

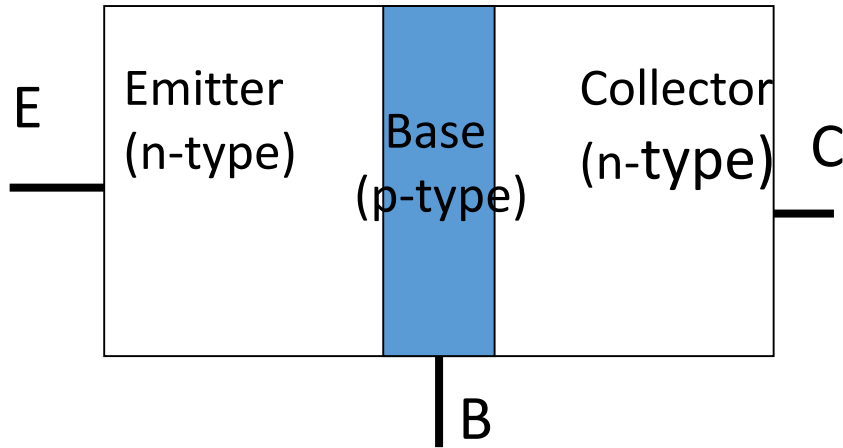
# **EEE109: Electronic Circuits**

## **The Bipolar Junction Transistor**

# Contents

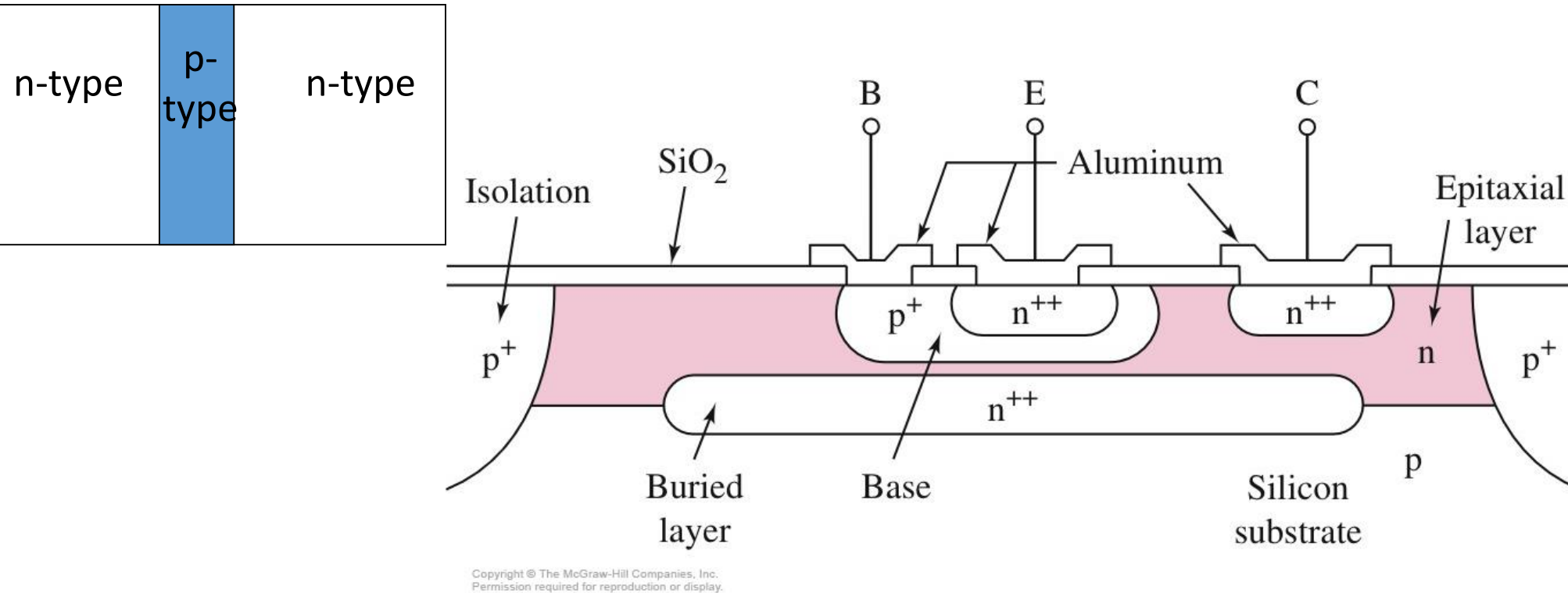
- Discuss the physical structure and operation of the bipolar junction transistor.
- Understand the dc analysis and design techniques of bipolar transistor circuits.
- Examine three basic applications of bipolar transistor circuits.
- Investigate various dc biasing schemes of bipolar transistor circuits, including integrated circuit biasing.
- Consider the dc biasing of multistage or multi-transistor circuits.

# Bipolar Junction Transistors (BJTs)



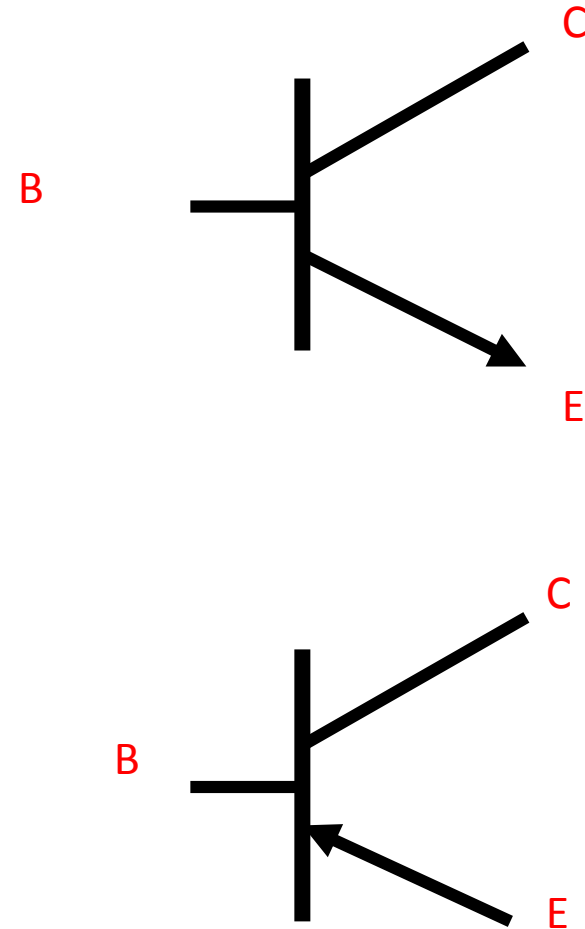
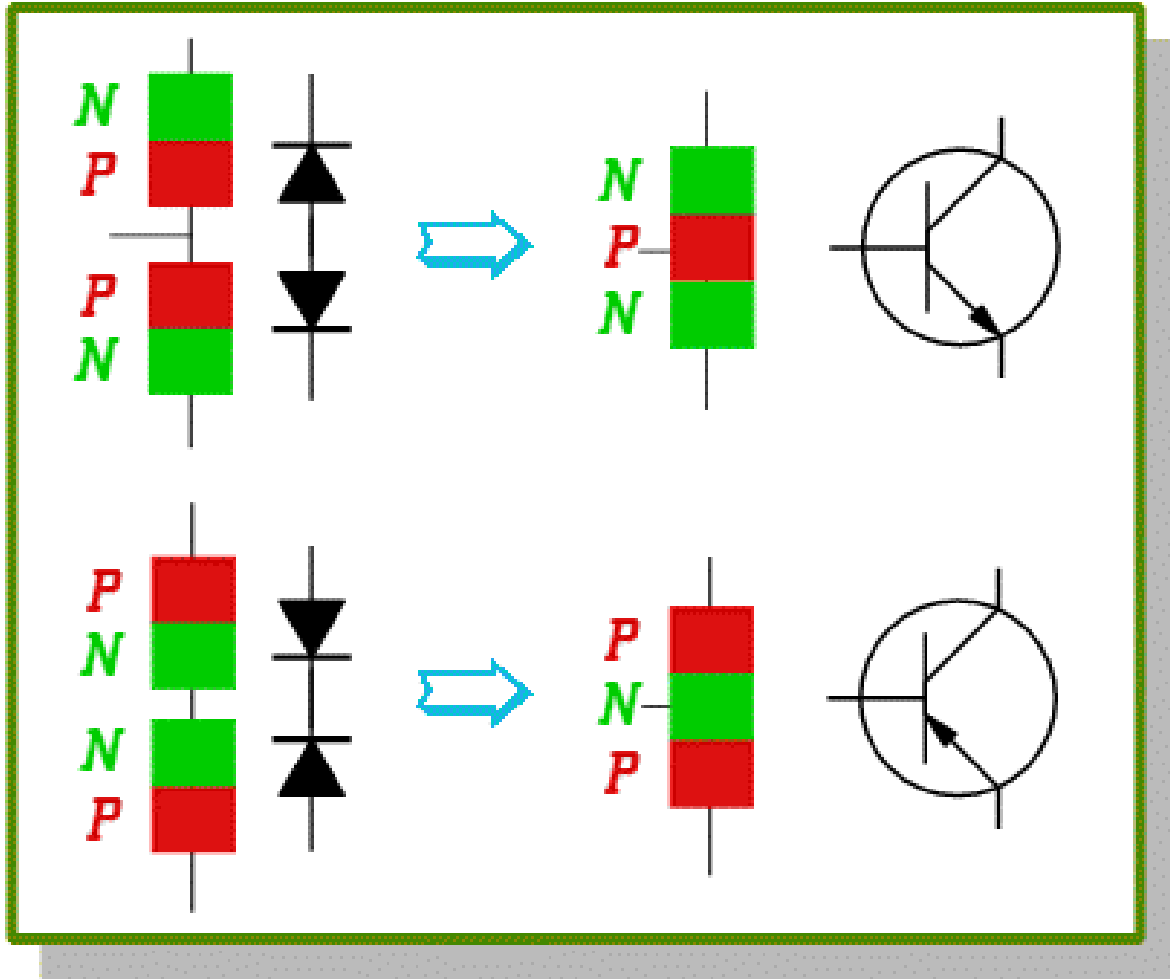
- The bipolar junction transistor is a semiconductor device constructed with three doped regions.
- These regions essentially form two 'back-to-back' p-n junctions in the same block of semiconductor material (silicon).
- The most common use of the BJT is in linear amplifier circuits (linear means that the output is proportional to input). It can also be used as a switch (in, for example, logic circuits).

# Cross Section of Integrated Circuit **npn** Transistor

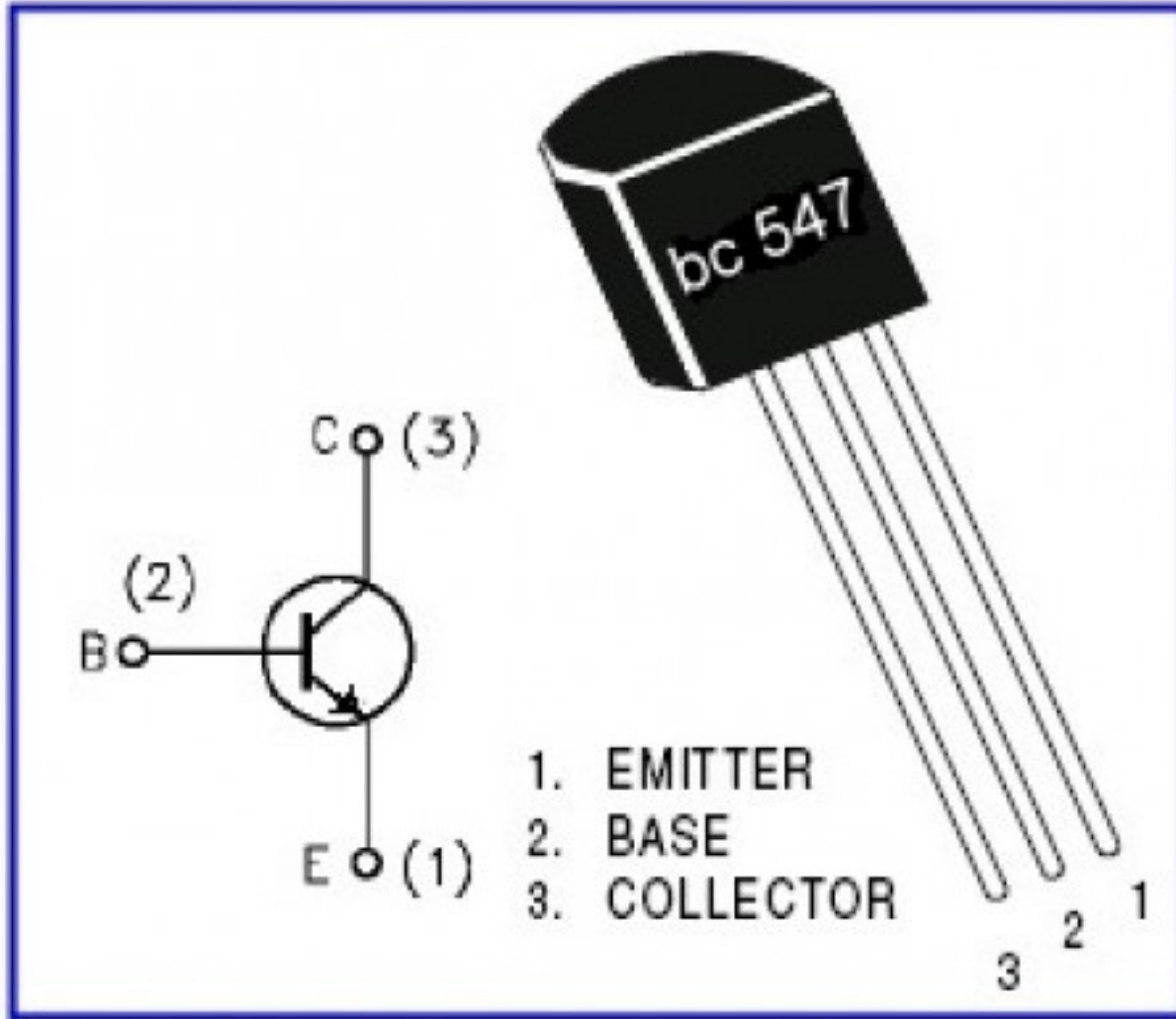


Impurity doping concentrations in the three regions are substantially different.

# npn BJT Symbol



The direction of the arrow on the emitter is reversed



BC 547 NPN transistor 45V 100mA hFE 150

Specifications:

BIPOLAR TRANSISTOR, NPN, 45V, TO-92

Transistor Polarity: NPN

Collector Emitter Voltage  $V_{(br)ceo}$ : 45V

Transition Frequency Typ ft: 300MHz

Power Dissipation Pd: 625mW

DC Collector Current: 100mA

DC Current Gain hFE: 150

Straight-lead housing

See more information on how to understand the specification:

[https://www.electronics-notes.com/articles/electronic\\_components/transistor/transistors-specifications.php](https://www.electronics-notes.com/articles/electronic_components/transistor/transistors-specifications.php)

# Common Configuration

- **NPN** Transistor Most Common Configuration

- Base, Collector, and Emitter
  - Base is a very thin region with **less dopants**
  - Base collector junction **reversed biased**
  - Base emitter junction **forward biased**

## **Current flow analogy:**

- If current flows into the base, a **much larger current** can flow from the collector to the emitter
  - If a signal to be amplified is applied as a current to the base, a valve between the collector and emitter opens and closes in response to signal fluctuations
- PNP Transistor essentially the same except for directionality

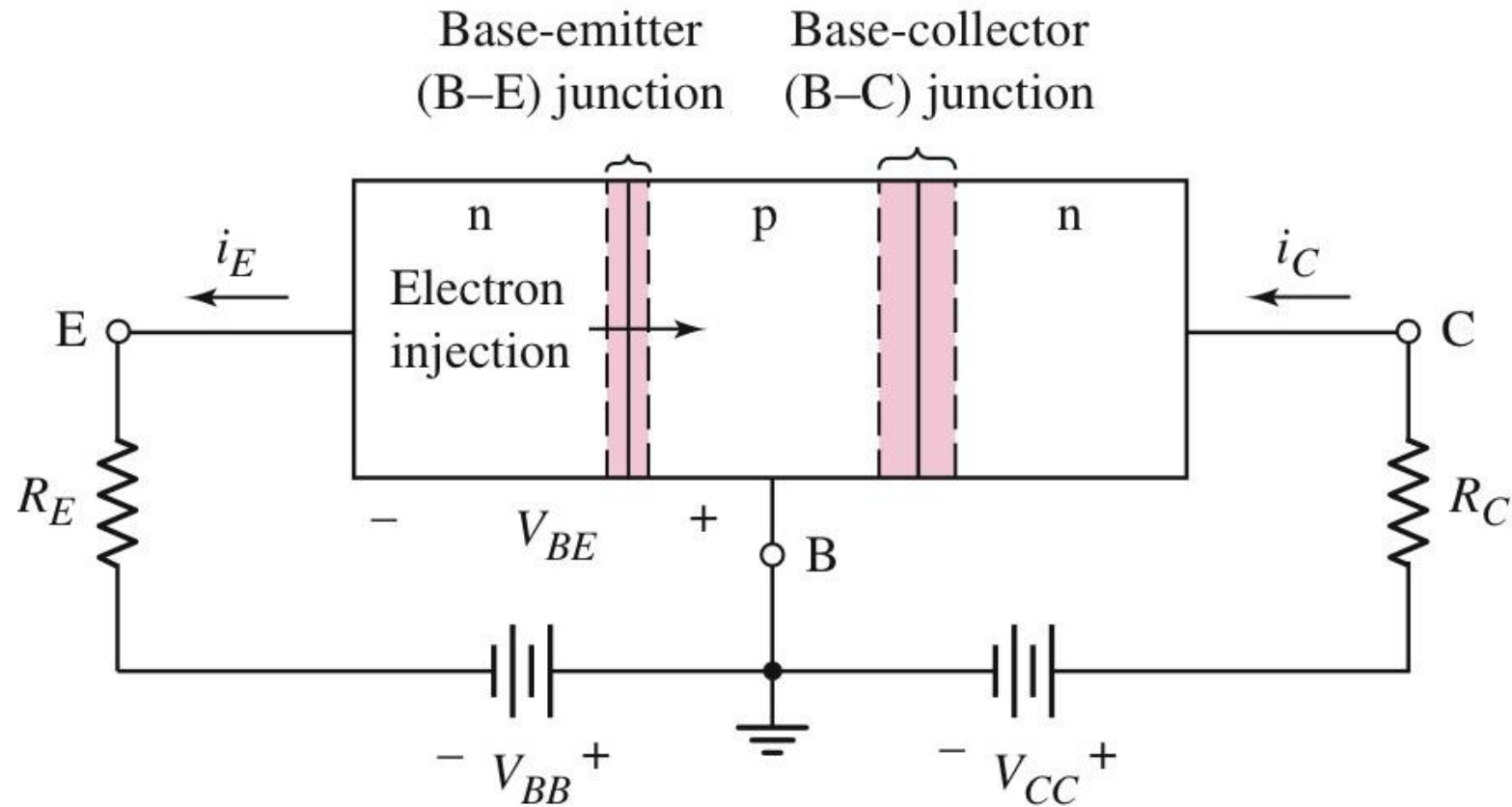
# Modes of Operation



# Modes of Operation

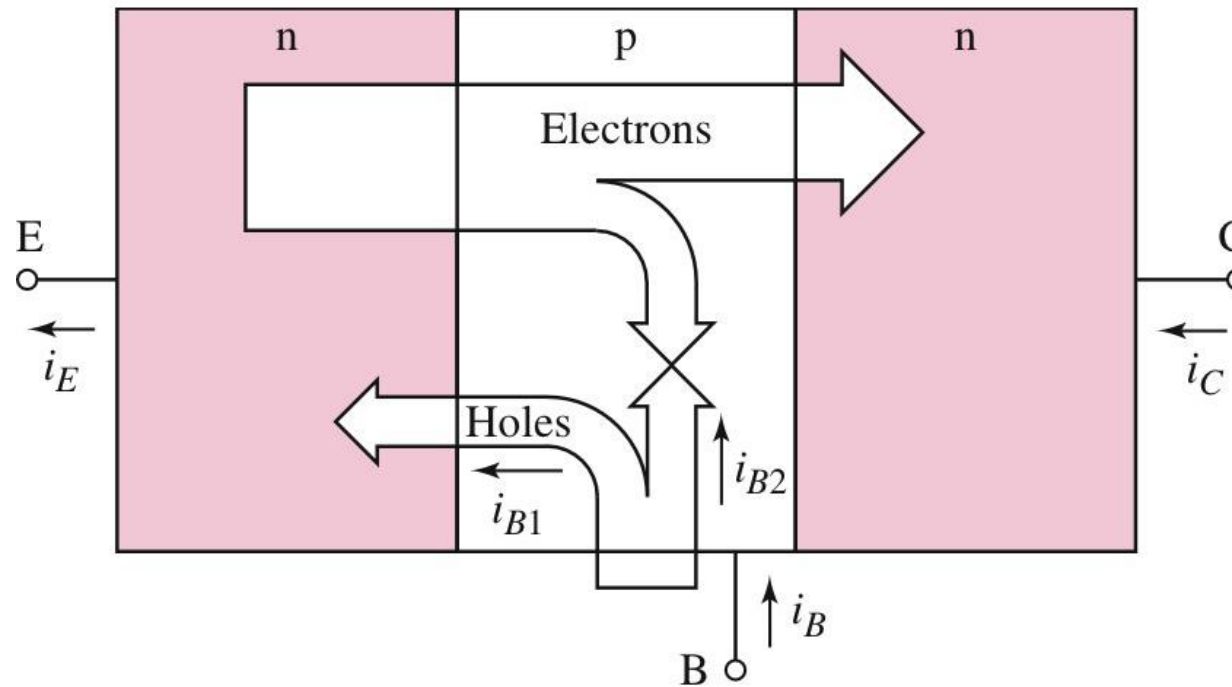
- Forward-Active
  - B-E junction is forward biased
  - B-C junction is reverse biased
- Saturation
  - B-E and B-C junctions are forward biased
- Cut-Off
  - B-E and B-C junctions are reverse biased
- Inverse-Active (or Reverse-Active)
  - B-E junction is reverse biased
  - B-C junction is forward biased

# npn BJT in Forward-Active



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# Electrons and Holes in npn BJT

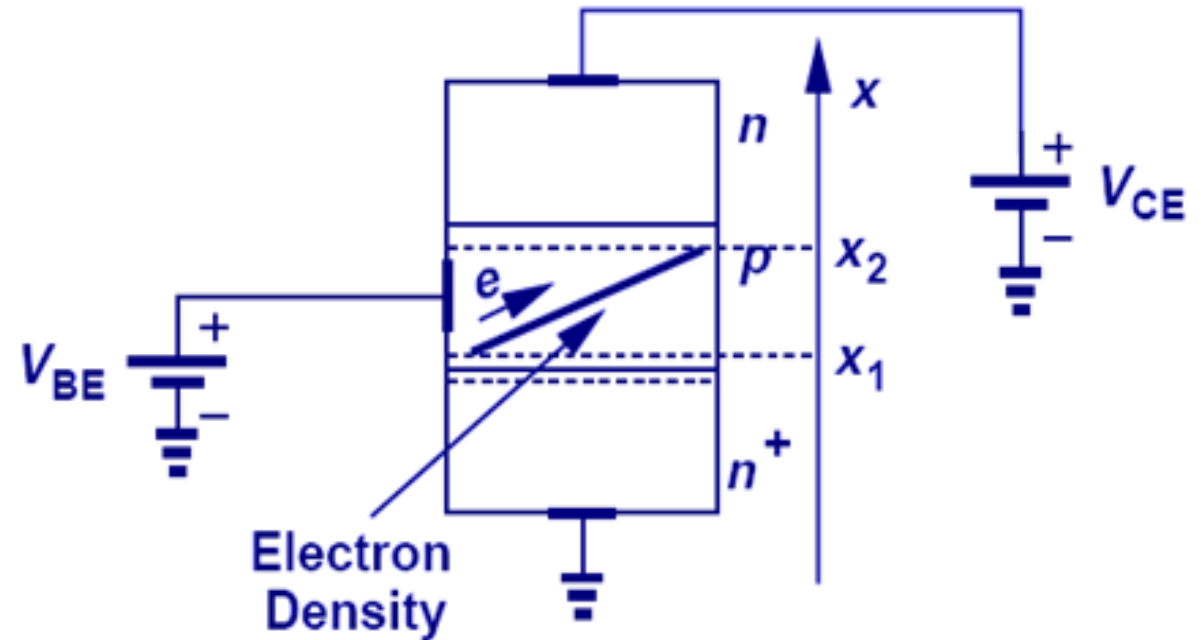


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# Carrier Transport in the Base Region

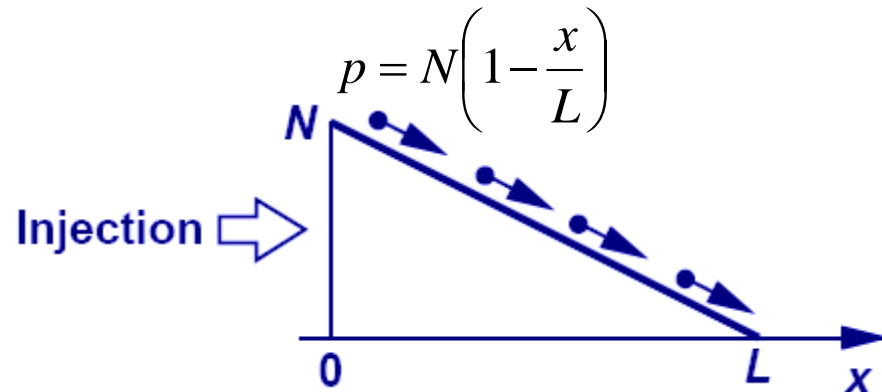
- Since the width of the quasi-neutral base region ( $W_B = x_2 - x_1$ ) is much smaller than the minority-carrier diffusion length, very few of the carriers injected (from the emitter) into the base recombine before they reach the collector-junction depletion region.
  - Minority-carrier diffusion current is ~constant in the quasi-neutral base

The minority-carrier concentration at the edges of the collector-junction depletion region are  $\sim 0$ .



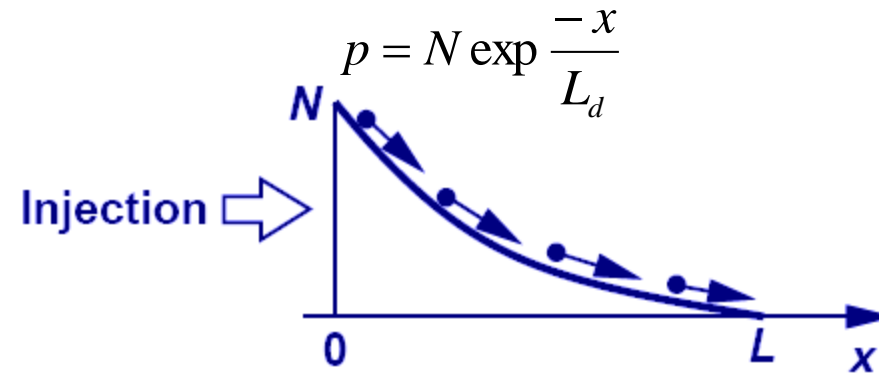
# Diffusion Example Redux

- Linear concentration profile  
→ constant diffusion current



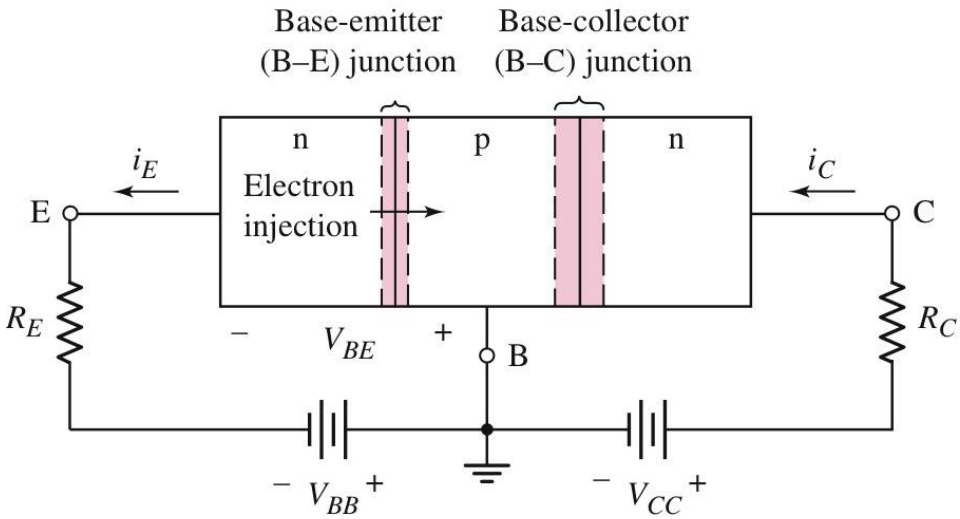
$$J_{p,diff} = -qD_p \frac{dp}{dx}$$
$$= qD_p \frac{N}{L}$$

- Non-linear concentration profile  
→ varying diffusion current

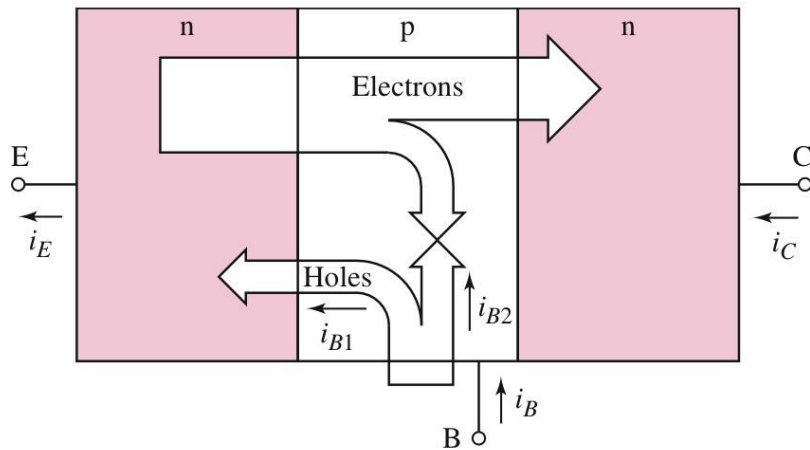


$$J_{p,diff} = -qD_p \frac{dp}{dx}$$
$$= \frac{qD_p N}{L_d} \exp \frac{-x}{L_d}$$

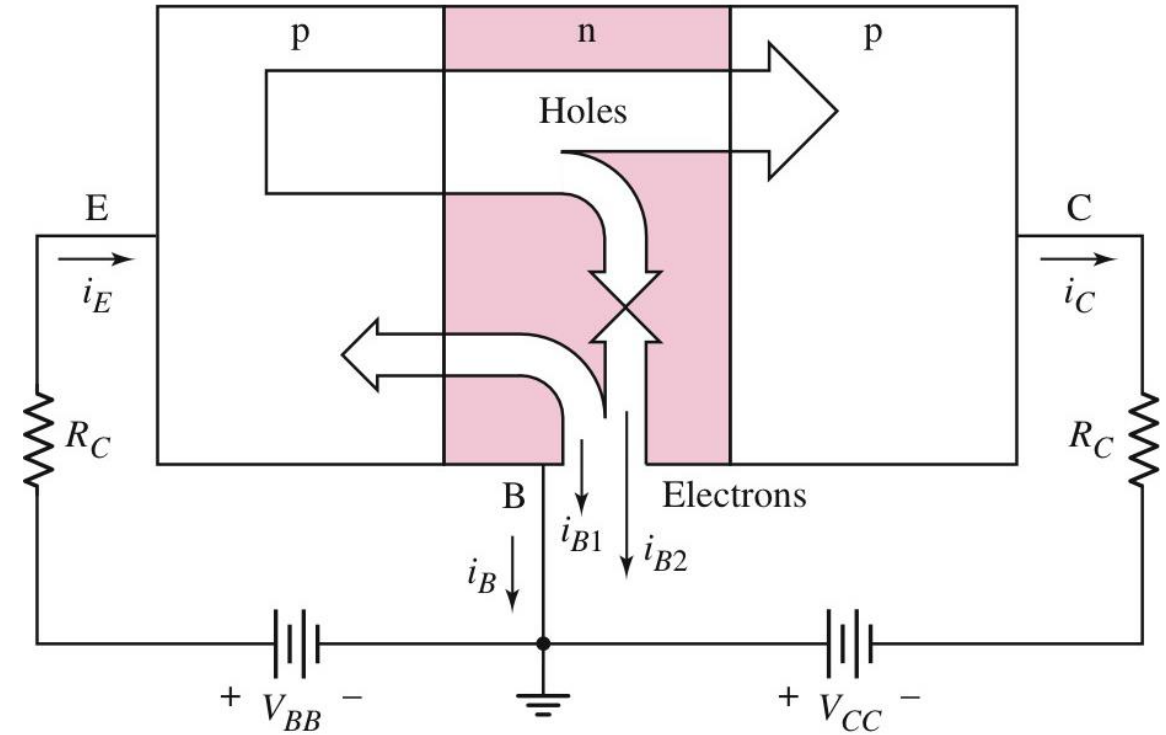
# Electrons and Holes in pnp BJT



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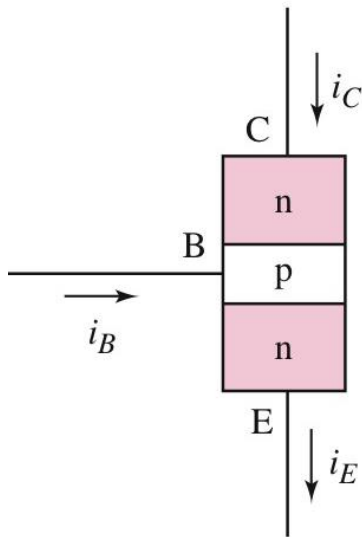


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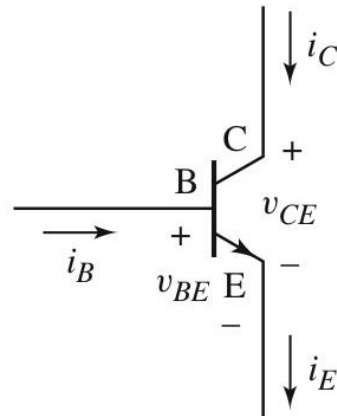
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# Circuit Symbols and Current Conventions

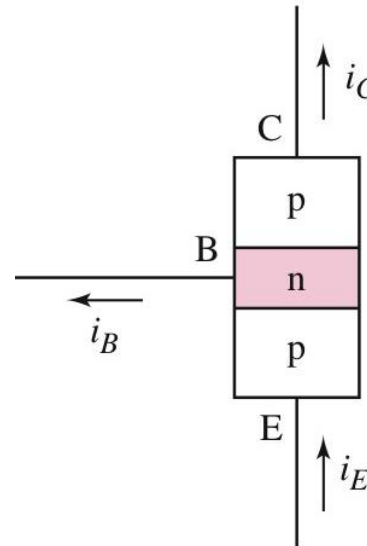


(a)

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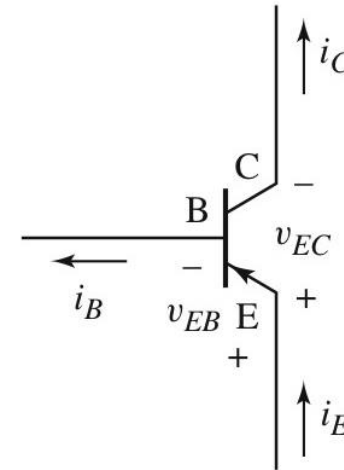


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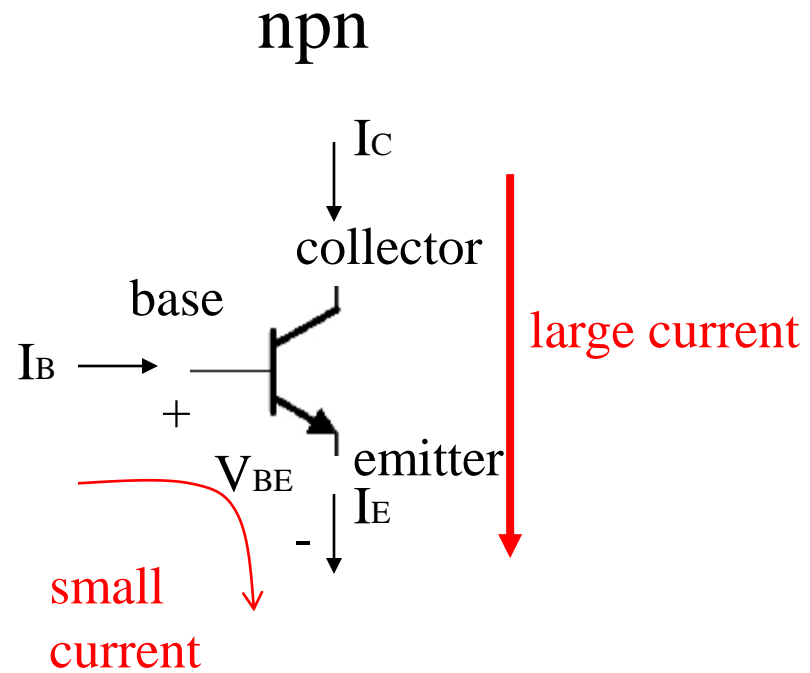
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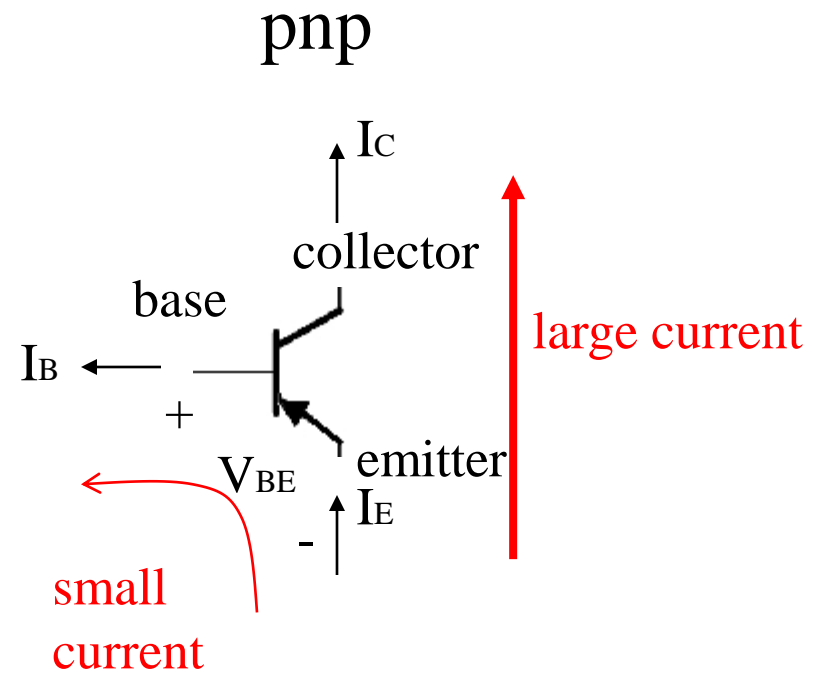
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# Summary of npn Transistor Behavior

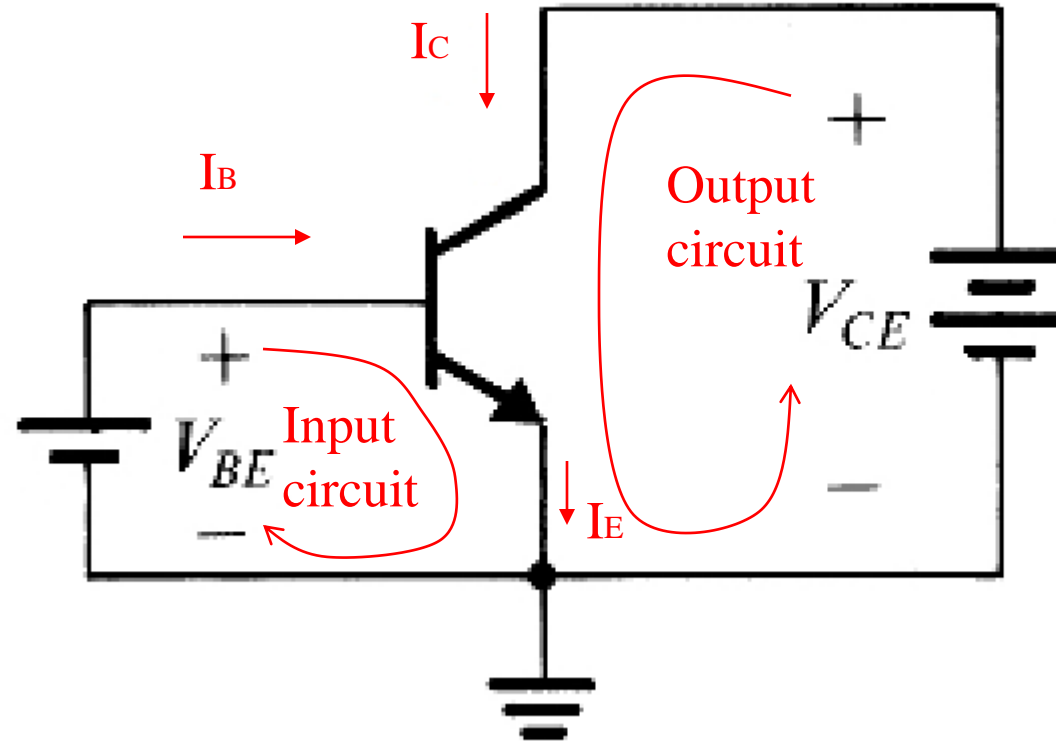




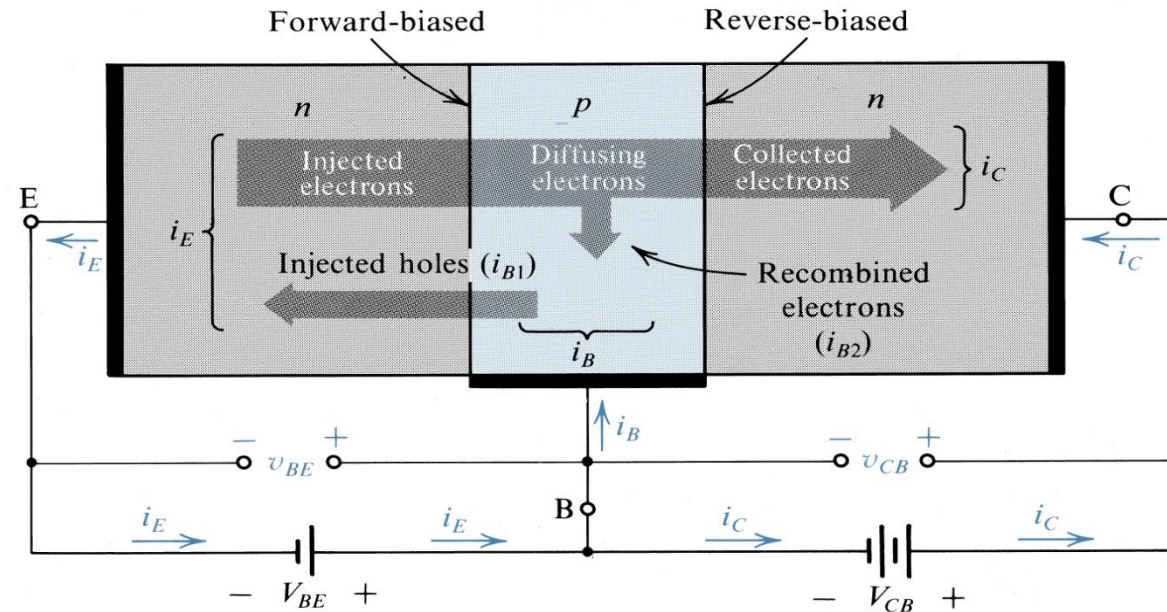
# Summary of pnp Transistor Behavior



# Graphical Representation of Transistor Characteristics



# BJT in Active Mode

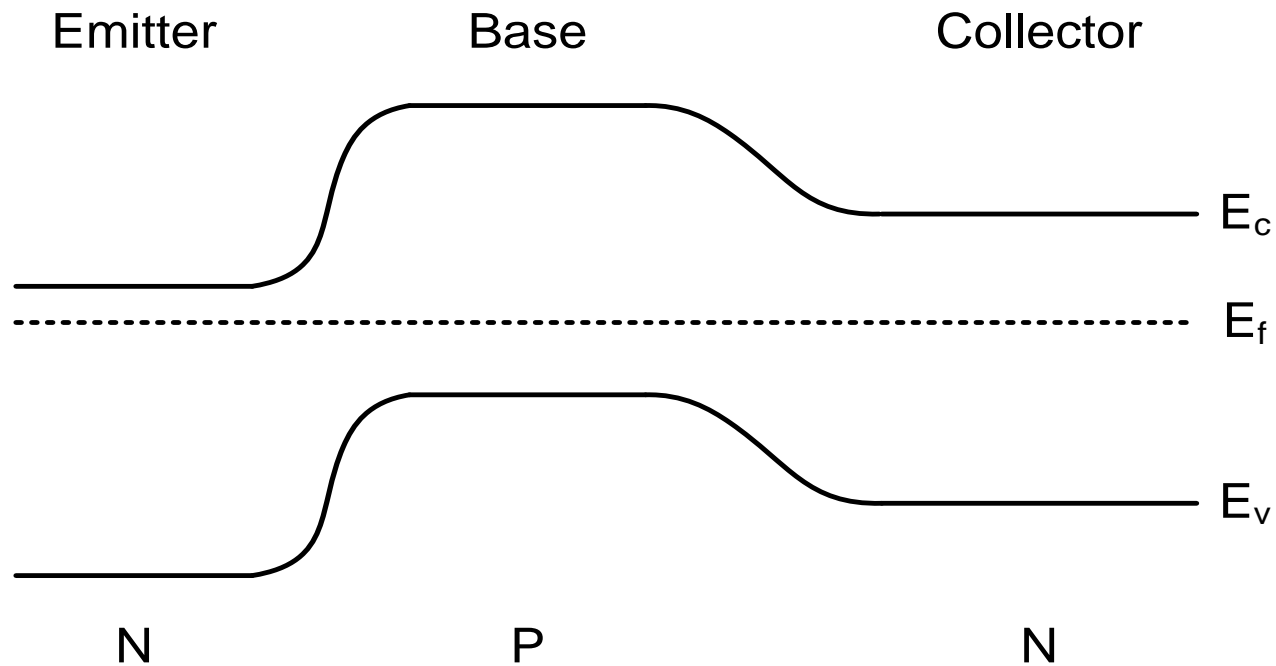


- Operation

- Forward bias of EBJ **injects electrons from emitter into base** (small number of holes injected from base into emitter)
- Most electrons shoot through the base into the collector across the reverse bias junction (think about band diagram)
- **Some electrons recombine with majority carrier** in (P-type) base region

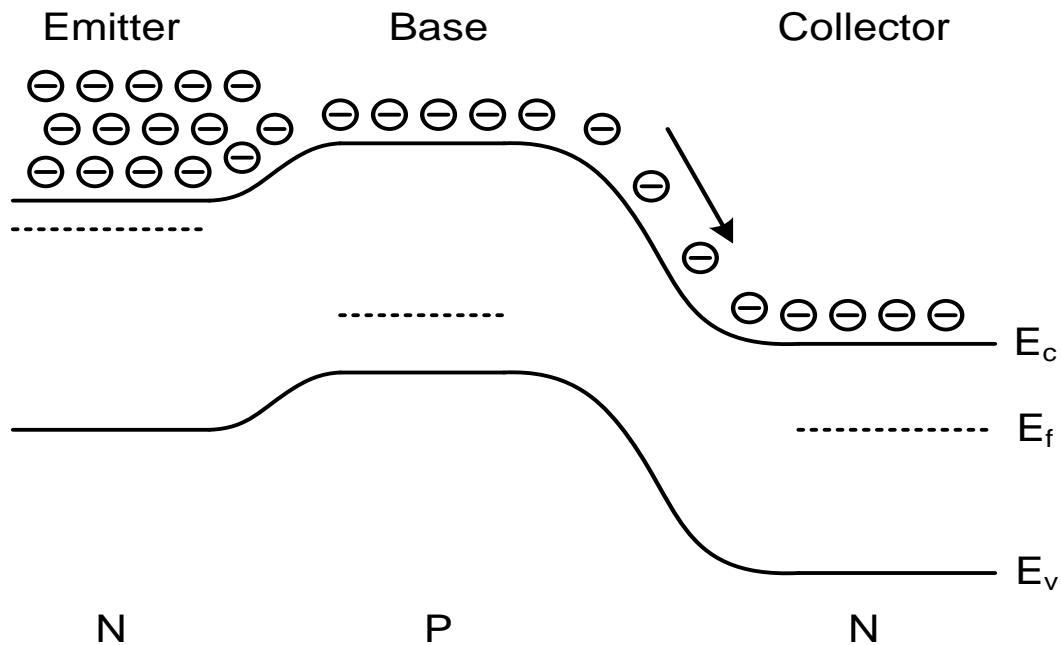
# Band Diagrams (In equilibrium)

- No current flow
- Back-to-back PN diodes



# Band Diagrams (Active Mode)

- EBJ forward biased
  - Barrier reduced and so electrons diffuse into the base
  - Electrons get **swept across** the base into the collector
- CBJ reverse biased
  - **Electrons roll down the hill (high E-field)**



# Current Relationships and IV Characteristics

# Collector Current

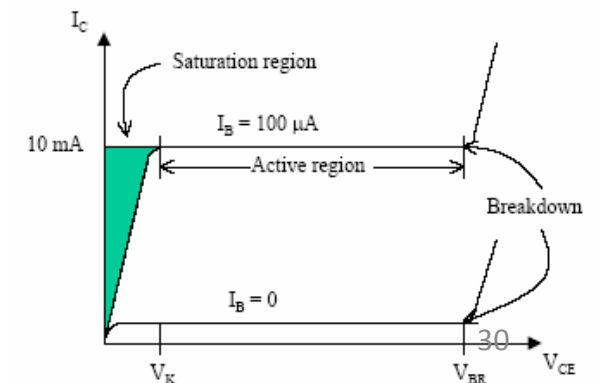
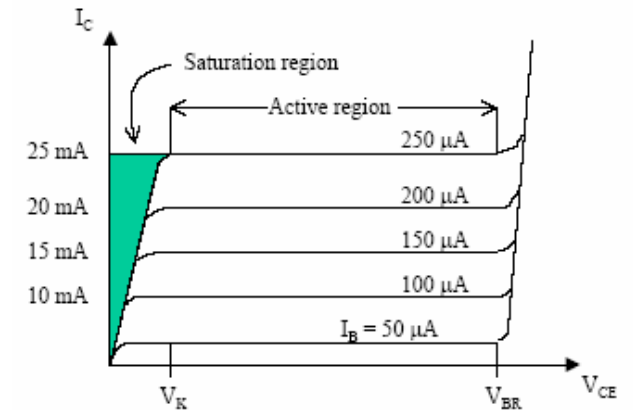
- Electrons that diffuse across the base to the CBJ junction are swept across the CBJ depletion region to the collector b/c of the higher potential applied to the collector.

$$i_C = I_S e^{v_{BE}/V_T} \text{ where the saturation current is } I_S = qA_E D_n n_{p0}/W$$

and we can rewrite the saturation current as:

$$I_S = \frac{qA_E D_n n_i^2}{N_A W}$$

- Note that  $i_C$  is independent of  $v_{CB}$  (potential bias across CBJ) ideally
- Saturation current is
  - inversely proportional to  $W$  and directly proportional to  $A_E$ 
    - Want short base and large emitter area for high currents
  - dependent on temperature due to  $n_i^2$  term



# Base Current

- Base current  $i_B$  composed of two components:
  - holes injected from the base region into the emitter region

$$i_{B1} = \frac{qA_E D_p n_i^2}{N_D L_P} e^{v_{BE}/V_T}$$

- holes supplied due to recombination in the base with diffusing electrons and depends on minority carrier lifetime  $\tau_b$  in the base

$$i_{B2} = \frac{Q_n}{\tau_b}$$

And the Q in the base is

$$Q_n = \frac{qA_E W n_i^2}{N_A} e^{v_{BE}/V_T}$$

So, current is

$$i_{B2} = \frac{qA_E W n_i^2}{N_A \tau_b} e^{v_{BE}/V_T}$$

- Total base current is

$$i_B = \left( \frac{qA_E D_p n_i^2}{N_D L_P} + \frac{qA_E W n_i^2}{N_A \tau_b} \right) e^{v_{BE}/V_T}$$



# Beta

- Can relate  $i_B$  and  $i_C$  by the following equation

$$i_B = \frac{i_C}{\beta} = \frac{I_S}{\beta} e^{v_{BE}/V_T}$$

and  $\beta$  is

$$\beta = \frac{1}{\frac{D_p}{D_n} \frac{N_A}{N_D} \frac{W}{L_p} + \frac{1}{2} \frac{W^2}{D_n \tau_b}}$$

- **Beta** is constant for a particular transistor
- On the order of 100-200 in modern devices (but can be higher)
- Called the **common-emitter current gain**
- For high current gain, want small  $W$ , low  $N_A$ , high  $N_D$

# Current Relationships

Common-emitter  
current gain:  $\beta$

$$i_E = i_C + i_B$$

$$i_C = \beta i_B$$

Common-base  
current gain:  $\alpha$

$$i_E = (1 + \beta i_B)$$

$$i_C = \alpha i_E$$

$$\beta = \frac{\alpha}{1 - \alpha}$$

# Current Relationships

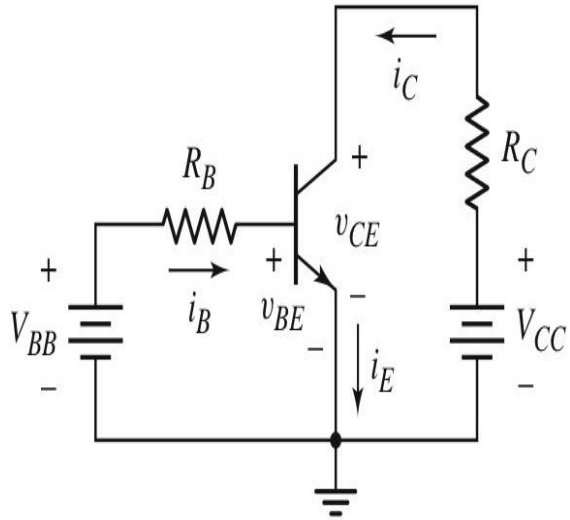
- Common-base current Gain  $\alpha$  :
  - $\alpha$  is the fraction of electrons that diffuse across the narrow Base region
  - $1 - \alpha$  is the fraction of electrons that recombine with holes in the Base region to create base current
- The common-emitter current Gain  $\beta$  is expressed in terms of the  $\beta$  (beta) of the transistor (often called  $h_{fe}$  by manufacturers).
- $\beta$  is **Temperature** and **Voltage** dependent.
- $\beta$  can vary a lot among transistors (common values for signal BJT: 20 - 200).

$$I_C = \alpha I_E$$

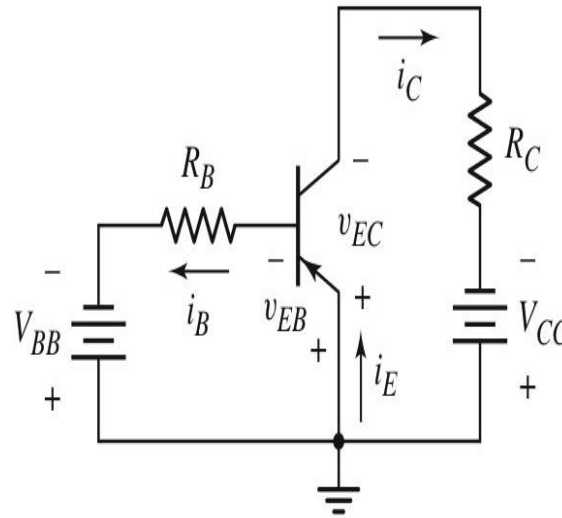
$$I_B = (1 - \alpha) I_E$$

$$\beta = \frac{I_C}{I_B} = \frac{\alpha}{1 - \alpha}$$

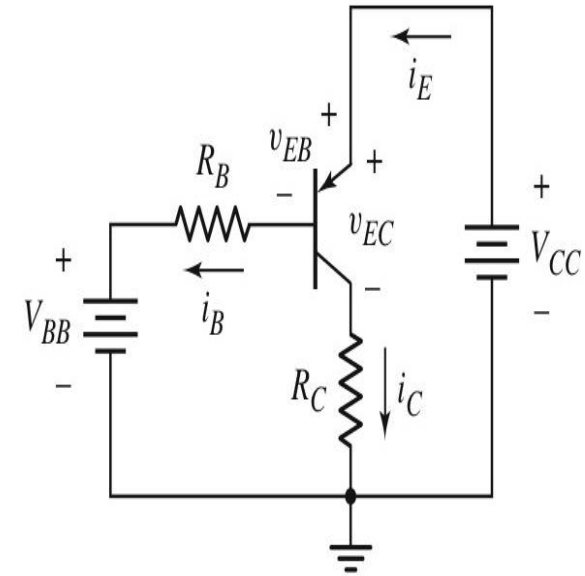
# Common-Emitter Configurations



(a)



(b)



(c)

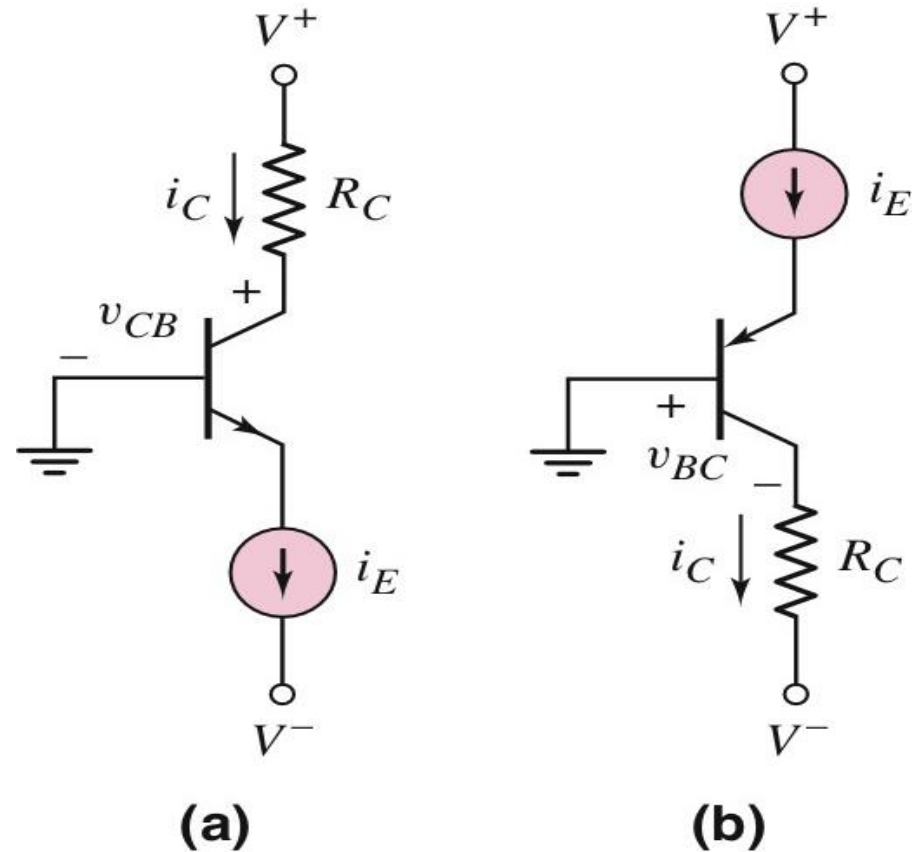
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(a) CE circuit with npn transistor

(b) CE circuit with pnp transistor

(c) CE circuit with pnp transistor with a positive voltage source

# Common-Base Configuration

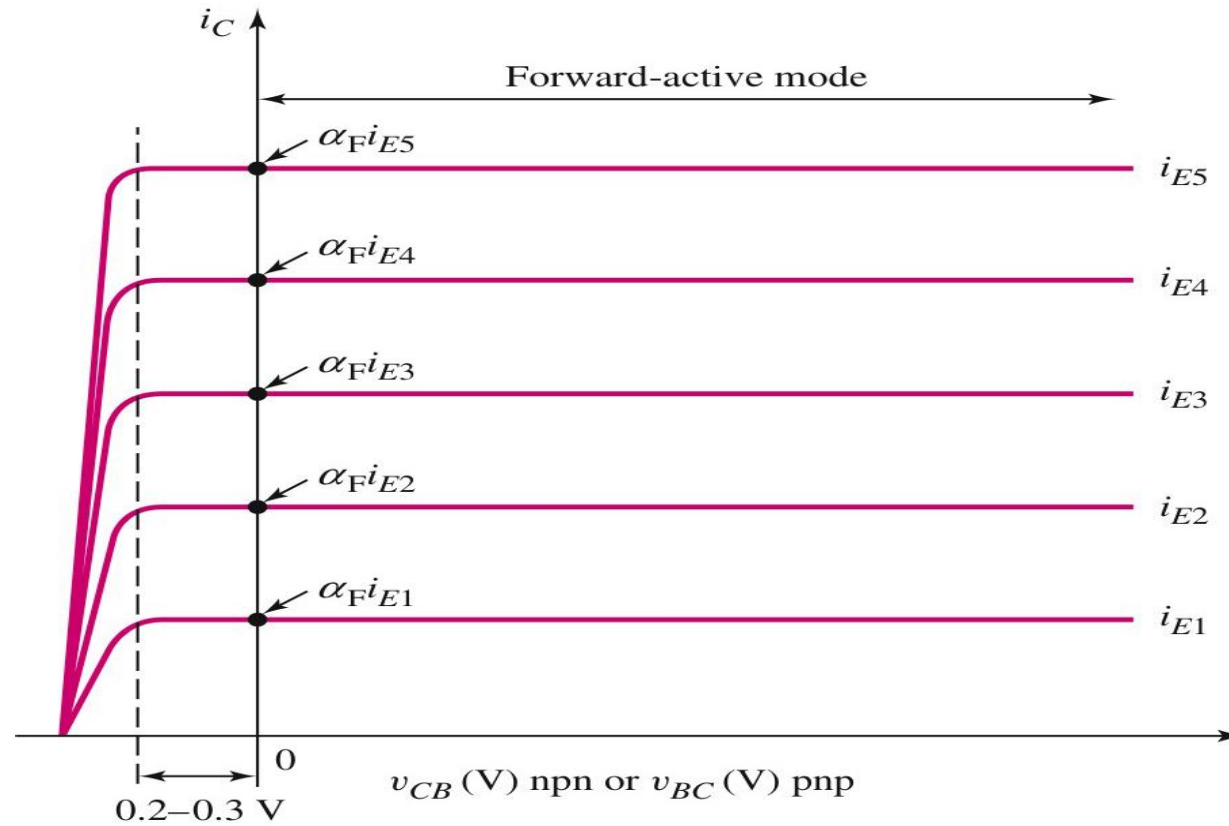


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The common-base device is nearly an ideal constant current source.

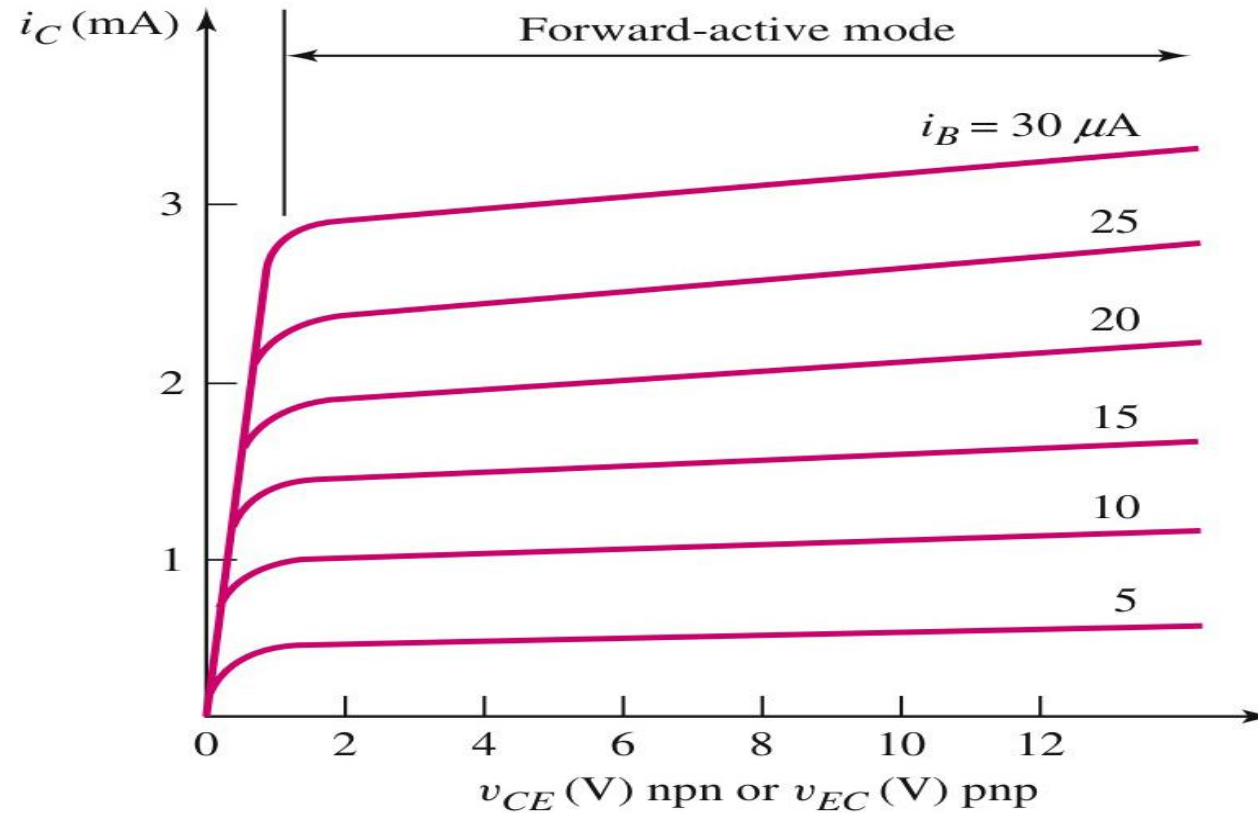
Common-base current gain:  $\alpha$

# Current-Voltage Characteristics of a Common-Base Circuit



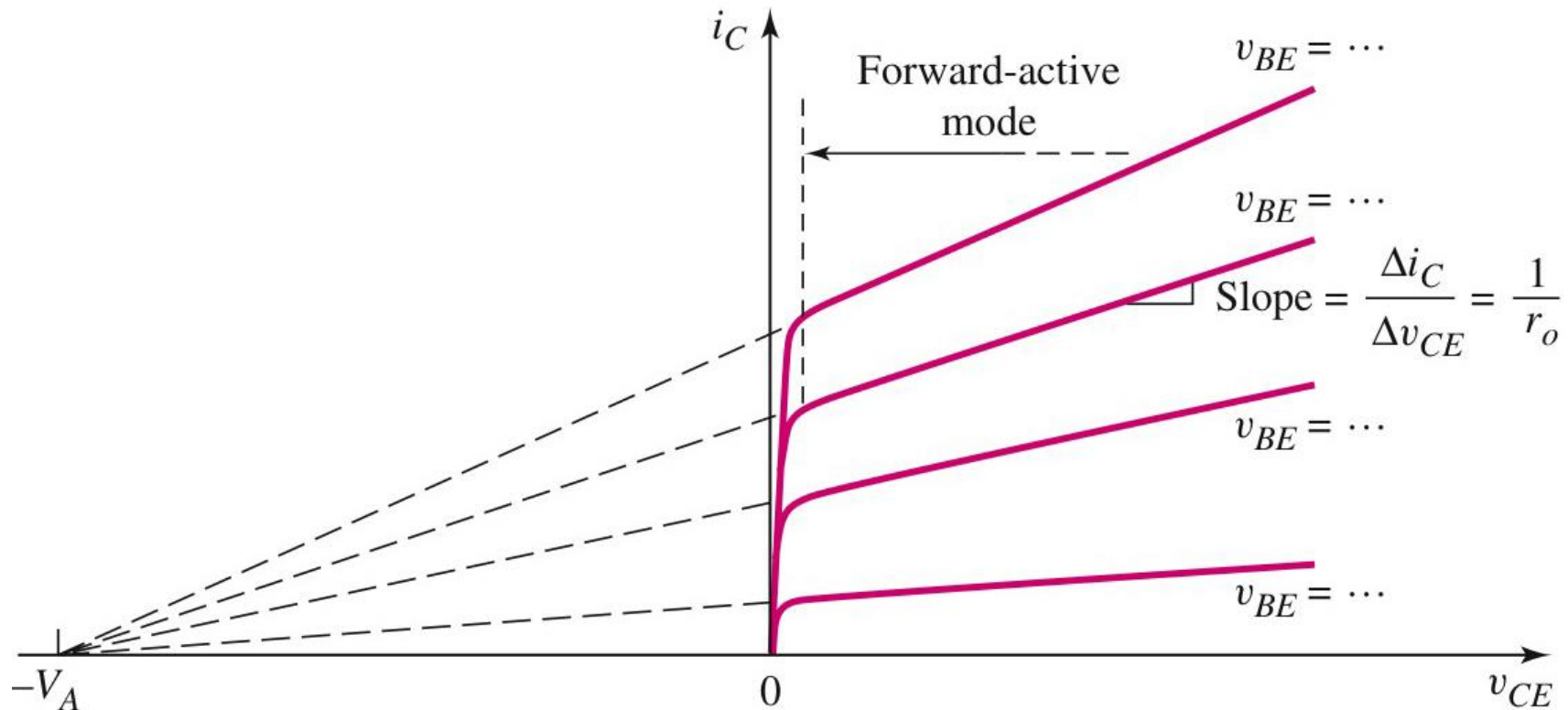
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# Current-Voltage Characteristics of a Common-Emitter Circuit



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# Early Voltage/Finite Output Resistance



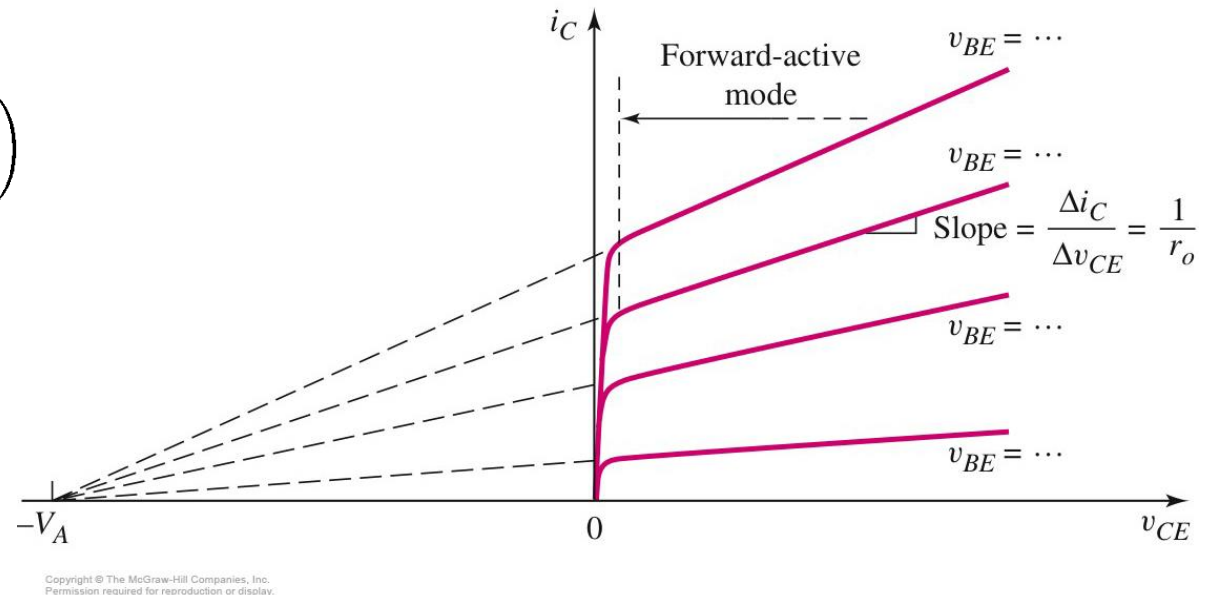
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**Base-width modulation – Early Effect!**



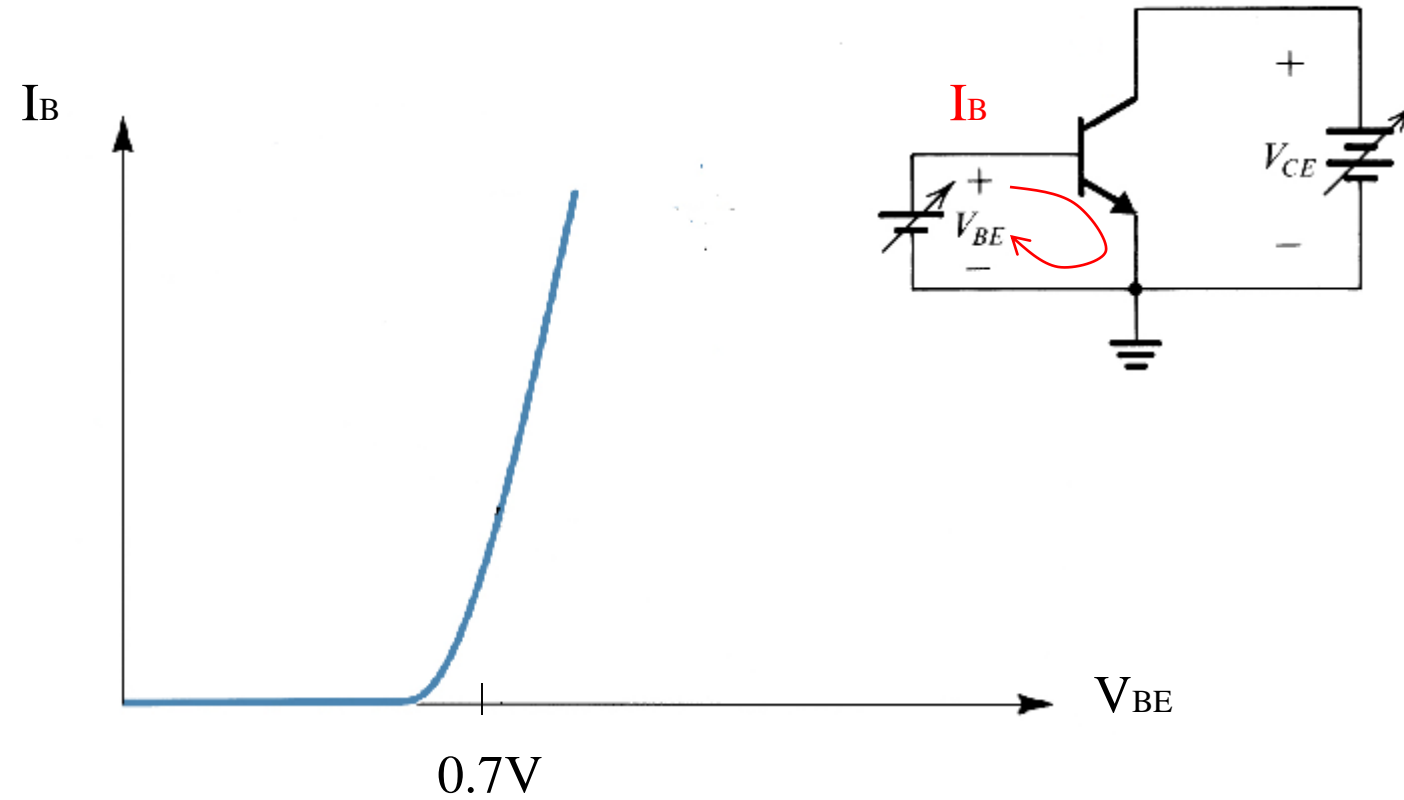
# Early Effect

$$I_C = I_S e^{V_{BE}/V_T} \left( 1 + \frac{V_{CE}}{V_A} \right)$$



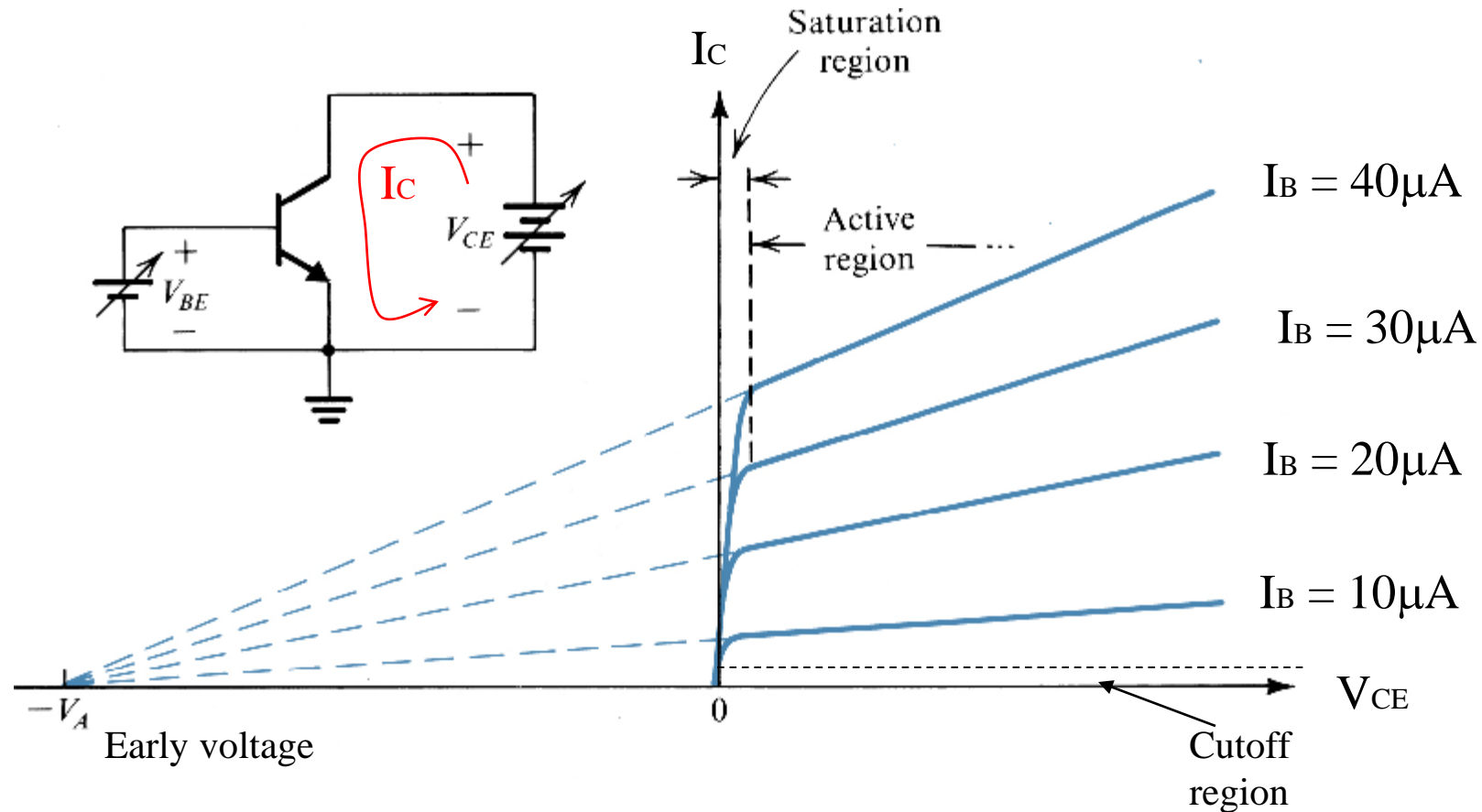
- Early Effect
  - Current in active region depends (slightly) on  $v_{CE}$
  - $V_A$  is a parameter for the BJT (50 to 100) and called the Early voltage
  - Due to a decrease in effective base width  $W$  as reverse bias increases
  - Account for Early effect with additional term in collector current equation
  - Nonzero slope means the output resistance is NOT infinite, but...
    - $I_C$  is collector current at the boundary of active region

## Summary: Input characteristics



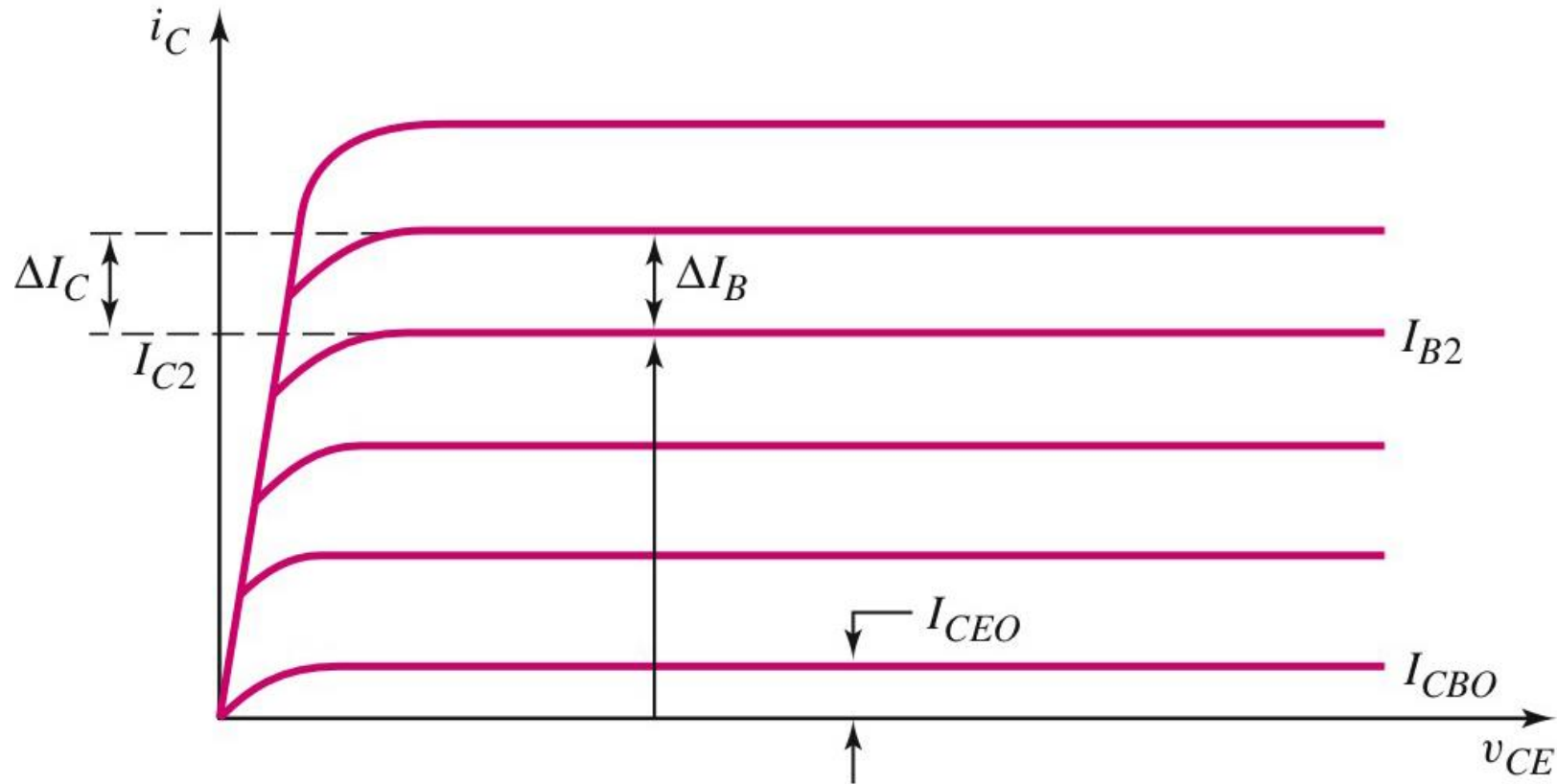
- Acts as a diode
- $V_{BE} \approx 0.7V$

# Summary: Output characteristics



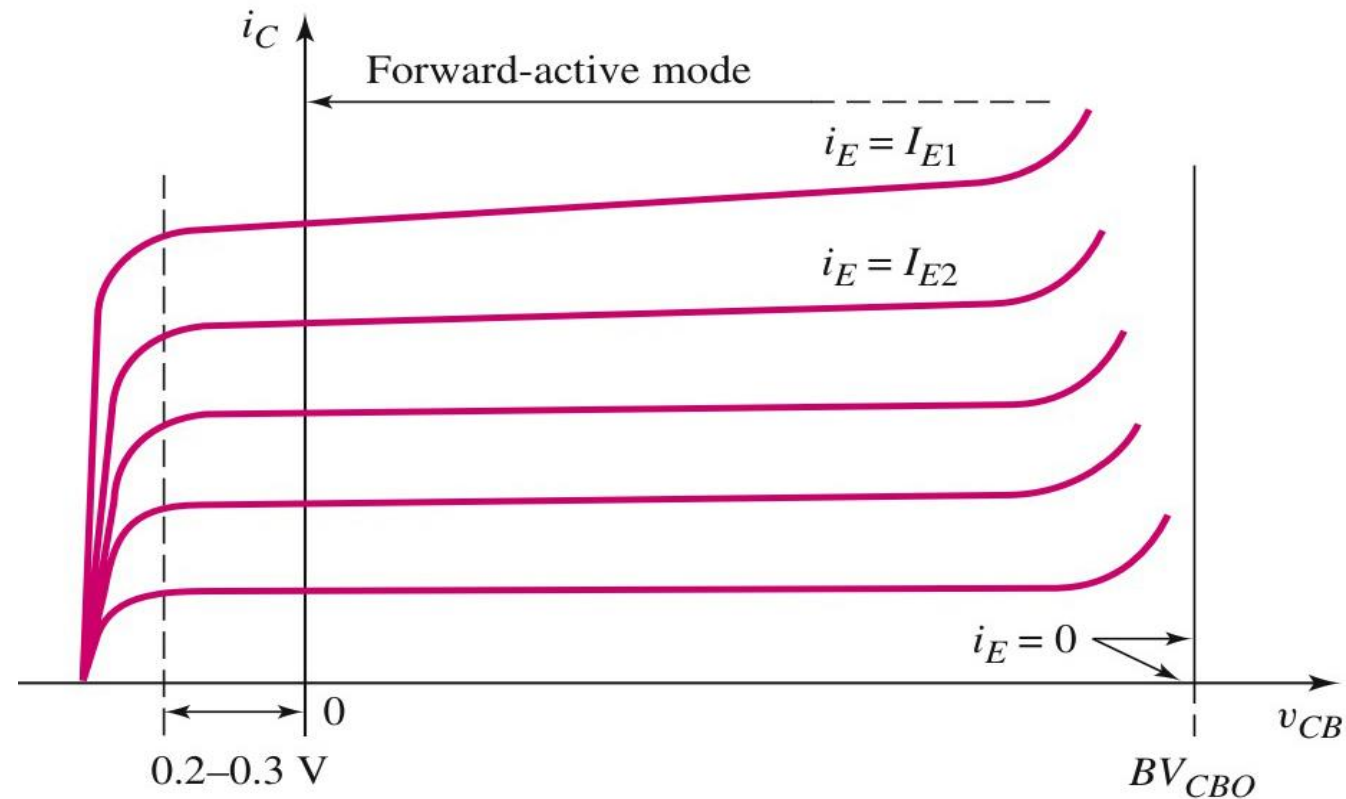
- At a fixed  $I_B$ ,  $I_C$  is not dependent on  $V_{CE}$
- Slope of output characteristics in linear region is near 0 (scale exaggerated)

# Effects of Leakage Currents on I-V Characteristics



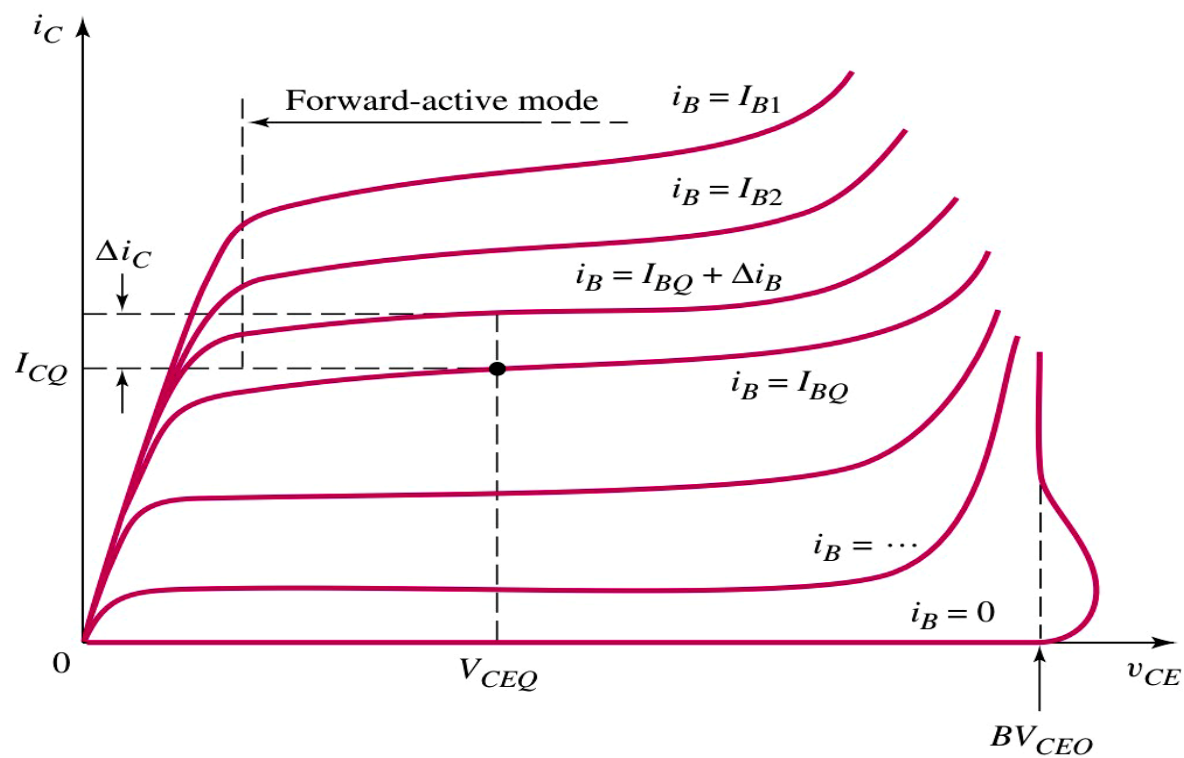
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# Effect of Collector-Base Breakdown on Common Base I-V Characteristics



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# Effect of Collector-Base Breakdown on Common Emitter I-V Characteristics



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# Breakdown Voltages

- The basic limitation of the max. voltage in a transistor is the same as that in a *pn* junction diode.
- However, the voltage breakdown depends not only on the nature of the junction involved but also on the external circuit arrangement.
- In **Common Base** configuration, the maximum voltage between the collector and base with the emitter open,  $BV_{CBO}$  is determined by the avalanche breakdown voltage of the CBJ.
- In **Common Emitter** configuration, the maximum voltage between the collector and emitter with the base open,  $BV_{CEO}$  can be much smaller than  $BV_{CBO}$ .

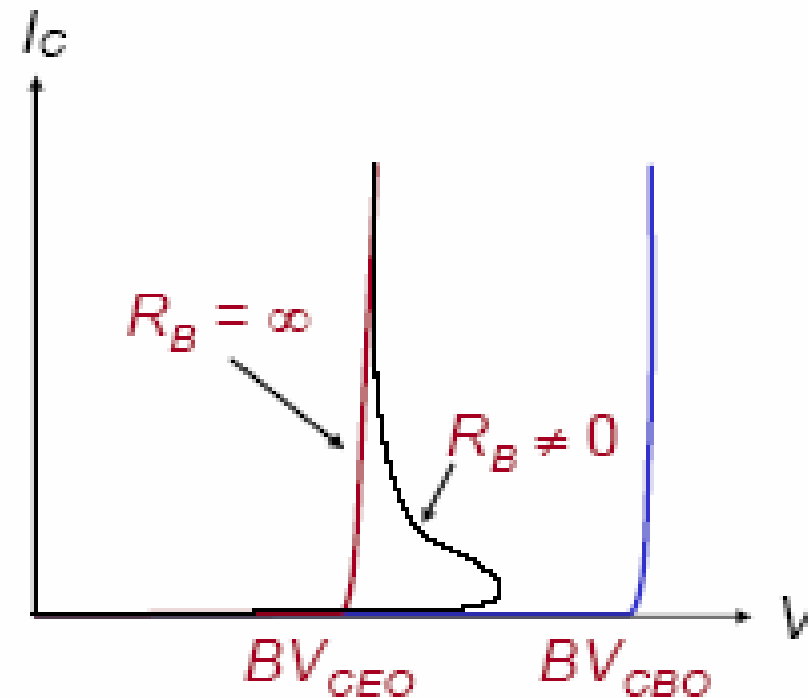
# Breakdown Voltages

In general,  $BV_{CEO}$  is related to  $BV_{CBO}$  by the following expression,

$$BV_{CEO} = BV_{CBO} \sqrt[n]{1 - \alpha} \approx BV_{CBO} / \sqrt[n]{\beta}$$

The typical value of  $n$  is between 2 to 4 in silicon.

In general, the actual breakdown voltage is between  $BV_{CEO}$  and  $BV_{CBO}$ , depending on the external resistance seen by the base,  $R_B$ .





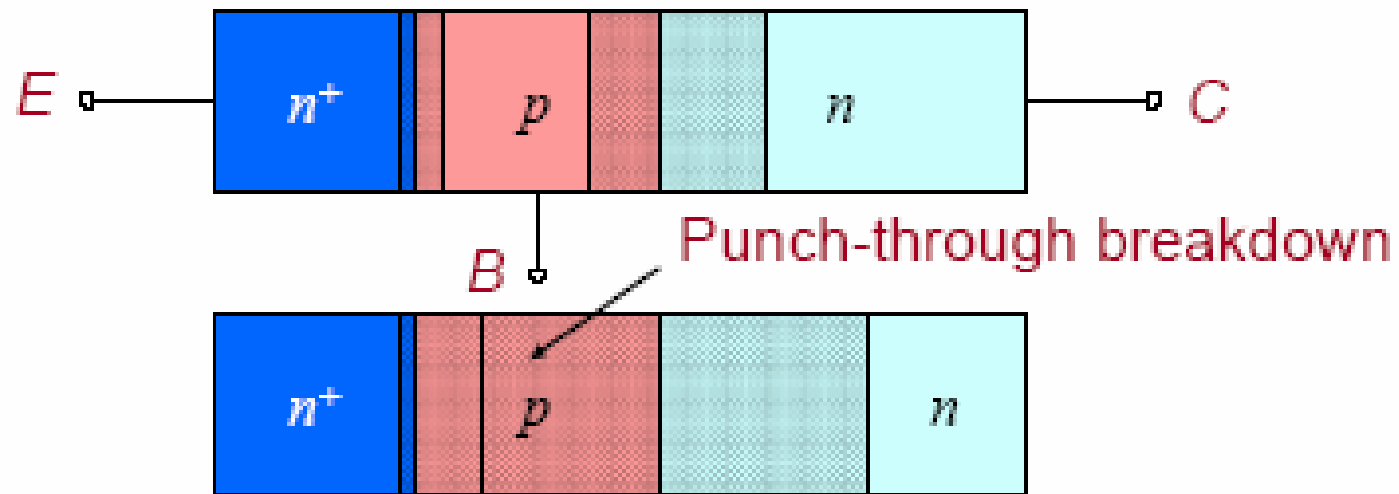
# Breakdown Voltages

- For a planar abrupt  $p+n$  junction, the avalanche breakdown voltage is given by

$$BV = \frac{\epsilon_s \epsilon_0 E_{crit}^2}{2qN_D}$$

where  $E_{crit}$  is the critical electric field, and  $N_D$  is the doping concentration for the low doping region.

# Breakdown Voltages



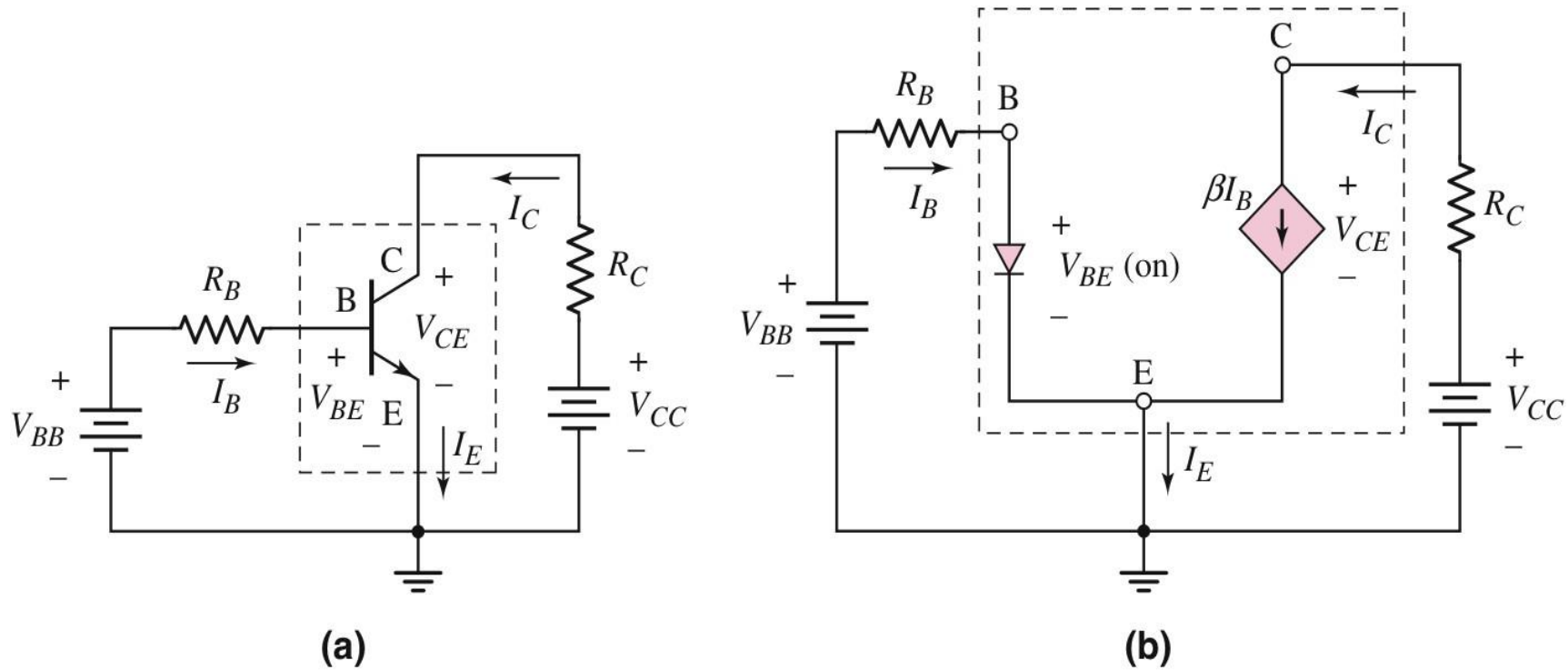
- As  $V_{CB}$  (or  $V_{CE}$ ) increases, the depletion region will continue to spread into the base region.
- If the base becomes completely depleted, the depletion region from the collector and emitter touch each other, resulting in a short between the  $n^+$  and  $n$  regions.

# Operation region summary

<b>Operation Region</b>	<b><math>I_B</math> or <math>V_{CE}</math> Char.</b>	<b>BC and BE Junctions</b>	<b>Mode</b>
<b>Cutoff</b>	$I_B$ = Very small	Reverse & Reverse	Open Switch
<b>Saturation</b>	$V_{CE}$ = Small	Forward & Forward	Closed Switch
<b>Active Linear</b>	$V_{CE}$ = Moderate	Reverse & Forward	Linear Amplifier
<b>Break-down</b>	$V_{CE}$ = Large	Beyond Limits	Overload

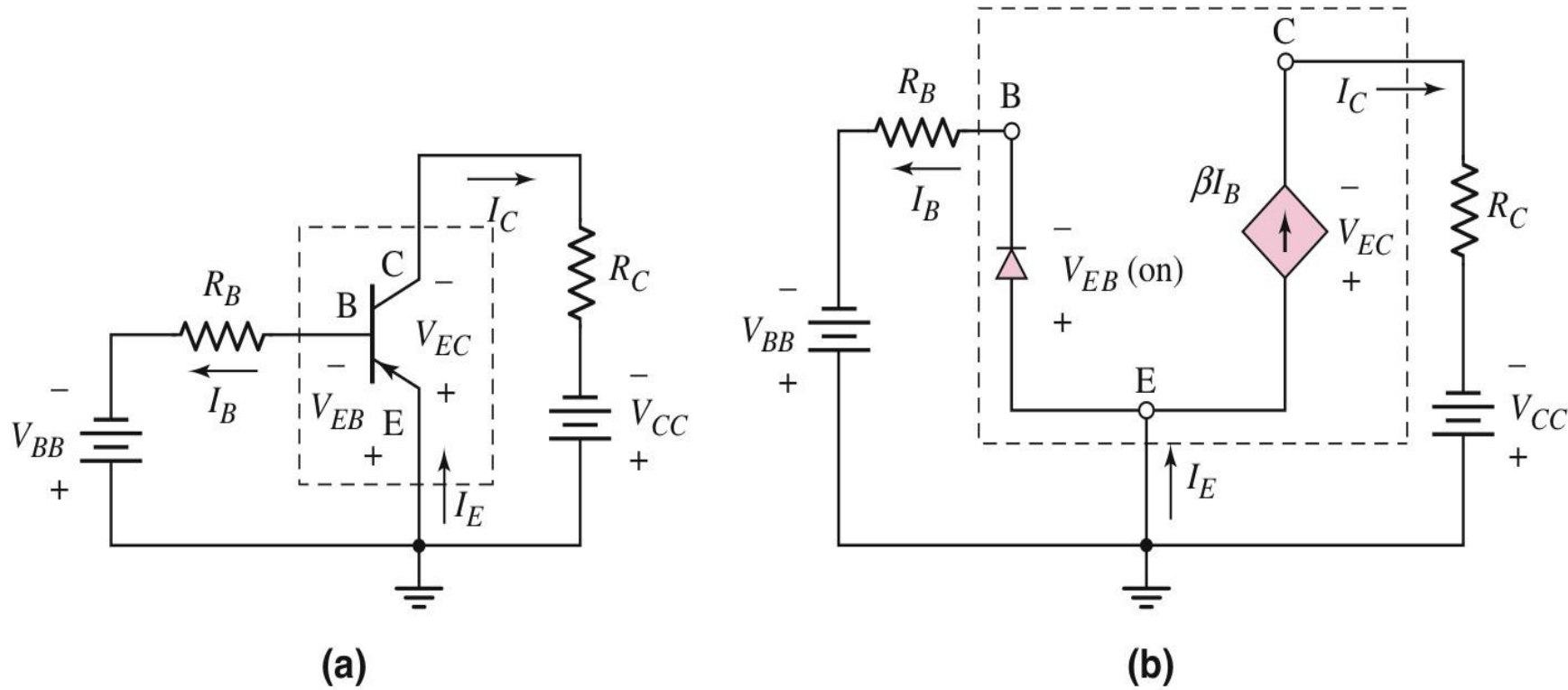
# DC Equivalent Circuit

# DC Equivalent Circuit for npn Common Emitter



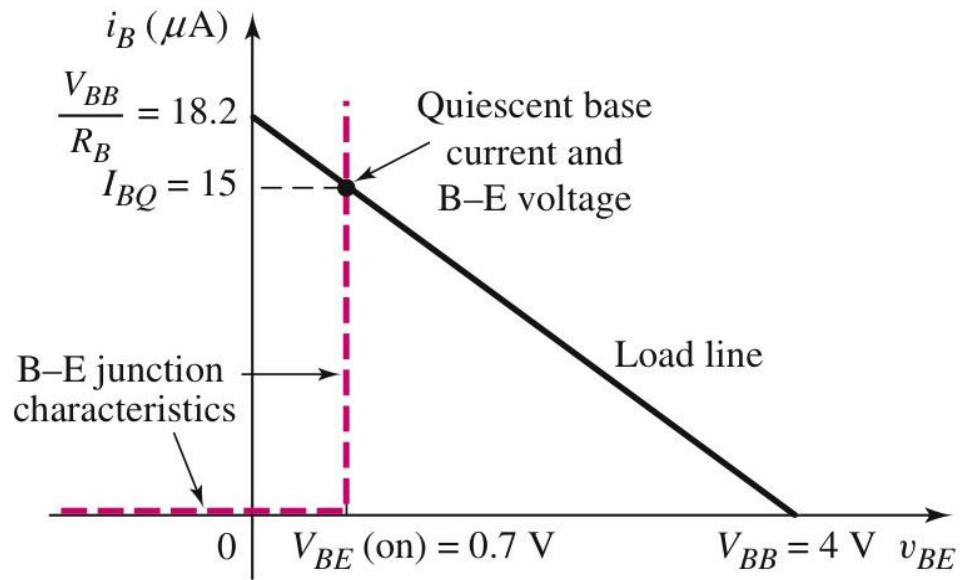
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# DC Equivalent Circuit for pnp Common Emitter

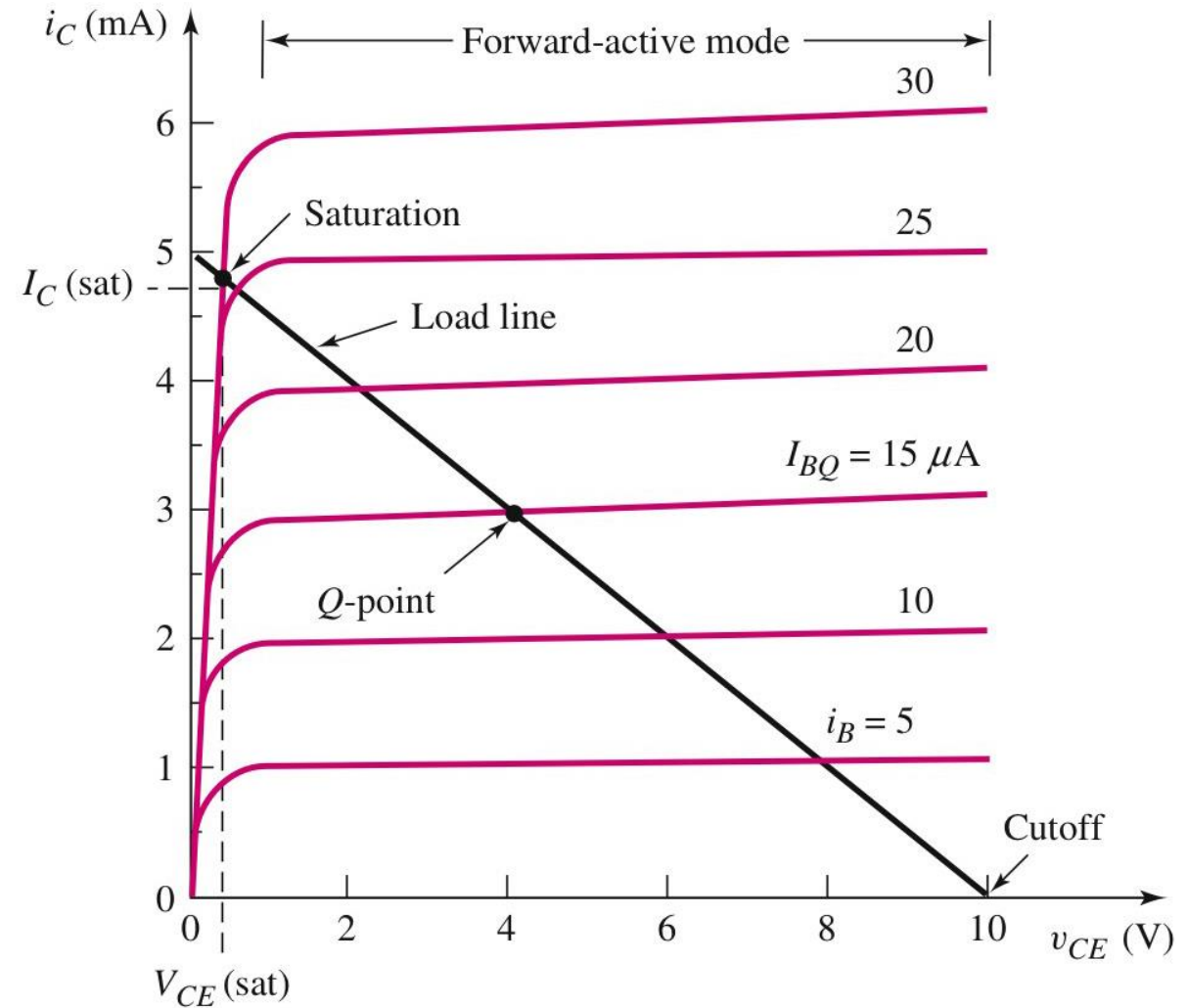


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# Load Line



(a)



(b)

# Problem-Solving Technique: Bipolar DC Analysis

1. Assume that the transistor is biased in forward active mode
  - a.  $V_{BE} = V_{BE}(\text{on})$ ,  $I_B > 0$ , &  $I_C = \beta I_B$
2. Analyze 'linear' circuit.
3. Evaluate the resulting state of transistor.
  - a. If  $V_{CE} > V_{CE}(\text{sat})$ , assumption is correct
  - b. If  $I_B < 0$ , transistor likely in cutoff
  - c. If  $V_{CE} < 0$ , transistor likely in saturation
4. If initial assumption is incorrect, make new assumption and return to Step 2.

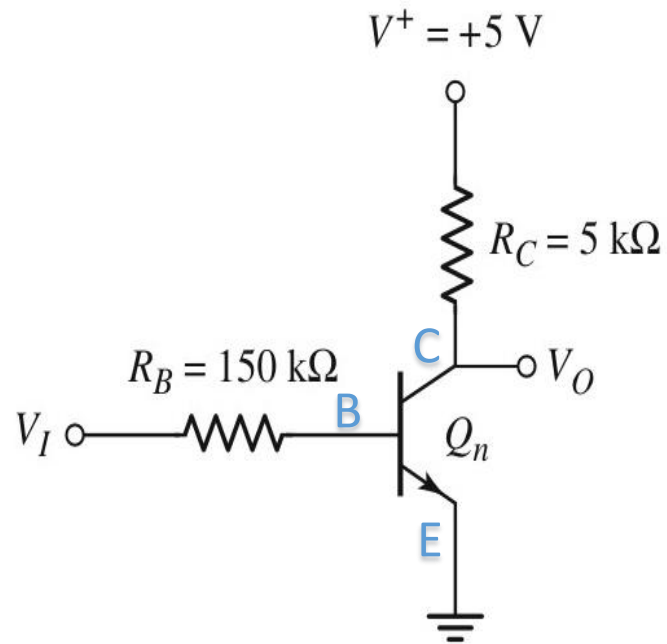


# Summary of DC Problem

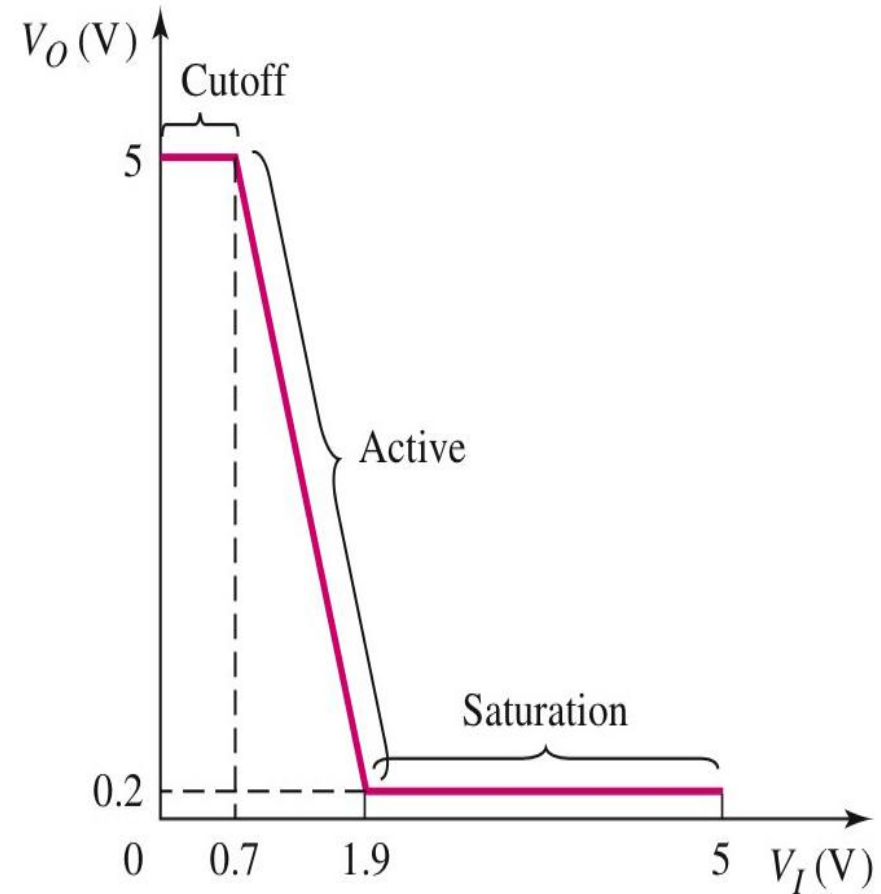
- Bias transistors so that they operate in the linear region B-E junction forward biased, C-E junction reversed biased
- Use  $V_{BE} = 0.7$  (npn),  $I_C \approx I_E$ ,  $I_C = I_B$
- Represent base portion of circuit by the Thevenin circuit
- Write B-E, and C-E voltage loops.
- For analysis, solve for  $I_C$ , and  $V_{CE}$ .
- For design, solve for resistor values ( $I_C$  and  $V_{CE}$  specified).

# Voltage Transfer Characteristic

# Voltage Transfer Characteristic for npn Circuit



(a)

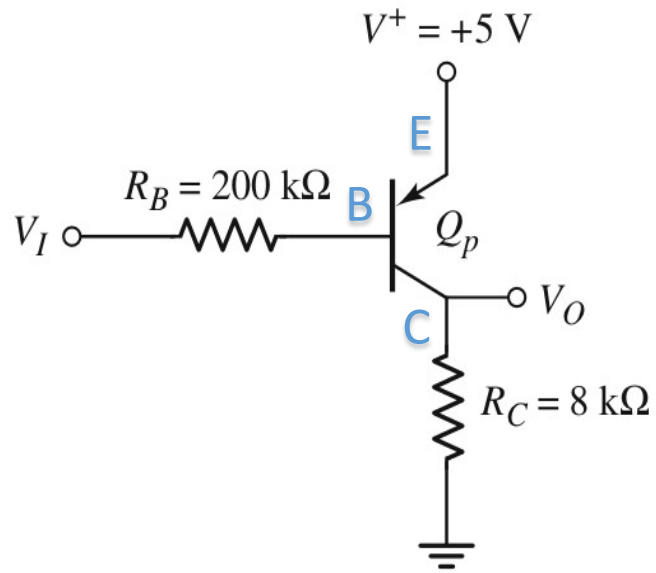


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$$V_{CE}(\text{sat}) = 0.2\text{ V}$$

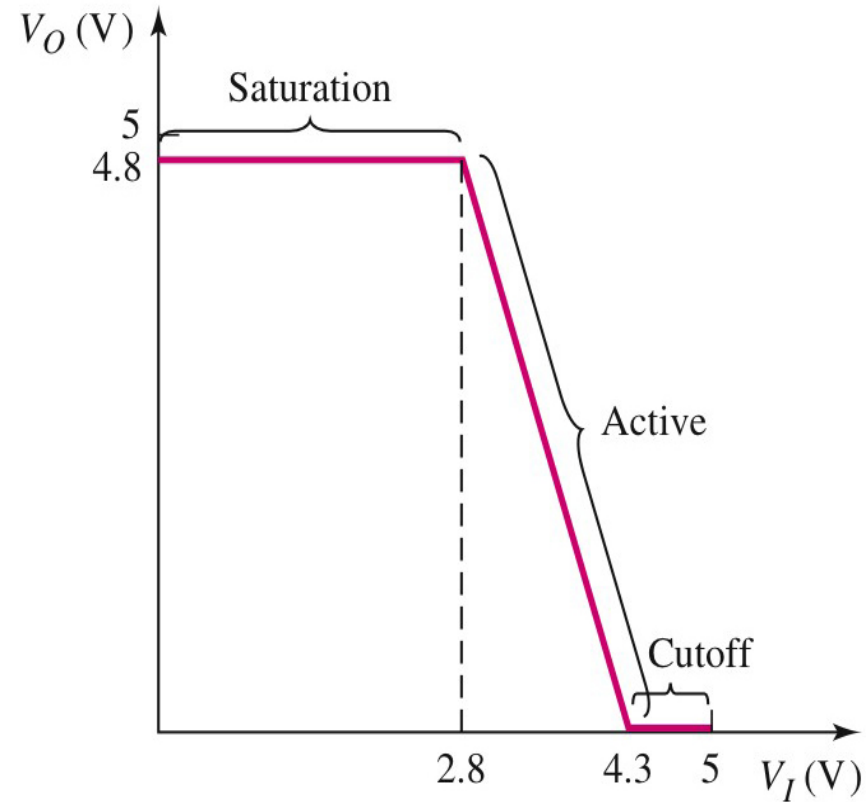
$$\beta = 120$$

# Voltage Transfer Characteristic for pnp Circuit



(b)

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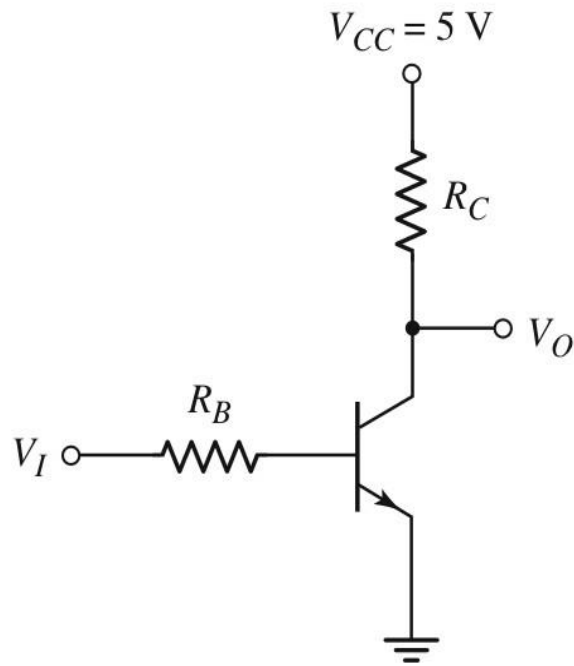
$$V_{EC}(\text{sat}) = 0.2\text{ V}$$

$$\beta = 80$$

$$V_{EB} < 0.7\text{ V}$$

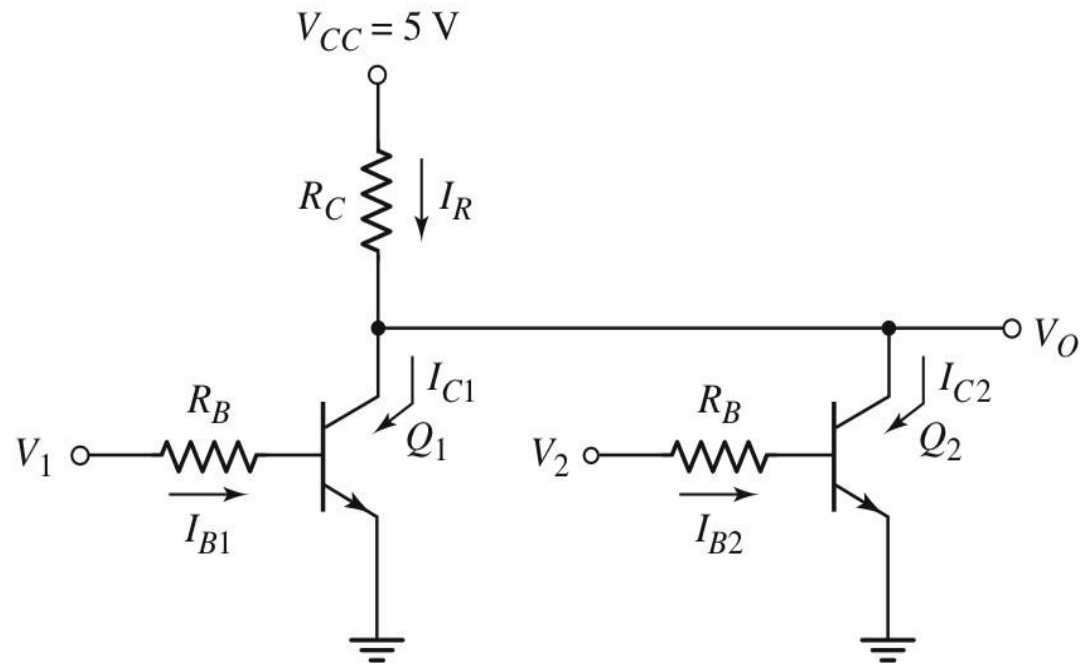
# Digital Logic Circuit

# Digital Logic



(a)

Inverter



(b)

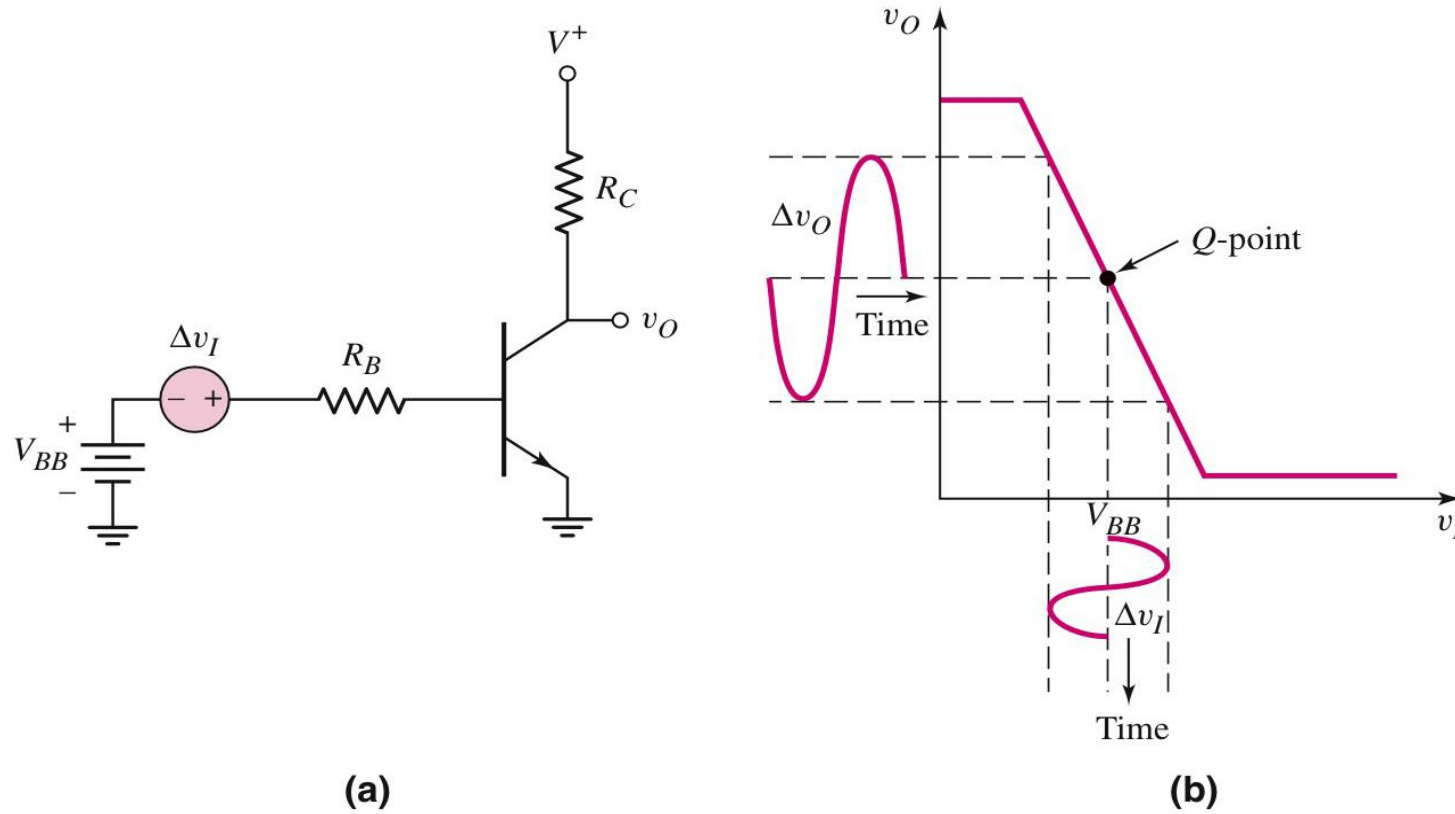
NOR gate

INPUT		OUTPUT
A	B	A NOR B
0	0	1
0	1	0
1	0	0
1	1	0

$V_1$ (V)	$V_2$ (V)	$V_O$ (V)
0	0	5
5	0	0.2
0	5	0.2
5	5	0.2

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# Bipolar Inverter as Amplifier

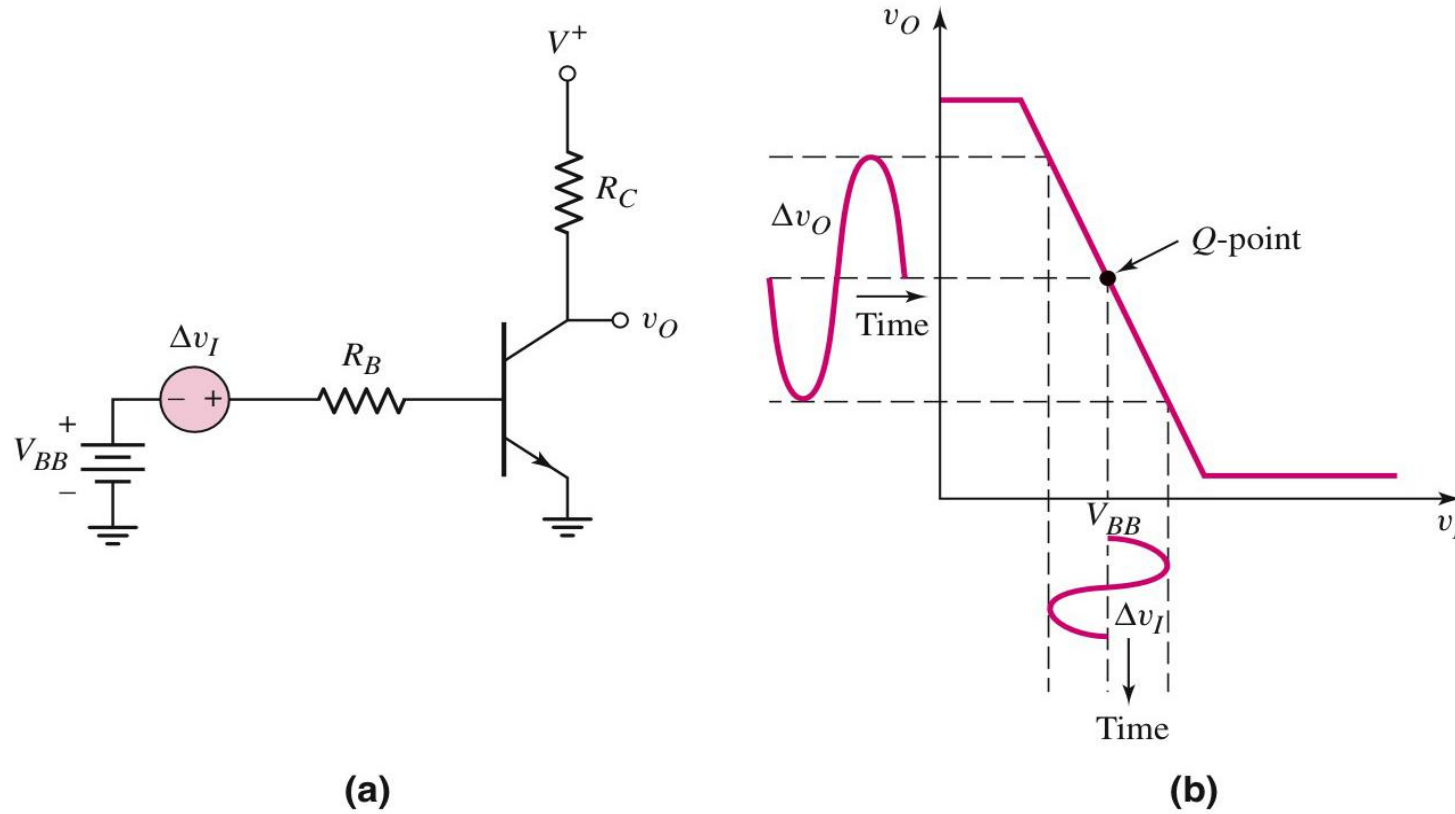


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# Bipolar Transistor Biasing

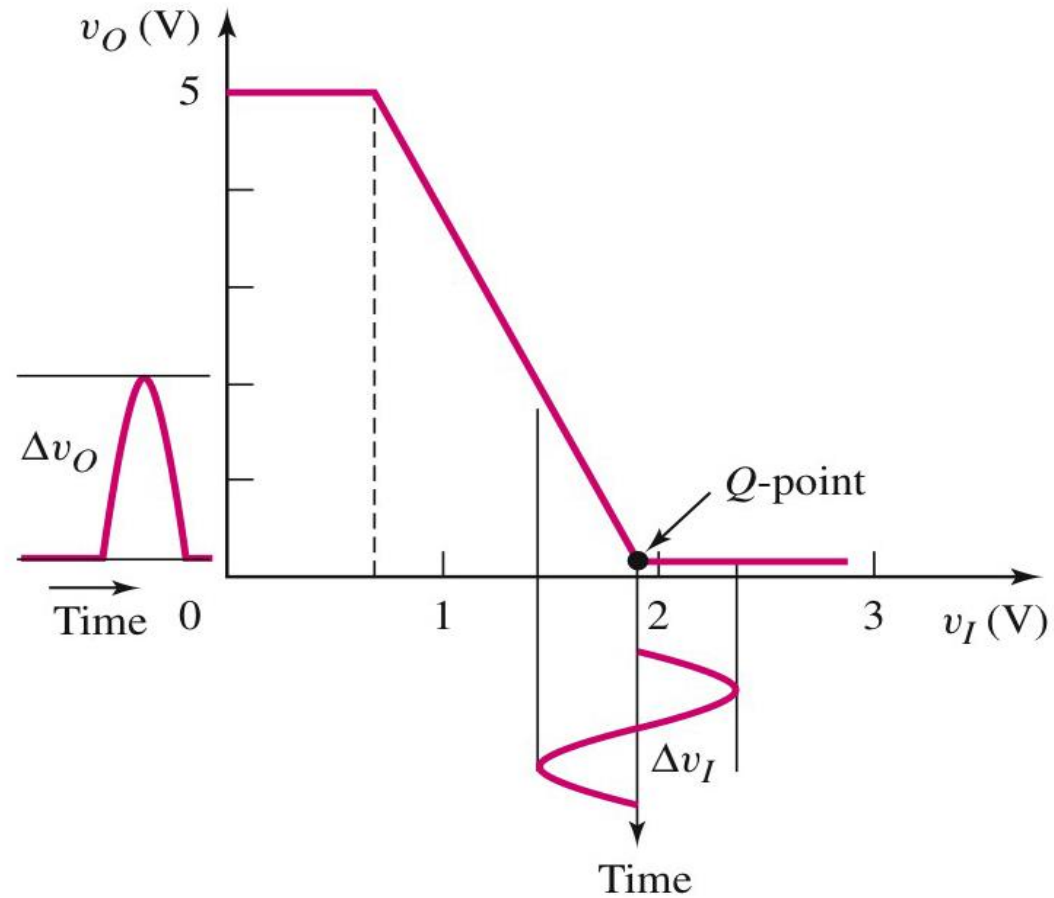


# Bipolar Inverter as Amplifier



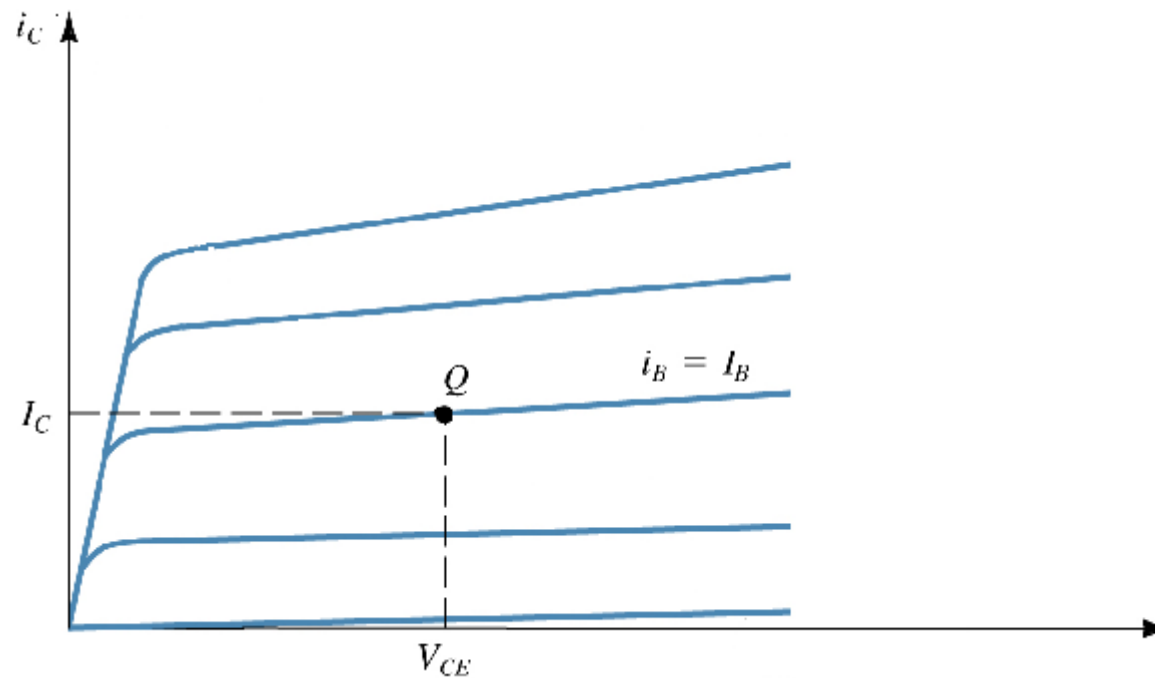
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# Effect of Improper Biasing on Amplified Signal Waveform

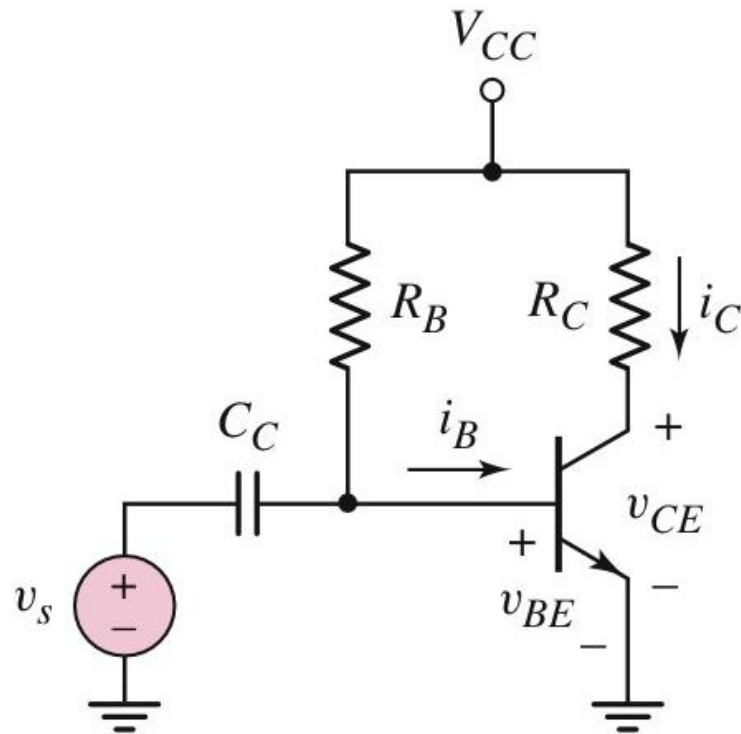


# Biasing a Transistor

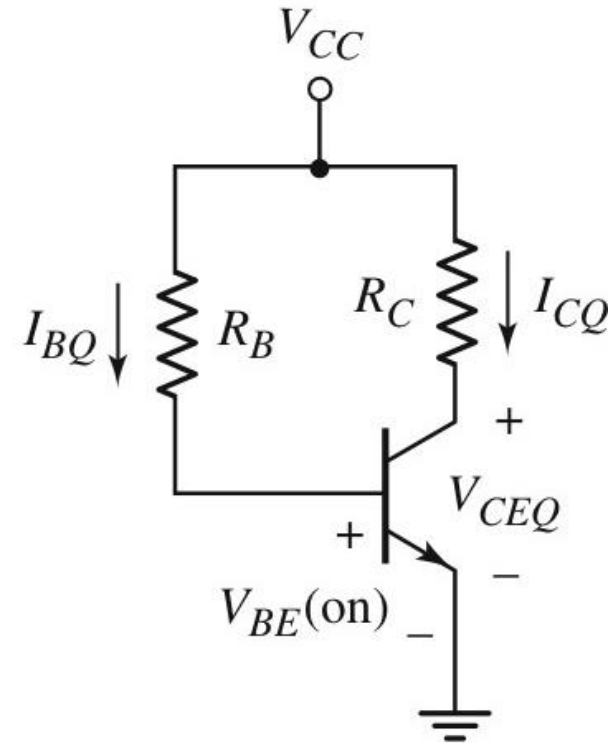
- We must operate the transistor in the linear region.
- A transistor's operating point (Q-point) is defined by  $I_C$ ,  $V_{CE}$ , and  $I_B$ .



# Single Base Resistor Biasing



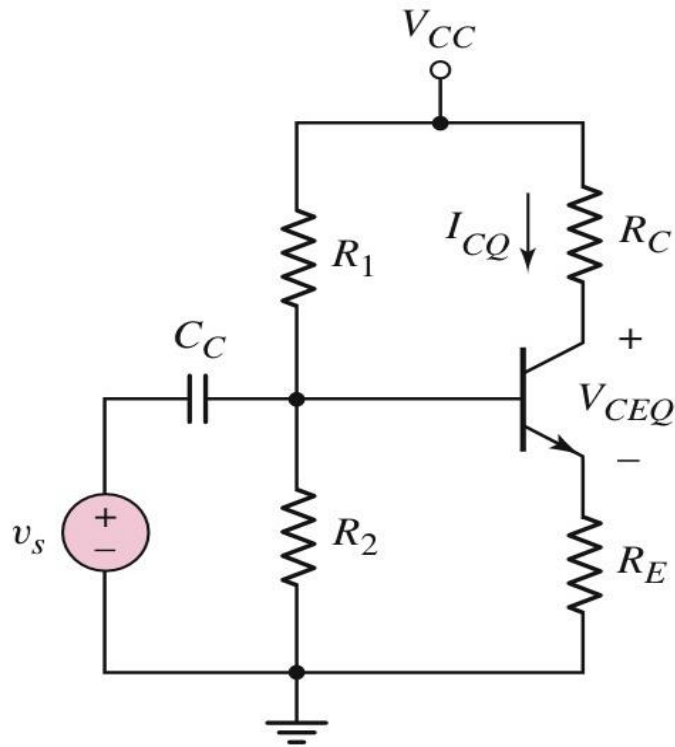
(a)



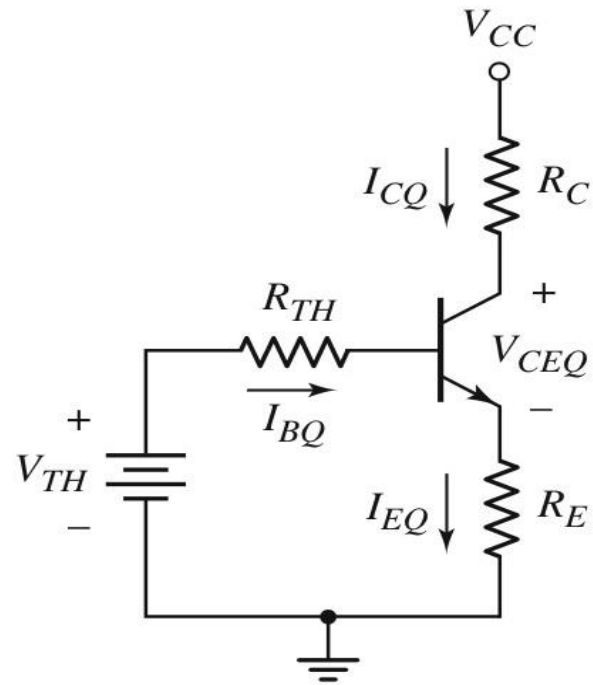
(b)

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# Common Emitter with Voltage Divider Biasing and Emitter Resistor



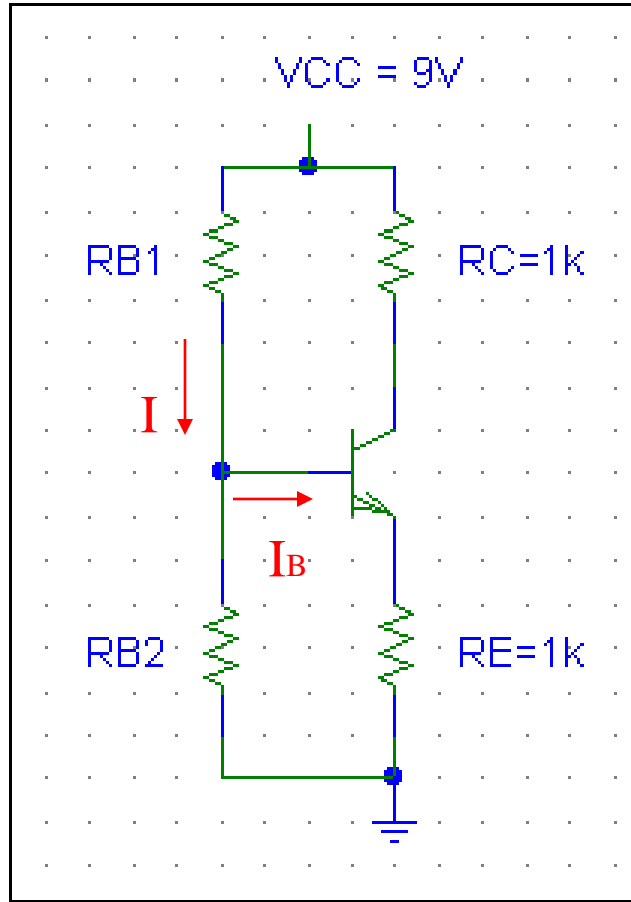
(a)



(b) 
$$V_{TH} = [R_2 / (R_1 + R_2)] V_{CC}$$

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## Example:



- Use a voltage divider,  $R_{B1}$  and  $R_{B2}$  to bias  $V_B$  to avoid two power supplies.
- Make the current in the voltage divider about 10 times  $I_B$  to simplify the analysis. Use  $V_B = 3V$  and  $I = 0.2mA$ .

(a)  $R_{B1}$  and  $R_{B2}$  form a voltage divider.

Assume  $I \gg I_B$   $I = V_{CC}/(R_{B1} + R_{B2})$

$$.2mA = 9 / (R_{B1} + R_{B2})$$

AND

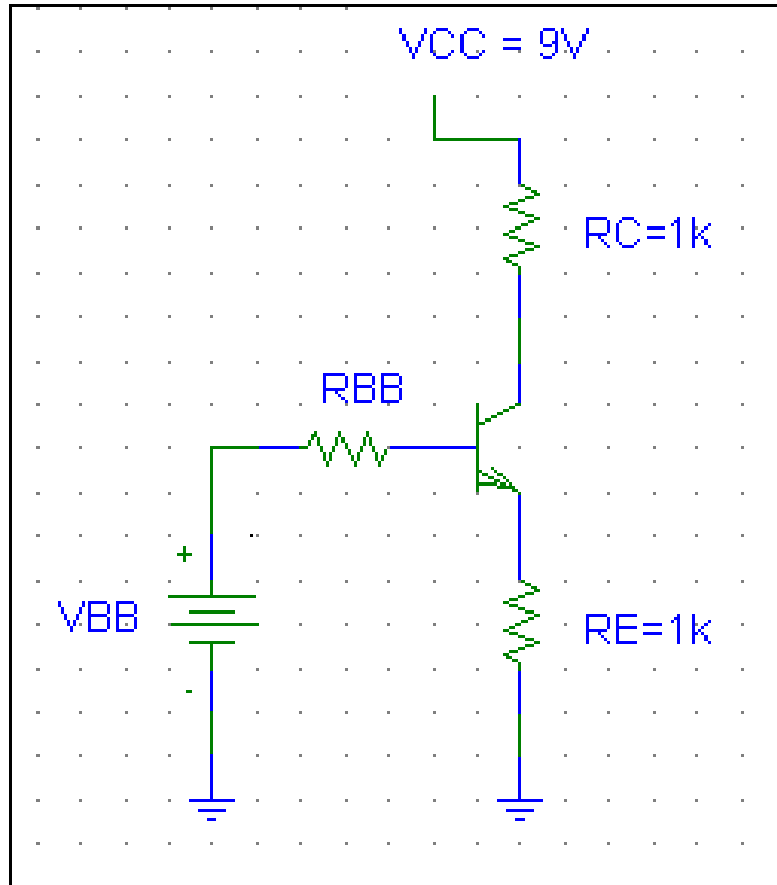
$$V_B = V_{CC}[R_{B2}/(R_{B1} + R_{B2})]$$

$3 = 9 [R_{B2}/(R_{B1} + R_{B2})]$ , Solve for  $R_{B1}$  and  $R_{B2}$ .

$R_{B1} = 30K\Omega$ , and  $R_{B2} = 15K\Omega$ .

## Example (Cont')

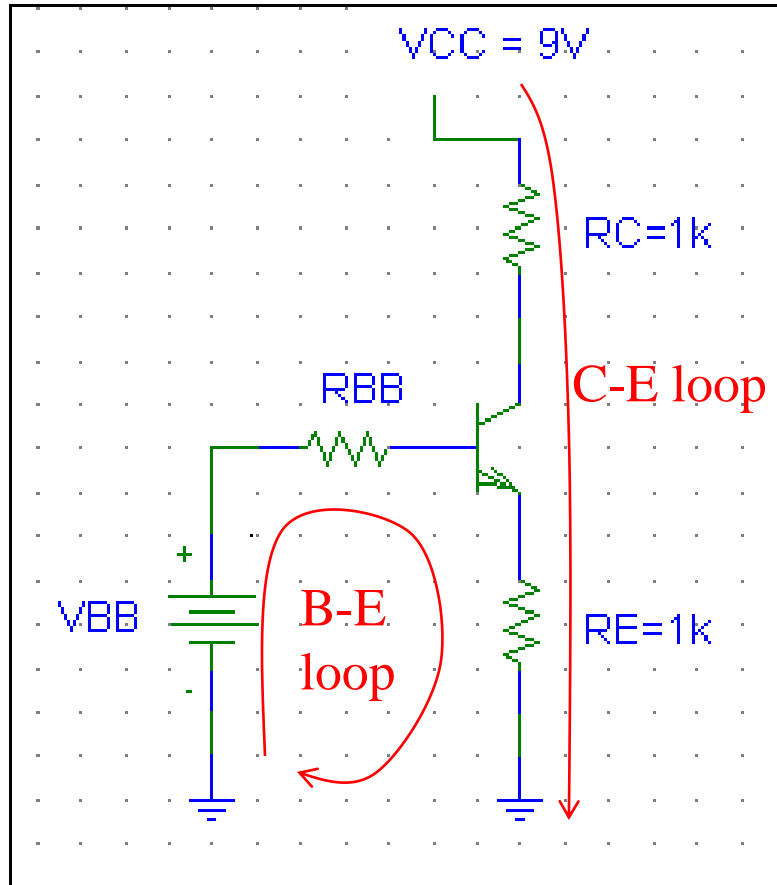
Find the operating point



- Use the Thevenin equivalent circuit for the base
- Makes the circuit simpler
- $V_{BB} = V_B = 3V$
- $R_{BB}$  is measured with voltage sources grounded
- $R_{BB} = R_{B1} \parallel R_{B2} = 30K\Omega \parallel 15K\Omega = 10K\Omega$

## Example (Cont')

Write B-E loop and C-E loop



B-E loop

$$V_{BB} = I_B R_{BB} + V_{BE} + I_E R_E$$

$$I_E = 2.09 \text{ mA}$$

C-E loop

$$V_{CC} = I_C R_C + V_{CE} + I_E R_E$$

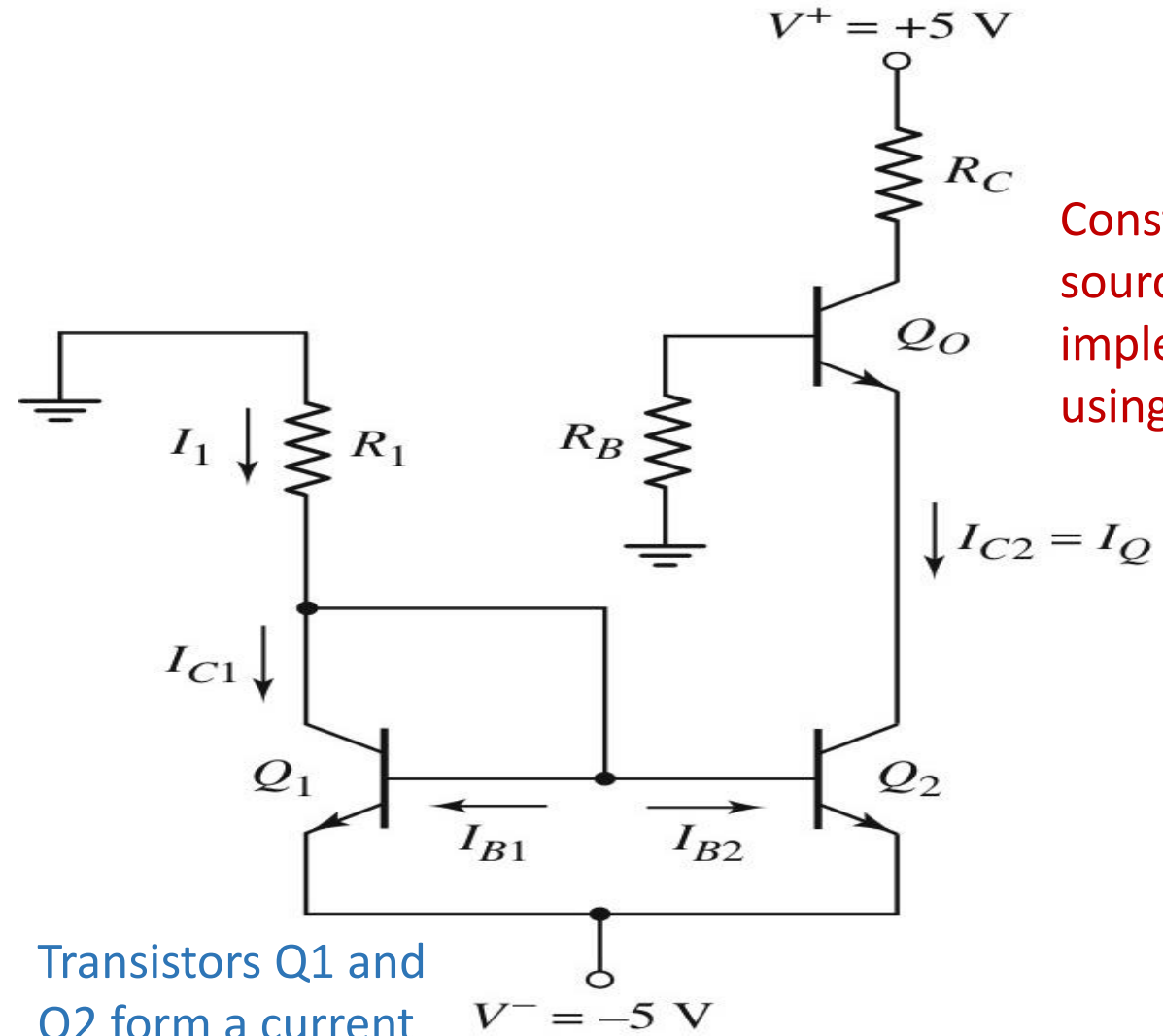
$$V_{CE} = 4.8 \text{ V}$$

This is how all DC circuits are analyzed  
and designed!



## Integrated Circuit Biasing

$$I_C = I_Q = \frac{I_1}{1 + \frac{2}{\beta}}$$



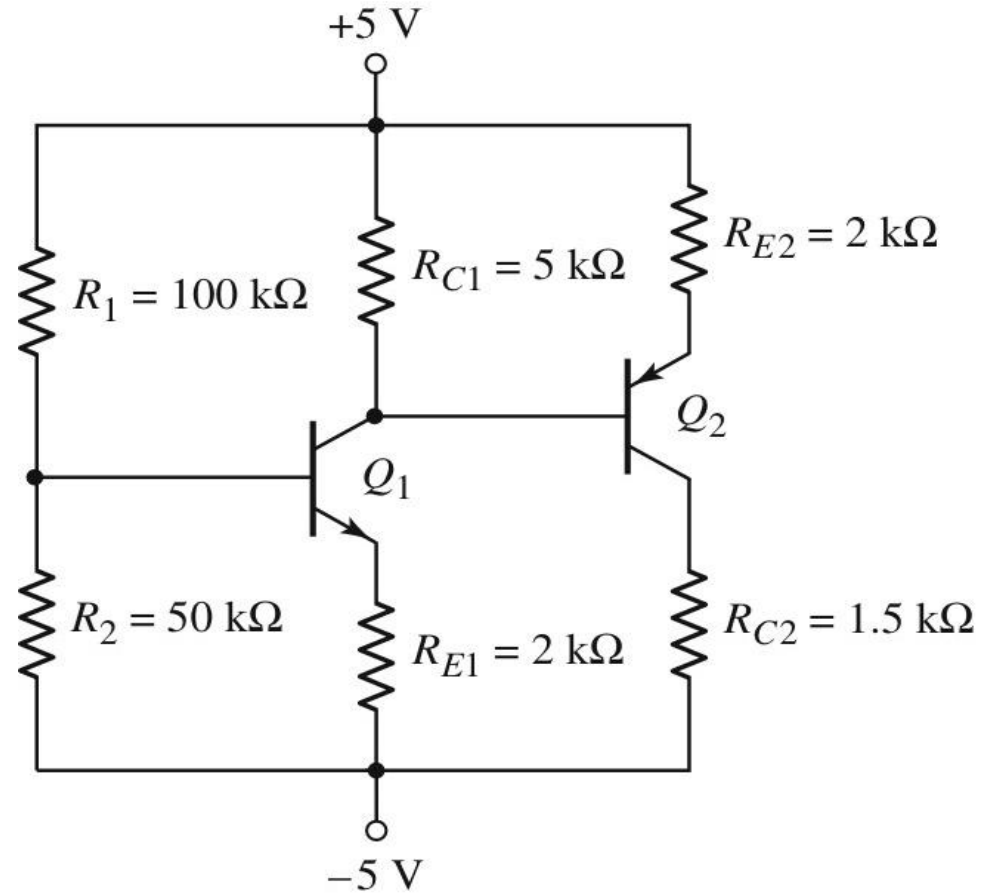
Constant current  
source  
implemented by  
using transistors.

Transistors  $Q_1$  and  
 $Q_2$  form a current  
mirror.

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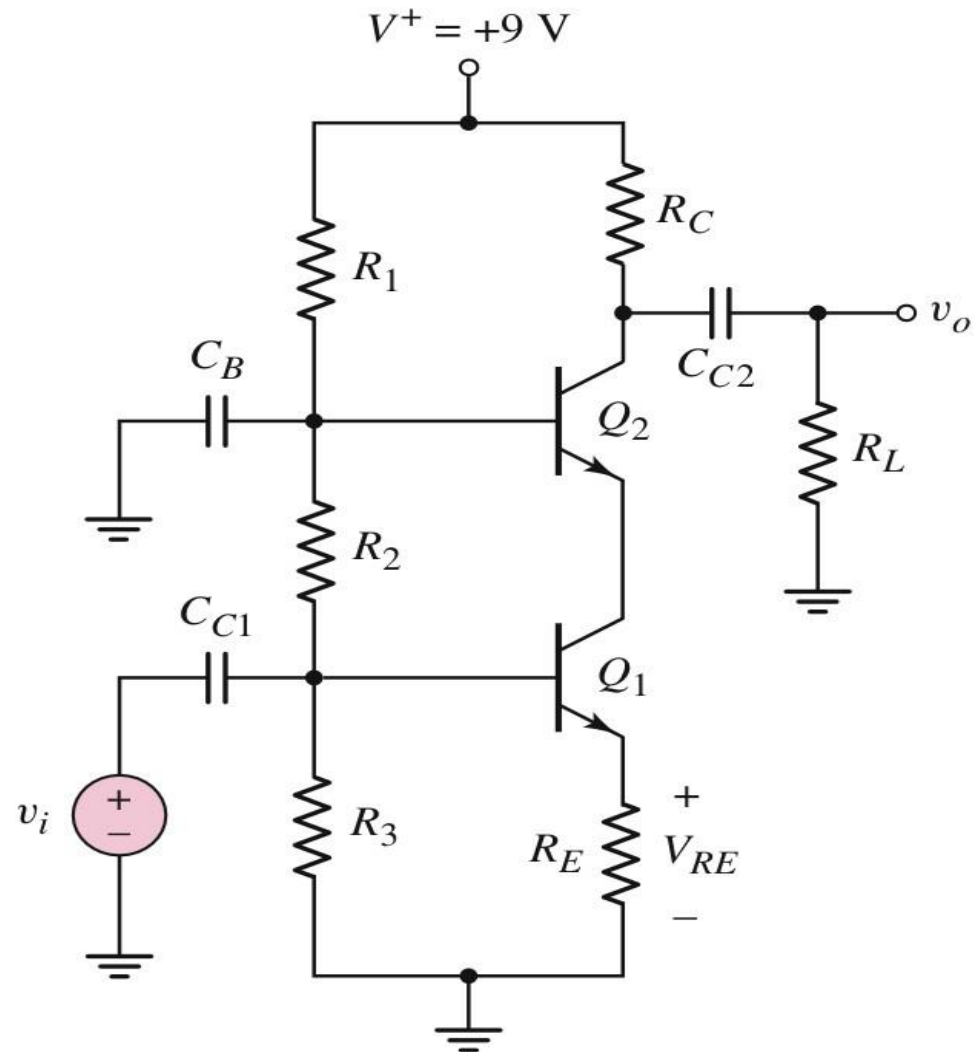
# Multistage Circuits

# Multistage Cascade Transistor Circuit



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# Multistage Cascode Transistor Circuit



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## MOFET VS BIPOLAR Comparison of Characteristics

- For **MOSFET**, the important feature is how  $V_{GS}$  controls  $I_D$ , shown as the **transfer characteristic**,  $I_D$  against  $V_{GS}$ .
- For a **BJT** the transfer characteristic is almost a straight line with slope  $\beta$  (transfer characteristics don't vary) so it is not necessary to examine it.
- For the **BJT** the **input characteristic** is examined ( $I_B$  as a function of  $V_{BE}$ ) whereas **no current** flows into a **MOSFET** so it has the input characteristic is  $I_G = 0$ .

An enhancement **MOSFET** is “on” – “active” - if  $V_{GS} > V_T$ , where  $V_T$  is the **threshold voltage**.

# Comparison of Characteristics

## ***Bipolar***

- $I_B$  controls the collector current
- Control varies greatly from transistor to transistor as  $\beta$  varies by a large amount
- Input voltage threshold is  $V_{BE} > 0.7\text{volts.}$
- When conducting  $V_{BE}$  is almost constant at about 0.7V

## ***MOSFET***

- $V_{GS}$  controls the drain current (strictly  $V_{GS} - V_T$ )
- Control varies greatly from transistor to transistor as  $V_T$  varies by a large amount
- Input voltage threshold is  $V_T$  - varies with transistor.
- $I_G = 0$  for all situations so is constant

# Contents of Chapter

- Discuss the physical structure and operation of the bipolar junction transistor.
- Understand the dc analysis and design techniques of bipolar transistor circuits.
- Examine three basic applications of bipolar transistor circuits.
- Investigate various dc biasing schemes of bipolar transistor circuits, including integrated circuit biasing.
- Consider the dc biasing of multistage or multi-transistor circuits.