

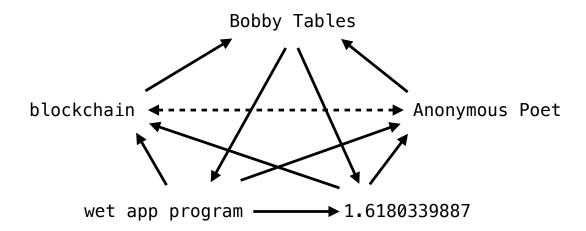


Congratulations to the Winners of the Hog Strategy Contest

1st Place with 146 wins:

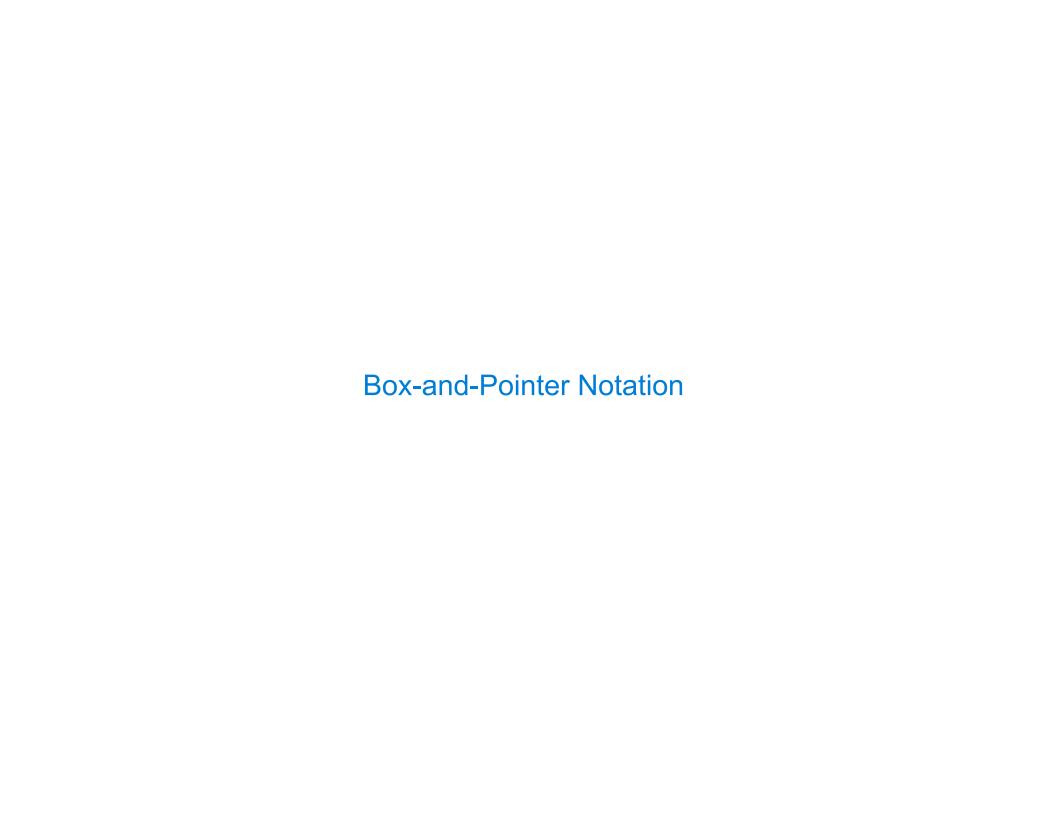
A five-way tie for first place!

"A submission scores a match point each time it has an expected win rate strictly above 50.0001%."



Congratulations to Timothy Guo, Shomini Sen, Samuel Berkun, Mitchell Zhen, Lucas Clark, Dominic de Bettencourt, Allen Gu, Alec Li, Aaron Janse

hog-contest.cs61a.org



The Closure Property of Data Types

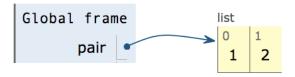
- A method for combining data values satisfies the *closure property* if:

 The result of combination can itself be combined using the same method
- Closure is powerful because it permits us to create hierarchical structures
- Hierarchical structures are made up of parts, which themselves are made up of parts, and so on

Lists can contain lists as elements (in addition to anything else)

Box-and-Pointer Notation in Environment Diagrams

Lists are represented as a row of index-labeled adjacent boxes, one per element Each box either contains a primitive value or points to a compound value

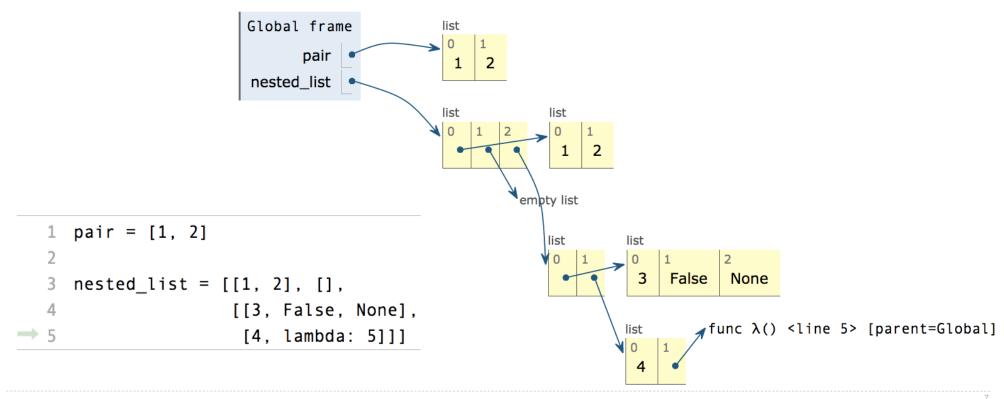


pair = [1, 2]

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Box-and-Pointer Notation in Environment Diagrams

Lists are represented as a row of index-labeled adjacent boxes, one per element Each box either contains a primitive value or points to a compound value

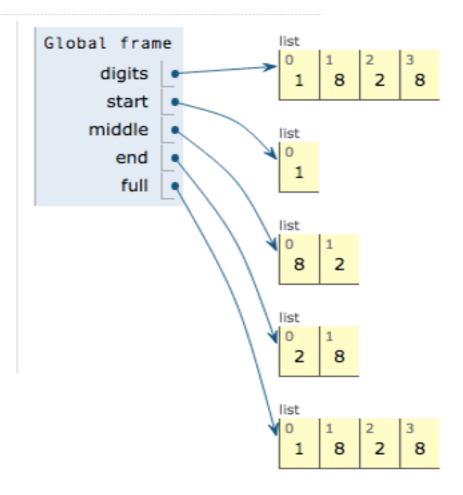


Slicing

Slicing Creates New Values

```
1 digits = [1, 8, 2, 8]
2 start = digits[:1]
3 middle = digits[1:3]
4 end = digits[2:]

> 5 full = digits[:]
```



pythontutor.com/composingprograms.html#code=digits%20%3D%20fijn=composingprograms.html#code=digits%20%3D%20digits[%3A]]%0Astart%20%3

Processing Container Values

Sequence Aggregation

Several built-in functions take iterable arguments and aggregate them into a value

- sum(iterable[, start]) -> value

 Return the sum of a 'start' value (default: 0) plus an iterable of numbers.
- max(iterable[, key=func]) -> value
 max(a, b, c, ...[, key=func]) -> value

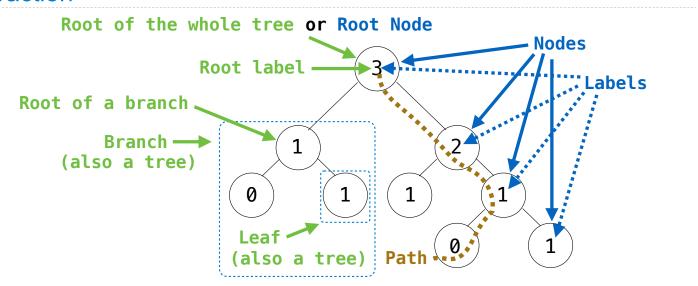
With a single iterable argument, return its largest item. With two or more arguments, return the largest argument.

• all(iterable) -> bool

Return True if bool(x) is True for all values x in the iterable. If the iterable is empty, return True.



Tree Abstraction



Recursive description (wooden trees):

A tree has a root label and a list of branches
Each branch is a tree
A tree with zero branches is called a leaf
A tree starts at the root

Relative description (family trees):

Each location in a tree is called a **node**Each **node** has a **label** that can be any value
One node can be the **parent/child** of another
The top node is the **root node**

People often refer to labels by their locations: "each parent is the sum of its children"

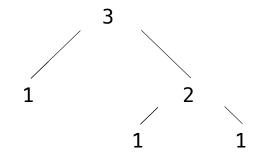
Implementing the Tree Abstraction

```
def tree(label, branches=[]):
    return [label] + branches

def label(tree):
    return tree[0]

def branches(tree):
    return tree[1:]
```

- A tree has a root label and a list of branches
- Each branch is a tree



```
>>> tree(3, [tree(1),
... tree(2, [tree(1),
... tree(1)])])
[3, [1], [2, [1], [1]]]
```

Implementing the Tree Abstraction

```
def tree(label, branches=[]):

    A tree has a root label

                                     Verifies the
   for branch in branches:
                                                             and a list of branches
                                   tree definition
        assert is tree(branch)

    Each branch is a tree

    return [label] + list(branches)
                                                                       3
                        Creates a list
def label(tree):
                       from a sequence
    return tree[0]
                         of branches
def branches(tree):
                      Verifies that
    return tree[1:]
                      tree is bound
                        to a list
def is_tree(tree):
                                                       >>> tree(3, [tree(1),
    if type(tree) != list or len(tree) < 1:</pre>
                                                                    tree(2, [tree(1),
        return False
                                                                              tree(1)1)1)
                                                       [3, [1], [2, [1], [1]]]
    for branch in branches(tree):
        if not is tree(branch):
                                                 def is leaf(tree):
            return False
                                                      return not branches(tree)
                                                                                         (Demo)
    return True
```

Tree Processing

Tree Processing Uses Recursion

Processing a leaf is often the base case of a tree processing function

The recursive case typically makes a recursive call on each branch, then aggregates

```
def count_leaves(t):
    """Count the leaves of a tree."""
    if is_leaf(t):
        return 1
    else:
        branch_counts = [count_leaves(b) for b in branches(t)]
        return sum(branch_counts)
```

Discussion Question

```
Implement leaves, which returns a list of the leaf labels of a tree
Hint: If you sum a list of lists, you get a list containing the elements of those lists
  >>> sum([ [1], [2, 3], [4] ], [])
                                       def leaves(tree):
  [1, 2, 3, 4]
                                           """Return a list containing the leaf labels of tree.
  >>> sum([ [1] ], [])
                                           >>> leaves(fib tree(5))
  [1]
  >>> sum([ [[1]], [2] ], [])
                                           [1, 0, 1, 0, 1, 1, 0, 1]
  [[1], 2]
                                           if is leaf(tree):
                                               return [label(tree)]
                                           else:
                                               return sum(List of leaf labels for each branch, [])
                                                   [b for b in branches(tree)]
       branches(tree)
       leaves(tree)
                                                   [s for s in leaves(tree)]
        [branches(b) for b in branches(tree)]
                                                   [branches(s) for s in leaves(tree)]
       [leaves(b) for b in branches(tree)]
                                                   [leaves(s) for s in leaves(tree)]
```

Creating Trees

def increment_leaves(t):
 """Return a tree like t but with leaf labels incremented."""
 if is_leaf(t):
 return tree(label(t) + 1)
 else:
 bs = [increment_leaves(b) for b in branches(t)]
 return tree(label(t), bs)

def increment(t):
 """Return a tree like t but with all labels incremented."""
 return tree(label(t) + 1, [increment(b) for b in branches(t)])

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Example: Printing Trees

Example: Summing Paths