

DSP Homework 03

Xu, Minhuan

September 19, 2022

Contents

1 Problem 1	1
1.1 Our Planet	1
1.2 Wireless Earbuds	2
1.3 Benefits of Exercise	2
2 Problem 2	2
2.1 Results	2
2.2 What school can do?	3
2.2.1 Time Manage	3
2.2.2 Help from Help Centres in Campus	3
2.2.3 Academic Advising	3
2.2.4 Conclusion	3
2.3 Other meaningful results	3
2.4 Teach Computers to Get Similar Results Automatically	3
3 Problem 3	4
3.1 Problem Restatement	4
3.2 Proof	4
4 conclusion	6

Abstract

Problem 1

We watched 3 videos this week. The first one tells us to protect the earth, the second one introduced the work theory of wireless earbuds, and the last one wants us to move more to keep our mind clever.

Problem 2

I did a research to find out When is average undergraduate students most or least happy during a day or a week, and taught my computer to do the same work.

Problem 3

Proof of some formulas.

1 Problem 1

Problem Restatement

1.1 Our Planet

This video is basically about how beautiful our planet is and the truth that we are breaking its stability.

Like how our human social works, the nature has its our system and every single pieces of our beautiful planet are firmly connected. For example, the sea water evaporates at all times. The water vapor full of air will always condensates into drops, and fall from the air in the form of rain at one time. This is the natural water cycle, and the strong proof of the internal connection of nature.

What we are doing is making our planet warmer and warmer, and one of the results is the melting of glaciers. The fresh water from the glaciers will disturb the sea's current, change the salinity, and eventually affect the nature ecology.

The nature is more complex than what we thought. The rapid development of mankind from last century has been damaging the health of our only Mother Earth. Just as somebody says, 'We're the first generation to know what we're doing, and the last who have a chance to put things right'. There definitely are something which must be preserved if we are to ensure a future where humans and nature can thrive.

1.2 Wireless Earbuds

This video do the 4 things below:

1. Earbuds Disassembly and Introduction to Every Module in the Earbuds
2. Discuss the Audio Codec
3. Sampling Rate and Bit-depth
4. Music File Formats

For wired headphones, electricity flows from our smartphones through the wires to the headphones. In the wire, there's only analog signals travel between the smartphone and the headphone. However, for wireless earbuds, this doesn't work because it's difficult to send analog signals to such a tiny thing through the channel of air. The AirPods 2 relies on the technology of Bluetooth, DAC and the theory of the speaker to provide its service.

About the audio codec, codec stands for coding and decoding. In playing music, codec do the decoding, which means it converts the music data from digital values to analog waves. So, the coding means the reverse of that process.

We were talking about the sampling rate last week, and that's how we make continuous waves into a set of discrete pulses. The most common rate is 44.1 kHz, and the second popular one is 48 kHz.

However, we cannot save the pulses with irrational size as binary, so we must do the quantization – making all numbers in an interval fall into the center point (or other certain points) of this interval. The bit-depth is the number how many binary numbers (this also means how many levels do we have in the process of quantization) we use to represent one pulse.

Audio File Format can be divided into lossy format and lossless format according to whether part of the original audio data will be deleted. MP3 and AAC is a common lossy format, and their algorithm will find and delete the part of the original audio data that is hard for human ears to detect. ALAC and FLAC are common lossless formats. They only compress the original audio data in use of lossless compression algorithm and don't delete any original data.

The wireless earbuds is everywhere in our life. Maybe we all know that the sound is wave and the earbuds are just the processor of them, but few of us try to know about how practically this tiny thing works. So, keep curiosity is crucial.

1.3 Benefits of Exercise

In this TED talks, we are suggested to do the proper amount of the exercise to improve our brain.

Our brains are get older while our bodies are getting older, especially Hippocampus, this talker mentioned. But we do have ways to slow that process – exercise.

She, the talker, experienced the change exercise gives her and her brain, so she shifted the goal of her lab and find out a new way to make or just keep people's minds brilliant.

Now, she's going to find out what the most proper amount of exercise of one specific person, and I think this means a lot for those who sit before their computers all day long.

Saying goes, life lies in sports, and we all know it. What's more, people today are clever enough to find out the most complex relationship between 'life' and 'sports'.

2 Problem 2

2.1 Results

I will show you what I know from my campus survey. If you want to see the original survey data, please see the file of [research.csv](#).

	Daily	Weekly
Most Happy	Evening	Friday or Saturday
Least Happy	Morning	Monday

I will answer your questions in the subsections below. Due to space barriers, the survey source data that cannot be fully displayed will be displayed in the attached [research.csv](#) file.

2.2 What school can do?

I'd like to introduce to you what schools can do to improve our campus life, as I saw in the survey results.

2.2.1 Time Manage

We can see that in the survey, there are some students who are happiest at night or at weekends, but also face academic problems. I think there are two reasons for this: 1. The student's curriculum arrangement is too tight, which makes him unable to get a good rest in the working day. At the same time, the accumulated fatigue will also accumulate at this time, leading to the problem of lack of energy and academic difficulty; 2. The student usually procrastinates and is lazy in studying on weekdays, which leads to the loss of interest in class and the desire to have a rest during the holidays.

For such students, we can ask counselors to give them suggestions to solve their academic problems, improve their learning efficiency, and make them calmly face the heavy study.

2.2.2 Help from Help Centres in Campus

In the questionnaire, there is a survey on emotions and recent troubles, which is to judge whether the respondents have mental health or life problems.

Due to learning pressure, family changes and other reasons, students may have too many bad emotions in their lives. If they do not solve them, they will have psychological problems. At this time, we should give full play to the role of the school's help organization and give adequate psychological guidance.

On the other hand, students who have difficulties in planning their own lives should also receive additional help from the Career Planning Center.

2.2.3 Academic Advising

It can be seen from the questionnaire that some students prefer working days to rest days, prefer morning to night, but think that their studies are difficult. This shows that they tend to love learning and can plan their time well, but still feel that the amount of knowledge they have learned or the difficulty of learning is their trouble.

For such problems, the school can make a good notice so that every student can know how to seize every opportunity to communicate with the teacher.

2.2.4 Conclusion

In the data table (research. csv), I judged which help the students participating in the survey might need according to my own cognition, and then marked it after the data (0 means the student's life is relatively happy).

It can be seen that there are relatively many student associations that need help from the school organization. The school can focus on improving the students' understanding of the mental health center and the career planning center according to this.

2.3 Other meaningful results

1. Students who find it difficult to control their emotions have love problems.
2. Most of the students who feel that their studies are heavy like morning and night.

2.4 Teach Computers to Get Similar Results Automatically

In my plan, I will use Python to build a simple machine learning model. However, it is very difficult to use Python to process Chinese, so I replaced all the options of the single choice questions in the questionnaire with integers. This process will make full use of Excel's search function and is very boring, so it will not appear in my report.

The full code is in the coding listing section.

3 Problem 3

3.1 Problem Restatement

The Fourier transform pair can be defined as

$$\begin{aligned}\tilde{x}(f) &= \int_{-\infty}^{\infty} x(t) e^{-j2\pi ft} dt \\ x(f) &= \int_{-\infty}^{\infty} \tilde{x}(f) e^{j2\pi ft} df\end{aligned}$$

Prove the following

(1)	$ax(t) + by(t) \leftrightarrow a\tilde{x}(f) + b\tilde{y}(f)$	Linearity
(2)	$x(st) \leftrightarrow \frac{1}{ s } \tilde{x}\left(\frac{f}{s}\right)$	Scaling
(3)	$x^*(t) \leftrightarrow \tilde{x}^*(-f)$	Conjugate
(4)	$\tilde{x}(t) \leftrightarrow x(-t)$	Duality
(5)	$x(t - t_0) \leftrightarrow e^{-j2\pi t_0 f} \tilde{x}(f)$	Time shift
(6)	$e^{-j2\pi f_0 t} x(st) \leftrightarrow \tilde{x}(f - f_0)$	Frequency shift
(7)	$x'(t) \leftrightarrow j2\pi f \tilde{x}(f)$	Differentiation
(8)	$\int x(\tau) y(t - \tau) d\tau \leftrightarrow \frac{1}{ s } \tilde{x}\left(\frac{f}{s}\right)$	Convolution

3.2 Proof

(1)

$$\begin{aligned}\mathcal{F}[ax(t) + by(t)] &= \int_{-\infty}^{\infty} [ax(t) + by(t)] e^{-j2\pi ft} dt \\ &= \int_{-\infty}^{\infty} ax(t) e^{-j2\pi ft} dt + \int_{-\infty}^{\infty} by(t) e^{-j2\pi ft} dt \\ &= a\tilde{x}(f) + b\tilde{y}(f)\end{aligned}$$

(2) if $s > 0$,

$$\begin{aligned}\mathcal{F}[x(st)] &= \int_{-\infty}^{\infty} x(st) e^{-j2\pi ft} dt \\ \mathcal{F}[x(st)] &= \frac{1}{s} \int_{-\infty}^{\infty} x(st) e^{-j2\pi (\frac{f}{s})(st)} d(st)\end{aligned}$$

let t' represent st ,

$$\begin{aligned}\mathcal{F}[x(t')] &= \frac{1}{s} \int_{-\infty}^{\infty} x(t') e^{-j2\pi (\frac{f}{s})(t')} dt' \\ &= \frac{1}{s} \tilde{x}\left(\frac{f}{s}\right) = \frac{1}{s} \tilde{x}\left(\frac{f}{|s|}\right)\end{aligned}$$

If $s \leq 0$,

$$\begin{aligned}\mathcal{F}[x(st)] &= \frac{1}{s} \int_{-\infty}^{-\infty} x(st) e^{-j2\pi(\frac{f}{s})(st)} d(st) \\ &= \frac{1}{-s} \int_{-\infty}^{\infty} x(st) e^{-j2\pi(\frac{f}{s})(st)} d(st) \\ &= \frac{1}{-s} \tilde{x}\left(\frac{f}{s}\right) = \frac{1}{|s|} \tilde{x}\left(\frac{f}{s}\right)\end{aligned}$$

(3)

$$\begin{aligned}\mathcal{F}[x^*(t)] &= \int_{-\infty}^{\infty} x^*(t) e^{-j2\pi ft} dt \\ &= \left[\int_{-\infty}^{\infty} [x^*(t) e^{-j2\pi ft}]^* dt \right]^* \\ &= \left[\int_{-\infty}^{\infty} [x(t)] e^{-j2\pi(-f)t} dt \right]^* \\ &= [\tilde{x}(-f)]^*\end{aligned}$$

(4)

$$\tilde{x}(f) = \int_{-\infty}^{\infty} x(t) e^{-j2\pi ft} dt$$

Exchange f and t ,

$$\begin{aligned}\tilde{x}(t) &= \int_{-\infty}^{\infty} x(f) e^{-j2\pi ft} df \\ &= \int_{\infty}^{-\infty} x(-f) e^{j2\pi ft} d(-f) \\ &= \int_{-\infty}^{\infty} x(-f) e^{j2\pi ft} df \\ &= \mathcal{F}[x(-f)]\end{aligned}$$

(5)

$$\mathcal{F}[x(t - t_0)] = \int_{-\infty}^{\infty} x(t - t_0) e^{-j2\pi ft} dt$$

let t be $t + t_0$,

$$\begin{aligned}\mathcal{F}[x(t - t_0)] &= \int_{-\infty}^{\infty} x(t) e^{-j2\pi f(t+t_0)} d(t + t_0) \\ &= e^{-j2\pi ft_0} \int_{-\infty}^{\infty} x(t) e^{-j2\pi ft} d(t) \\ &= e^{-j2\pi ft_0} \tilde{x}(t)\end{aligned}$$

(6)

$$\begin{aligned}\mathcal{F}[e^{-j2\pi f_0 t} x(t)] &= \int_{-\infty}^{\infty} x(t) e^{-j2\pi(f-f_0)t} dt \\ &= \tilde{x}(f - f_0)\end{aligned}$$

(7)

$$\begin{aligned}
\frac{d}{dt}x(t) &= \frac{d}{dt}\mathcal{F}^{-1}[\tilde{x}(f)] \\
&= \frac{d}{dt} \int_{-\infty}^{\infty} \tilde{x}(f) \cdot e^{j2\pi ft} \cdot df \\
&= \int_{-\infty}^{\infty} \tilde{x}(f) \cdot \frac{d}{dt}e^{j2\pi ft} \cdot dt \\
&= \int_{-\infty}^{\infty} \tilde{x}(f) \cdot j2\pi f \cdot e^{j2\pi ft} \cdot dt \\
&= \int_{-\infty}^{\infty} [j2\pi f \cdot \tilde{x}(f)] \cdot e^{j2\pi ft} dt \\
&= \mathcal{F}[j2\pi f \cdot \tilde{x}(f)]
\end{aligned}$$

(8)

$$\begin{aligned}
\mathcal{F}[x_1(t) * x_2(t)] &= \int_{-\infty}^{\infty} \left[\int_{-\infty}^{\infty} x_1(\tau) x_2(t - \tau) d\tau \right] e^{-j2\pi ft} dt \\
&= \int_{-\infty}^{\infty} x_1(\tau) e^{-j2\pi f\tau} d\tau \int_{-\infty}^{\infty} x_2(t - \tau) e^{-j2\pi f(t - \tau)} d(t - \tau) \\
&= \int_{-\infty}^{\infty} x_1(\tau) e^{-j2\pi f\tau} d\tau \int_{-\infty}^{\infty} x_2(t) e^{-j2\pi ft} dt \\
&= \tilde{x}_1(f) \cdot \tilde{x}_2(f)
\end{aligned}$$

4 conclusion

1. After watching the first video, I became interested in the website supporting the video, and saw many simple ways to protect the earth, such as refusing plastic bags and low-carbon travel, which have been proposed for a long time, as well as some new ways. If more people can know and practice these tips, this documentary will achieve its very important mission.

The principle of wireless headphones in the second video is what I have always wanted to know.

In the third video, the talker's idea is very exciting, which makes people want to do some sports immediately. This kind of vitality is exactly what we need.

2. It can be seen from the thermal diagram (appendix) that the results in the report are not satisfactory. If we can have a larger number of data and have enough time to process these data, we will get a model to judge whether students need school help once and for all.
3. We have learned these knowledge from previous studies, but some of them have forgotten that they need to be consolidated again. It is a good way to prove the formulas.

Appendix A Code Listing