

Chem 30324, Spring 2020, Homework3

Due February 5, 2020

▼ Heat capacity of solids

1. In Einstein's [original paper](#) on the heat capacity of solids, he compared his model for diamond, using a frequency for the vibrating C atoms $\nu = 2.75 \times 10^{13} \text{s}^{-1}$. What is the frequency of the vibrating C atoms to describe the heat capacity of diamond?

1. Each solid is composed of a lattice structure consisting of N atoms. Each atom is treated as moving independently (3 degrees of freedom). The entire lattice's vibrational motion could be described by a total of 3N motions, or 3N degrees of freedom.
2. The atoms inside the solid lattice do not interact with each other.
3. All of the atoms inside the solid vibrate at the same frequency.

▼ 2. Plot the Einstein model for the heat capacity of diamond from 0 to 1500 K.

```
import numpy as np
import matplotlib.pyplot as plt
h = 6.626e-34 #Planck constant in m^2*kg/s
f = 2.75e13 #Vibrating frequency of carbon in s^-1
kB = 1.38e-23 #Boltzmann const in m^2*kg/s^2/K
T = np.arange(0,1500,1) # Temperature range from 0 to 1500 K
R = 8.314 #Gas constant m^2*kg/s^2/K/mol
def Cv(T):
    return (3*R)*(h*f/kB/T)**2*np.exp(h*f/kB/T)/(np.exp(h*f/kB/T)-1)**2
plt.plot(T,Cv(T))
```

```
plt.title('Einstein model for the heat capacity of diamond from 0 to 1500K')
plt.xlabel('T(K)')
plt.ylabel('Heat capacity(J/(mol*K))')
plt.show()
```

```
[> /usr/local/lib/python3.6/dist-packages/ipykernel_launcher.py:9: RuntimeWarning
    if __name__ == '__main__':
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Einstein model for the heat capacity of diamond from 0 to 1500K
```

