



Grid Filter Design

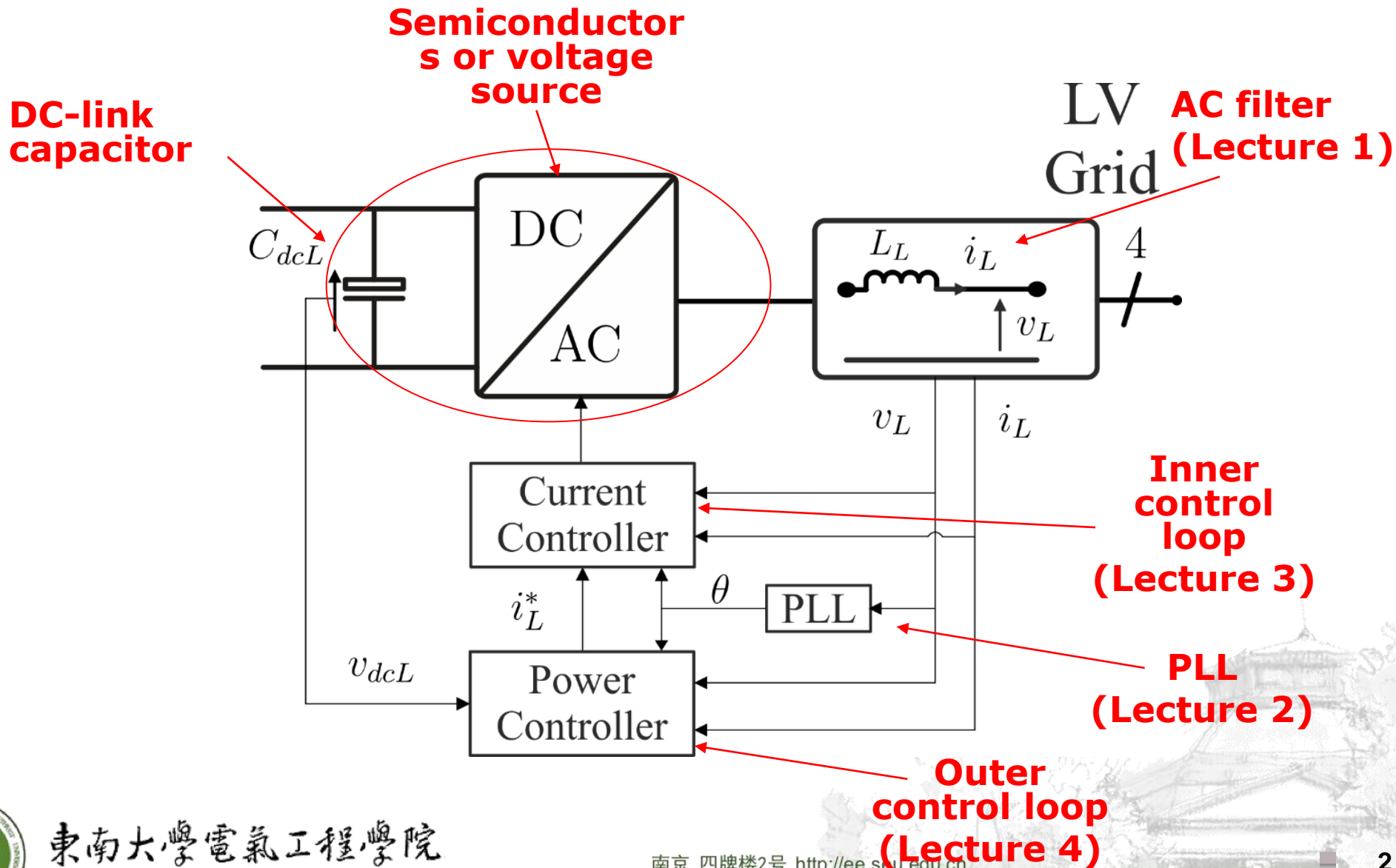
April 28, 2021

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Key Components of Grid Converters



- Filter topologies and model
- LCL-filter design
- Practical Examples of LCL Filters and Grid Interactions
- Resonance problems and damping solutions



Filter topologies

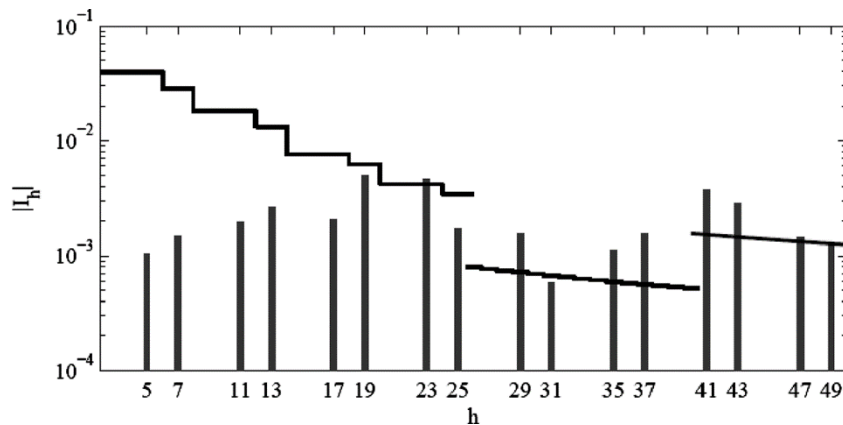


The role of the grid filters in VSC-based grid converter operation is twofold:

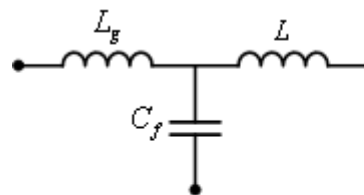
1. Allow the control of active and reactive power with the control of phase and magnitude of the voltage
2. Reduce PWM harmonics caused by the grid-converter

The two most adopted approaches are:

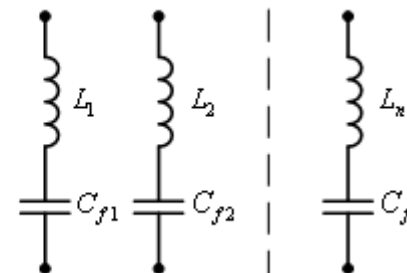
- L-filter plus tuned LC filters (typically at a system level to meet requirements related to the voltage quality)
- Low-pass LCL filter



Harmonic spectrum compared
to German VDEW limit



Low-pass filter



Trap filter



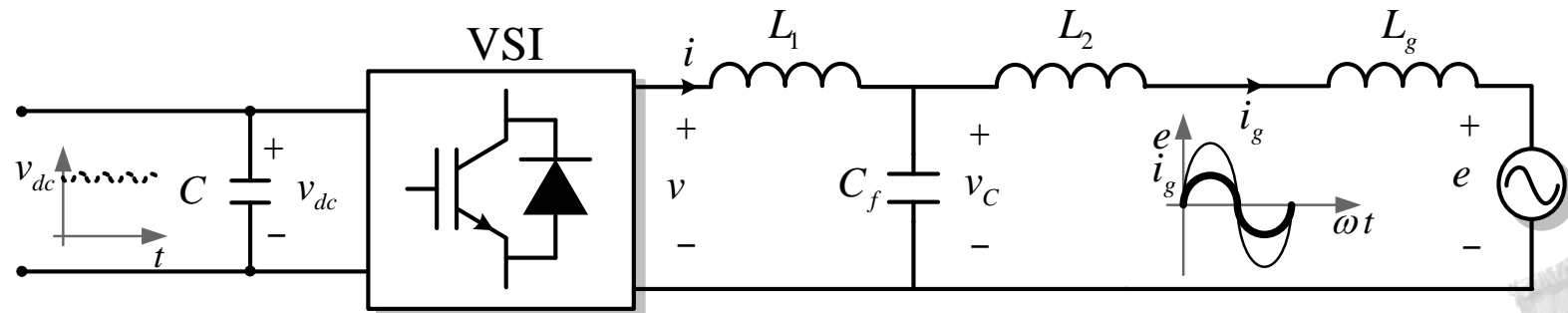
LCL-filter design



The passive elements of the system have both storage and filtering functions

The elements on the ac side have mainly filtering function since the stored energy is typically less than 5% of all the energy stored

LCL-filter design is a trade-off between filtering and dynamics

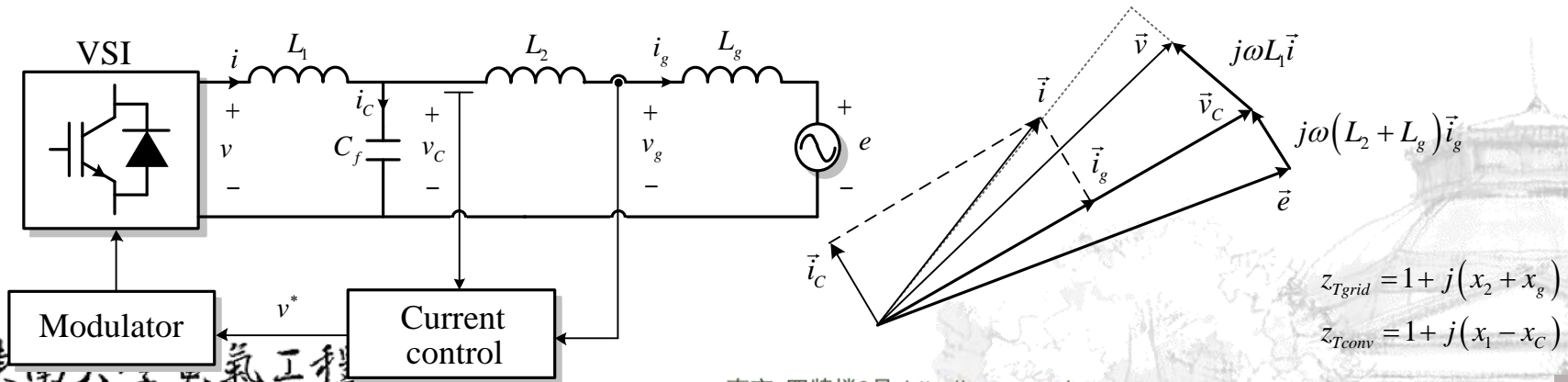
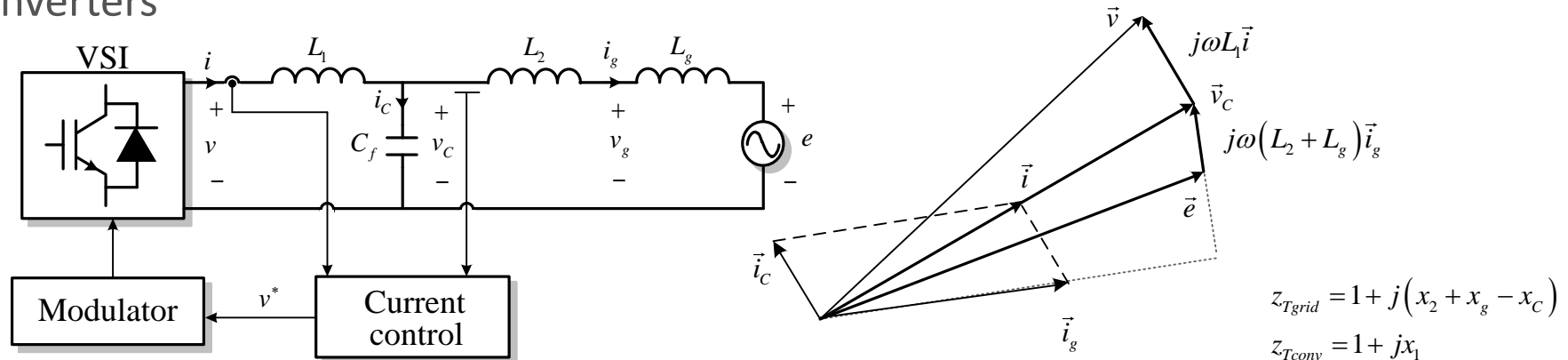


LCL-filter design: sensor position influence

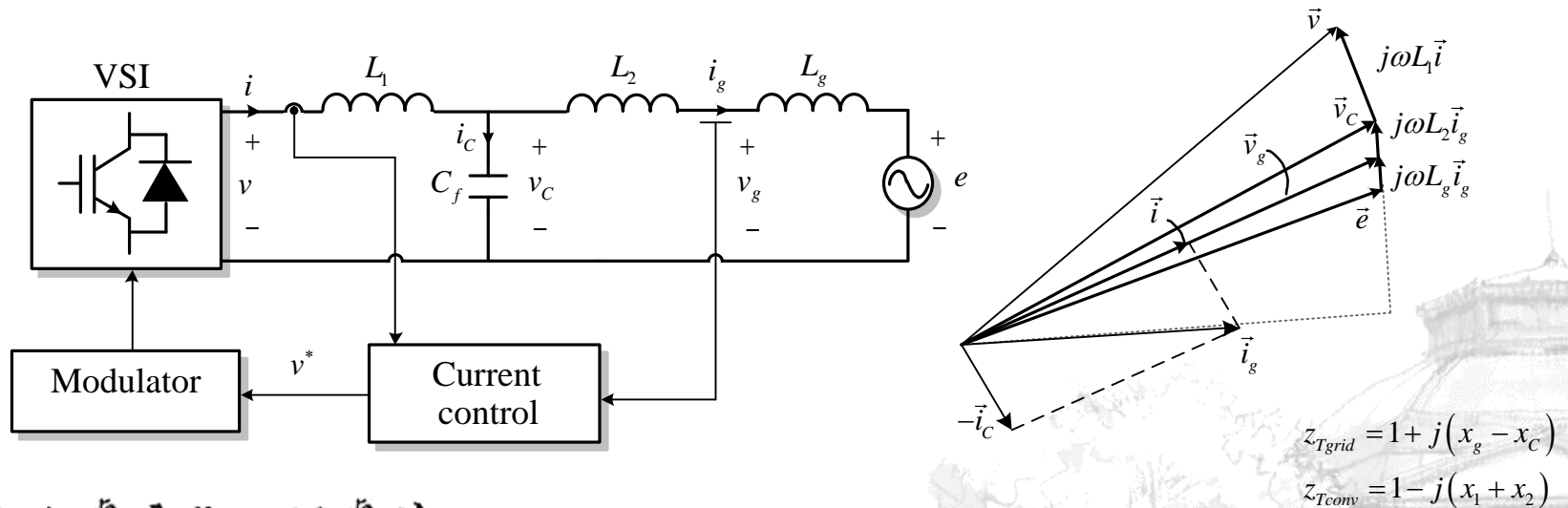
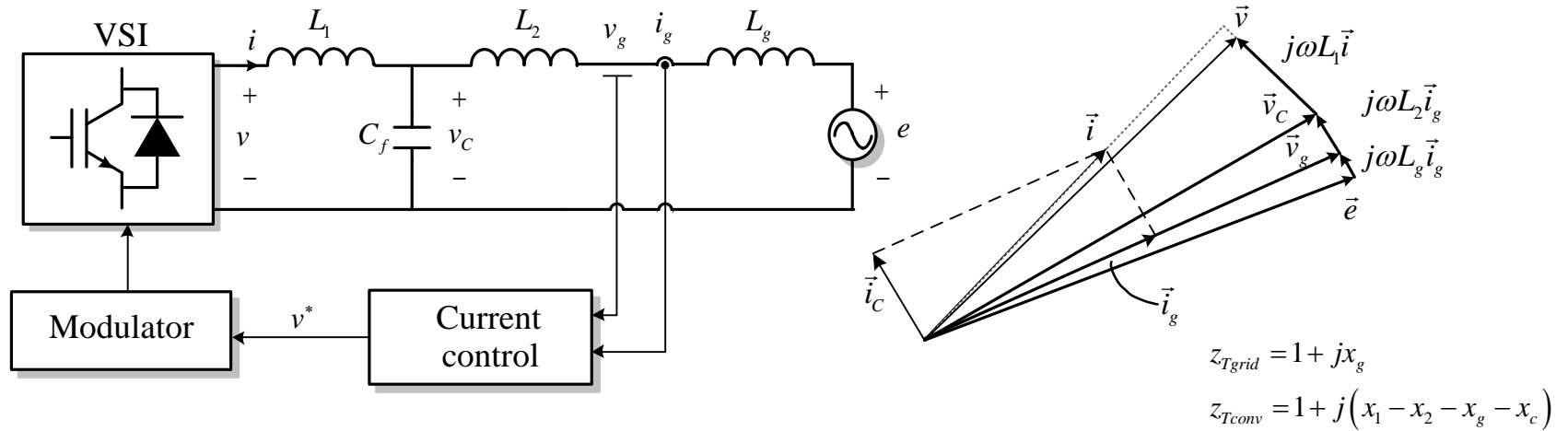


Sensors position has an effect on the equivalent impedance seen from the grid z_{Tgrid} or from the converter z_{Tconv}

The energy stored in the filter can be seen also in terms of equivalent impedance to be minimized from the grid side to minimize the exchanged reactive power and from the converter side to minimize the rating of the converters



LCL-filter design: sensor position influence

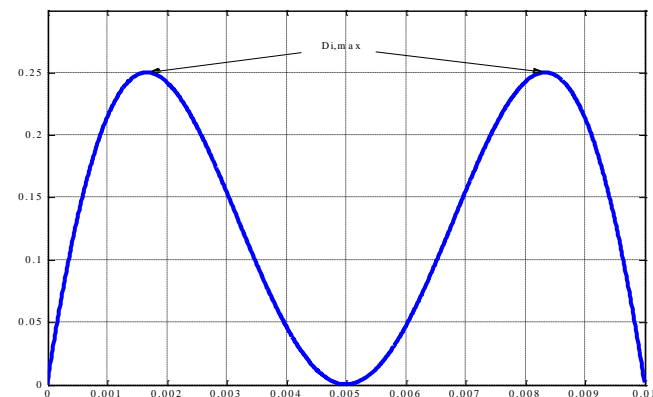
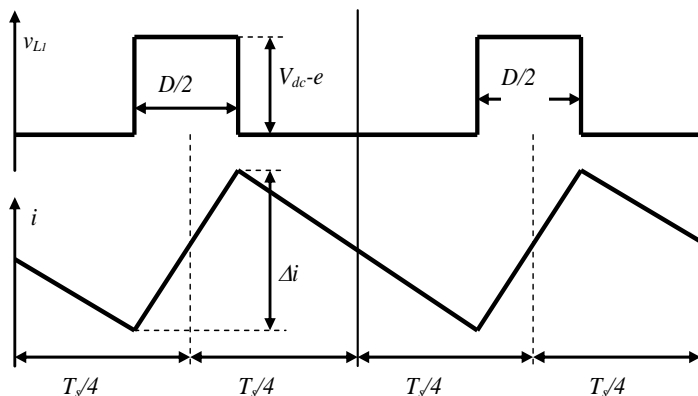


LCL-filter design: choice of L_1



Current ripple in the inverter-side inductor L_1 in case of unipolar modulation

$$\Delta i'(\omega t) = \frac{\Delta i(\omega t)}{\frac{V_{dc} \cdot T_s}{2L_1}} = (1 - |M \cdot \sin(\omega t)|) \cdot |M \sin(\omega t)|$$

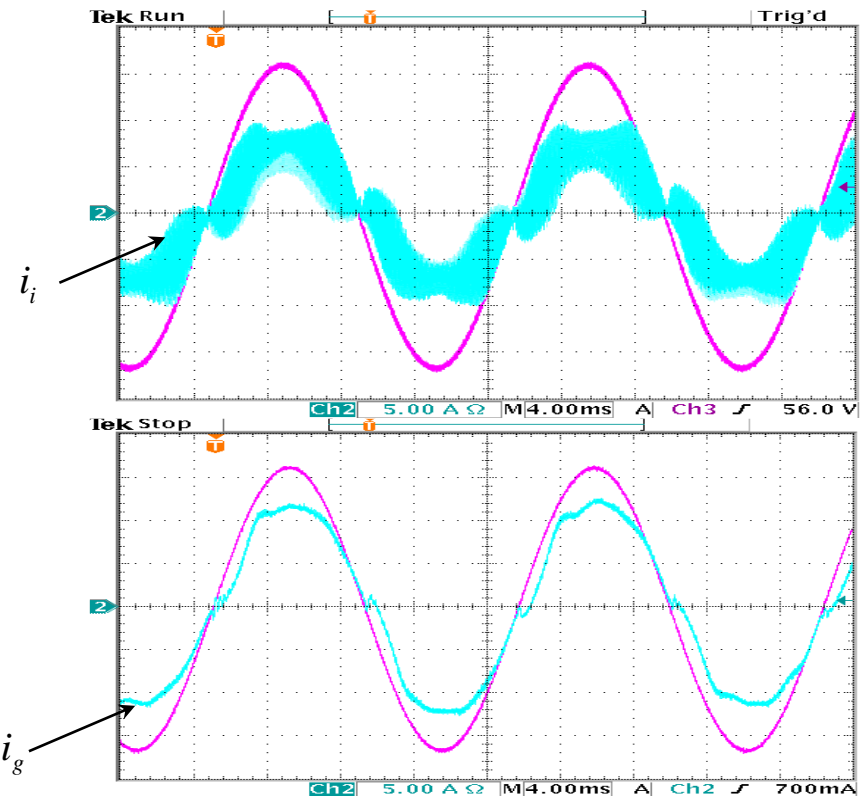
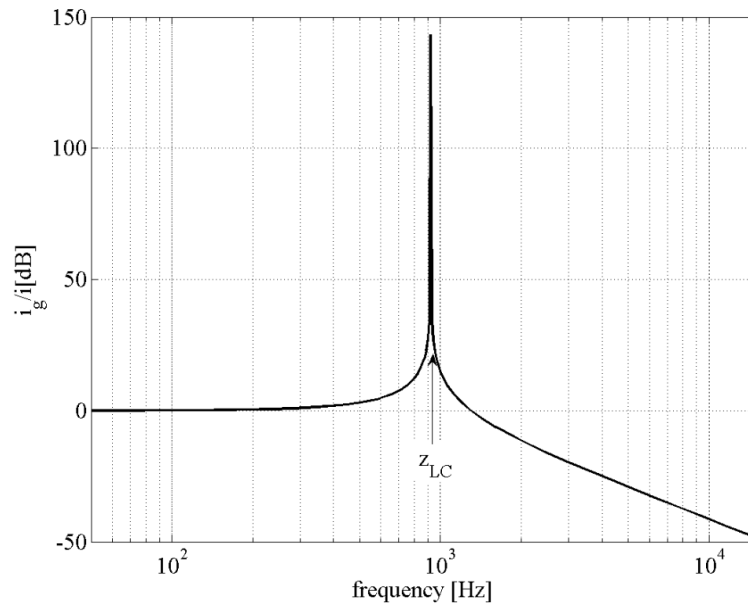


- For a generic type of modulation the maximum ripple is $\Delta I_{MAX} = \frac{1}{n} \frac{V_{dc}}{L_1 f}$ where n depends on the modulation
- The inductor side inductor L_1 is first determined by limiting the max. current ripple at a certain value for a given dc voltage and switching frequency
- Knowing the maximum ripple, the peak current can be calculated and used for the choice of the IGBTs, design of the current protection and design of L_1



LCL-filter design: choice of $L_2 C_f$

$$\frac{i_g(s)}{i_i(s)} = \frac{1}{1 + C_f \cdot (L_2 + L_g) \cdot s^2}$$



Ripple attenuation

$$\frac{i_g(\omega)}{i(\omega)} = \frac{z_{LC}^2}{|z_{LC}^2 - \omega^2|} \quad \text{where} \quad z_{LC}^2 = \frac{1}{(L_g + L_2)C_f} \quad \text{is selected on the basis of the needed attenuation of the current ripple at the frequency } \omega$$



Design of LCL filter: choice of C_f and L_2



- C_f is then sized with two goals:

1. Minimize the installed reactive power of the filter or z_{Tconv} and z_{Tgrid}
2. Robustness of the resonance frequency and as a consequence of the filter attenuation to the grid impedance variation

$$\Delta\omega_{res} = \frac{1}{2\omega_{res}C_f} \left(\frac{1}{L_2 + L_{g1}} - \frac{1}{L_2 + L_{g2}} \right)$$

- Finally, the L_2 is determined
- The effect of passive damping on the filter attenuation should be calculated

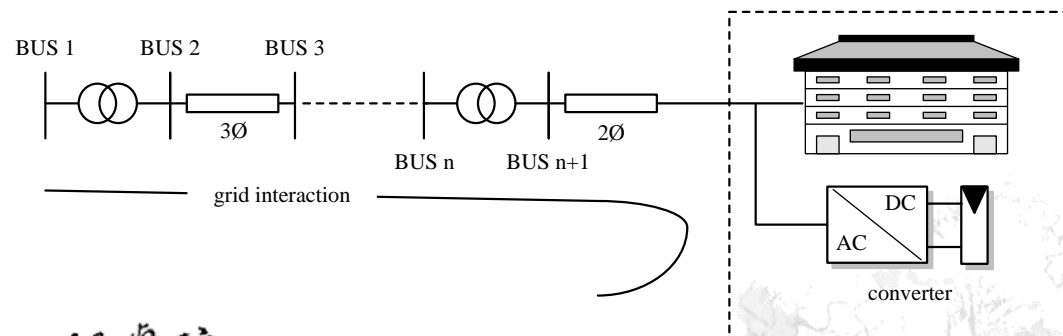


- The possible wide range of grid impedance values (distributed generation is suited for remote areas with radial distribution plants) challenge:
 1. the stability of the system
 2. the effectiveness of the LCL-filter
- The topic will be discussed both for PV and WT systems



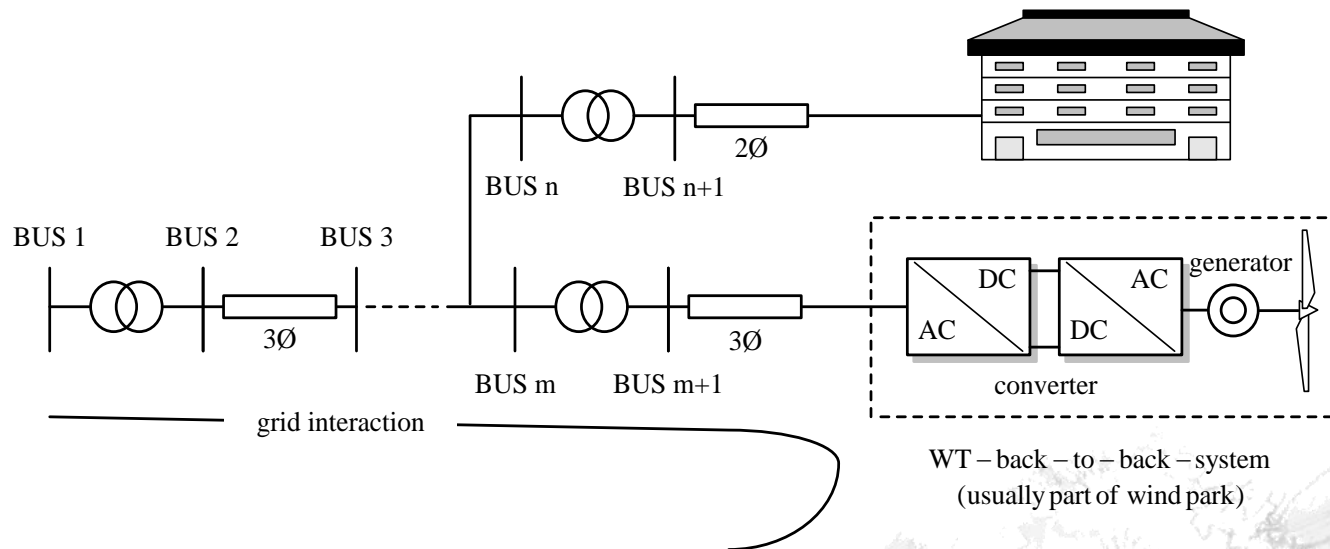
Practical Examples: PV-system

- The High-Voltage/Medium-Voltage transformer as well as a three-phase cable to the MV transformer introduce only a small impedance
- If the PV-house is located in a remote area the medium voltage line can be very extended (hundreds of km's) and its cables can introduce reactive reactance
- The MV/LV transformer introduces a reactance that could be considerably higher in locations where the transformer rated power is considerable lower
- Then the low voltage cable introduces a prevalently resistive impedance that varies with the distance of the PV-inverter from the transformer
- Capacitive loads (e.g. refrigerators) could introduce a capacitive impedance that can create low frequency resonances



Practical Examples: WT-system

- The system is similar to the previous one (hence also in this case a radial plant typical of a rural zone can introduce a very high impedance) up to the MV/LV transformer, to which the wind turbine converter is connected
- Hence the impedance seen by the grid connected inverter can be mainly inductive and can be different depending on the plant configuration
- However, the system present less interaction with domestic loads, avoiding possible low frequency resonances



WT – back – to – back – system
(usually part of wind park)

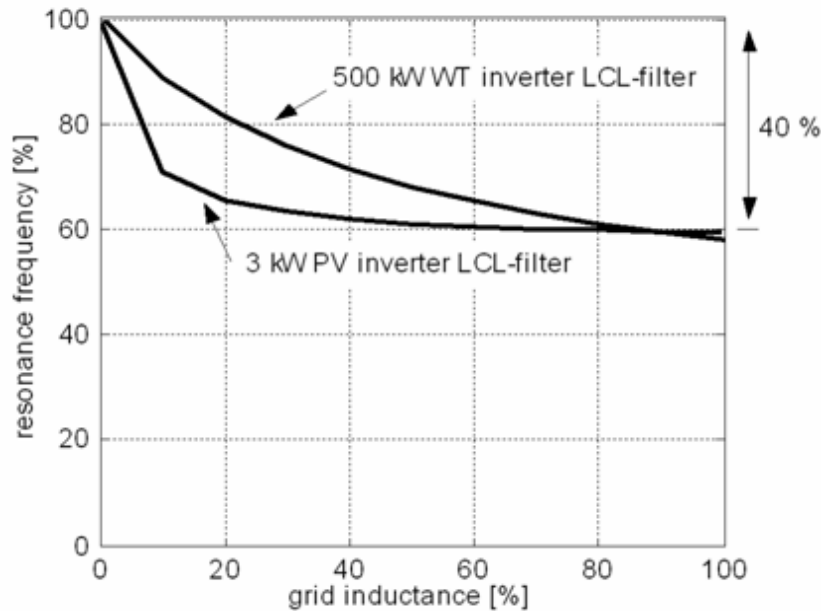
Example of two systems 500 kW WT and 3 kW PV



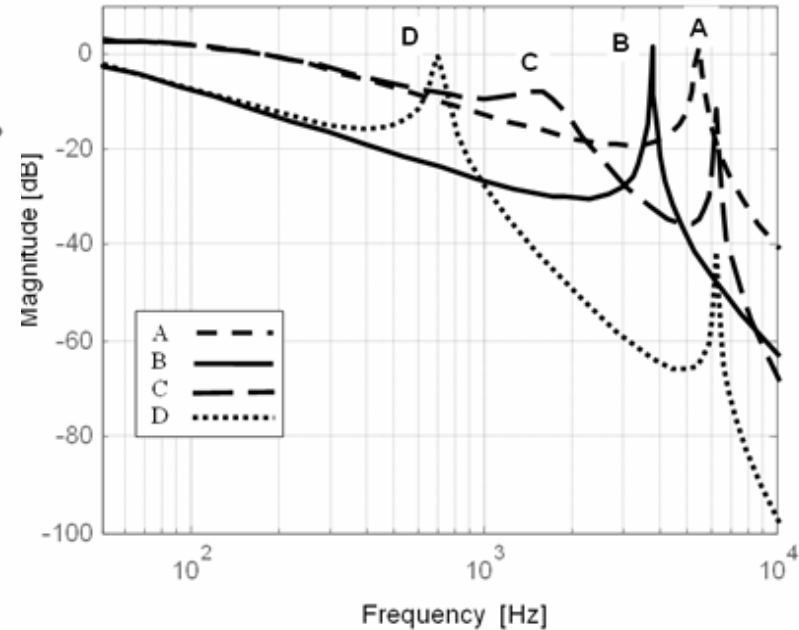
LCL-filter		500 kW WT system		3 kW PV-system	
	Boost inductance	0.2 mH	23 %	0.4 mH	1 %
	Grid side inductance	0.03 mH		0.2 mH	
	Filter capacitor	83 μ F	1 %	5 μ F	3 %
Grid impedance	Maximum value (weak grid)	0.03 Ω (inductive)	10 %	2.7 Ω (41% inductive)	15 %
	Minimum value (stiff grid)	0.003 Ω (inductive)	1 %	0.4 Ω (resistive)	2 %



Example of two systems 500 kW WT and 3 kW PV



Variable inductance



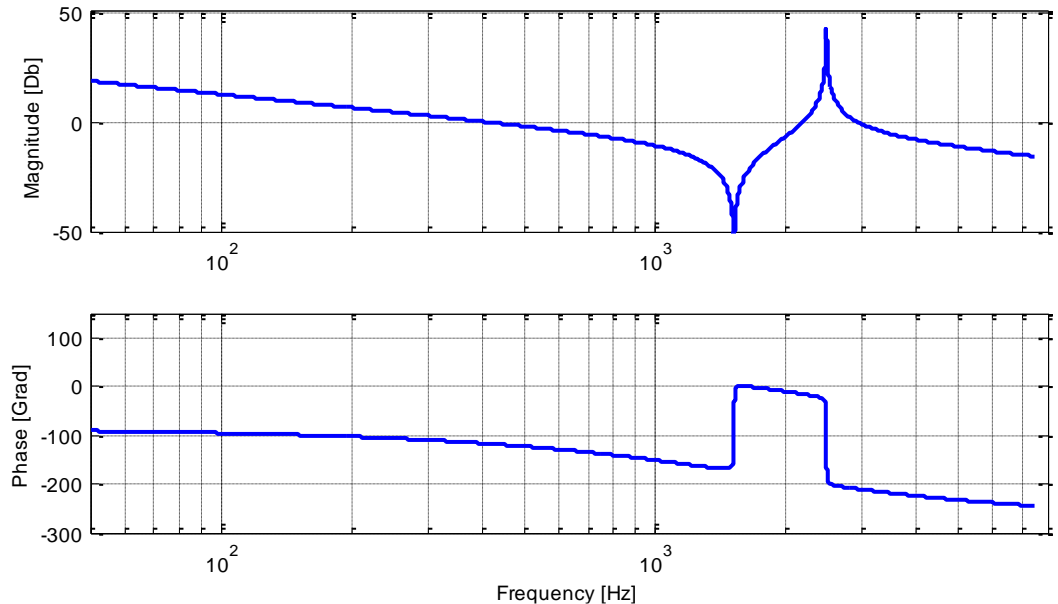
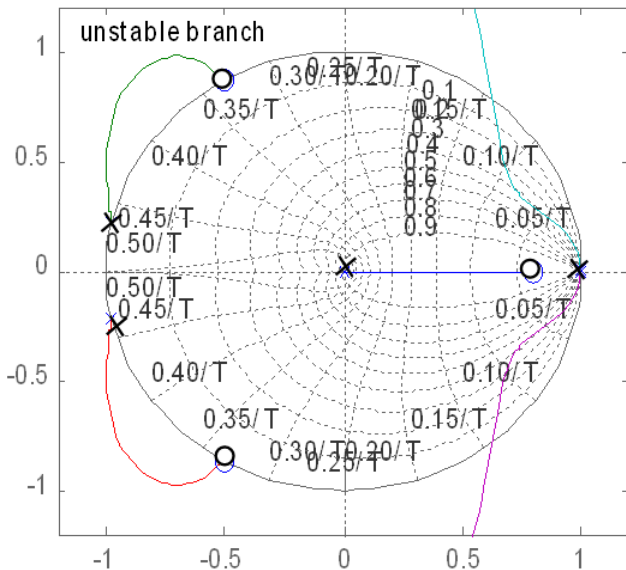
Introduction of 100 μ F capacitance



- LCL-filter effectiveness changes with the grid stiffness
- Damping is difficult since the plant changes with the grid stiffness (active one is more flexible)
- The grid stiffness influence can be limited using more inductance in the filter but it leads to a bulky inverter and to packaging problems (i.e. the automatic mounting of the components is not possible) in case of PV systems
- The presence of capacitive loads create other resonance peaks, active damping can be effective also in these cases



Resonance problems and damping solutions

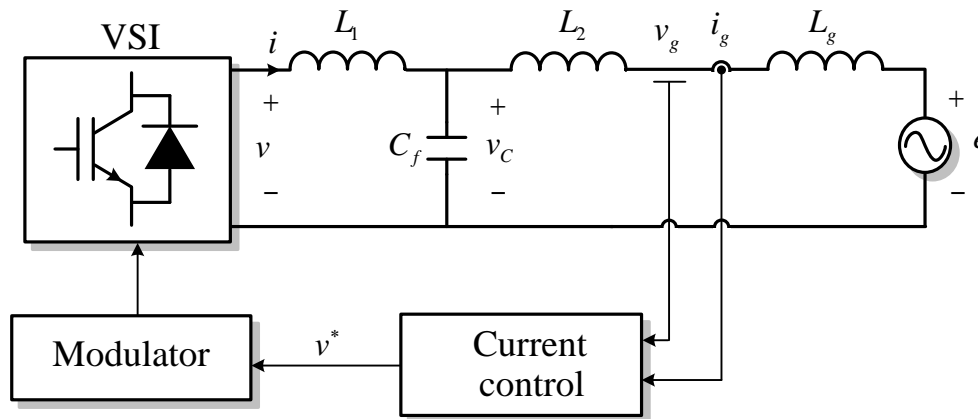


- The LCL-filter challenges the system stability
- There is a resonant peak associated to two resonant poles
- Their position changes as the grid inductance changes



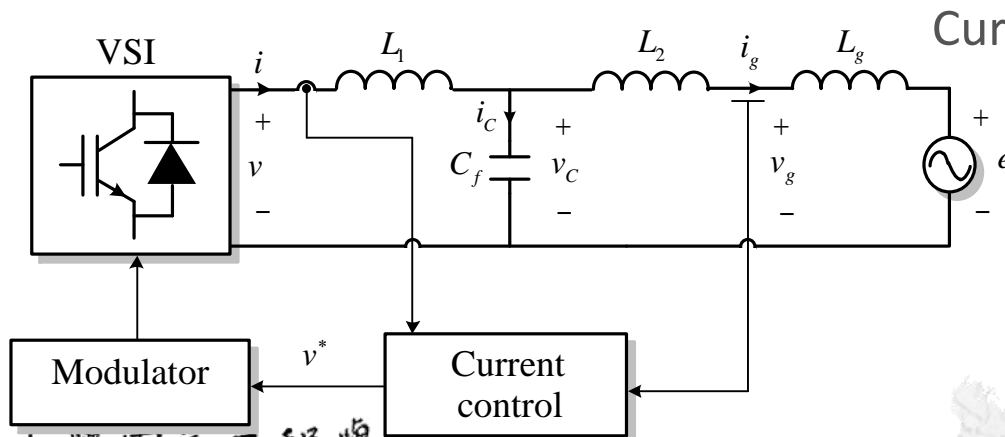
Resonance problems and damping solutions

- The plant depends on the position of the current sensors: grid-side (more typical in low power PV-system) or converter-side (more typical in high power WT-system)



Current sensors on the grid side

$$G_f(s) = \frac{i(s)}{v(s)} = \frac{1}{Ls} \frac{z_{LC}^2}{(s^2 + \omega_{res}^2)}$$



Current sensors on the converter side

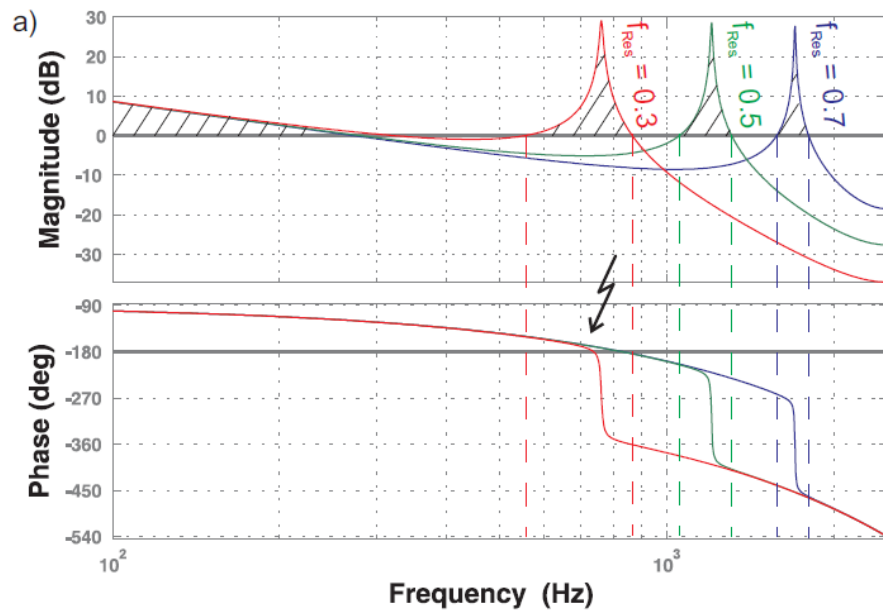
$$G_f(s) = \frac{i(s)}{v(s)} = \frac{1}{Ls} \frac{(s^2 + z_{LC}^2)}{(s^2 + \omega_{res}^2)}$$



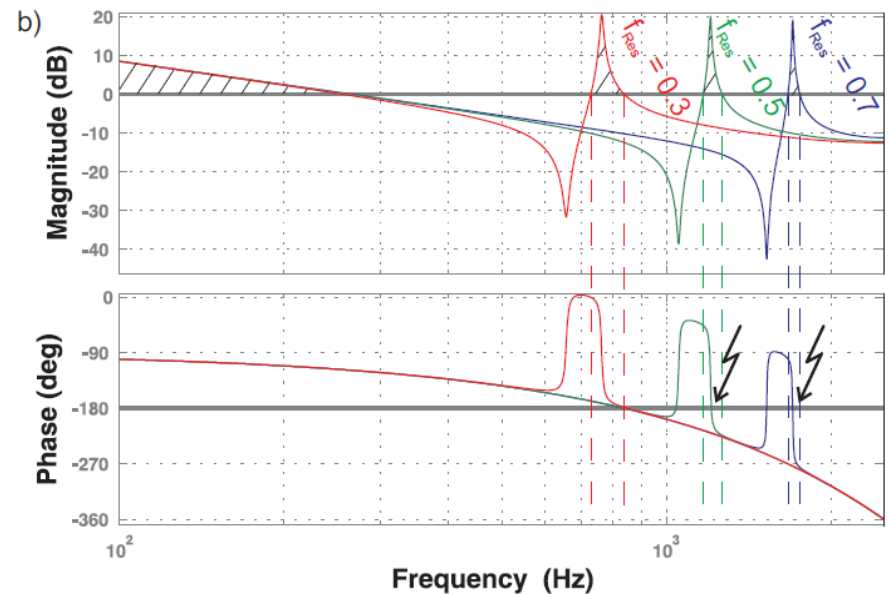
Resonance problems and damping solutions

- Sensing the grid current create conditions more favorable for the stability if the resonance frequency is high

Current sensors on the grid side



Current sensors on the converter side



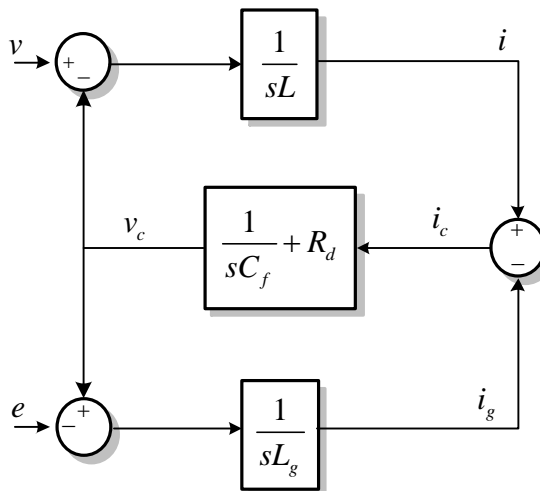
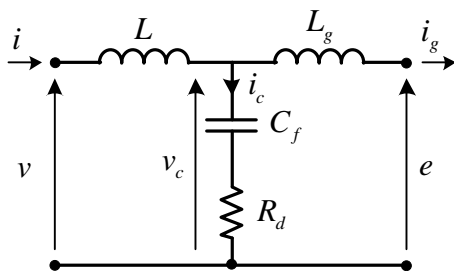
J. Dannehl, M. Liserre, F. Fuchs, F.; , "Filter-based Active Damping of Voltage Source Converters with LCL-filter," IEEE Transactions on Industrial Electronics, 2011.



Passive damping



- As the damping resistor increases, both stability is enforced and the losses grow but at the same time the LCL-filter effectiveness is reduced



Losses

$$P_d = 3R_d \sum_h [i(h) - i_g(h)]^2$$

- Main terms of the sum are for the index h near to the multiples of the switching frequency order

f_{sw}	5 kHz	6 kHz	7kHz	8 kHz
abs value	32 W	20 W	13 W	10 W
% of rated power	0.8 %	0.5 %	0.3 %	0.2 %

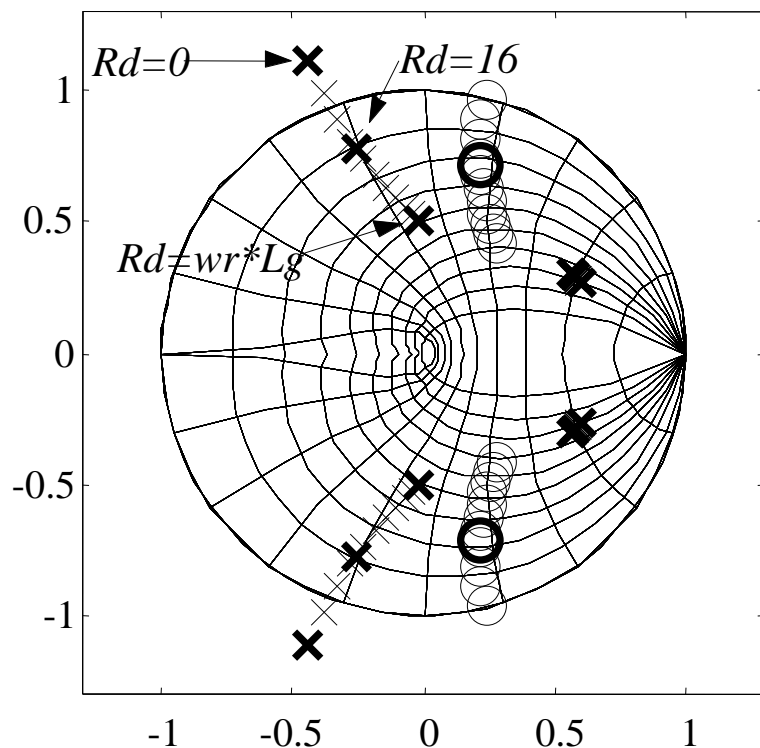
Increasing the switching/sampling frequency, the losses decrease but at the same time the damping becomes less effective



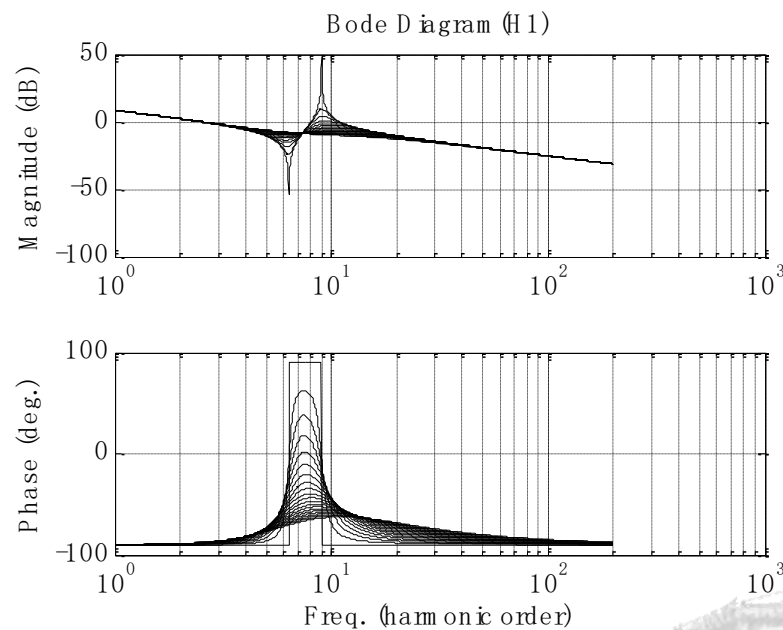
Passive damping



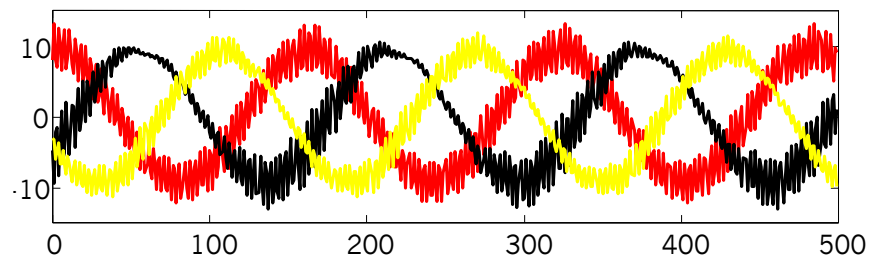
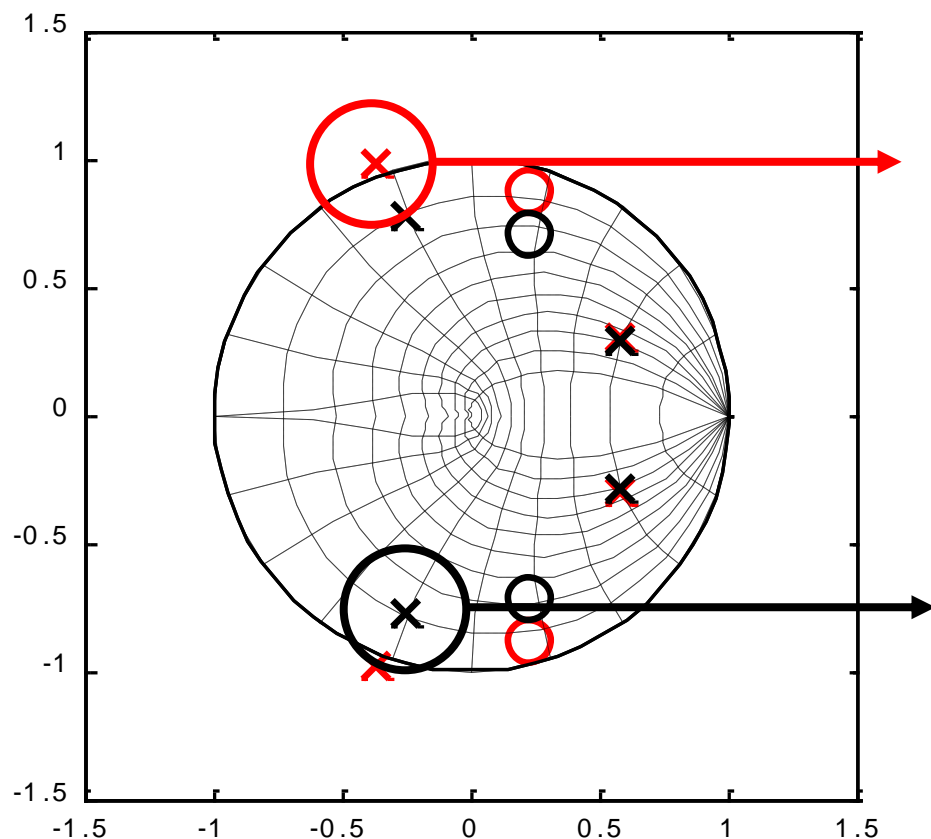
Root locus



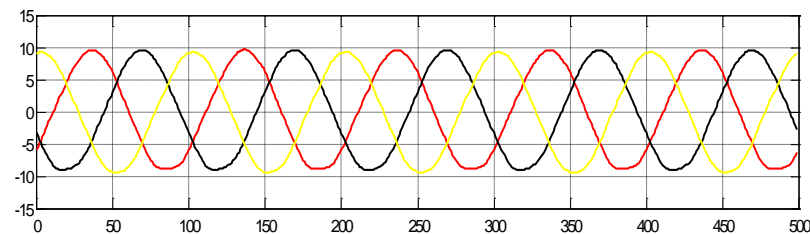
Bode plot



Passive damping

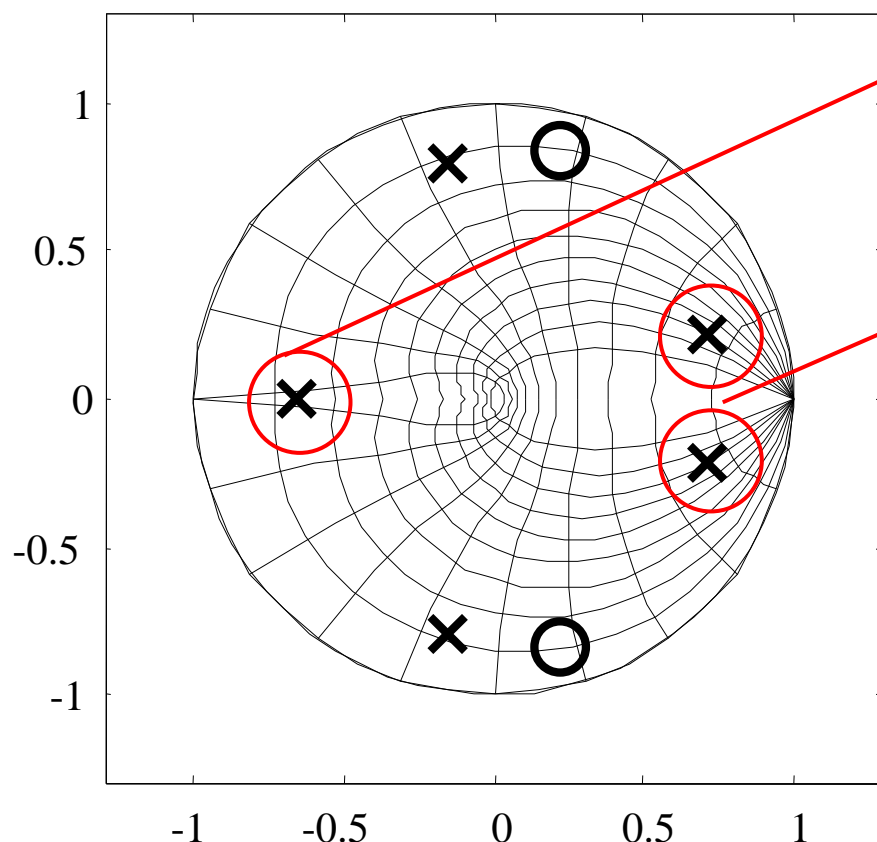


Converter side current



Passive damping in case of one delay in the control loop

Root locus



Pole introduced by the delay

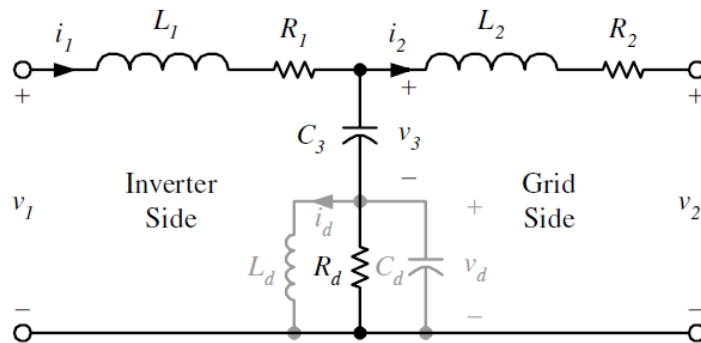
Reduction of the bandwidth from 350 Hz to 200 Hz

Good method to reduce losses in high power applications at the price of a slow down of the dynamic, as a consequence in case of voltage sag an higher overcurrent is obtained

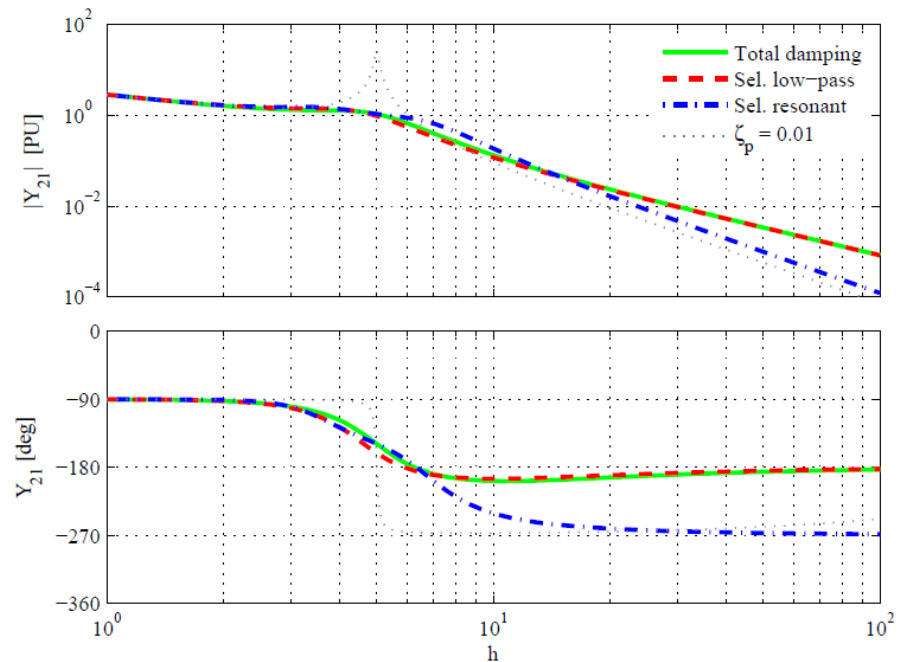
Passive damping: selective damping



Higher power DPGS (like MW WT-systems) switch at low frequency and resonance frequency needs to be damped selectively



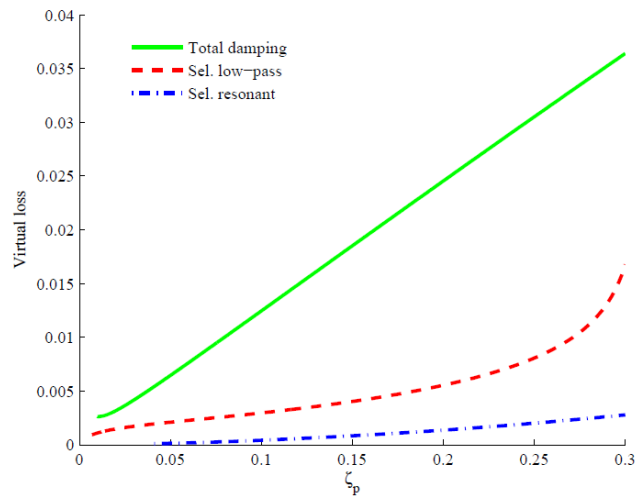
Damping resistor in parallel with inductor and capacitor to achieve selective damping



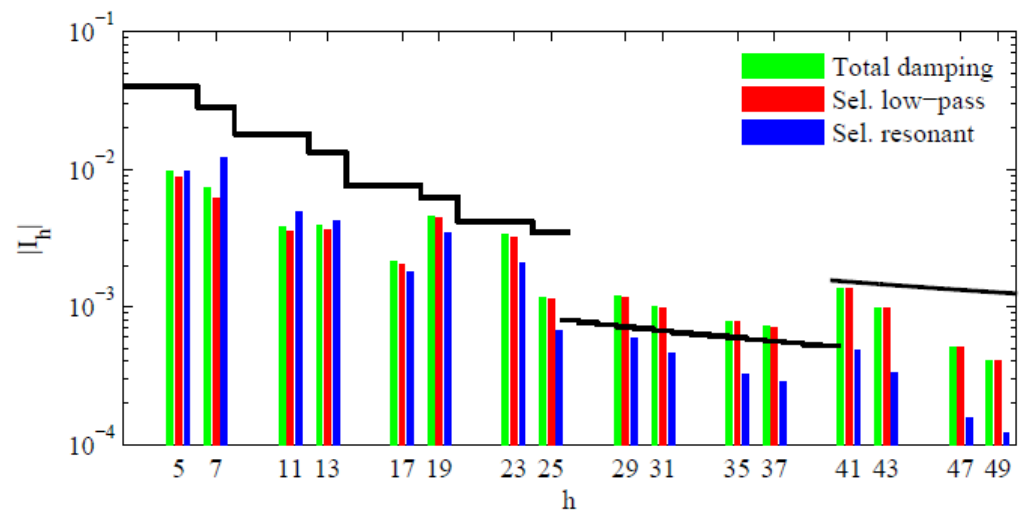
Passive damping: selective damping



Virtual Losses



Harmonic Spectrum



A. Rockhill, M. Liserre, R. Teodorescu, P. Rodriguez, "Grid Filter Design for a Multi-Megawatt Medium-Voltage Voltage Source Inverter," IEEE Transactions on Industrial Electronics, 2011.



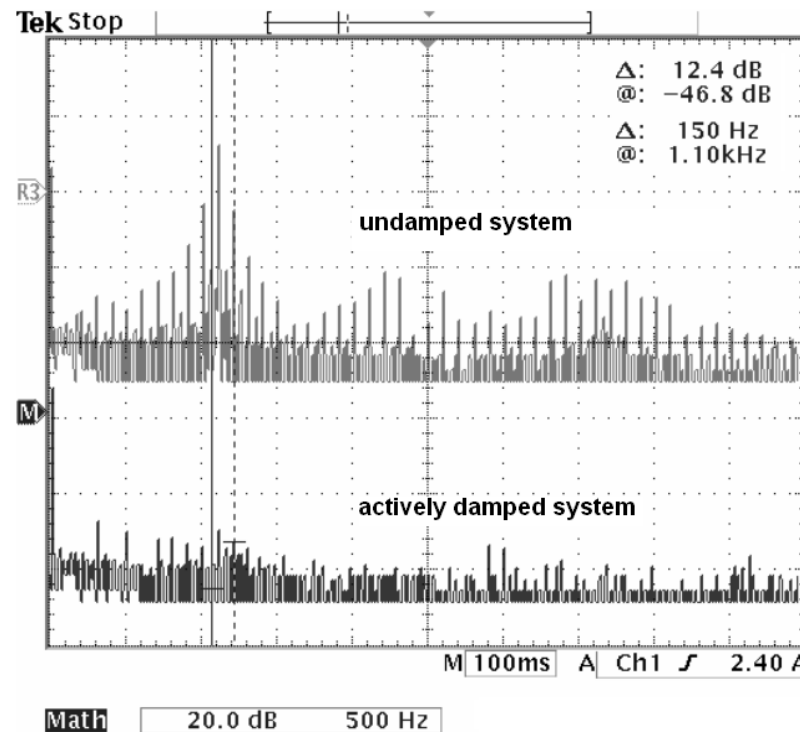
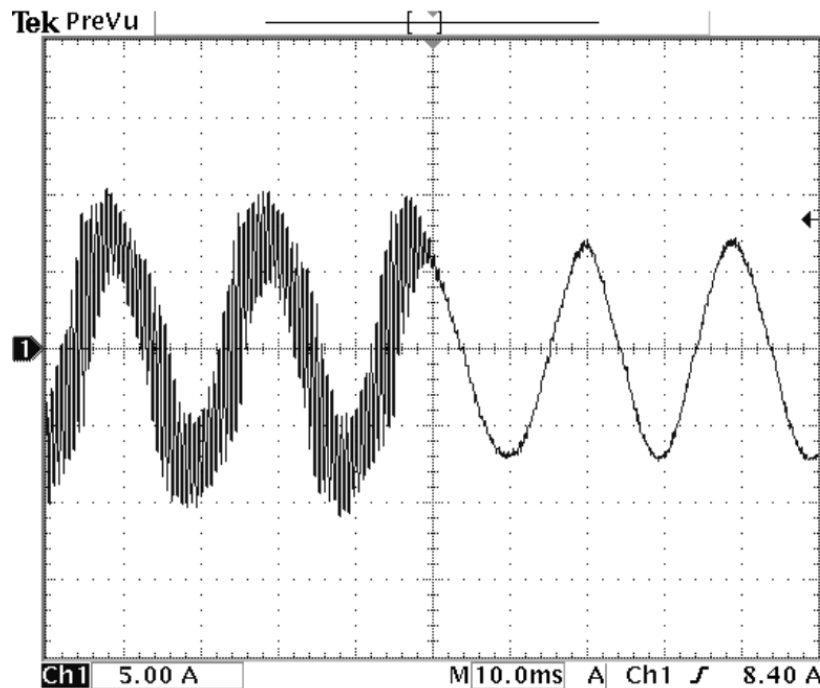
Active damping



- Obtain stability without additional losses
- Modify the control algorithm
- Various techniques based also on the use of more sensors
- Two main possibilities:
 - Multiloop
 - Filter-based



Active damping



Active damping plug-in

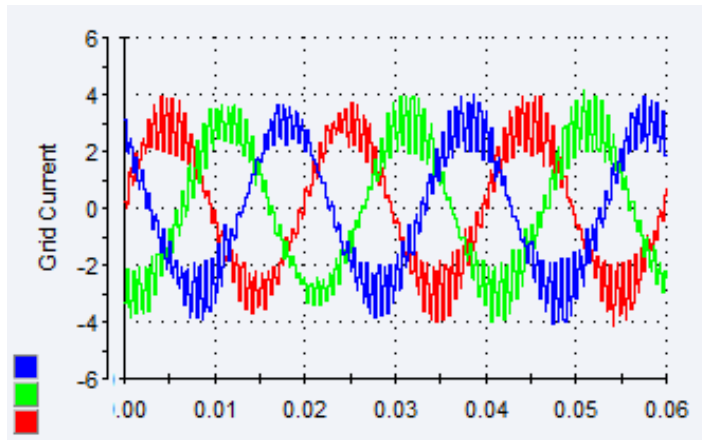
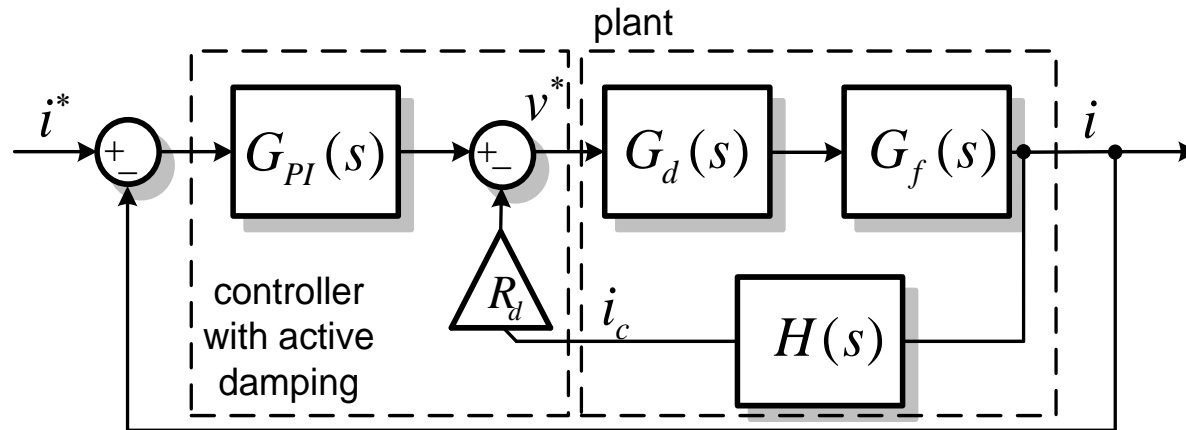


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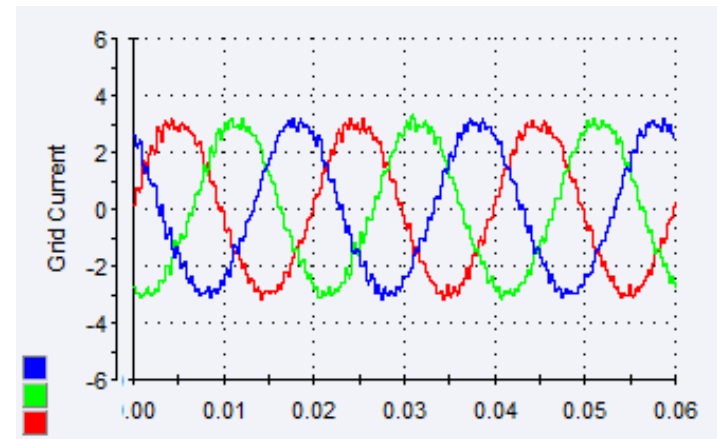
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Multiloop methods: Virtual resistor

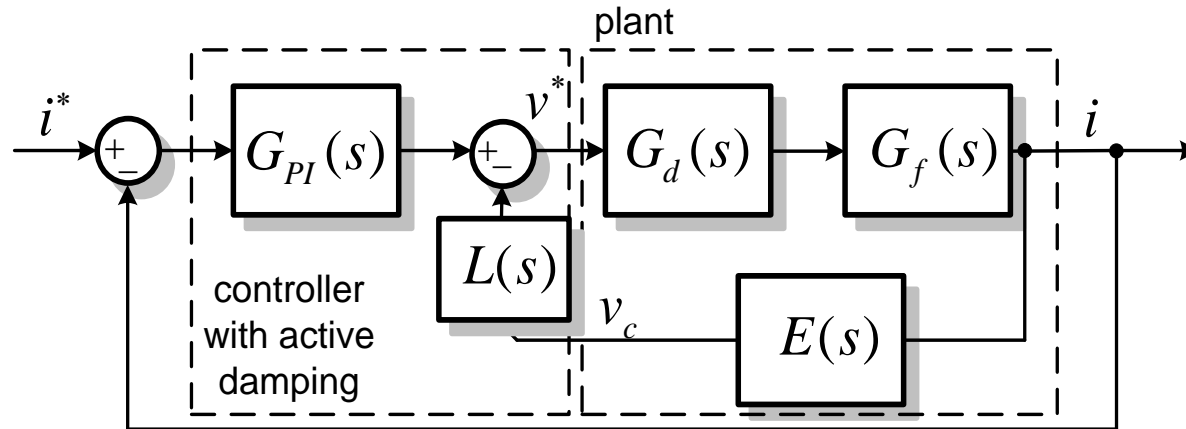


$R_d = 4$

$R_d = 14$



Multiloop methods: lead network



- The LCL-filter capacitor voltage should be measured or estimated
- A lead network is used to create the control action that should damp the resonance adding phase lead

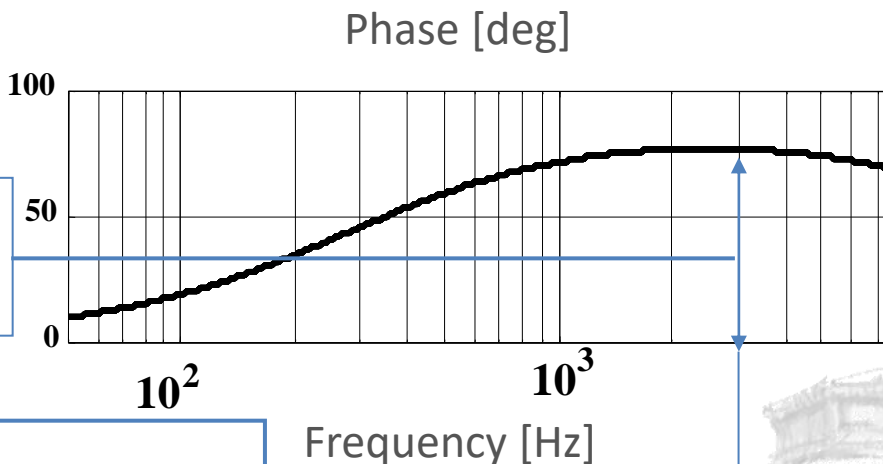
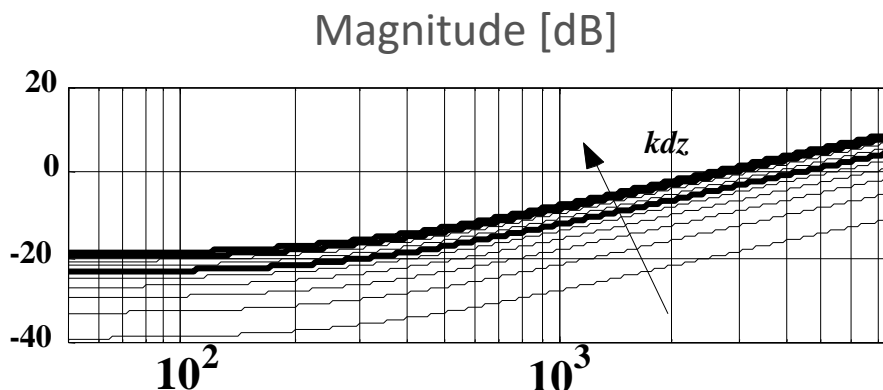


Multiloop methods: lead network



Lead network

$$L(s) = k_d \frac{T_d s + 1}{\alpha T_d s + 1}$$



Principle of operation

$$\phi_{MAX} = \arcsin \frac{1 - \alpha}{1 + \alpha}$$

$$f < \frac{1}{T_d} \rightarrow L(s) = k_d \quad f \geq \frac{1}{\alpha T_d} \rightarrow L(s) = 10k_d$$

$$f_{MAX} = \frac{1}{T_d \sqrt{\alpha}}$$



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Multiloop methods: lead network



- The increase of the lead ratio $1/\alpha$ increases the phase lead but it produces higher amplifications at higher frequencies
- Adopting a low-pass filter, it is possible to select a high phase margin (80°) around the resonance frequency (2.5 kHz)

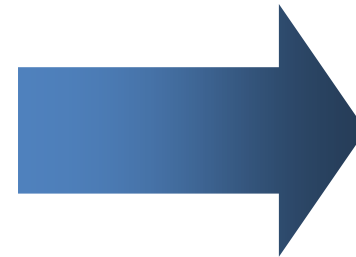
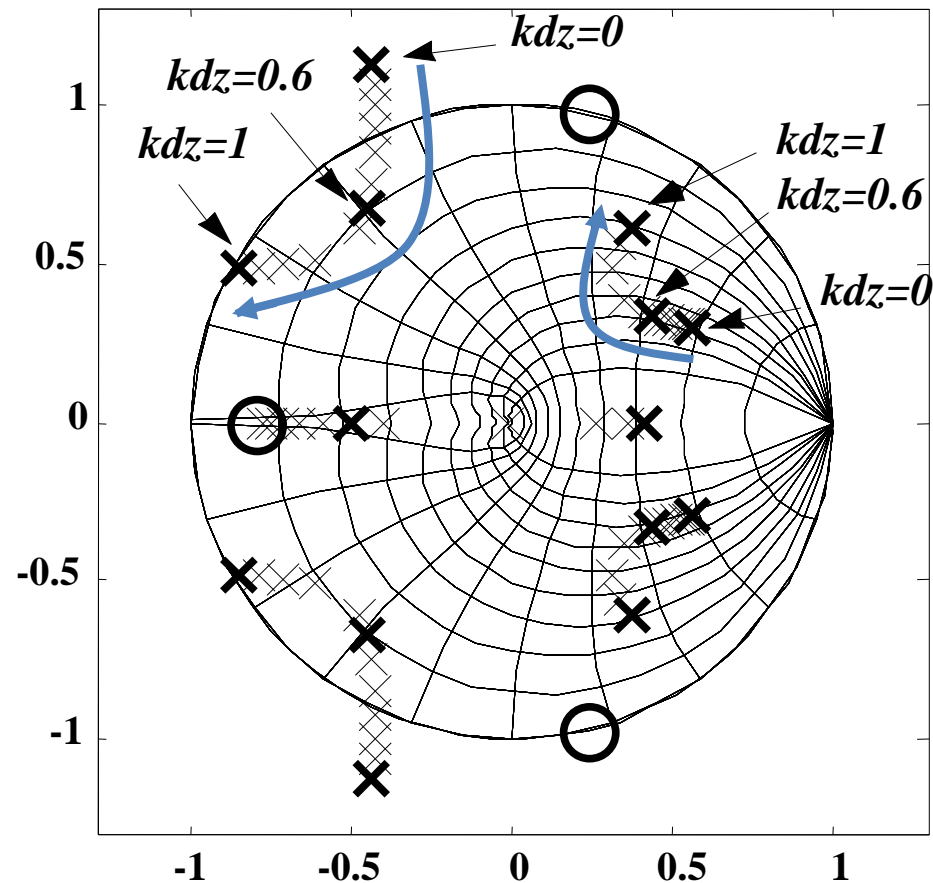
$$T_d = 5.6 * 10^{-4} \quad a = 1.2 * 10^{-2}$$

k_d has to be chosen both on damping and dynamic considerations

Discretization $L(z) = k_{dz} \frac{z + z_o}{z + p_o}$



Multiloop methods: lead network

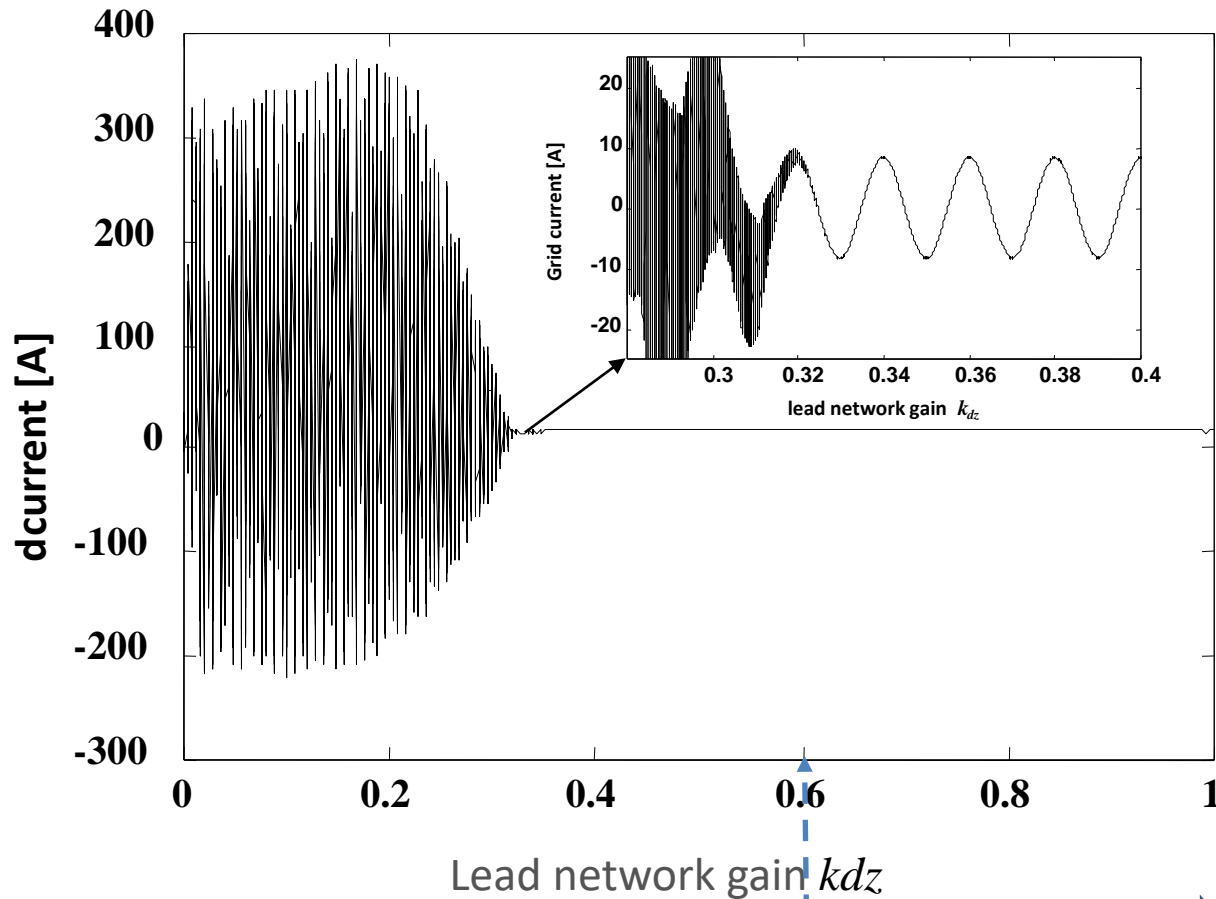


$kdz = 0.6$

- Best damping
- Good dynamic



Multiloop methods: lead network



$THD = 1.6\%$
 $THFHD = 0.6\%$

Optimum steady-state performance

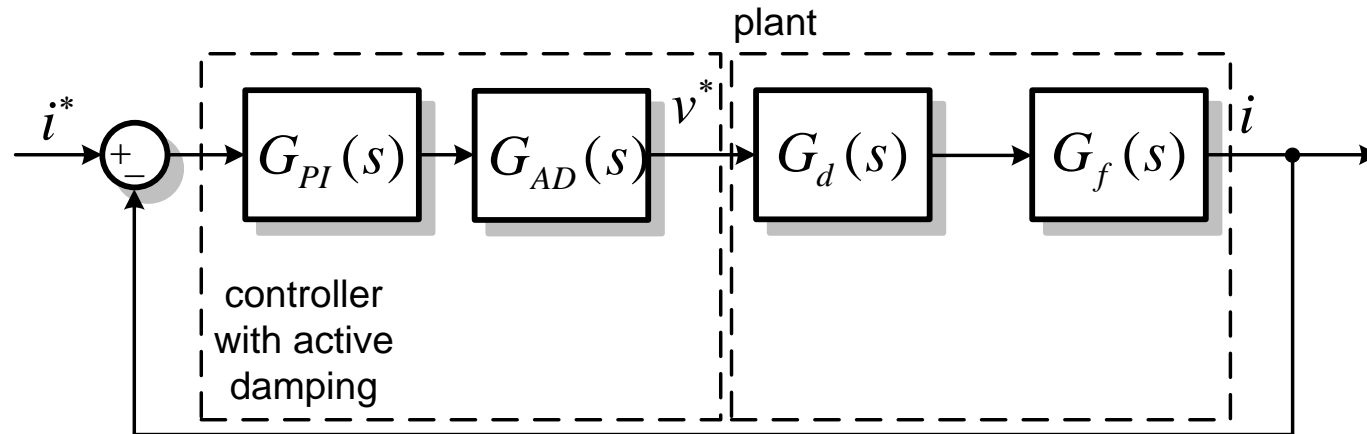


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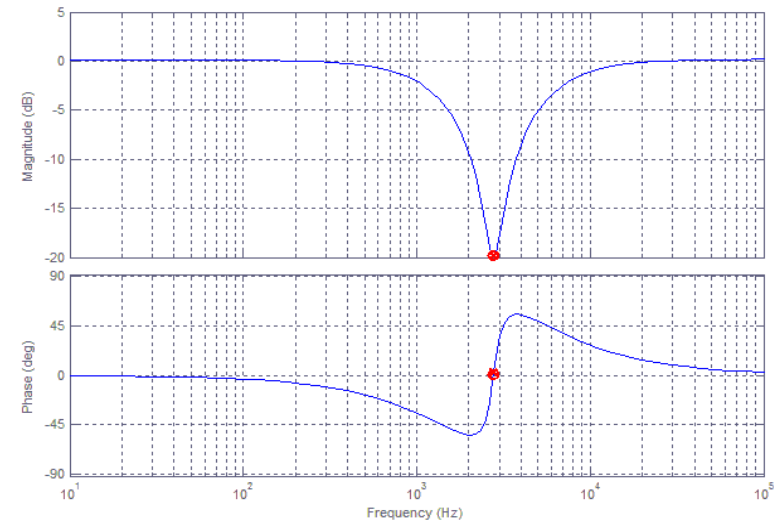
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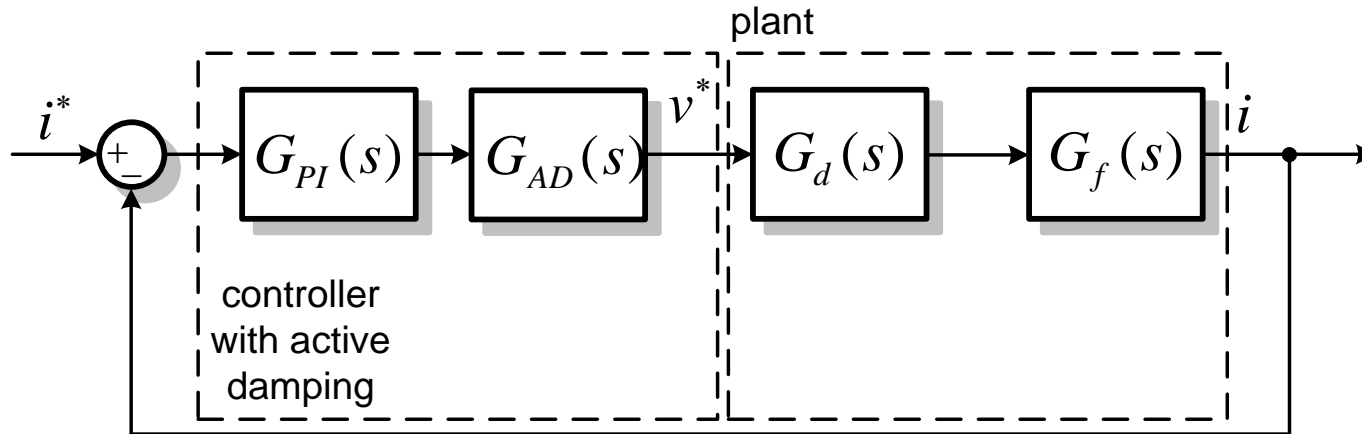
Filter-based methods: Notch filter



- The notch filter is tuned at the resonance frequency



Filter-based methods: Bi-quad filter

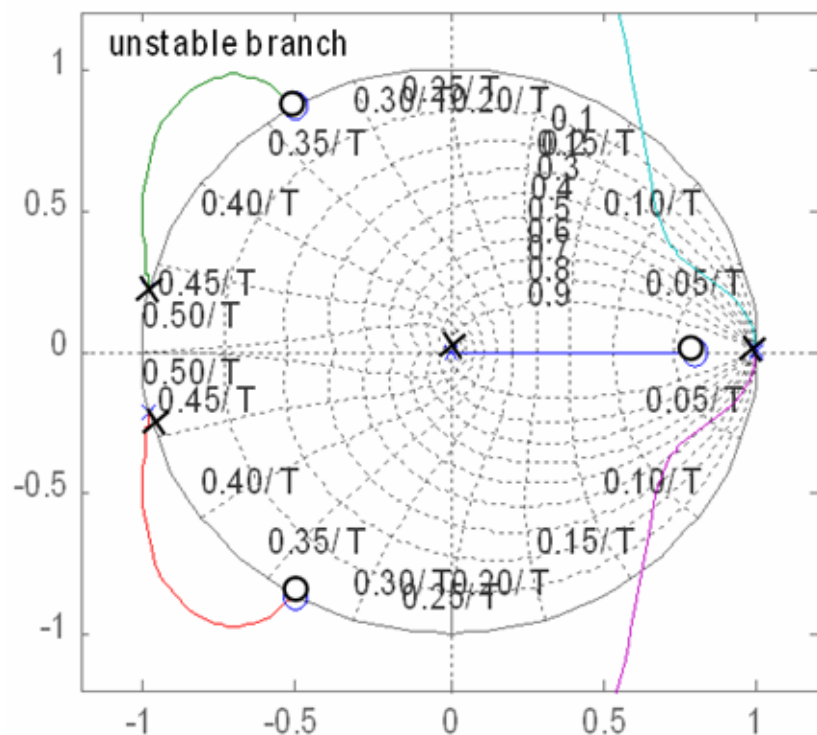


- The bi-quad filter complex conjugate zeros and poles have different frequencies
- They can be used to cancel resonance and anti-resonance

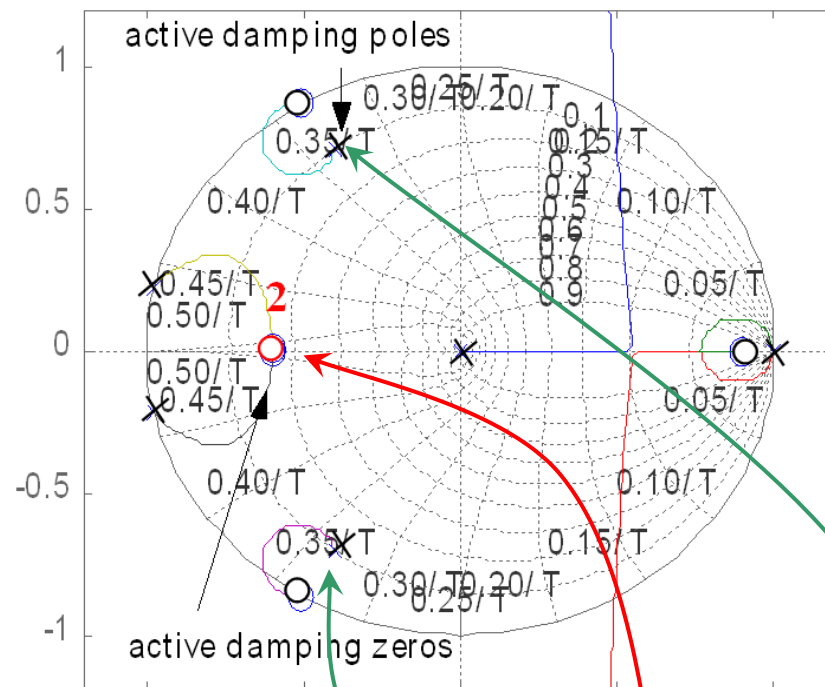
$$G_{AD}(s) = \frac{s^2 + 2D_p\omega_p s + \omega_p^2}{s^2 + 2D_z\omega_z s + \omega_z^2}$$



Filter-based methods: Bi-quad filter



Undamped



$$G_{AD}(z) = \frac{z^2 - z_o^2}{z^2 - p_o^2}$$



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Conclusions of grid filter design



- LCL-filter is used to reduce the switching ripple but it challenges the stability of the current control loop
- The different sensors position changes the 50 Hz impedance of the filter and the plant of the current control loop
- Passive damping can solve stability problems but it has been proven how the excessive damping leads to low frequency ripple, reduced filter effectiveness and high losses
- A reduced passive damping can be used if: the converter current is controlled with one sample delay or the grid current is controlled without delays
- A selective passive damping can be an interesting solution in MW range
- Active damping is an interesting alternative to passive damping, two approaches are possible: multiloop or notch filter
- Robustness to parameters variation, use of more sensors and tuning problems are open issues
- Many methods exist: virtual resistor is straightforward, filter-based methods are also intuitive and do not need more sensors

