

# HW2

January 10, 2020

## 1 Chem 30324, Spring 2019, Homework 2

### 1.1 Due: January 29, 2020

### 1.2 Problem 1. Gases on a table top

In class we derived the properties of a 3-dimensional gas from the Boltzmann distribution and three postulates, and you studied a 1-dimensional gas in Homework 1. Suppose you were interested instead in a 2-dimensional gas, for example gas molecules able to freely skate around on a surface but that couldn't escape the surface.

**1.2.1 1. Derive the Maxwell-Boltzmann speed distribution for a 2-dimensional gas. (*Hint: Think polar coordinates.*)**

**1.2.2 2. Plot this 2-dimensional speed distribution for  $O_2$  molecules at 200, 400 and 600 K.**

**1.2.3 3. Calculate the mean (expected value) of the speed of a 2-dimensional gas of molecules. How does your answer compare to a 3-dimensional gas?**

**1.2.4 4. Calculate the mean kinetic energy of a 2-dimensional gas. How does your answer compare to a one and 3-dimensional gas?**

### 1.3 Problem 2. (Kinetics and Transport)

In junior Chemical Engineering laboratory, you will study the diffusion and solubility of  $CO_2$  in an organic solvent using a diffusion cell like the one sketched here. Let's suppose that the gas space at the top of the diffusion cell is approximately 2 cm high and 4 cm in diameter. Further suppose that the gas in the head of the cell is pure  $CO_2$  at 298 K and 1 bar pressure. Note that  $CO_2$  has a collision diameter  $d$  of 0.40 nm.

- 1.3.1 5. What does gas kinetic theory predict for the gas self-diffusion constant  $D_{11}$  of  $\text{CO}_2$  gas in the cell, in  $\text{cm}^2\text{s}^{-1}$ ?
- 1.3.2 6. Use the Stokes-Einstein relationship to estimate the diffusion constant of  $\text{CO}_2$  in the Stoddard solvent. How does this compare with the diffusion constant in the gas phase? Why?
- 1.3.3 7. We found in class that the probability for a molecule to diffuse a distance  $x$  in time  $t$  is Gaussian with mean 0 and standard deviation  $\sigma = \sqrt{2D_{11}t}$ . About how long will it take for 1/3 of the molecules starting at the center of the gas space to diffuse all the way to the surface of the liquid, i.e.,  $> 1 \text{ cm}$ ?
- 1.3.4 8. How many collisions on average does one of these diffusing  $\text{CO}_2$  molecule make with other gas molecules on the way from the middle of the vapor space to the surface of the solvent?
- 1.3.5 9. How far in total distance does this typical  $\text{CO}_2$  molecule travel in the time it takes to reach the solvent surface from the middle of the cell?
- 1.3.6 10. How many  $\text{CO}_2$  molecules impinge on the surface of the Stoddard solvent in one second?
- 1.3.7 11. Using your estimate of the diffusion constant in the solvent, how long does it take the same fraction  $\text{CO}_2$  molecules to diffuse a similar distance in 1-dimension in the liquid phase?
- 1.3.8 12. Is it safe to assume that any  $\text{CO}_2$  that travels from the surface into the bulk of the solvent is rapidly replaced from the gas phase?
- 1.3.9 13. Suppose the volume of the gas-handling manifold is  $100 \text{ cm}^3$  and is pressurized with  $\text{CO}_2$  in the morning to 1.1 atm. What will the pressure in the manifold be four hours later, when lab starts, if the manifold has a pinhole of  $1 \text{ m}^2$ ?