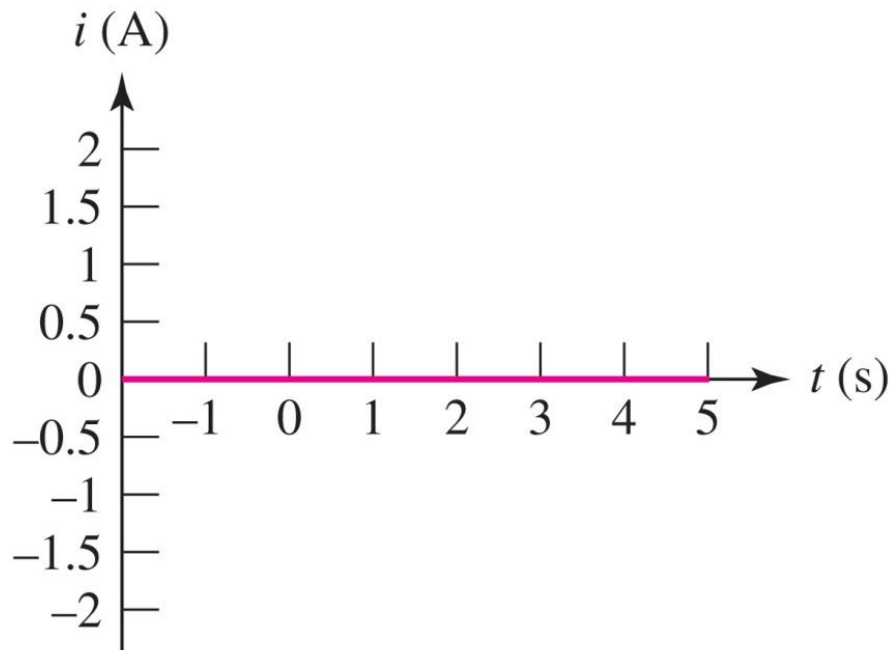
(a)



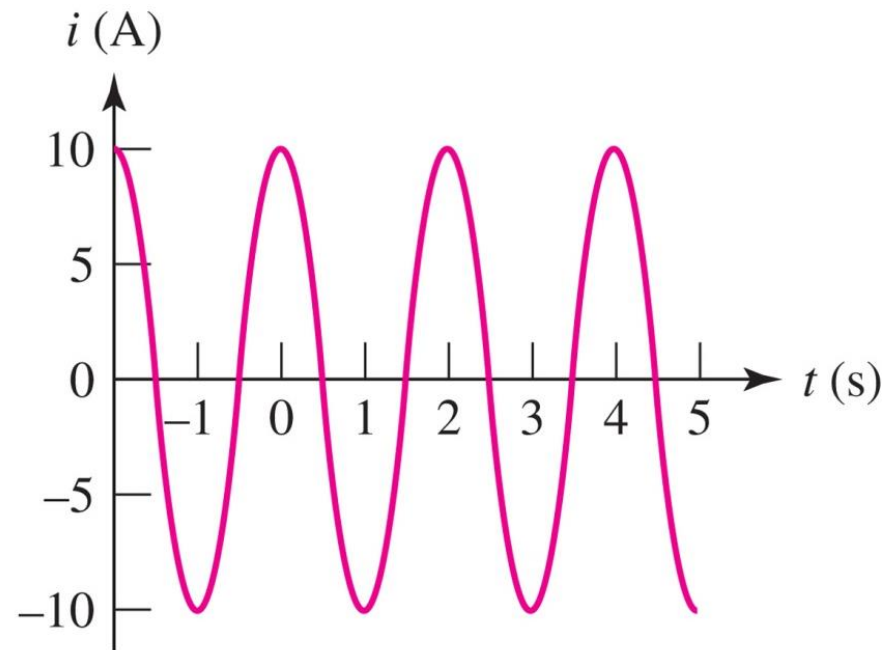
(b)

# Example: i-v Curves (part 2 of 2)

Solution: apply  $i(t) = 2dv/dt$  and graph:



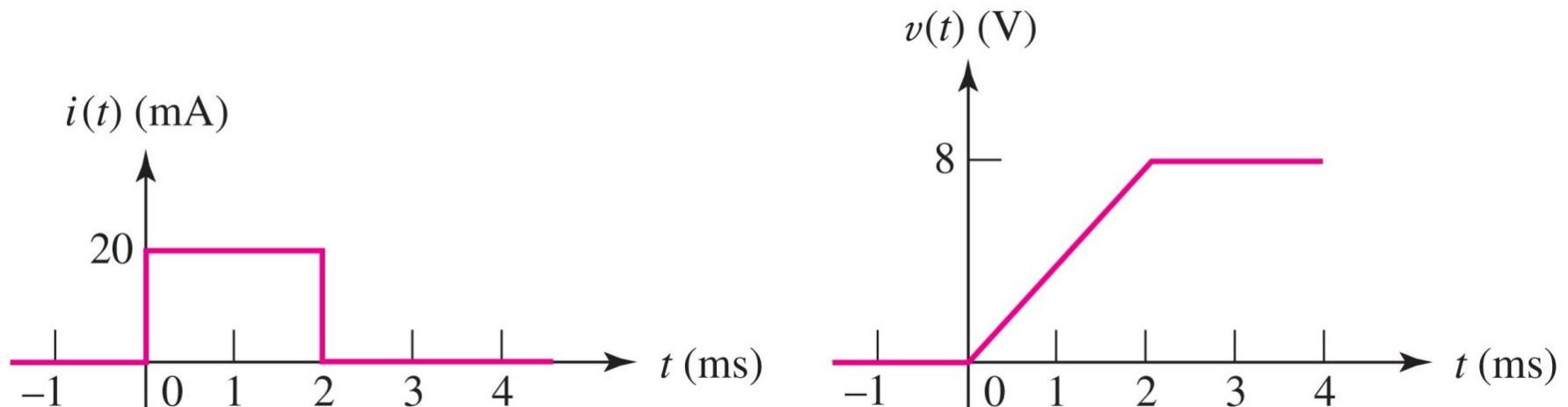
(a)



(b)

# Example: i-v Curves

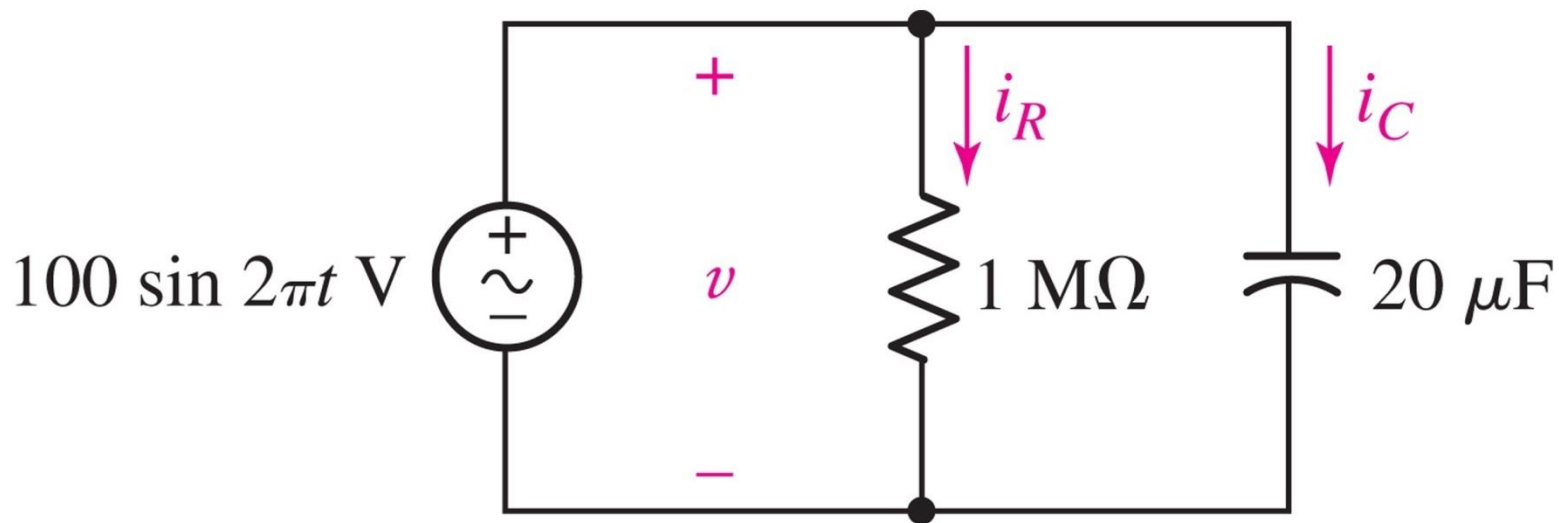
Show that the following graphs are matching voltage and current graphs for a capacitor of  $C=5\mu\text{F}$ .





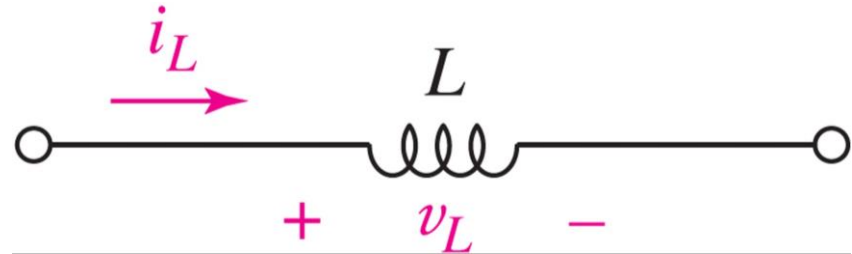
# Example: Capacitor Energy

Determine the maximum energy stored in the capacitor, and plot  $i_R$  and  $i_C$ .



# The Inductor

- the ideal inductor is a passive element with circuit symbol



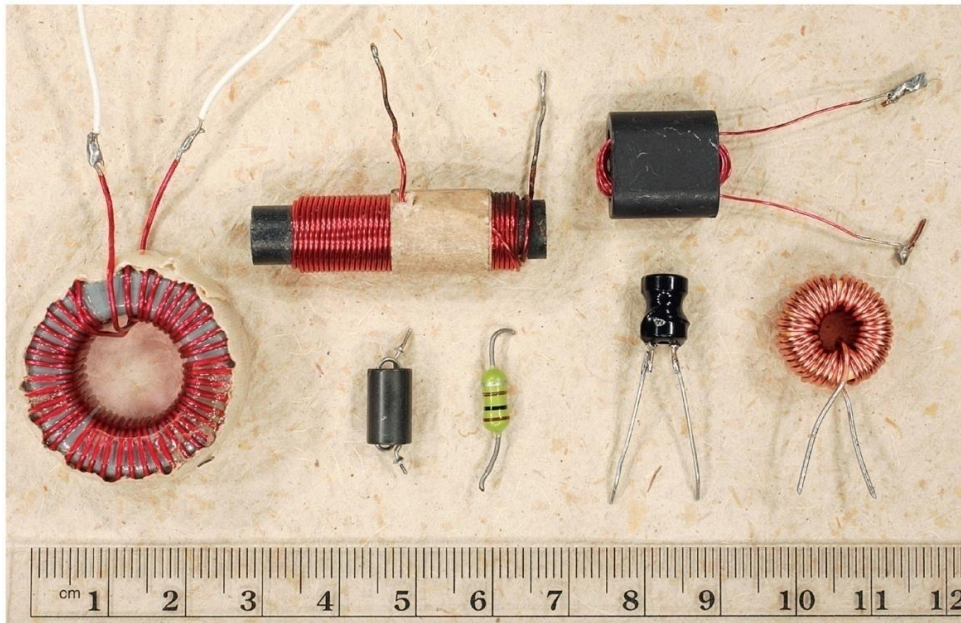
- the current-voltage relation is

$$v = L \frac{di}{dt}$$

- the unit of inductance  $L$  is henry (H)

# Some Inductors

- inductors can be bulky and typical values range from  $\mu\text{H}$  to H



(a)



(b)

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# Inductors Store Energy

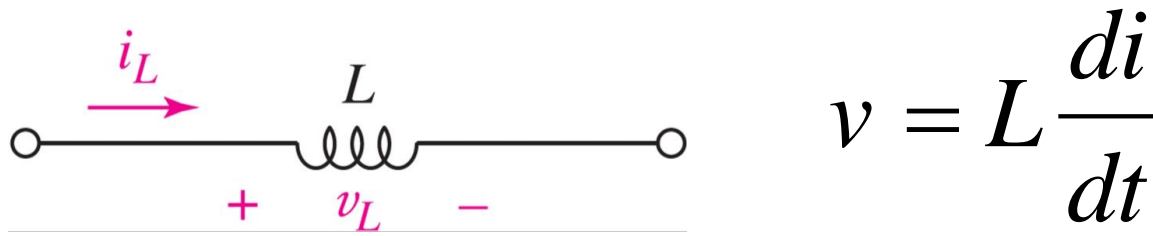
Since  $p(t) = i(t)v(t) = \left( L \frac{di}{dt} \right) i = \frac{dw}{dt}$

then the energy stored in a inductor is

$$w = \frac{1}{2} Li^2$$

# Key Inductor Behaviors

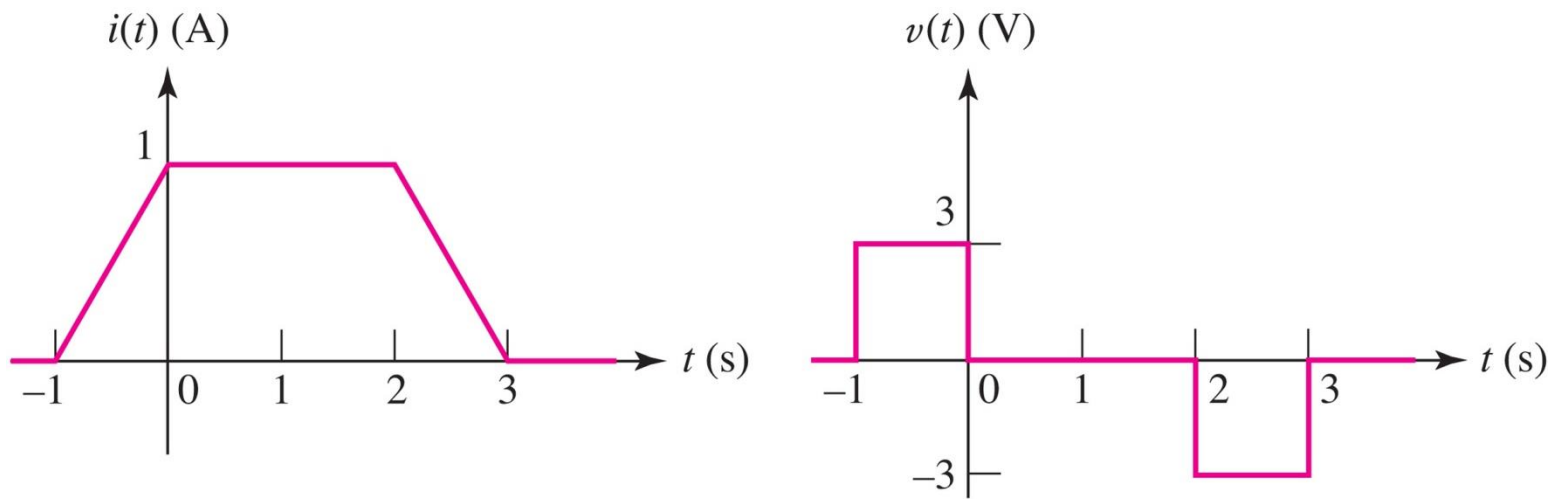
- inductors are short circuits to dc voltages
- the current through an inductor *cannot* jump
- inductors store energy ( $iv > 0$ ) or deliver energy ( $iv < 0$ )



$$v = L \frac{di}{dt}$$

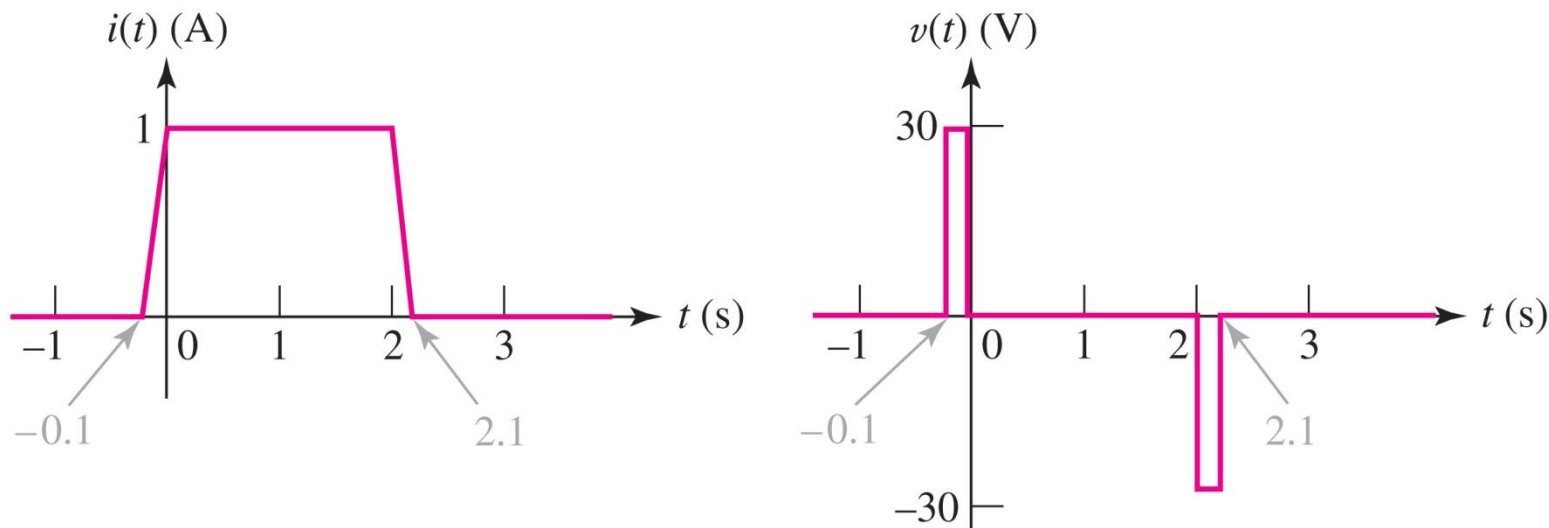
# Example: i-v Curves for L

Show that the following graphs are matching voltage and current graphs for an inductor of  $L=3$  H.



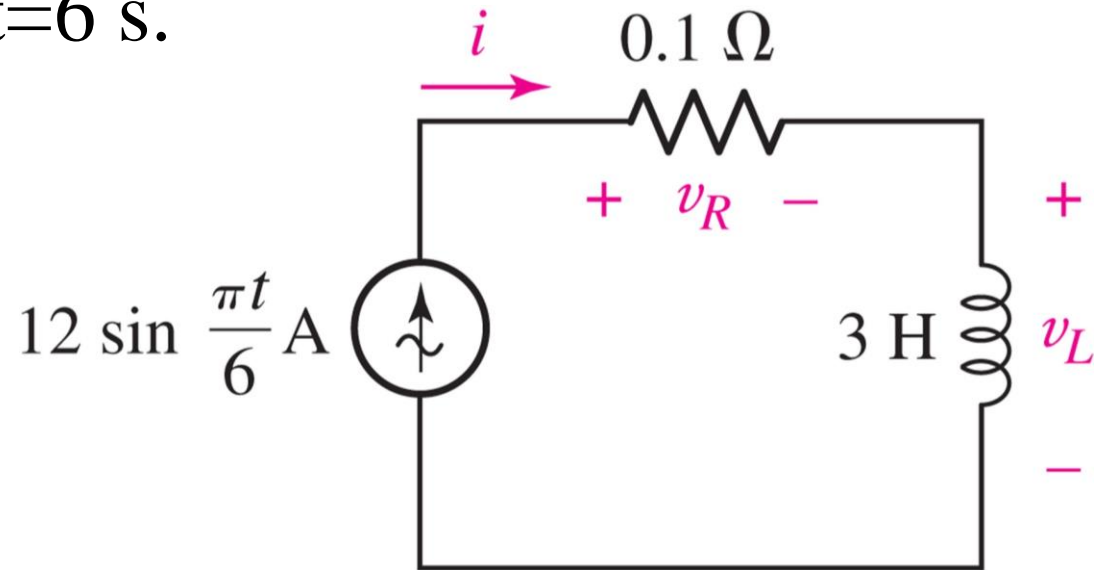
# Example: i-v Curves for L

For the same 3-H inductor, the voltages are 10 times larger when the current is ramped 10 times faster:



# Example: Energy in L

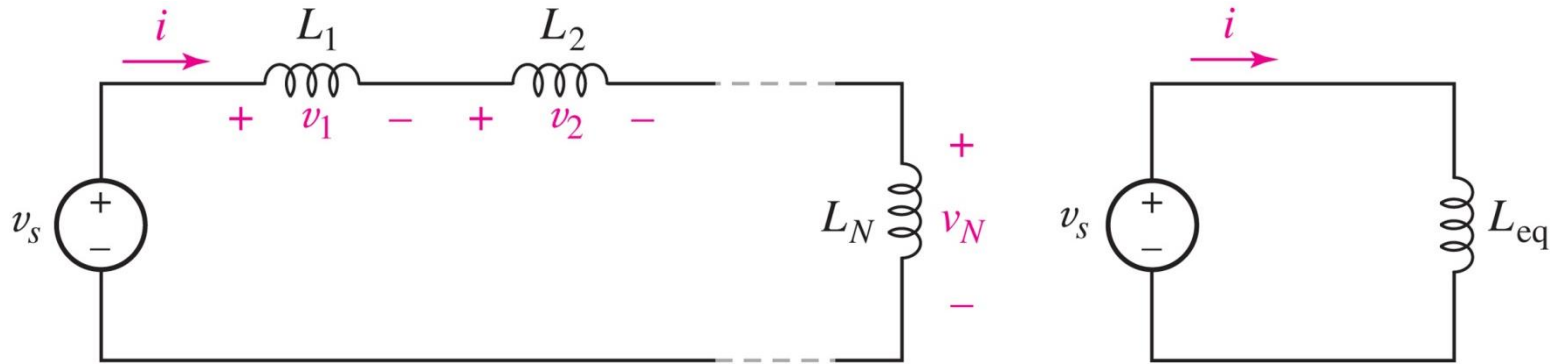
Determine the maximum energy stored in the inductor, and find the energy lost to resistor from  $t=0$  to  $t=6$  s.



*Answer: 216 J, 43.2 J*



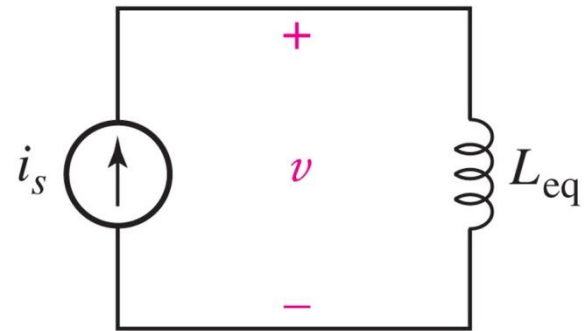
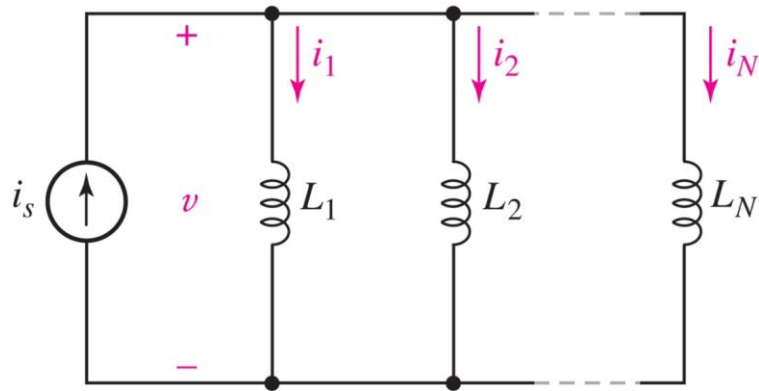
# Inductors in Series



Apply KVL to show:

$$L_{eq} = L_1 + L_2 + \dots + L_N$$

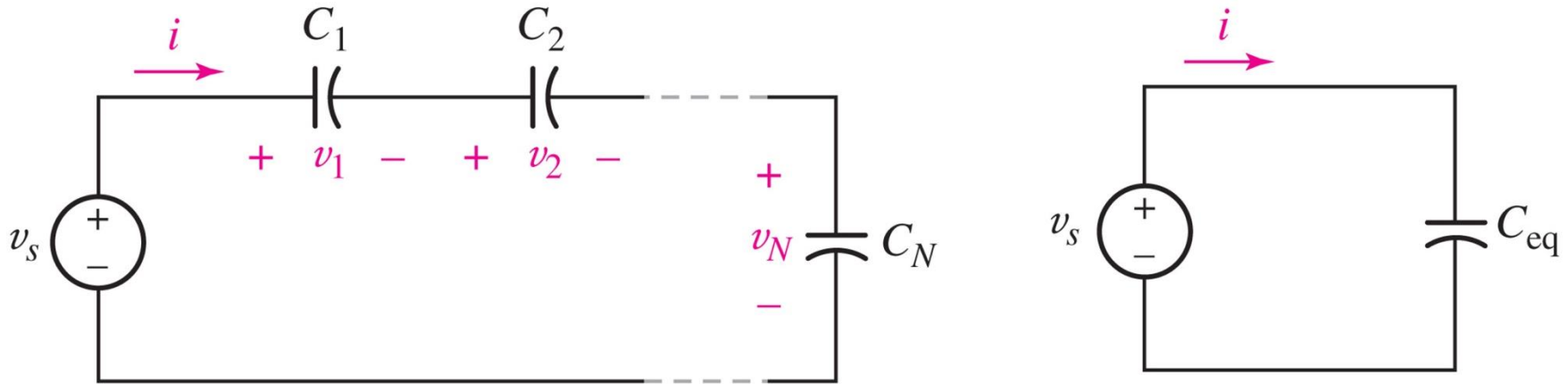
# Inductors in Parallel



Apply KCL to show

$$L_{eq} = \frac{1}{\frac{1}{L_1} + \frac{1}{L_2} + \dots + \frac{1}{L_N}}$$

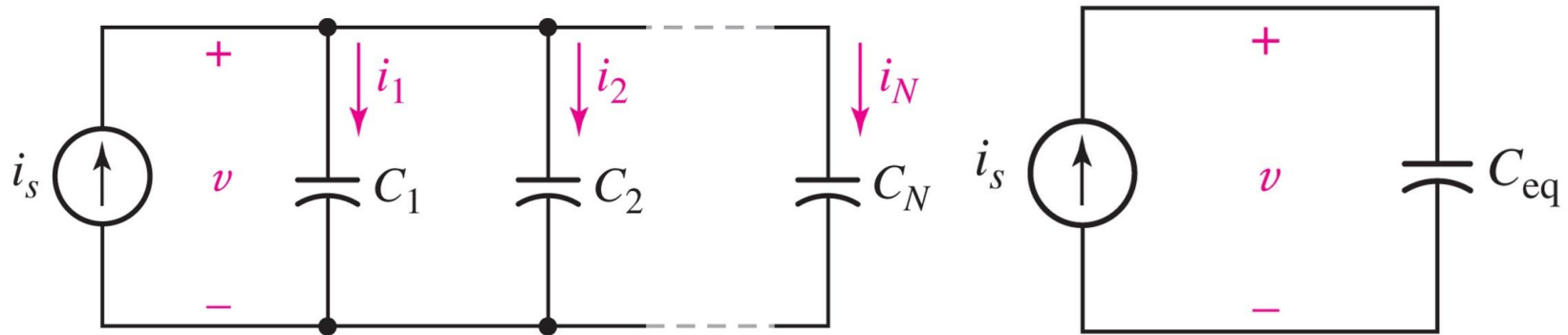
# Capacitors in Series



Apply KVL to show:

$$C_{eq} = \frac{1}{\frac{1}{C_1} + \frac{1}{C_2} + \dots + \frac{1}{C_N}}$$

# Capacitors in Parallel



Apply KCL to show:

$$C_{eq} = C_1 + C_2 + \dots + C_N$$

# Two-Element Shortcuts

Two capacitors in *series*:

$$C_{eq} = \frac{C_1 C_2}{C_1 + C_2}$$

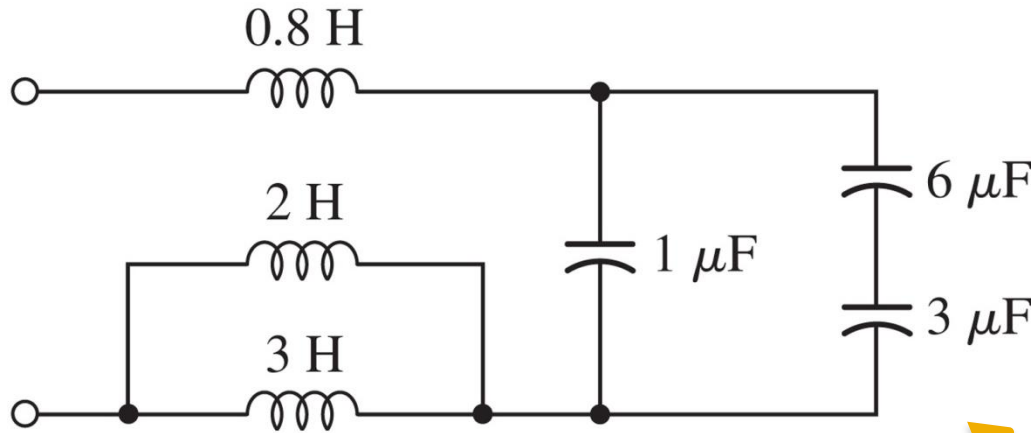
Two inductors in parallel:

$$L_{eq} = \frac{L_1 L_2}{L_1 + L_2}$$

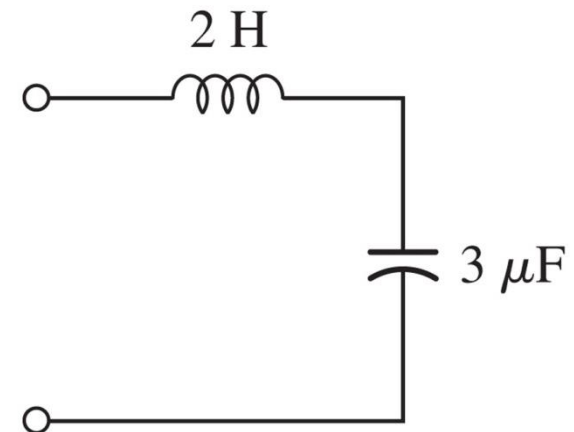
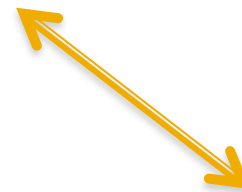
Two resistors in parallel:

$$R_{eq} = \frac{R_1 R_2}{R_1 + R_2}$$

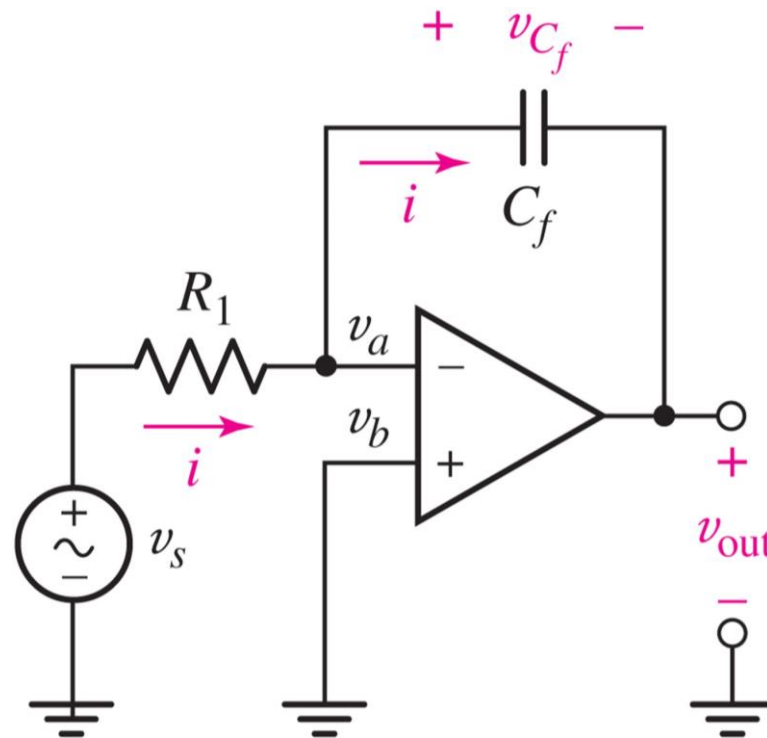
# Example: Simplifying LC



Show that these circuits are equivalent using series and parallel combinations.

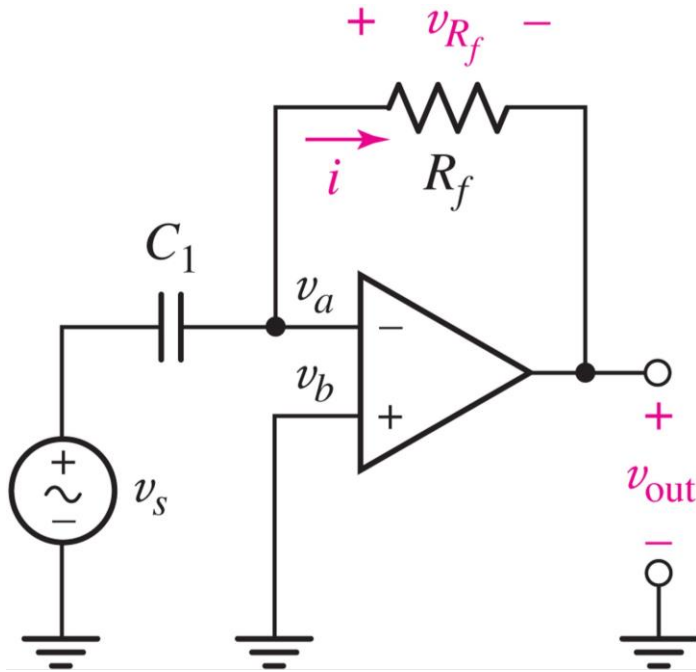


# Op Amp Integrator



$$v_{out} = -\frac{1}{R_1 C_f} \int_0^t v_s dt' - v_{C_f}(0)$$

# Op Amp Differentiator



$$v_{out} = -C_1 R_f \frac{dv_s}{dt}$$