

习题 7.3

1. 求下列微分方程的通解:

(1) $\frac{dy}{dx} = \frac{y}{x} + \cot \frac{y}{x};$

(2) $2xydx - (x^2 + y^2)dy = 0;$

(3) $x \frac{dy}{dx} + 2\sqrt{xy} = y \quad (x < 0);$

(4) $(1 + 2e^{\frac{x}{y}})dx + 2e^{\frac{x}{y}}(1 - \frac{x}{y})dy = 0.$

2. 求微分方程 $\frac{dy}{dx} = \frac{x}{y} + \frac{y}{x}$ 满足初值条件 $y|_{x=1} = 2$ 的特解:

3. 作适当的变量变化求下列微分方程的通解:

(1) $\frac{dy}{dx} = \frac{1}{(x+y)^2};$

(2) $\frac{dy}{dx} = \frac{y-x-2}{x+y+4};$