

MODULE *PODCommit*

This specification is the very basic version of POD (Proof of Devotion) from *Nebulas*. In this specification, we have the following assumptions to simplify the basic idea.

- No dumber node.
- No dynasty change.
- No node change or abdication.
- Assume one node only propose one value.
- Assume there is no failure node, and eventually all nodes should be consistent.
- We don't consider the liveness problem.
- We don't consider normal nodes besides validators.

CONSTANT *Validator*, The set of validators

*Majority*  $1 + n * 2/3$  validators

VARIABLES *vrState*, *vrState*[*r*] is the state of validator

*vrPrepared*, *vrPrepared*[*r*] is the set of validators from which *r* has received "Prepared" messages for *v*'s proposal

*vrCommitted*, *vrCommitted*[*r*] is the set of validators from which *r* has received "vote" messages for *v*'s proposal

*vrFinal*, *vrFinal*[*r*] is the final value, which the proposer.

*msgs*

In the protocol, processes communicate with one another by sending messages. For simplicity, we represent message passing with the variable *msgs* whose value is the set of all messages that have been sent. A message is sent by adding it to the set *msgs*. An action that, in an implementation, would be enabled by the receipt of a certain message is here enabled by the presence of that message in *msgs*. For simplicity, messages are never removed from *msgs*. This allows a single message to be received by multiple receivers. Receipt of the same message twice is therefore allowed; but in this particular protocol, that shouldn't be a problem.

ASSUME

$\wedge \text{Majority} \subseteq \text{SUBSET } \text{Validator}$

$\wedge \forall MS1, MS2, MS3 \in \text{Majority} : MS1 \cap MS2 \cap MS3 \neq \{\}$

All we assume about the set *Majority* of majorities is that any three majorities have non-empty intersection, which makes sure *Majority* is at least 2/3 validators.

*Messages*  $\triangleq$

The set of all possible messages. The *ins* field indicates the sender. For "propose" message, the "*ins*" field means she propose a block. Since we do not mind the proposed value, we do not record the proposed value here. The *acc* field indicates the sender of a message.

$[type : \{\text{"propose"}\}, ins : \text{Validator}, acc : \text{Validator}]$

$\cup$

$[type : \{\text{"prepare"}\}, ins : \text{Validator}, acc : \text{Validator}]$

$\cup$

$[type : \{\text{"vote"}\}, ins : \text{Validator}, acc : \text{Validator}]$

*PODTypeOK*  $\triangleq$

$\wedge vrState \in [\text{Validator} \rightarrow \{\text{"working"}, \text{"prepared"}, \text{"committed"}, \text{"finality"}\}]$

$\wedge vrPrepared \in [\text{Validator} \rightarrow \{\text{Validator}\}]$

$\wedge vrCommitted \in [\text{Validator} \rightarrow \{\text{Validator}\}]$

$\wedge vrFinal \in [\text{Validator} \rightarrow \text{Validator} \cup \{\text{"none"}\}]$

$\wedge \text{msgs} \subseteq \text{Messages}$

$\text{PODInit} \triangleq$  The initial predicate  
 $\wedge \text{vrState} = [v \in \text{Validator} \mapsto \text{"working"}]$   
 $\wedge \text{vrPrepared} = [v \in \text{Validator} \mapsto \{\}]$   
 $\wedge \text{vrCommitted} = [v \in \text{Validator} \mapsto \{\}]$   
 $\wedge \text{vrFinal} = [v \in \text{Validator} \mapsto \text{"none"}]$   
 $\wedge \text{msgs} = \{\}$

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**THE ACTIONS**

$\text{Send}(m) \triangleq \text{msgs}' = \text{msgs} \cup \{m\}$

An action expression that describes the sending of message  $m$ .

$\text{PreparedSet}(\text{set}, r) \triangleq \{m \in \text{set} : m.\text{acc} = r\}$   
 $\text{CommittedSet}(\text{set}, r) \triangleq \{m \in \text{set} : m.\text{acc} = r\}$

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**Validator ACTIONS**

$\text{ValidatorPropose}(r) \triangleq$

Validator try to propose a block

$\wedge \text{vrState}[r] = \text{"working"}$   
 $\wedge \text{vrState}' = [\text{vrState} \text{ EXCEPT } ![r] = \text{"prepared"}]$   
 $\wedge \text{vrPrepared}' = [\text{vrPrepared} \text{ EXCEPT } ![r] = \{\text{[type} \mapsto \text{"prepare", ins} \mapsto r, \text{acc} \mapsto r]\}]$   
 $\wedge \text{Send}([\text{type} \mapsto \text{"propose", ins} \mapsto r, \text{acc} \mapsto r])$   
 $\wedge \text{Send}([\text{type} \mapsto \text{"prepare", ins} \mapsto r, \text{acc} \mapsto r])$   
 $\wedge \text{UNCHANGED } \langle \text{vrCommitted}, \text{vrFinal} \rangle$

$\text{ValidatorChooseToCommit} \triangleq$

Validator try to vote a block

$\wedge \text{LET } \text{ChooseToCommit}(r, v) \triangleq$   
 $\quad \wedge \text{LET } \text{Prepared} \triangleq \{m.\text{ins} : m \in \text{PreparedSet}(\text{vrPrepared}[r], v)\}$   
 $\quad \text{IN } \text{Prepared} \in \text{Majority}$   
 $\quad \wedge \text{vrState}[r] = \text{"prepared"}$   
 $\quad \wedge \text{vrState}' = [\text{vrState} \text{ EXCEPT } ![r] = \text{"committed"}]$   
 $\quad \wedge \text{vrCommitted}' = [\text{vrCommitted} \text{ EXCEPT } ![r] = \text{vrCommitted}[r] \cup \{\text{[type} \mapsto \text{"vote", ins} \mapsto r, \text{acc} \mapsto v]\}]$   
 $\quad \wedge \text{Send}([\text{type} \mapsto \text{"vote", ins} \mapsto r, \text{acc} \mapsto v])$   
 $\text{IN}$   
 $\quad \forall r \in \text{Validator}, v \in \text{Validator} : \text{ChooseToCommit}(r, v)$   
 $\wedge \text{UNCHANGED } \langle \text{vrPrepared}, \text{vrFinal} \rangle$

$\text{ValidatorChooseToFinal} \triangleq$

Validator try to final a block.

$\wedge \text{LET } \text{ChooseToFinal}(r, v) \triangleq$   
 $\quad \wedge \text{LET } \text{Committed} \triangleq \{m.\text{ins} : m \in \text{CommittedSet}(\text{vrCommitted}[r], v)\}$

IN  $Committed \in Majority$   
 $\wedge vrState[r] = \text{"committed"}$   
 $\wedge vrState' = [vrState \text{ EXCEPT } ![r] = \text{"finality"}]$   
 $\wedge vrFinal' = [vrFinal \text{ EXCEPT } ![r] = v]$   
 IN  
 $\forall r \in Validator, v \in Validator : ChooseToFinal(r, v)$   
 $\wedge \text{UNCHANGED } \langle vrPrepared, vrCommitted \rangle$

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*RECV* messages

$RecvPropose(r, v) \triangleq$

The action when recv a prepare message.

$\wedge vrState[r] = \text{"working"}$   
 $\wedge \exists m \in msgs :$   
 $\quad \wedge m.type = \text{"propose"}$   
 $\quad \wedge m.ins = v$   
 $\wedge vrState' = [vrState \text{ EXCEPT } ![r] = \text{"prepared"}]$   
 $\wedge Send([type \mapsto \text{"prepare"}, ins \mapsto r, acc \mapsto v])$   
 $\wedge vrPrepared' = [vrPrepared \text{ EXCEPT } ![r] = \{[type \mapsto \text{"prepare"}, ins \mapsto r, acc \mapsto v]\}]$   
 $\wedge \text{UNCHANGED } \langle vrCommitted, vrFinal \rangle$

$RecvPrepare(r, from, v) \triangleq$

The action when recv a prepare message.

$\wedge vrState[r] = \text{"prepared"}$   
 $\wedge \exists m \in msgs :$   
 $\quad \wedge m.type = \text{"prepare"}$   
 $\quad \wedge m.acc = v$   
 $\quad \wedge m.ins = from$   
 $\wedge vrPrepared' = [vrPrepared \text{ EXCEPT } ![r] = vrPrepared[r] \cup \{[type \mapsto \text{"prepare"}, ins \mapsto r, acc \mapsto v]\}]$   
 $\wedge \text{UNCHANGED } \langle vrCommitted, vrState, vrFinal \rangle$

$RecvVote(r, from, v) \triangleq$

The action when recv a vote message.

$\wedge vrState[r] = \text{"prepared"}$   
 $\wedge \exists m \in msgs :$   
 $\quad \wedge m.type = \text{"vote"}$   
 $\quad \wedge m.acc = v$   
 $\quad \wedge m.ins = from$   
 $\wedge vrCommitted' = [vrCommitted \text{ EXCEPT } ![r] = vrCommitted[r] \cup \{[type \mapsto \text{"prepare"}, ins \mapsto r, acc \mapsto v]\}]$   
 $\wedge \text{UNCHANGED } \langle vrPrepared, vrState \rangle$

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$PODNext \triangleq$

$\vee \exists r \in Validator : ValidatorPropose(r)$   
 $\vee ValidatorChooseToCommit$

$$\begin{aligned}
& \vee \text{ValidatorChooseToFinal} \\
& \vee \exists r, v \in \text{Validator} : \text{RecvPropose}(r, v) \\
& \vee \exists r, \text{from}, v \in \text{Validator} : \vee \text{RecvPrepare}(r, \text{from}, v) \\
& \quad \vee \text{RecvVote}(r, \text{from}, v)
\end{aligned}$$


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$\text{PODConsistent} \triangleq$

A state predicate asserting that two *Validators* have not arrived at conflicting decisions. It is an invariant of the specification. Actually, *PoD* don't need this, so no consistency requirement.

$$\begin{aligned}
& \wedge \forall r1, r2 \in \text{Validator} : \neg \wedge \text{vrState}[r1] = \text{"aborted"} \\
& \quad \wedge \text{vrState}[r2] = \text{"finality"} \\
& \wedge \text{LET } \text{FinalValidators} \triangleq \{r \in \text{Validator} : \\
& \quad \text{vrState}[r] = \text{"finality"}\} \\
& \text{IN } \forall r1, r2 \in \text{FinalValidators}: \\
& \quad \text{vrFinal}[r1] = \text{vrFinal}[r2]
\end{aligned}$$


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$\text{PODSpec} \triangleq \text{PODInit} \wedge \Box[\text{PODNext}]_{\langle \text{vrState}, \text{vrPrepared}, \text{vrCommitted}, \text{vrFinal} \rangle}$

THEOREM  $\text{PODSpec} \Rightarrow \Box (\text{PODTypeOK} \wedge \text{PODConsistent})$

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\ \* Modification History  
\ \* Last modified Sat Jan 06 20:12:31 CST 2018 by xuepeng  
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