

APM466 Assignment 1: Canadian Government Bonds Analysis

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Fundamental Questions

1. Government Bond Issuance and Economic Policy

(a) **Why issue bonds?** Governments issue bonds to finance deficits without causing inflation. Printing money leads to hyperinflation and currency devaluation.

(b) **Yield curve flattening example:** Central bank raises short-term rates while long-term growth expectations weaken. Example: 2-year yields rise from 2% to 3% but 10-year yields only to 3.2%.

(c) **Quantitative easing:** Central banks purchase government bonds to inject liquidity. During COVID-19, the US Fed implemented \$4.5 trillion QE.

2. Bond Selection

Bond	Coupon	Maturity	Years
CAN 4.0 Aug 26	4.000%	2026-08-03	0.58
CAN 3.0 Feb 27	3.000%	2027-02-01	1.07
CAN 2.5 Aug 27	2.500%	2027-08-01	1.57
CAN 2.25 Feb 28	2.250%	2028-02-01	2.07
CAN 2.0 Jun 28	2.000%	2028-06-01	2.40
CAN 4.0 Mar 29	4.000%	2029-03-01	3.15
CAN 2.25 Jun 29	2.250%	2029-06-01	3.40
CAN 2.25 Dec 29	2.250%	2029-12-01	3.90
CAN 2.75 Sep 30	2.750%	2030-09-01	4.65
CAN 2.75 Mar 31	2.750%	2031-03-01	5.15

Selection: Maturities closest to 0.5-5 years, large issue volumes (\$20B), recent issue dates.

3. PCA Concept

Eigenvalues = variance explained by each component. Eigenvectors = direction of max variance. For rates: PC1=parallel shift, PC2=slope, PC3=curvature.

Empirical Analysis

4(a) Yield Curves

YTM solves $P = \sum_{k=1}^{2T} \frac{C/2}{(1+y/2)^k} + \frac{100}{(1+y/2)^{2T}}$

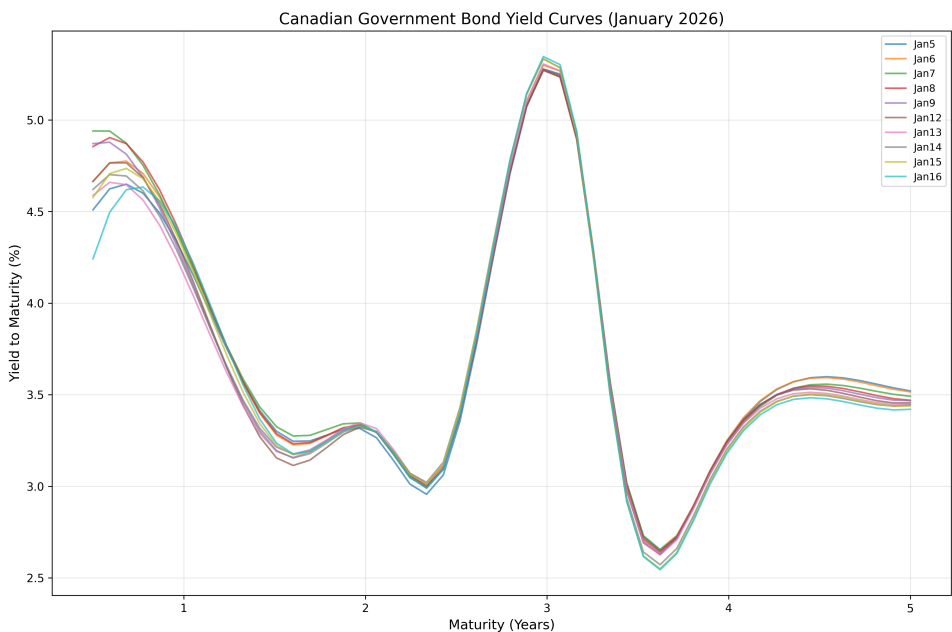


Figure 1: 5-Year Yield Curves (Jan 5-16, 2026)

4(b) Spot Curves

Bootstrapping: 1) Sort bonds by maturity. 2) For each bond i , solve $\text{Price}_i = \sum \frac{C_i/2}{(1+r_t)^{t/2}} + \frac{100}{(1+r_{T_i})^{T_i}}$. 3) Interpolate.

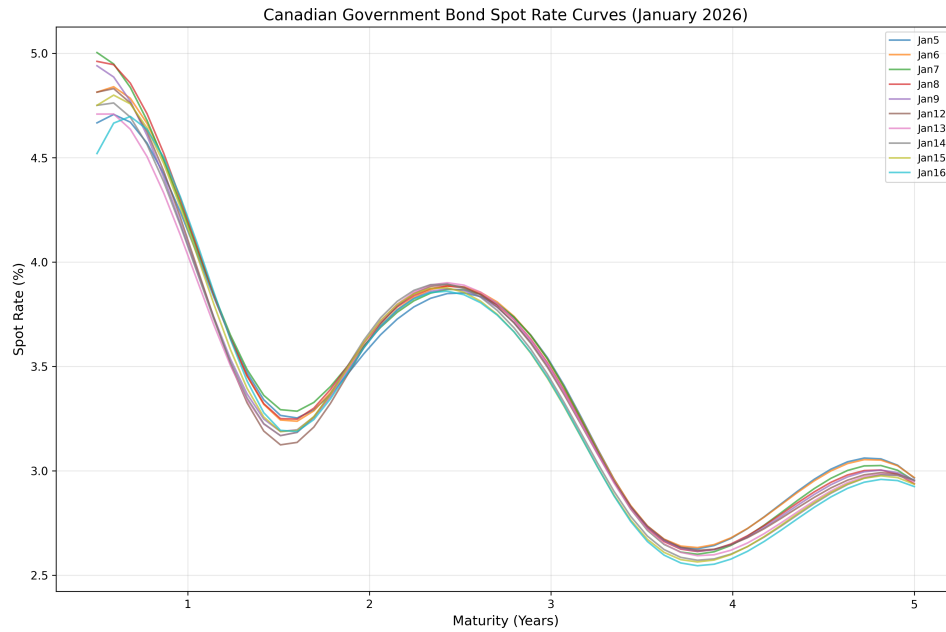


Figure 2: 5-Year Spot Rate Curves

4(c) Forward Curves

Calculation: $F_{t,T} = \left[\frac{(1+S_T)^T}{(1+S_t)^t} \right]^{1/(T-t)} - 1$, where $t = 1, T = 2, 3, 4, 5$.

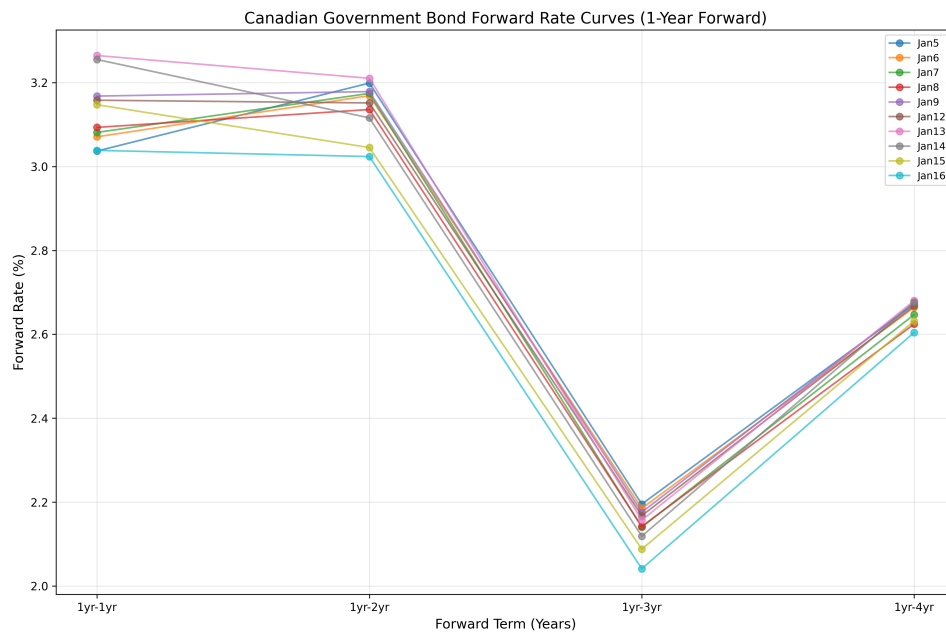


Figure 3: 1-Year Forward Rate Curves

5. Covariance Matrices

Daily log returns: $X_{i,j} = \ln(r_{i,j+1}/r_{i,j})$ for yields (1-5yr) and forwards (1yr-1yr to 1yr-4yr). Matrices show strong positive correlation.

6. Principal Component Analysis

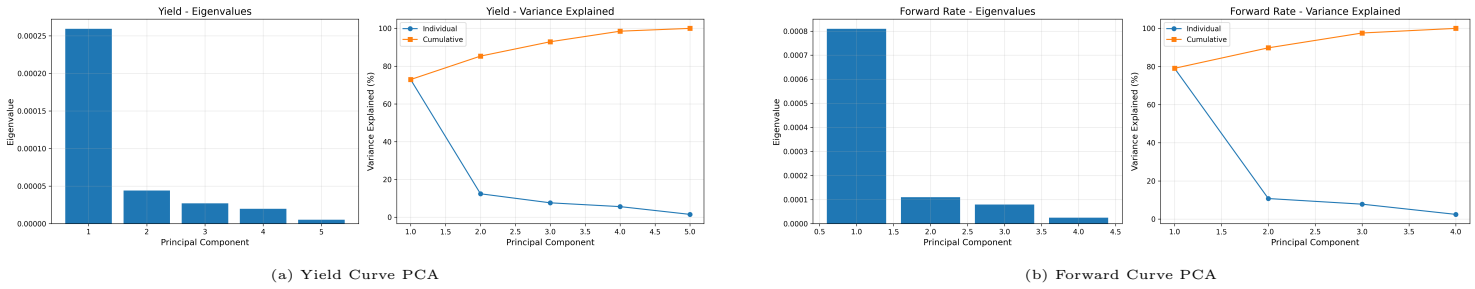


Figure 4: PCA Analysis Results

Comp.	Eigenvalue	Variance
PC1	2.59×10^{-4}	72.91%
PC2	4.41×10^{-5}	12.40%
PC3	2.71×10^{-5}	7.61%
PC4	1.99×10^{-5}	5.60%
PC5	5.28×10^{-6}	1.49%

Comp.	Eigenvalue	Variance
PC1	8.10×10^{-4}	79.06%
PC2	1.10×10^{-4}	10.73%
PC3	7.97×10^{-5}	7.78%
PC4	2.48×10^{-5}	2.42%

PCA Interpretation

First principal component explains 72.91% (yield) and 79.06% (forward) of variance, representing parallel shifts of the entire curve. This indicates level changes are the dominant risk factor, driven by monetary policy and macroeconomic expectations. Second component explains slope changes, third explains curvature.

Conclusion

Successfully constructed yield, spot, and forward curves using bootstrapping. PCA analysis shows parallel shifts account for 72.91% of daily yield movements and 79.06% of forward rate movements, consistent with fixed income literature where level factor dominates term structure dynamics.

References

[1] Bank of Canada. Valet Web Services: Government of Canada benchmark bond yields (CSV). https://www.bankofcanada.ca/valet/observations/group/bond_yields_benchmark/csv

[2] Markets Insider. Bond market data. <https://markets.businessinsider.com/bonds>

[3] Hull, J. C. (2021). *Options, Futures, and Other Derivatives* (11th ed.). Pearson. <https://www.pearson.com/en-us/subject-catalog/p/options-futures-and-other-derivatives/P200000005938/9780136939917>

[4] Litterman, R. B., & Scheinkman, J. (1991). Common factors affecting bond returns. *The Journal of Fixed Income*, 1(1), 54–61. <https://www.pm-research.com/content/iiijfixinc/1/1/54>

Code Repository

<https://github.com/XuxuZhou02/apm466-assignment1>