

# MTH101: Tutorial 9

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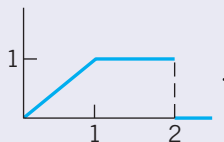
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## Exercise 1.1

*Find the transform for the following functions.*

1.  $e^{-t} \sinh 4t,$

2.



## Exercise 1.2

Given  $F(s) = \mathcal{L}[f]$ , find  $f(t)$  for the following functions.

1.  $\frac{4s + 32}{s^2 - 16},$

2.  $\frac{4}{s^2 - 2s - 3}.$

## Exercise 2.1

Find  $f(t)$  if  $\mathcal{L}[f]$  equals

$$\frac{2(e^{-s} - e^{-3s})}{(s^2 - 4)}.$$

### Exercise 3.1

*Find the solution to the initial value problem.*

$$y'' + 4y' + 5y = \delta(t - 1), \quad y(0) = 0, \quad y'(0) = 3.$$

### Exercise 3.2

*Find the solution to the initial value problem.*

$$y'' + 3y' + 2y = 10 [\sin t + \delta(t - 1)], \quad y(0) = 1, \quad y'(0) = -1.$$

### Exercise 4.1

Find  $\mathcal{L}[f]$  or  $\mathcal{L}^{-1}[F(s)]$  for the following functions

1.  $\cos^2(2t),$
2.  $\frac{3s + 4}{s^4 + k^2 s^2}.$