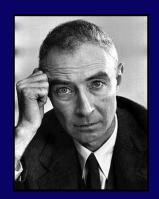
ChIP-seq and its analysis

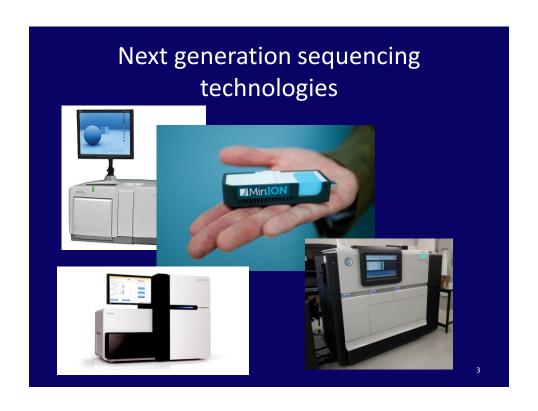
Steve Qin
Department of Biostatistics
and Bioinformatics
Rollins School of Public Health
Emory University

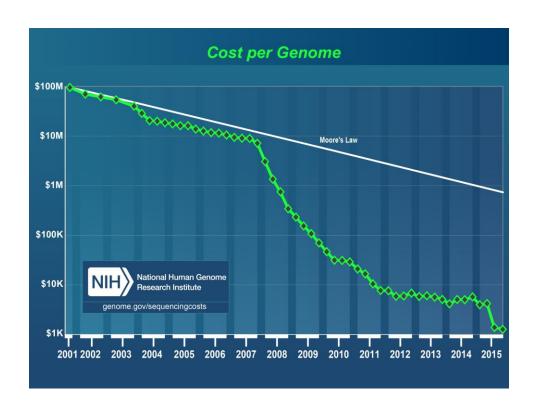


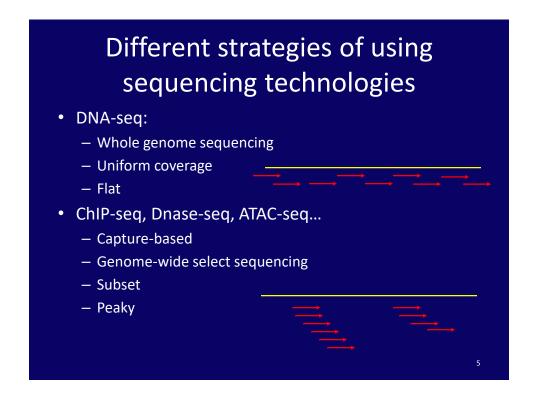


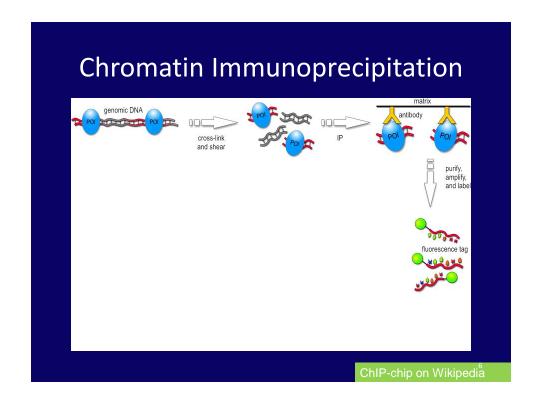
"... deep things in science are not found because they are useful; they are found because it was possible to find them"

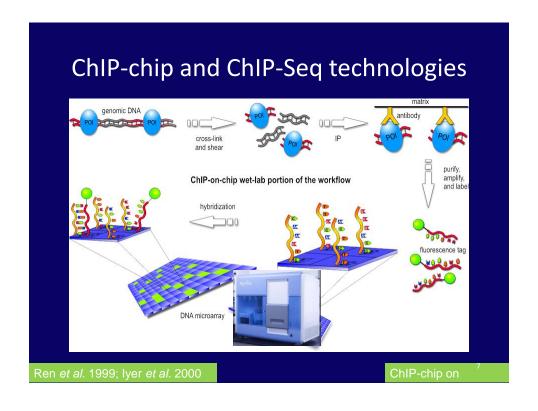
-- Robert Oppenheimer

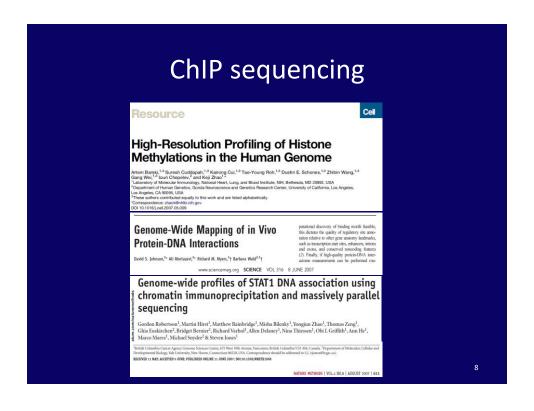








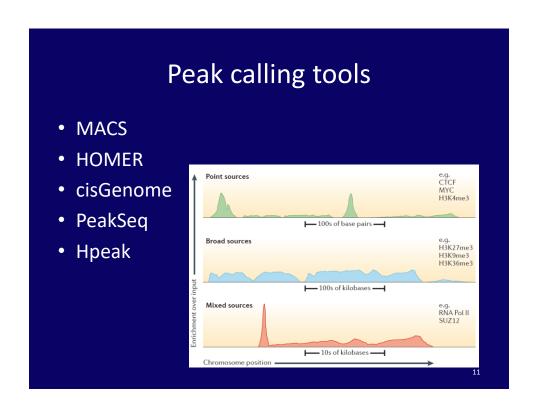


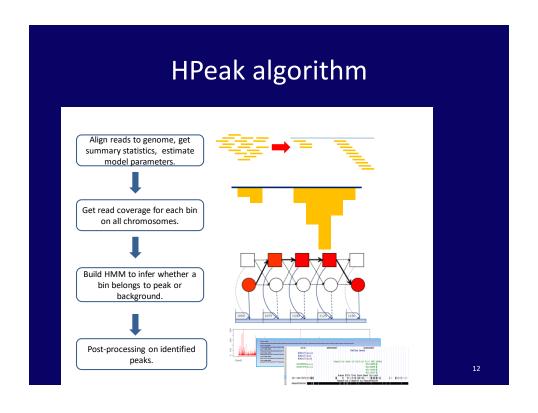


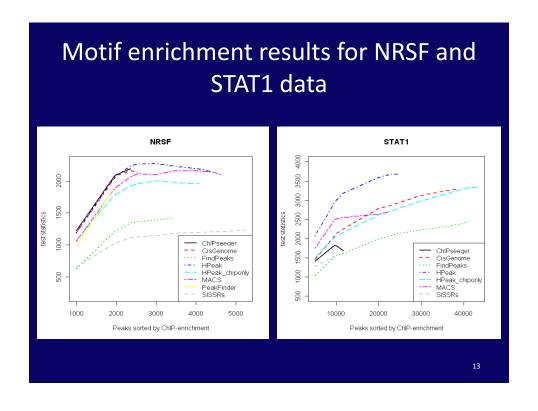
Using model-based methods to analyze ChIP-seq data

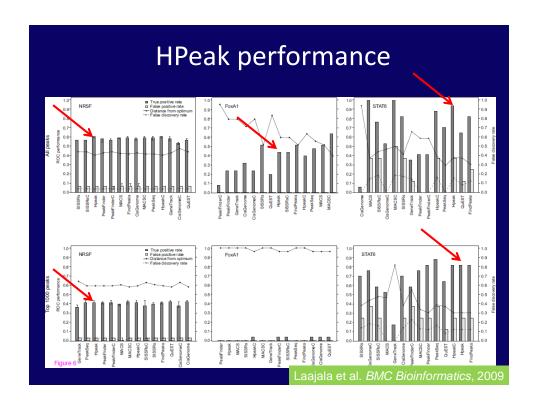
Outline

- Hidden Markov model for peak detection
- Hierarchical Hidden Markov model for combining ChIP-seq and ChIP-chip data, or analyze multiple ChIP-seq data
- Hybrid Monte Carlo strategy for Motif finding









GP and **ZIP** distribution

 Do not require mean equal to variance which is useful to model over-dispersion and underdispersion.

$$P(Y = y \mid \lambda, \phi) = \left(\frac{\lambda}{1 + \phi\lambda}\right)^{y} \frac{(1 + \phi\lambda)^{y-1}}{y!} \exp\left\{\frac{-\lambda(1 + \phi\lambda)}{1 + \phi\lambda}\right\}$$

$$E(Y) = \lambda$$

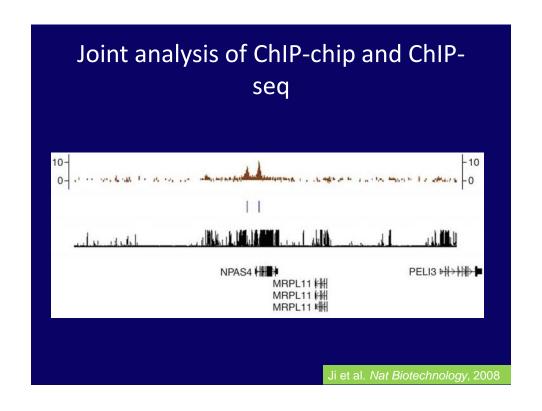
$$Var(Y) = \lambda(1 + \phi\lambda)^{2}$$

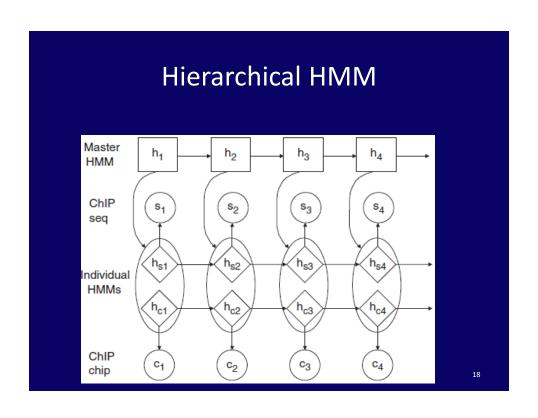
• Zero-inflated Poisson distribution

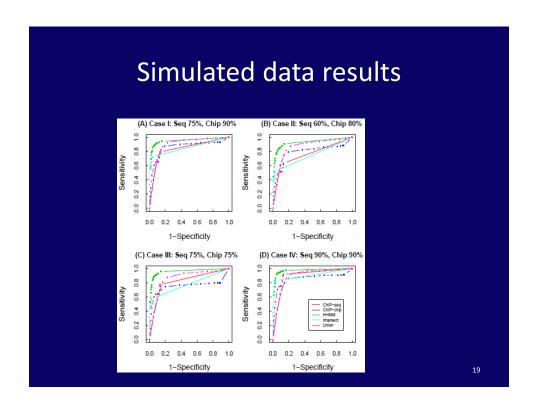
$$f(Y \mid \pi, \mu) = \begin{cases} (1 - \pi) + \pi e^{-\mu} & \text{if } x = 0\\ \frac{\pi e^{-\mu} \mu^{x}}{x!} & \text{if } x = 0 \end{cases}$$

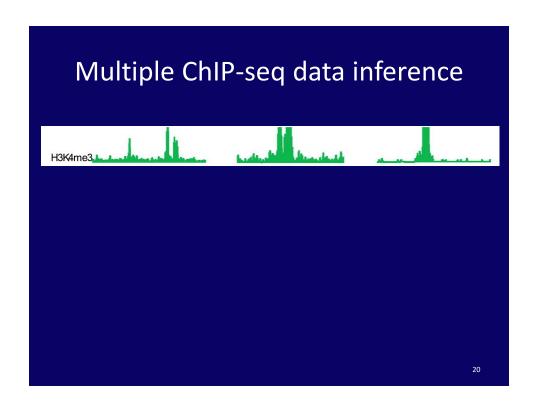
Outline

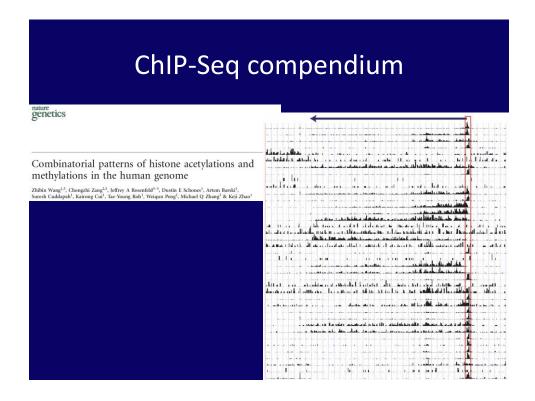
- Hidden Markov model for peak detection
- Hierarchical Hidden Markov model for combining ChIP-seq and ChIP-chip data
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The problem

- N series of data, each can be modeled by an HMM,
- The goal is to infer the hidden states for all series,
- Suppose there are k states for each chain, then the total number of possible states for the whole datasets is k^N , the size of the transition matrix is k^{2N} ,
 - Independent: ignore correlation among the data series,
 - A single HMM to model all data together: intractable for large N.

Our goal

- Allow coupling among the chains,
- The goal is to borrow information across different experiments/datasets,
- Limit the amount of coupling allowed to reduce computation cost

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Our learning plan

- Perform inference one series a time,
- Incorporate knowledge of hidden states in other series into the learning process,
- Assume sparsity in the correlation matrix.

Our model

- Use an inhomogeneous HMM to incorporate correlation,
- Define the transition kernel for series *j* and time t as:

$$K_j(t) = \begin{pmatrix} 1 - p_{jt} & p_{jt} \\ 1 - q_{jt} & q_{jt} \end{pmatrix}$$

$$p_{jt} = Pr(h_{j,t} = 1 | h_{j,t-1} = 0)$$
 and $q_{jt} = Pr(h_{j,t} = 1 | h_{j,t-1} = 1)$.

$$p_{jt} = Pr(h_{j,t} = 1 | h_{j,t-1} = 0) \text{ and } q_{jt} = Pr(h_{j,t} = 1 | h_{j,t-1} = 1).$$

$$\log \left(\frac{p_{jt}}{1 - p_{jt}}\right) = \beta_{j0}^p + \sum_{k \neq j} \left(\beta_{jk}^p h_{k,t-1} + \beta_{jk}^c h_{k,t}\right)$$

$$\log \left(\frac{q_{jt}}{1 - q_{jt}}\right) = \gamma_{j0}^p + \sum_{k \neq j} \left(\gamma_{jk}^p h_{k,t-1} + \gamma_{jk}^c h_{k,t}\right)$$

Our algorithm I

- Estimate regression parameters
 - Conditional on the current states, run penalized logistic regression to get model parameters,
 - LASSO penalty

$$\begin{array}{lcl} y_t & = & h_{j,t} \\ x_t & = & (h_{1,t-1}, \dots, h_{j-1,t-1}, h_{j+1,t-1}, \dots, h_{N,t-1}, h_{1,t}, \dots, h_{j-1,t}, h_{j+1,t}, \dots, h_{N,t}) \end{array}$$

$$\min_{(\beta_{j0}, \vec{\beta}_{j}^{p}, \vec{\beta}_{j}^{c})} \left\{ -\ell(\beta_{j0}, \vec{\beta}_{j}^{p}, \vec{\beta}_{j}^{c}) + \lambda P(\vec{\beta}_{j}^{p}, \vec{\beta}_{j}^{c}) \right\}$$

$$P(\vec{\beta}_j^p, \vec{\beta}_j^c) = \sum_{k \neq j} |\beta_{jk}^p| + \sum_{k \neq j} |\beta_{jk}^c|.$$

2

Our algorithm II

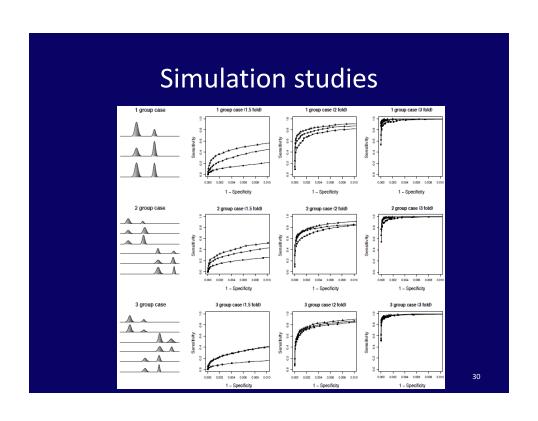
- Estimate transition kernel
 - Use the regression parameters estimated in step 1 and the current states of chains other than j, to get log odds for chain j at all time point t, then get estimated transition kernel.

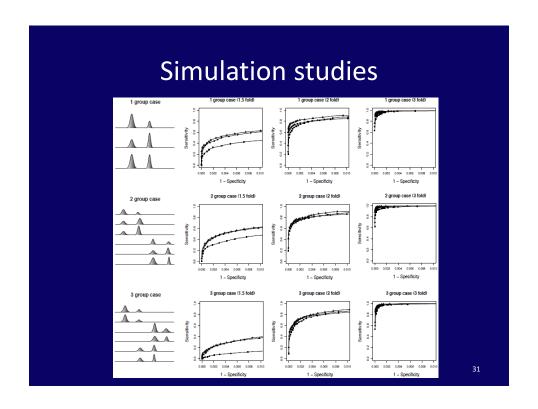
$$\log\left(\frac{p_{jt}}{1 - p_{jt}}\right) = \beta_{j0}^{p} + \sum_{k \neq j} \left(\beta_{jk}^{p} h_{k,t-1} + \beta_{jk}^{c} h_{k,t}\right)$$

$$\log\left(\frac{q_{jt}}{1 - q_{jt}}\right) = \gamma_{j0}^p + \sum_{k \neq j} \left(\gamma_{jk}^p h_{k,t-1} + \gamma_{jk}^c h_{k,t}\right)$$

Our algorithm III

- Infer hidden states
 - Use the transition kernel estimated in step 2, current emission probabilities and observed data to run regular HMM (forward-backward algorithm) to get updated hidden states,
- Estimate the emission probabilities
 - Use the hidden states estimated in step 3 and observed data to update emission probabilities.

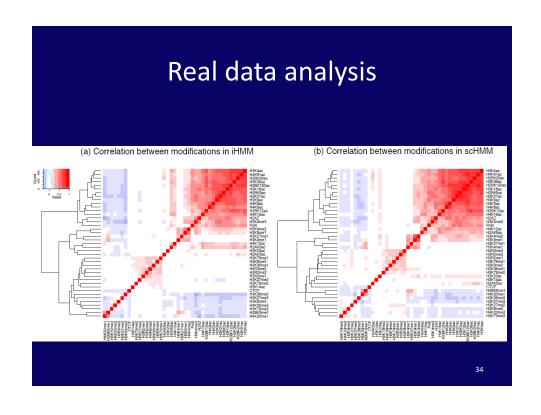


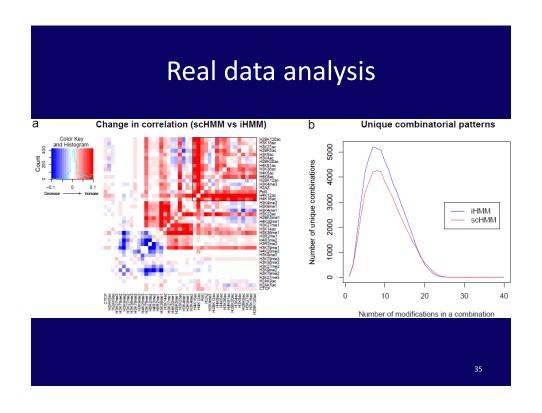


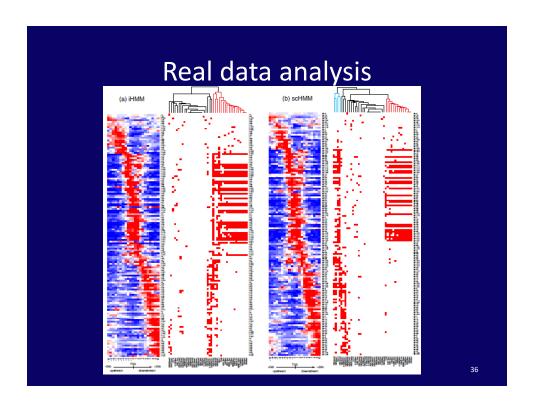
Real data

- In human CD4+ T cells,
- 39 histone acetylations and methylations marks + RNA polII + CTCF,
- 200 bp bin,
- 5kb up/downstream of TSS,
- Barski et al. Cell 2007, Wang et al. Nature Genetics, 2008.

		Dool	data	dacarin	+104		
		Kea	uala	descrip	lloi	1	
Modification	iHMM	scHMM	Total reads	Modification	iHMM	scHMM	Total reads
H2AK5ac	5,618	5,347	374,870	H3K36ac	32,380	31,862	655,289
H2AK9ac	3,998	4,060	201,966	H3K36me1	1,439	2,605	555,151
H2AZ	63,152	60,553	1,088,361	H3K36me3	35,439	35,541	819,837
H2BK5ac	56,892	48,426	881,711	H3K79me1	587	718	661,148
H2BK5me1	67,631	61,727	1,194,491	H3K79me2	78	81	104,286
H2BK12ac	30,013	$24,\!872$	500,166	H3K79me3	14,430	14,639	622,602
H2BK20ac	47,266	39,299	777,904	H4K5ac	33,974	33,154	590,147
H2BK120ac	53,868	$46,\!389$	808,654	H4K8ac	29,350	30,995	559,846
H3K4ac	38,632	33,967	628,729	H4K12ac	5,081	7,100	332,176
H3K4me1	82,169	79,515	1,481,457	H4K16ac	19,485	20,141	656,318
H3K4me2	46,714	$44,\!310$	795,272	H4K20me1	$116,\!137$	113,497	2,013,252
H3K4me3	92,959	89,257	5,897,624	H4K20me3	8,561	8,275	353,438
H3K9ac	40,946	37,891	698,889	H4K91ac	49,753	47,362	823,478
H3K9me1	78,438	77,059	1,314,559	H3R2me1	3,487	4,412	$695,\!472$
H3K9me2	560	634	371,501	H3R2me2	794	949	393,897
H3K9me3	5,719	5,616	204,051	H3R3me2	669	651	429,036
H3K14ac	141	227	239,242	CTCF	11,851	12,284	368,552
H3K18ac	54,268	$49,\!589$	809,752	Pol II	42,267	43,032	702,721
H3K23ac	1,303	2,434	206,604				
H3K27ac	58,177	54,879	847,666				
H3K27me1	22,060	24,774	722,841				
H3K27me2	1,586	1,860	383,301				
H3K27me3	28,286	28,622	767,709				







Joint inference of multiple ChIP-seq data

- JAMIE
 - Joint analysis of multiple ChIP-chip data
 - Wu, Ji Bioinformatics 2010
- HHMM
 - Joint analysis of ChIP-seq and ChIP-chip data
 - Choi et al. Bioinformatics 2009
- scHMM
 - Joint analysis of multiple ChIP-seq data
 - Choi et al. bioinformatics 2013

3

Acknowledgement



Hyung Won Choi National University of Singapore

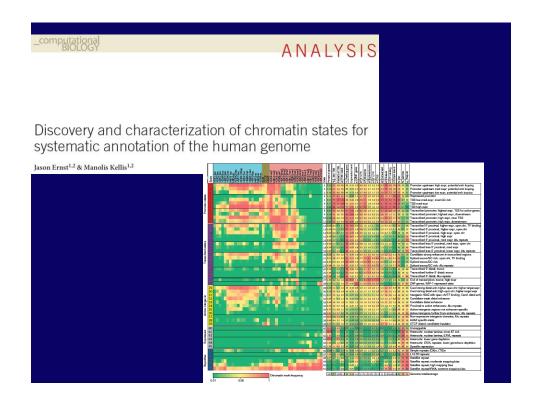


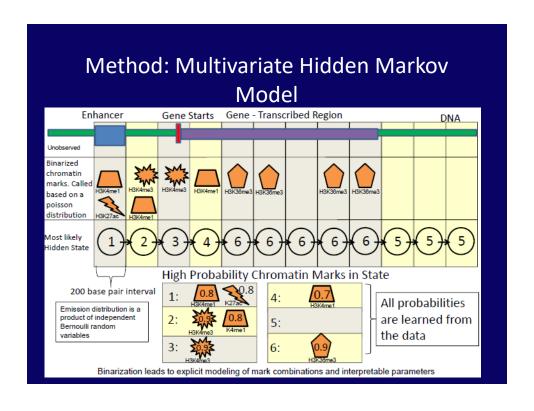
Debashis Ghosh Colorado School of Public Health

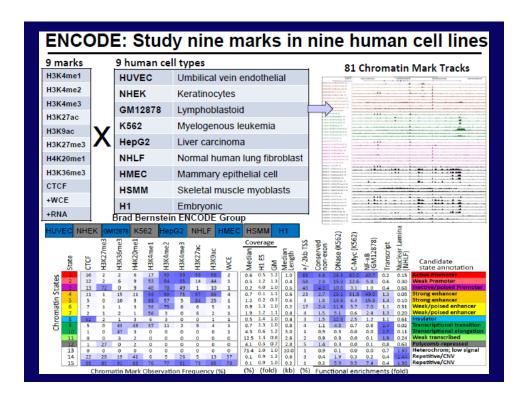
Alexey Nesvizhskii

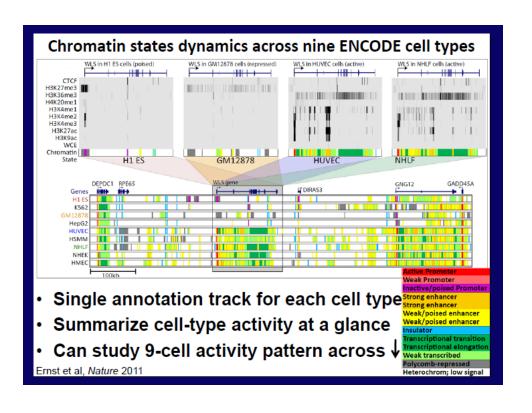
Damian Fermin

University of Michigan









Outline

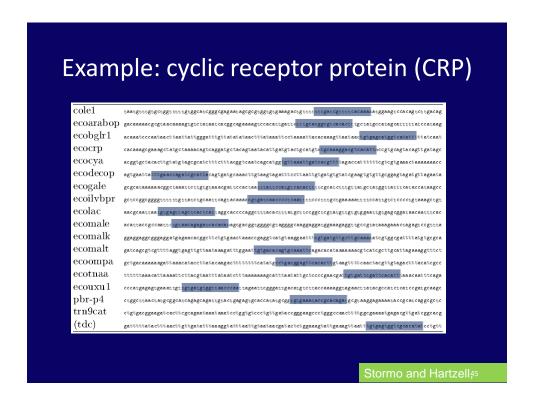
- Hidden Markov model for peak detection
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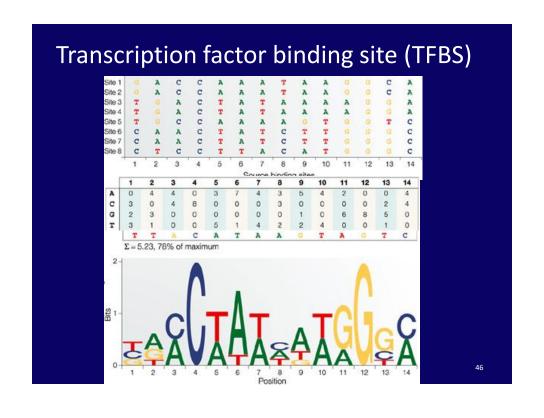
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Example: cyclic receptor protein (CRP)

cole1 ecocrp cacaaagcgaaagctatgctaaaacagtcaggatgctacagtaatacattgatgtactgcatgtatgcaaaggacgtcacattaccgtgcagtacagttgatagc ecocya $ecode cop \quad {\tt agtgaattatttgaaccagatcgcattacagtgatgcaaacttgtaagtagatttccttaattgtgatgtgtatcgaagtgtttgcggagtagatgttagaatagttagaattacttgaagtgatgttagaattacttagatgtattagaattacttagatgtattagaattacttagatgtattagaattacttagatgtattagaattacttagatgtattagaattacttagatgtattagaattacttagatgtattagaattacttagatgtattagaattacttagatgtattagaattacttagatgtattagatgtattagaattacttagatgtattagaattacttagatgtagatgtattagatgtattagatgtagatgtattagatgtattagatgtagatgtattagatgtag$ ecogale ecoilvbpr geteeggeggggttttttgttatetgeaatteagtacaaaacgtgateaacceeteaatttteeetttgetgaaaaatttteeattgteteeettgtaaagetgt ecolac ecomale $_{
m ecomalk}$ $_{
m ecomalt}$ ecotnaa ecouxu1 cccatgagagtgaaattgttgtgatgtggttaacccaattagaattcgggattgacatgtcttaccaaaaggtagaacttatacgccatctcatccgatgcaagc pbr-p4 trn9cat (tdc)

Stormo and Hartzell 1989





Existing *de novo* motif finding algorithms

Consensus

Gibbs Motif Sampler

• MEME

AlignACE

BioProspector

MDScan

Mobydick

•••

Review

Hertz *et al.* 1<u>990</u>

Lawrence et al. 1993

Bailey and Elkan 1994

Roth et al. 1998

Liu *et al.* 2001

Liu *et al.* 2002

Bussemaker et al. 2000

Tompa et al. 2005

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Motif identification model

```
aaaggtegagtagetactegategatactageaategttaccetagetegategaaa a_2
```

Alignment variable $A = \{a_1, a_2, ..., a_J\}$

Posterior distributions

 The posterior conditional distribution for alignment variable A

$$p(a_j = l \mid \boldsymbol{\theta_0}, \boldsymbol{\Theta}, \boldsymbol{R_j}, \boldsymbol{A_{-j}}) \propto \prod_{k=1}^4 \theta_{0k}^{h_k(\boldsymbol{R_j})} \prod_{i=1}^w \prod_{k=1}^4 \left(\frac{\theta_{ik}}{\theta_{0k}}\right)^{h_k(r_{j,l+i-1})} \propto \prod_{i=1}^w \prod_{k=1}^4 \left(\frac{\theta_{ik}}{\theta_{0k}}\right)^{h_k(r_{j,l+i-1})}$$

DNA sequence data

$$\boldsymbol{R} = (\boldsymbol{R}_1, ..., \boldsymbol{R}_J)$$

Lawrence et al. Science 1993, Liu et al. JASA 1995

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Why de novo motif search

- The only option when the TF binding motif pattern is unknown.
- Reassuring to be able to rediscover the known TFBS motif.
- Many "known" motif patterns are biased and inaccurate.
- Multiple co-factors are often required in transcription regulation in eukaryotes.
- Binding specificity for some TFs may change under different conditions.

Challenges faced

- How to handle large number of input sequences?
- How to utilize sequencing depth information?



Johnson et al. Science

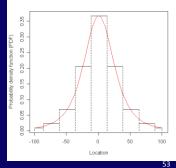
Features of our new algorithm

- Incorporate sequencing depth information in the statistical model.
- Generalize the product multinomial model to allow inter-dependent positions within the motif.
- Adopt a hybrid Monte Carlo strategy to speed up the traditional Gibbs sampler-based algorithm.

The informative prior

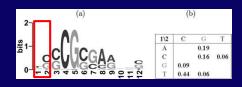
- The prior is symmetric and centered at the peak summit.
- The prior probabilities stem from Student's tdistribution with df=3.

$$p(a_j = l) \propto t_3 \left[\inf \left[\frac{|l + w/2 - s_j| + u/2}{u} \right] \right]$$

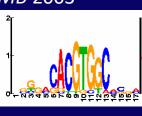


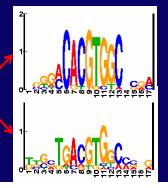
Modeling inter-dependent positions

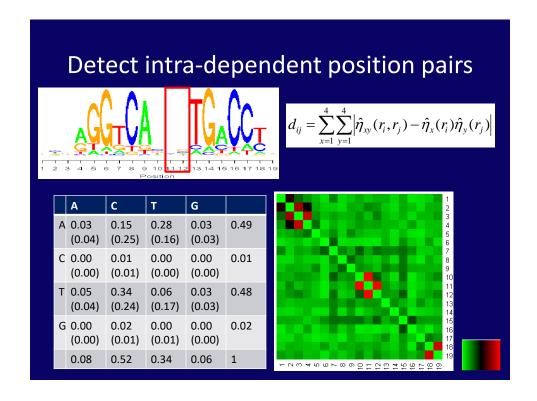
• Zhou and Liu Bioinformatics 2005



• Barash et al. RECOMB 2003







New algorithm

 The posterior conditional distribution of alignment variable A under the new statistical model.

$$p(a_{j} = l | \boldsymbol{\theta_{0}}, \boldsymbol{\Theta}, \boldsymbol{R_{j}}, \boldsymbol{A_{-j}}) \propto \frac{I_{\{z_{j} > 1\}} \cdot U \cdot V \cdot p(a_{j} = l)}{P \text{ (Background}_{j, l})}$$

$$U = \prod_{i \in S} \prod_{k=1}^{4} \hat{\theta}_{ik}^{h_{k}(r_{j, l+i-1}) + \alpha_{0, k}}$$

$$V = \prod_{i_{1}, i_{2} \in P} \prod_{k_{1}=1}^{4} \prod_{k_{2}=1}^{4} \hat{\theta}_{i_{1}, i_{2}}^{h_{k_{1}k_{2}}(r_{j, l+i_{1}-1}, r_{j, l+i_{2}-1}) + \beta_{0, k_{1}, k_{2}}}$$

Prioritized hybrid Monte Carlo

- Subject each sequence to either stochastic sampling or greedy search.
- Input sequences are not created equal.
- ChIP-enrichment is indicative of binding affinity.

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Implementation

- Hybrid Motif Sampler (HMS).
- Gibbs sampler type iterative procedure.
- Run multiple chains to avoid trapping in local mode.

Performance comparison

- Two established and popular motif discovery tools:
 - MEME (Bailey and Elkan 1994),
 - EM-based motif finding algorithm,
 - widely used.
 - MDscan (Liu et al. 2002),
 - designed to analyze ChIP-chip data,
 - combines word enumeration and probability matrix updating,
 - take into account ChIP-chip ranking,
 - very fast.

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Real data analysis

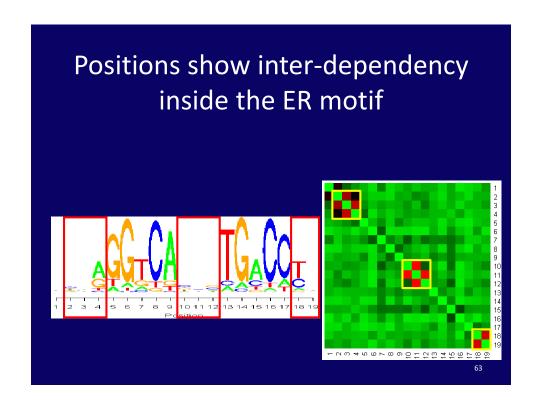
TF	Cell type Antibody		# of peaks	Coverage	Reference
		Monoclonal			
NRSF	Jurkat T cell	12C11	4,982	1.4 MB	Johnson et al. (2007)
STAT1	HeLa S3 cell	Polyclonal	27,470	8.1 MB	Robertson et al. (2007)
CTCF	CD4+ T cell	Upstate 07-729	22,159	7.4 MB	Barski et al. (2007)
ER	MCF7 cell	ER Q (HC-20)	10,072	2.5 MB	

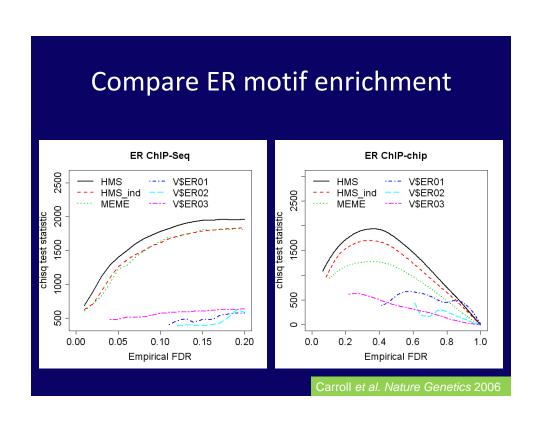
Performance evaluation

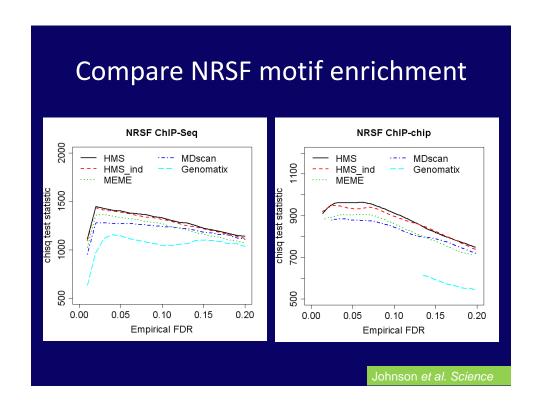
- Cross validation
 - Randomly separate all peaks into two halves: training and testing.
 - Run motif finding algorithms on the training data to predict the motif pattern.
 - Scan testing data using the identified motif pattern and compare to a set of control sequences.
- Testing
 - Using Chi-square test statistics to quantify motif enrichment .
 - Estimate FDR and plot FDR versus Chi-square test statistics.

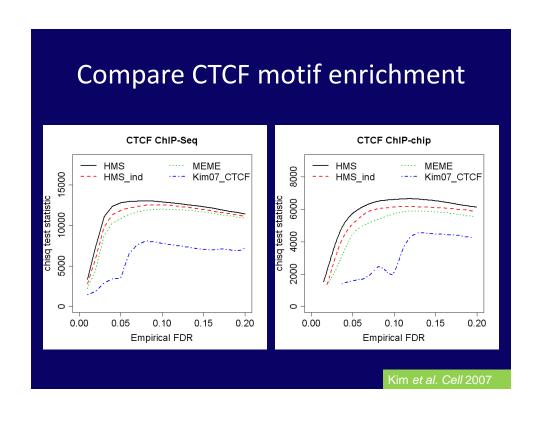
6:

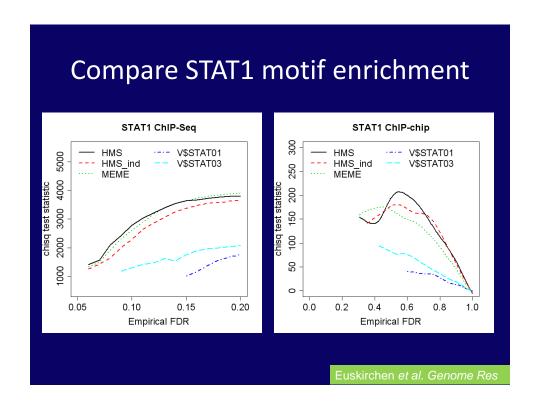
Compare ER motif patterns • V\$ER01* • V\$ER02* • V\$ER03* • MEME • HMS

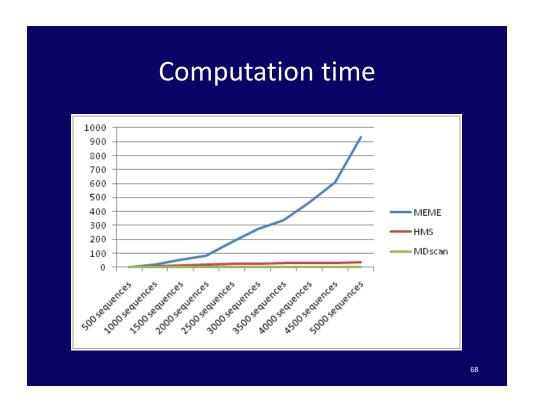












Summary

- ChIP-Seq data offers abundant information and provides much improved opportunity for studying protein-DNA interaction.
- There are many biological and technical factors that affect the ChIP-Seq data we observe, careful modeling is critical in order to process ChIP-Seq data efficiently and thoroughly.
- New sequencing data are different from microarray, ChIP-chip data. Methods developed there do not work well for analyzing sequencing data, new models and algorithms need to be developed.

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Apply to cancer genomics Cancer Cell Article Cancer Cell Article An Integrated Network of Androgen Receptor, Polycomb, and TMPRSS2-ERG Gene Fusions in Prostate Cancer Progression Jindar Yu.1-3-A.7 Janjun Yu.1-3 Ram-Shankar Man (1-3 O Cao.1-3 Chad. J. Brenner, 1-3 Xuhong Cao,1-2-3 Xiaoja Wang, 1-3 Sunits Shankar, 1-3 Yong Di, 1-3 Sarawan Monache Androgen Receptor, Polycomb, And TMPRSS2-ERG Gene Fusions in Prostate Cancer Progression Jindar Yu.1-3-A.7 Janjun Yu.1-3 Ram-Shankar Man (1-3 O Cao.1-3 Chad. J. Brenner, 1-3 Xuhong Cao,1-2-3 Xiaoja Wang, 1-3 Sunits Shankar, 1-3 Yong Di, 1-3 Sarawan And Di, 1-3 Sarawan And Di, 1-3 Sarawan And Disnasaskaran, 1-3 Roger Money, 1-3 Termone Barretts, 1-3 Robert J. Lonigro, 1-3 Scott A. Tomins, 1-3 Sooryanarayana Varambaly, 1-3-4 Zhaohul S. Oin, 2 and And M. Chinnalyann-2-3-6.8-7

Reference

 Qin ZS, Yu J, Shen J, Maher CA, Hu M, Kalyana-Sundaram S, Yu J, Chinnaiyan AM. (2009) HPeak: An HMM-based Algorithm for Defining Read-enriched Regions in ChIP-Seq Data. BMC Bioinformatics. 11 369.

http://www.sph.umich.edu/csg/qin/HPeak/

 Choi H, Nesvizhskii A, Ghosh D, Qin ZS. (2009) Hierarchical Hidden Markov Model with Application to Joint Analysis of ChIP-chip and ChIP-seq Data. *Bioinformatics* 25 1715-1721.

http://sourceforge.net/projects/chipmeta/

 Hu M, Yu J, Taylor, JMG, Chinnaiyan AM, Qin ZS. (2010) On the Detection and Refinement of Transcription Factor Binding Sites Using ChIP-Seq Data. Nucleic Acids Res. 38 2154-2167.

http://www.sph.umich.edu/csg/qin/HMS/

 Hu M, Zhu Y, Taylor JMG, Liu JS, Qin ZS (2011). Using Poisson mixedeffects model to quantify exon-level gene expression in RNA-seq. Bioinformatics. 28 63-68.

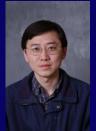
http://www.stat.purdue.edu/~yuzhu/pome.html

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Michael Yu Zhu
Purdue University