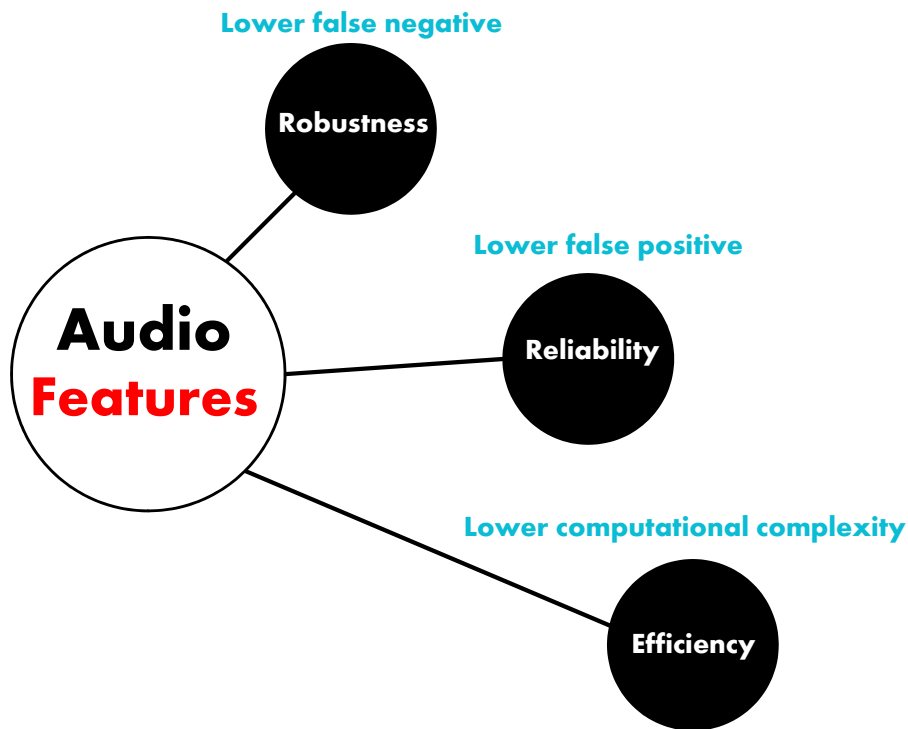


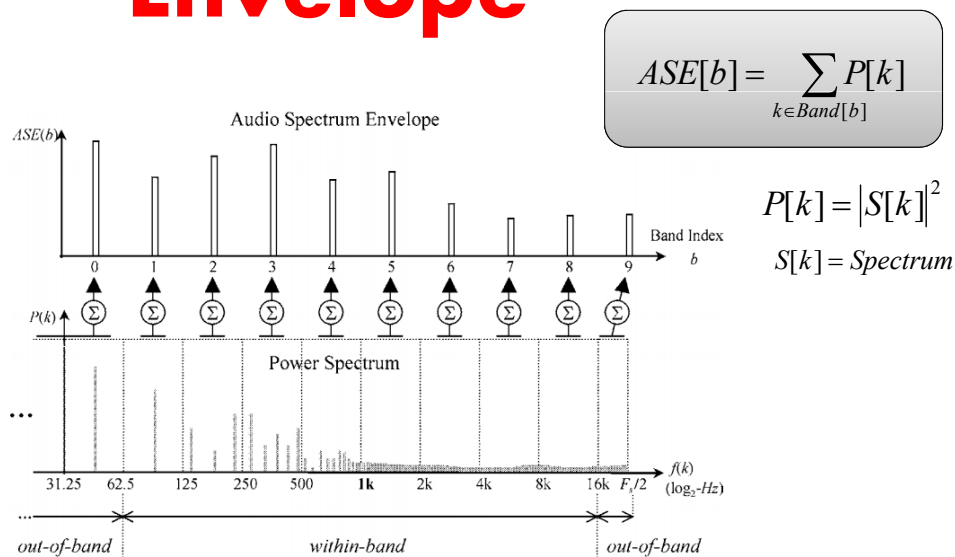
Audio & Speech Technology

[4] Audio Features



Audio Spectral Envelope

3



Audio Spectral Flatness

4

$$ASF[b] = \frac{\sqrt[N_b]{\prod_{k \in \text{Band}[b]} P[k]}}{\frac{1}{N_b} \sum_{k \in \text{Band}[b]} P[k]}$$

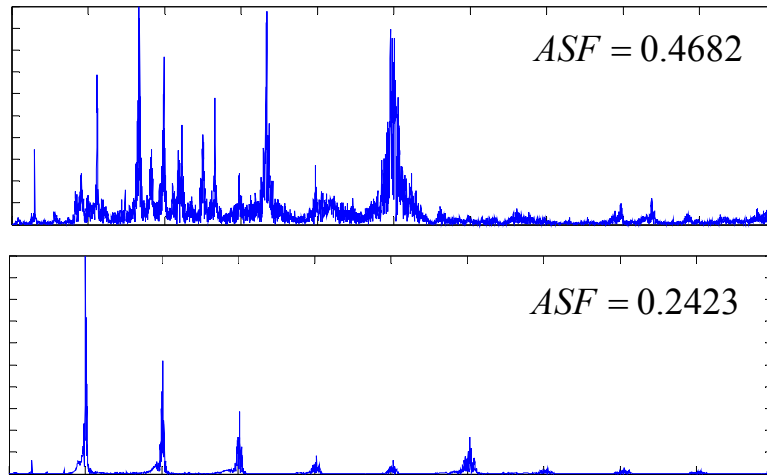
Geometric Mean

Arithmetic Mean

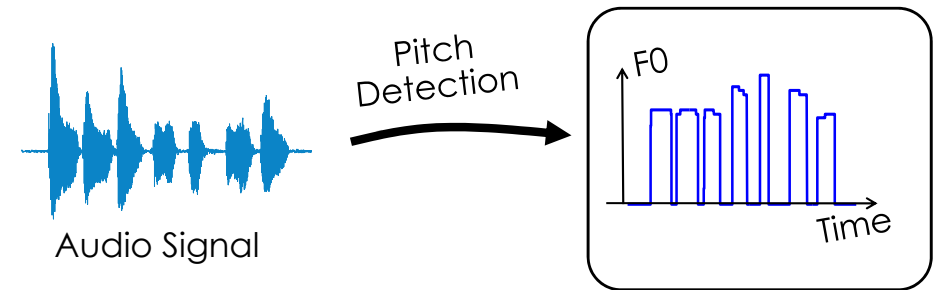
N_b = No. of frequencies in each band

$$\sqrt[N_b]{\prod_{k \in \text{Band}[b]} P[k]} = \exp\left(\frac{1}{N_b} \sum_{k \in \text{Band}[b]} \ln P[k]\right)$$

Audio Spectral Flatness



Fundamental Audio Frequency

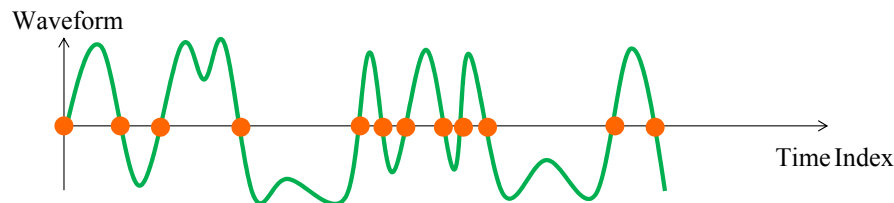


Zero Crossing Rate

$$ZCR = \frac{F_s}{2N} \sum_{n=1}^{N-1} |sign(s[n]) - sign(s[n-1])|$$

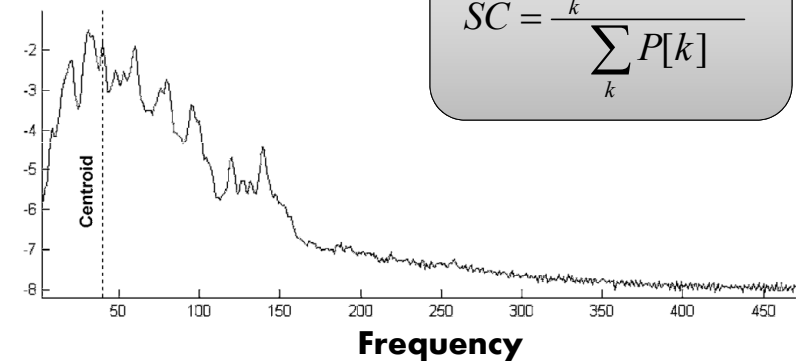
N = No. samples in $s[i]$

F_s = Sampling Frequency



Spectral Centroid

Power Spectrum (log)



$$SC = \frac{\sum_k f[k]P[k]}{\sum_k P[k]}$$

Harmonic Ratio

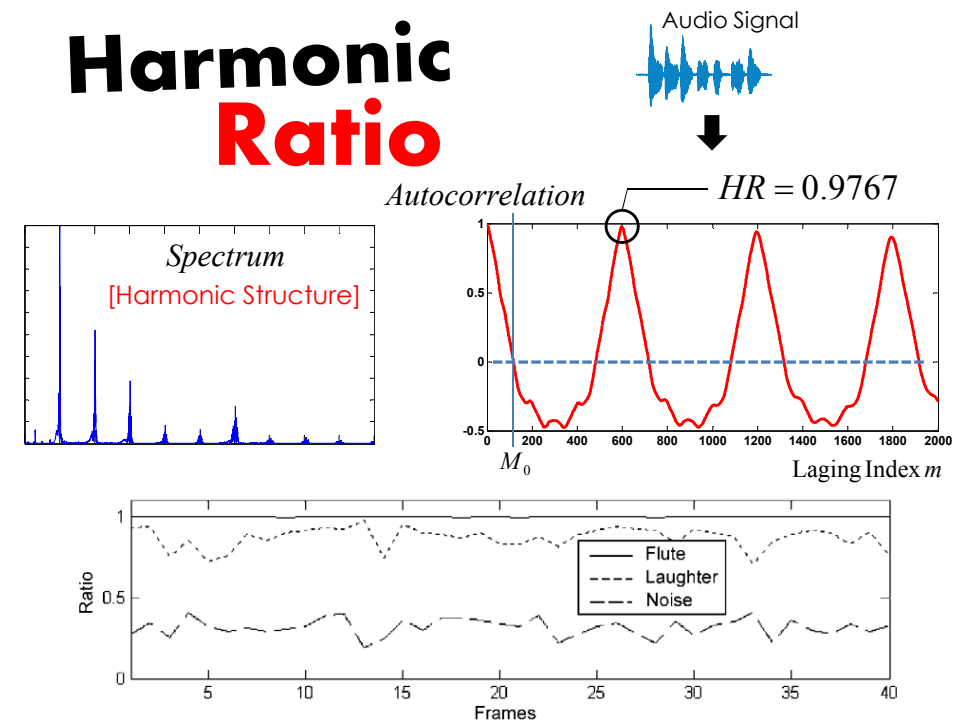
$$R[m] = \frac{\sum_{n \in \text{Frame}} s[n]s[n-m]}{\sqrt{\sum_{n \in \text{Frame}} s^2[n] \sum_{n \in \text{Frame}} s^2[n-m]}} \Rightarrow HR = \max_{m \geq M_0} R[m]$$

R = Autocorrelation Function

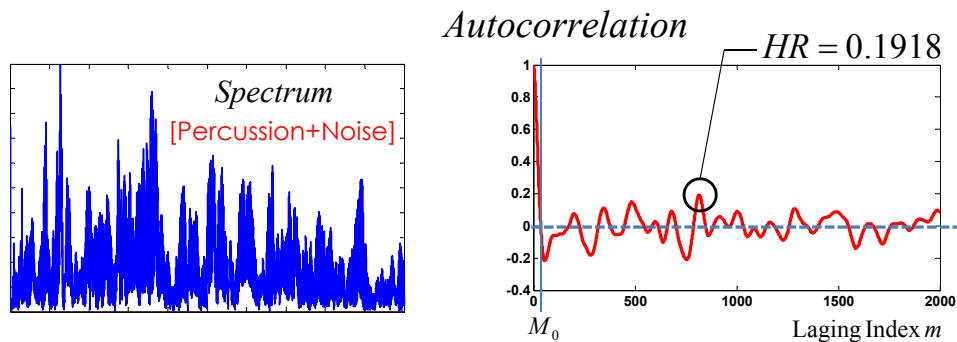
m = Lagging index

M_0 = Position of the first zero crossing of autocorrelation R

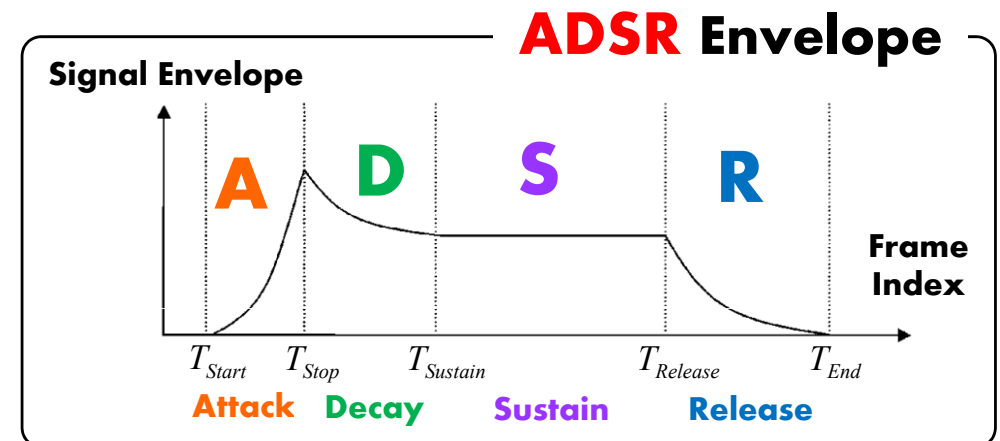
Harmonic Ratio



Harmonic Ratio



Log Attack Time

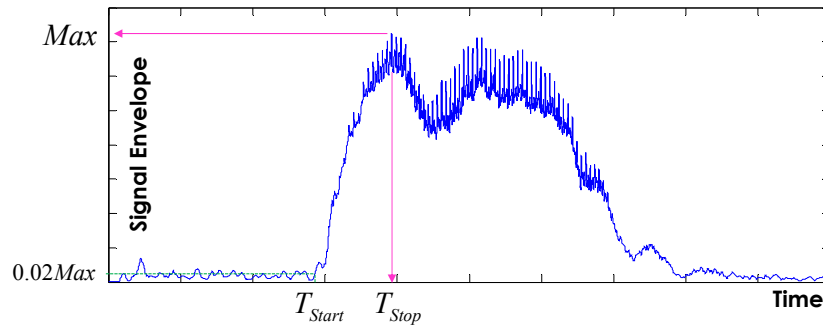


Log Attack Time

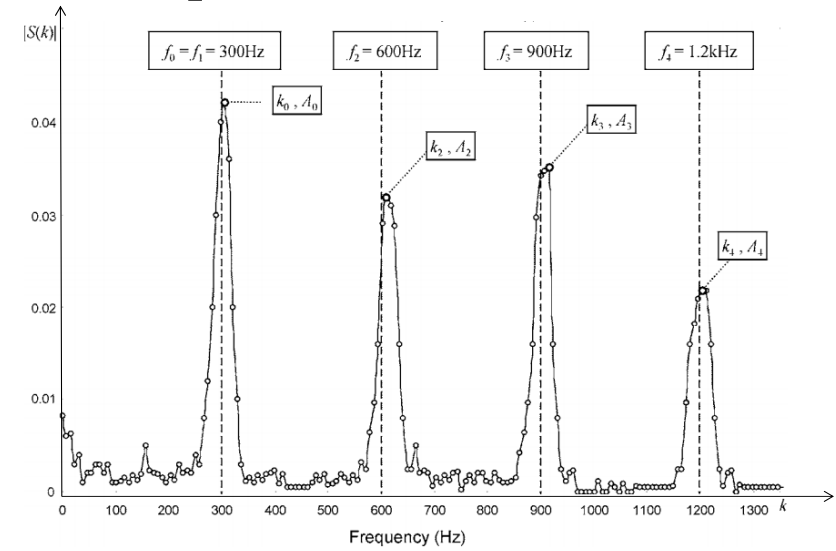
$$LAT = \log_{10}(T_{Stop} - T_{Start})$$

T_{Start} = The time the signal envelope exceeds 2% of its maximal value

T_{Stop} = The time the signal envelope reaches its maximal value



Harmonic Spectral Centroid



MPEG-7 Audio and Beyond: Audio Content Indexing and Retrieval, Hyoung-Gook Kim, et. al.

Harmonic Spectral Centroid

LHSC = Local Harmonic Spectral Centroid of Audio Frame

$$LHSC = \frac{\sum_{h=1}^{N_H} f_h A_h}{\sum_{h=1}^{N_H} A_h}$$

f_h = Frequency of the h^{th} harmonic

A_h = Amplitude of the h^{th} harmonic

N_H = No. of harmonic peaks

$$HSC = \frac{1}{L} \sum_{i=1}^L LHSC[i]$$

L = No. of time frames

Harmonic Spectral Deviation

Spectral Envelope

$$SE_h = \begin{cases} (A_h + A_{h+1})/2 & h=1 \\ (A_{h-1} + A_h + A_{h+1})/2 & h \in [2, N_H - 1] \\ (A_{h-1} + A_h)/2 & h = N_H \end{cases}$$

$$LHSD = \frac{\sum_{h=1}^{N_H} |\log_{10} A_h - \log_{10} SE_h|}{\sum_{h=1}^{N_H} \log_{10} A_h}$$



$$HSD = \frac{1}{L} \sum_{i=1}^L LHSD[i]$$

Harmonic Spectral Spread

17

$$LHSS = \sqrt{\frac{\sum_{h=1}^{N_H} (f_h - LHSC)^2 A_h^2}{\sum_{h=1}^{N_H} A_h^2}}$$



$$HSS = \frac{1}{L} \sum_{i=1}^L LHSS[i]$$

Harmonic Spectral Variation

18

$$LHSV[i] = 1 - \frac{\sum_{h=1}^{N_H} A_h[i-1]A_h[i]}{\sqrt{\sum_{h=1}^{N_H} A_h^2[i-1]} \sqrt{\sum_{h=1}^{N_H} A_h^2[i]}}$$



$$HSS = \frac{1}{L} \sum_{i=1}^L LHSV[i]$$

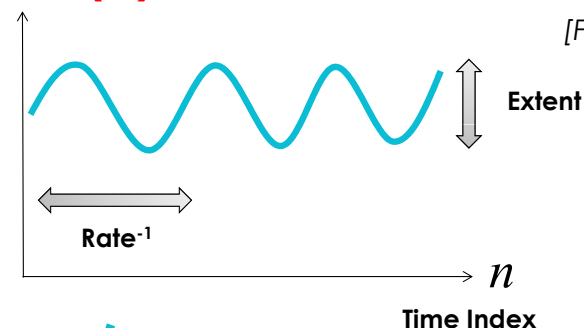
Vibrato

[Frequency Modulation]

19

- Variation of pitch.
- **Extent of vibrato**
= Amount of pitch variation
- **Rate of vibrato**
= Speed which the pitch is varied
- String instruments produce the FM dominant sounds

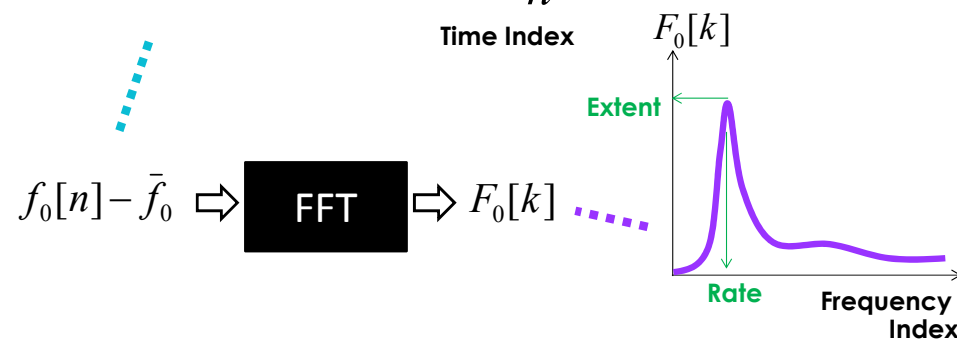
$f_0[n]$
Pitch (f_0)



Vibrato

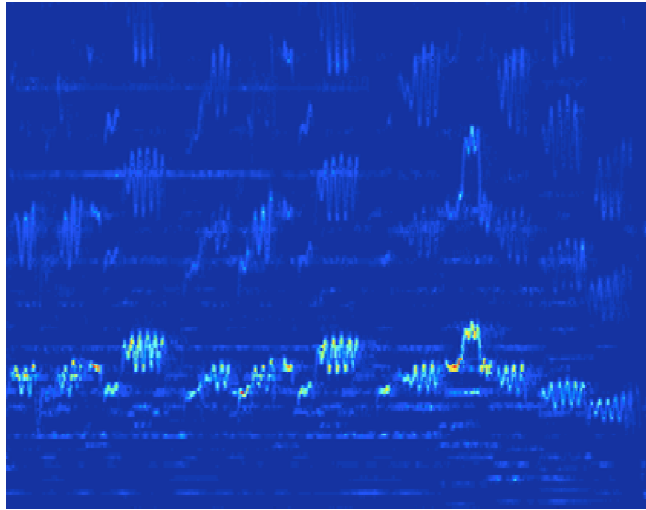
[Frequency Modulation]

20



Vibrato

[Frequency Modulation]



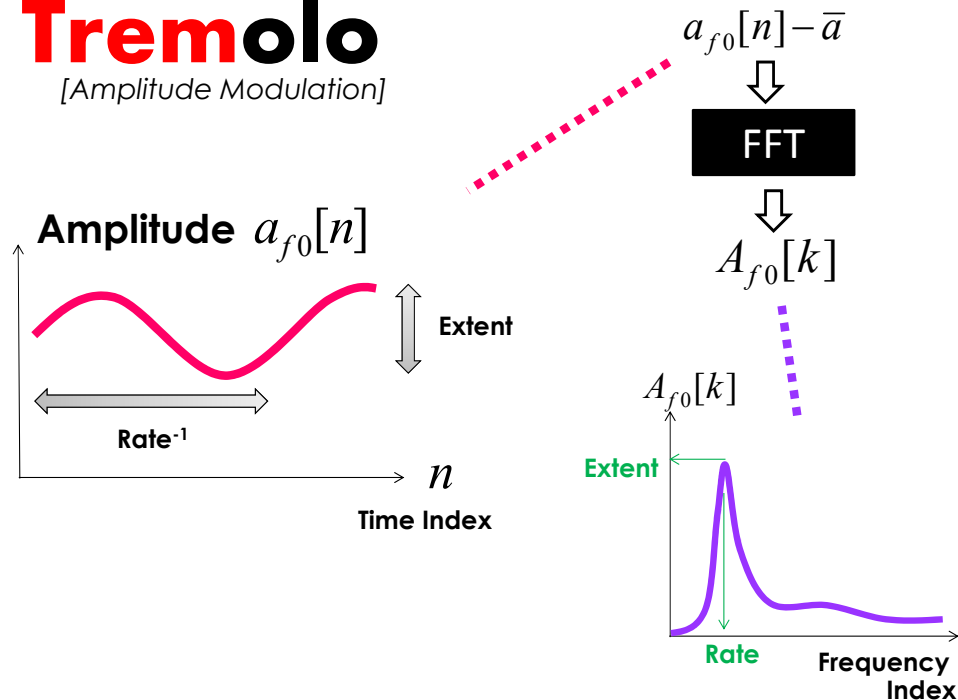
Tremolo

[Amplitude Modulation]

- Variation of sound intensity.
- **Extent of vibrato**
= Amount of intensity variation
- **Rate of vibrato**
= Speed which the intensity is varied
- Wind and brass instruments produce AM dominant sounds.

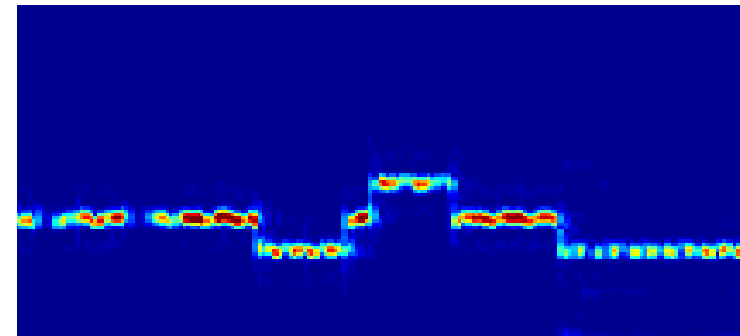
Tremolo

[Amplitude Modulation]



Tremolo

[Amplitude Modulation]



Linear Predictive Coding

- A model used for predicting a value of current sample of signal from the previous samples
- Used in Speech Analysis, Speech Synthesis, Audio Classification, Audio Compression

Current sample $s[n]$ is predicted from Previous samples $s[n-k]$ using LPC Coefficients a_k and Prediction Error $\varepsilon[n]$.

$$s[n] = \sum_{k=1}^P a_k s[n-k] + \varepsilon[n]$$

Linear Predictive Coding



Training LPC

- Find $\{a_k\}$
- To minimize $\sum_n \varepsilon^2[n]$

$$\varepsilon[n] = s[n] - \hat{s}[n]$$

$$\hat{s}[n] = \sum_{k=1}^P a_k s[n-k]$$

Linear Predictive Coding

$$E = \sum_n \varepsilon^2[n] = \sum_n \left(s[n] - \sum_{k=1}^P a_k s[n-k] \right)^2$$

$$\frac{\partial E}{\partial a_i} = \sum_n (-2s[n-i]) \left(s[n] - \sum_{k=1}^P a_k s[n-k] \right)$$

$$0 = \sum_n s[n]s[n-i] - \sum_n s[n-i] \sum_{k=1}^P a_k s[n-k]$$

$$0 = \sum_n s[n]s[n-i] - \sum_{k=1}^P a_k \sum_n s[n-k]s[n-i]$$

Linear Predictive Coding

$$0 = \sum_n s[n]s[n-i] - \sum_{k=1}^P a_k \sum_n s[n-k]s[n-i]$$

$$0 = R[i] - \sum_{k=1}^P a_k R[k-i]$$

$$\sum_{k=1}^P a_k R[k-i] = R[i]$$

Autocorrelation Function $R[i-j] = R[j-i] = \frac{\sum_n s[n-i]s[n-j]}{\sum_n s^2[n]}$

Linear Predictive Coding

$$\frac{\partial E}{\partial a_1} = 0 \Rightarrow \sum_{k=1}^P a_k R[k-1] = R[1]$$

$$\frac{\partial E}{\partial a_2} = 0 \Rightarrow \sum_{k=1}^P a_k R[k-2] = R[2]$$

$$\vdots$$

$$\frac{\partial E}{\partial a_P} = 0 \Rightarrow \sum_{k=1}^P a_k R[k-P] = R[P]$$

Linear Predictive Coding

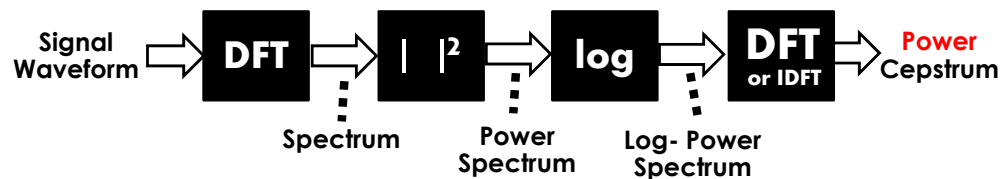
$$\begin{bmatrix} R[0] & R[1] & R[2] & \cdots & R[P-1] \\ R[1] & R[0] & R[1] & \cdots & R[P-2] \\ R[2] & R[1] & R[0] & \cdots & R[P-3] \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ R[P-1] & R[P-2] & R[P-3] & \cdots & R[0] \end{bmatrix} \begin{bmatrix} a_1 \\ a_2 \\ a_3 \\ \vdots \\ a_P \end{bmatrix} = \begin{bmatrix} R[1] \\ R[2] \\ R[3] \\ \vdots \\ R[P] \end{bmatrix}$$



$$\begin{bmatrix} a_1 \\ a_2 \\ a_3 \\ \vdots \\ a_P \end{bmatrix} = \begin{bmatrix} R[0] & R[1] & R[2] & \cdots & R[P-1] \\ R[1] & R[0] & R[1] & \cdots & R[P-2] \\ R[2] & R[1] & R[0] & \cdots & R[P-3] \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ R[P-1] & R[P-2] & R[P-3] & \cdots & R[0] \end{bmatrix}^{-1} \begin{bmatrix} R[1] \\ R[2] \\ R[3] \\ \vdots \\ R[P] \end{bmatrix}$$

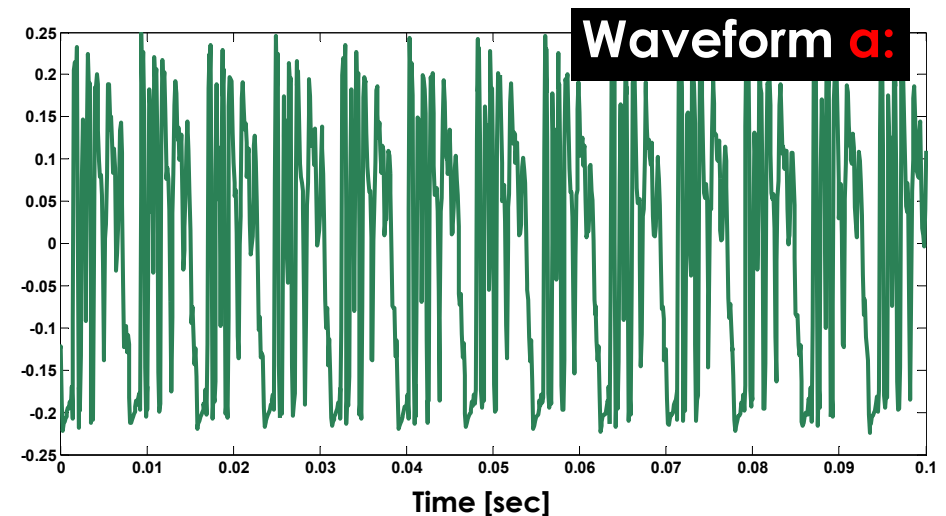
Cepstrum

Fourier transform of the logarithm of the spectrum of signal

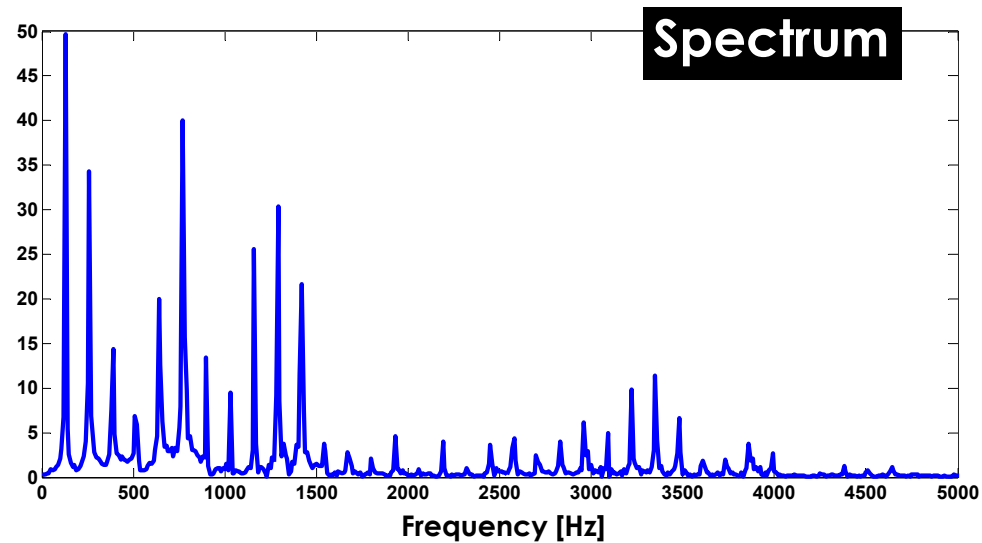


Spectrum \Rightarrow **Cepstrum**
Frequency \Rightarrow **Quefrequency**
Filter \Rightarrow **Lifter**

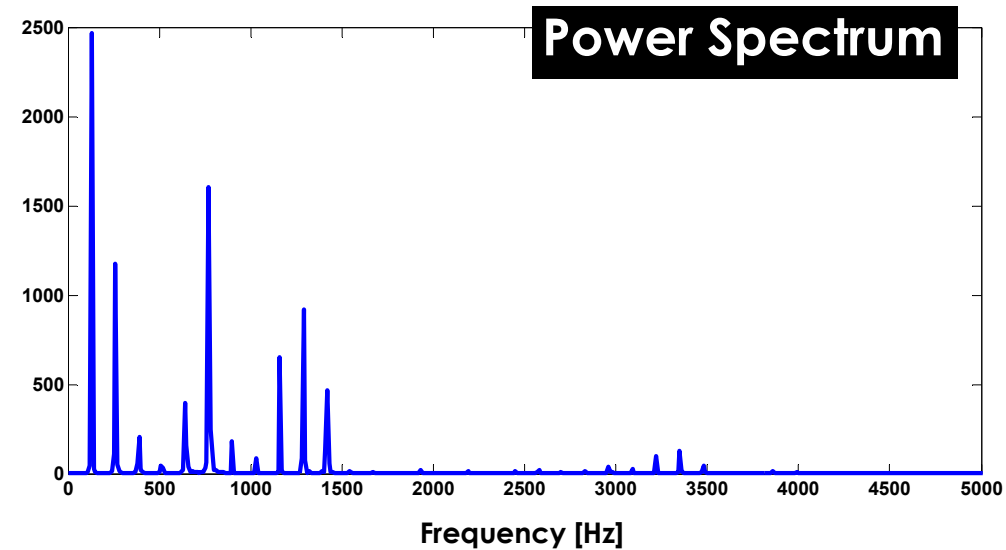
Cepstrum



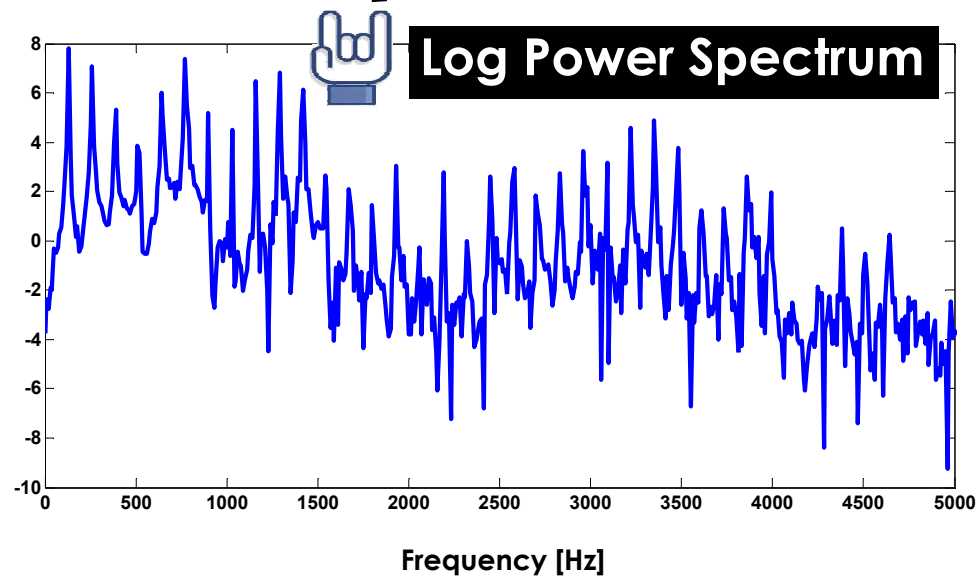
Cepstrum



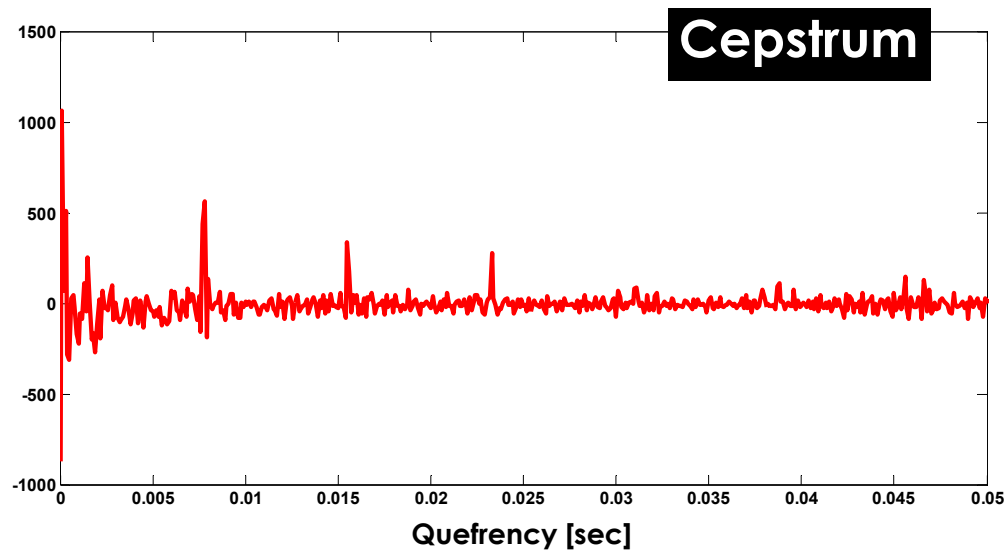
Cepstrum



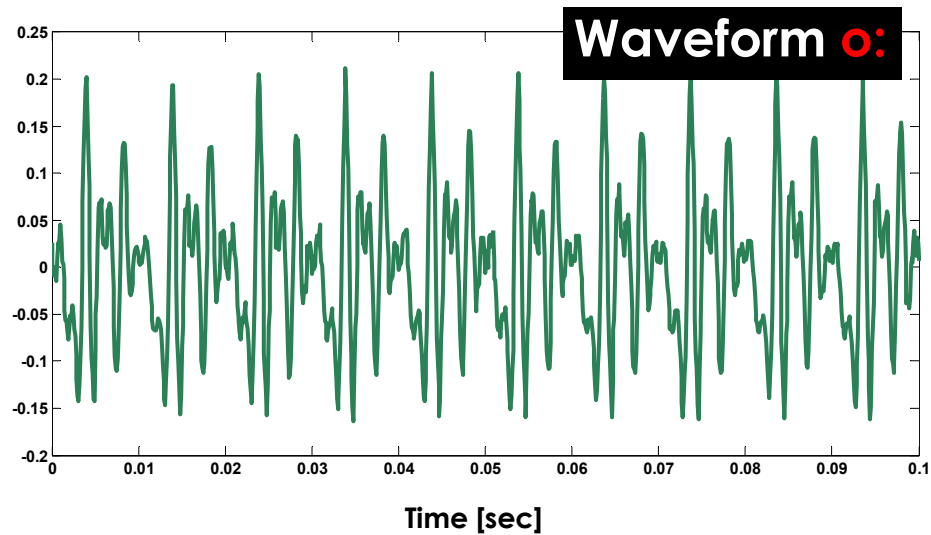
Cepstrum



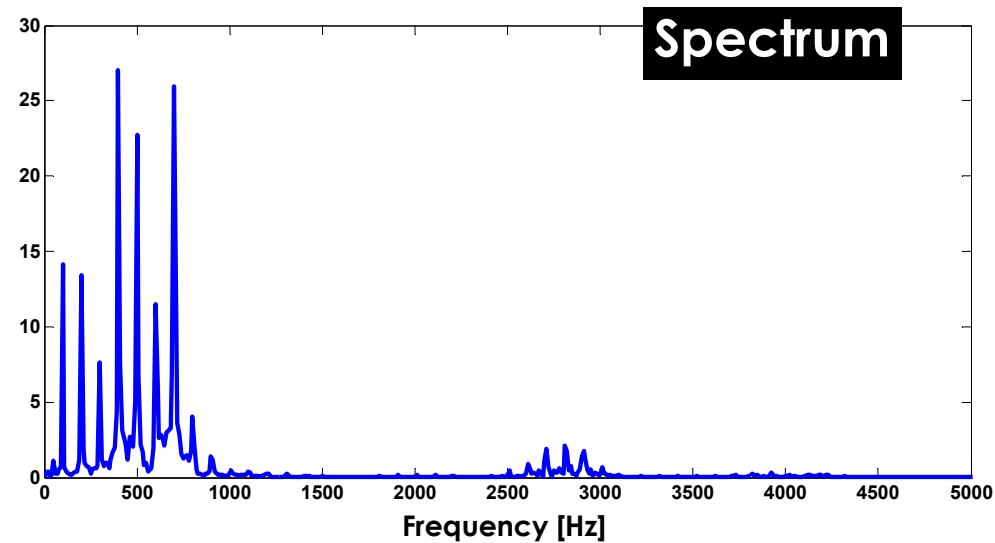
Cepstrum



Cepstrum



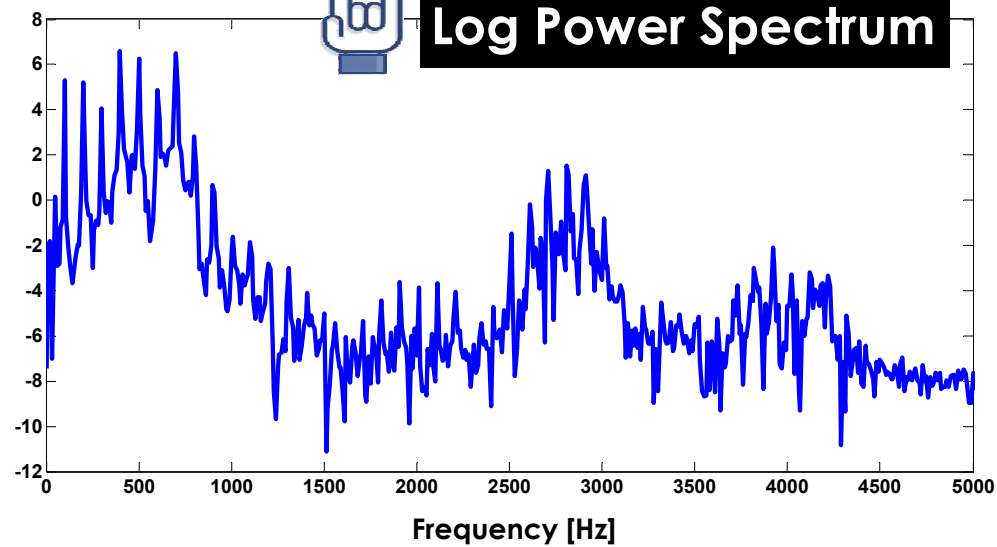
Cepstrum



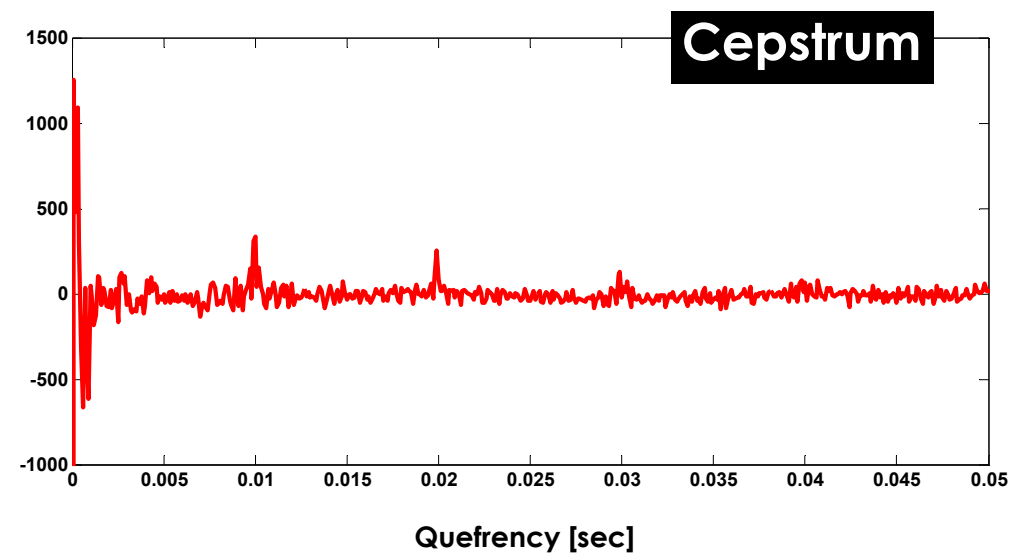
Cepstrum



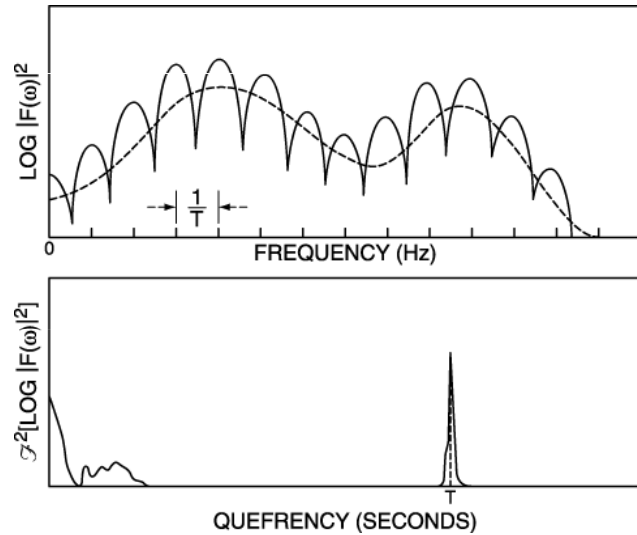
Log Power Spectrum



Cepstrum

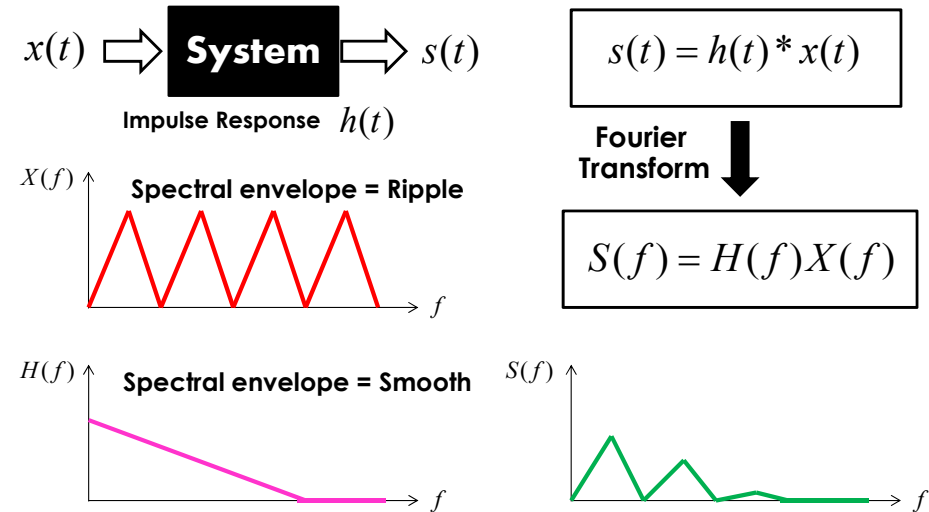


Cepstrum

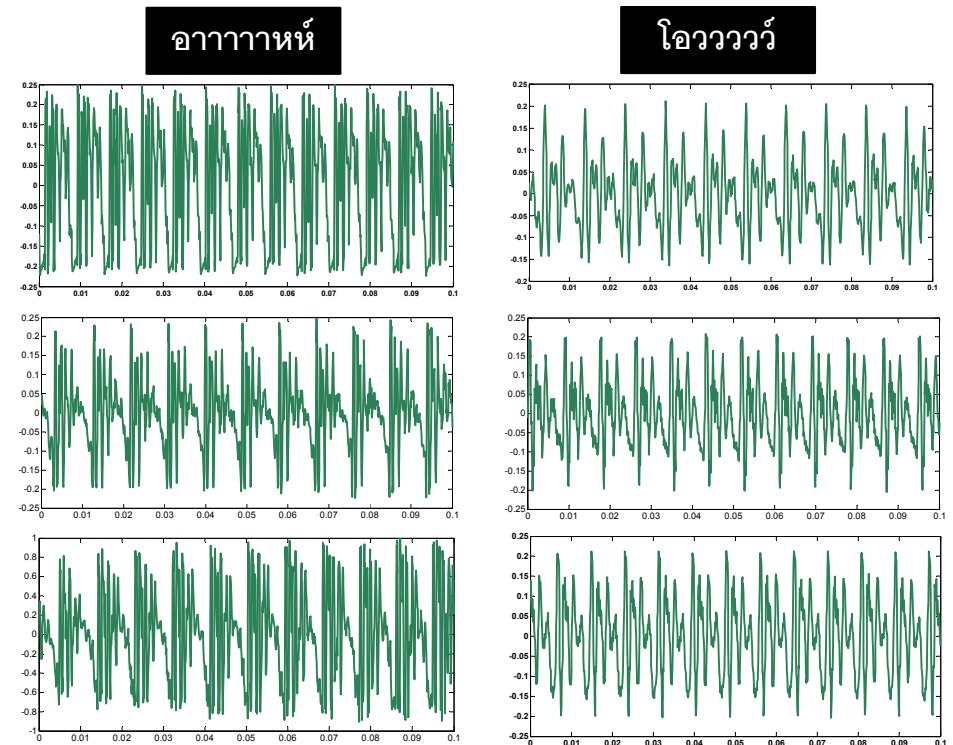
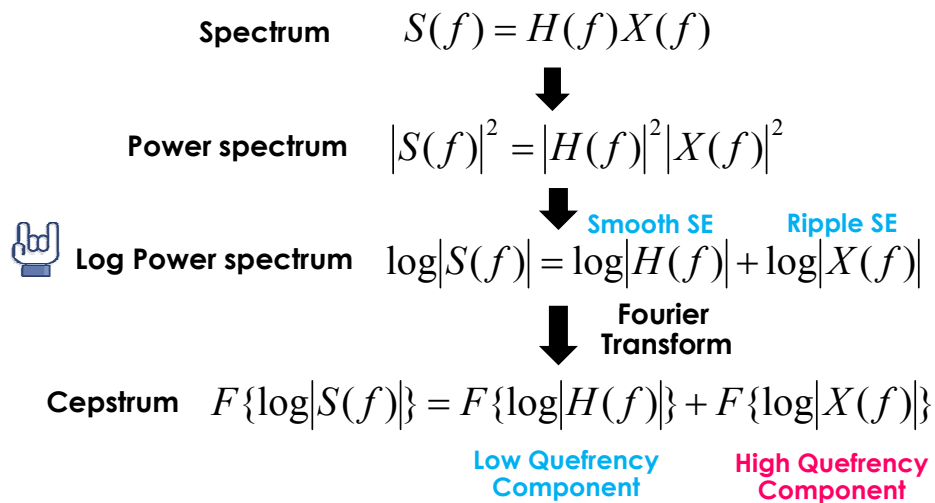


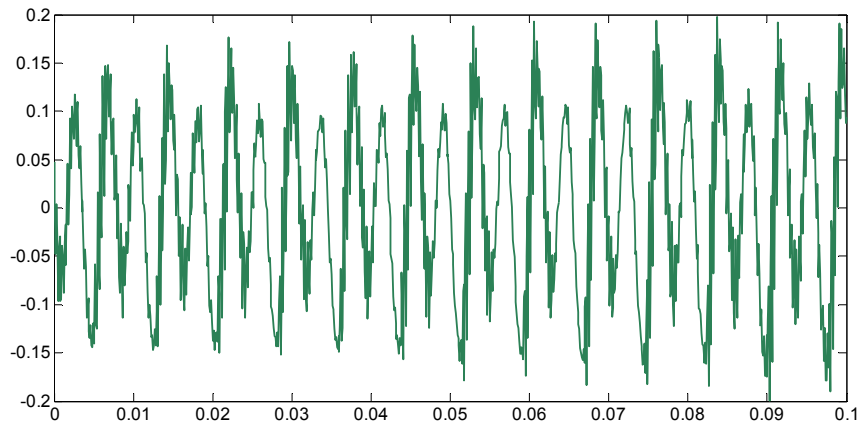
http://postgavindisorder.blogspot.com/2010_09_01_archive.html

Cepstrum



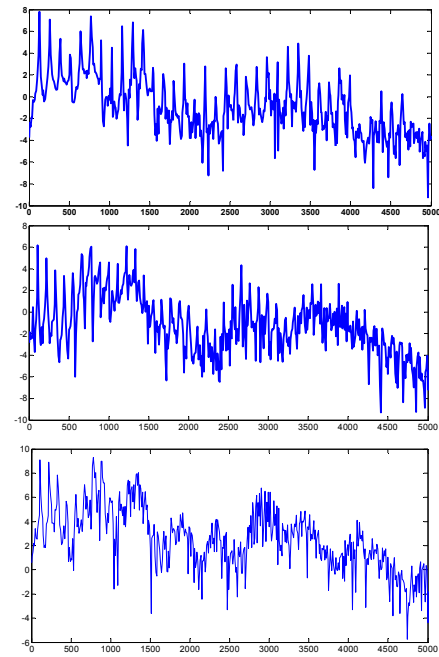
Cepstrum



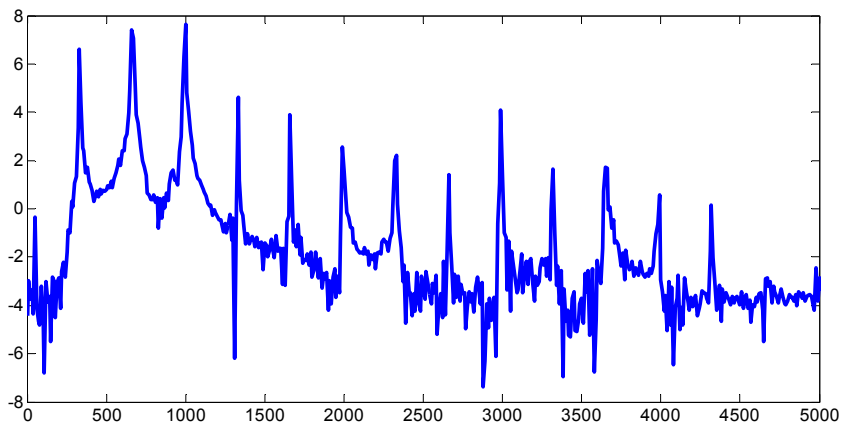
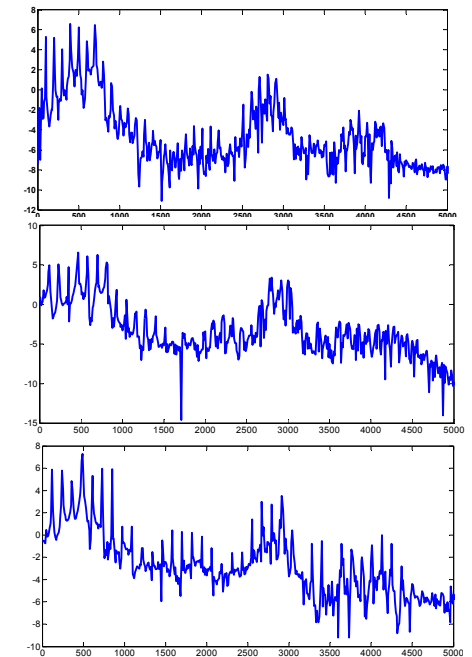


ให้ทายว่าเสียงอะไร?

อากาาห์

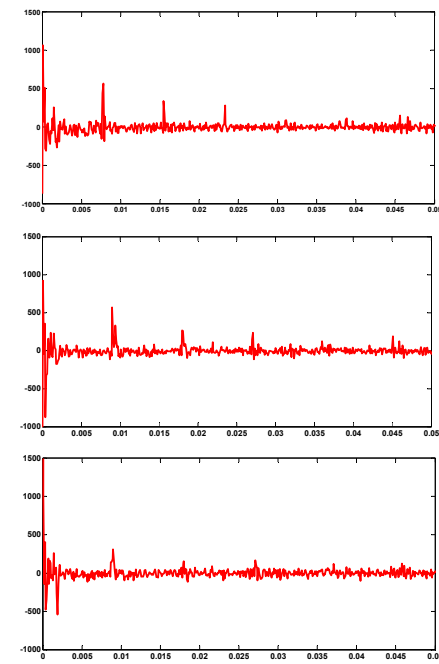


โอวรวว์

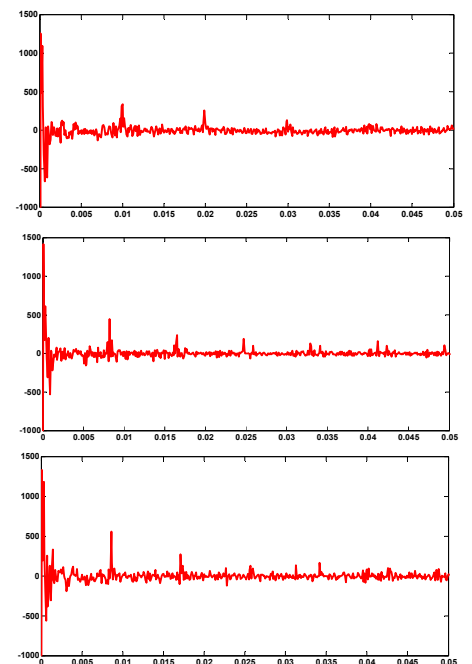


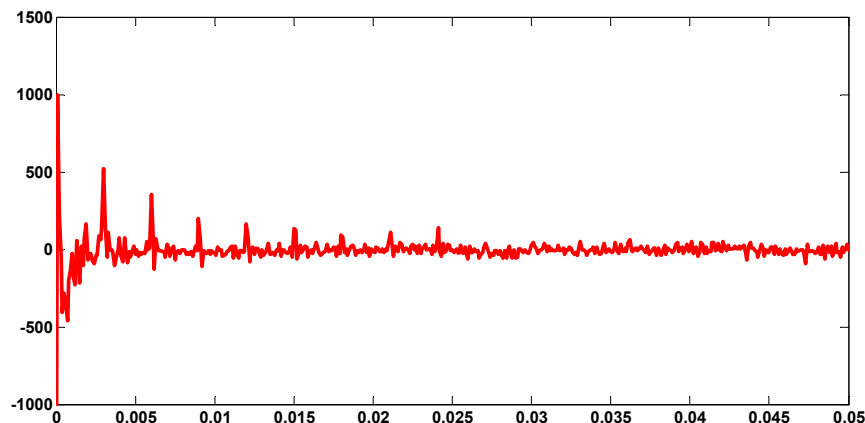
ให้ทายว่าเสียงอะไร?

อากาาห์



โอวรวว์

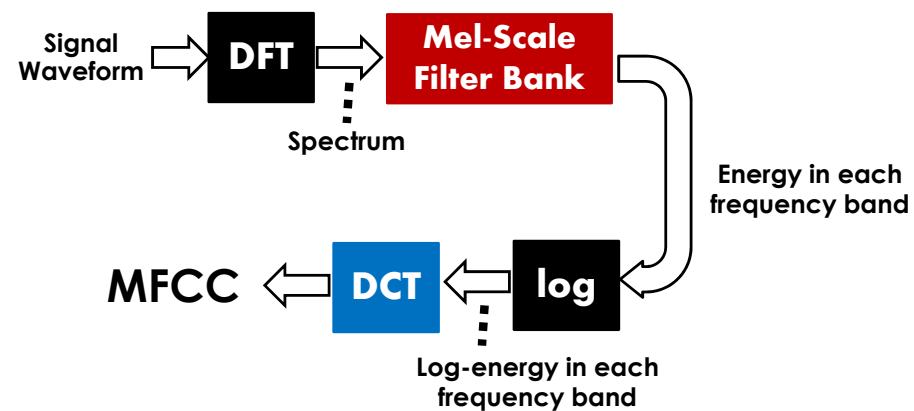




ให้ทายว่าเสียงอะไร?

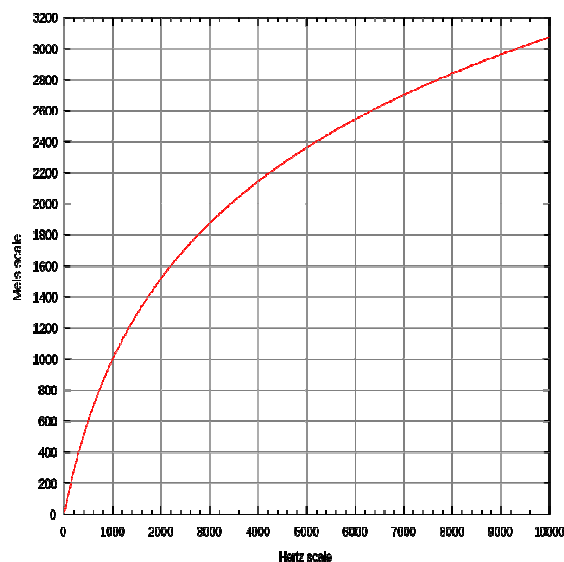
Mel-Frequency Cepstrum Coefficient

[MFCC]



DCT = Discrete Cosine Transform

Mel-Scale

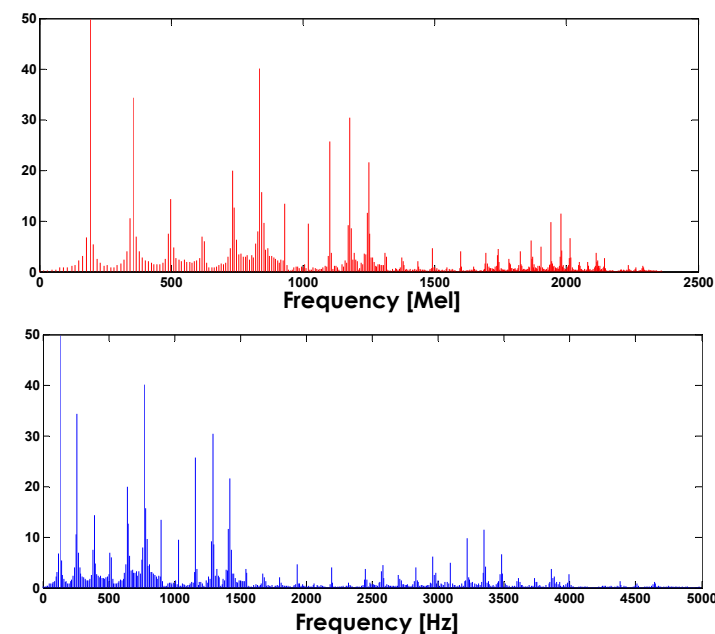


$$f_{[mel]} = 1127.0148 \ln \left(1 + \frac{f_{[Hz]}}{700} \right)$$

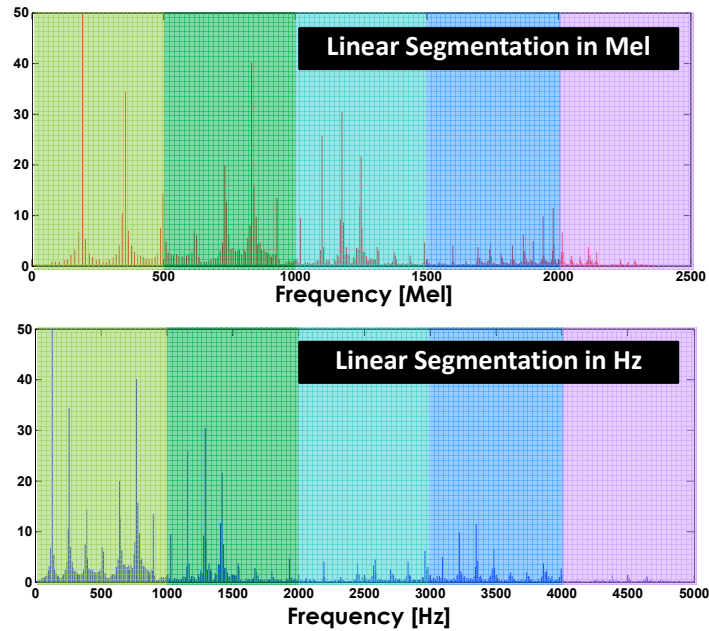
• Perceptual scale of pitches

Hertz	Mel
174	250
391	500
662	750
1000	1000
1949	1500
3429	2000
5734	2500

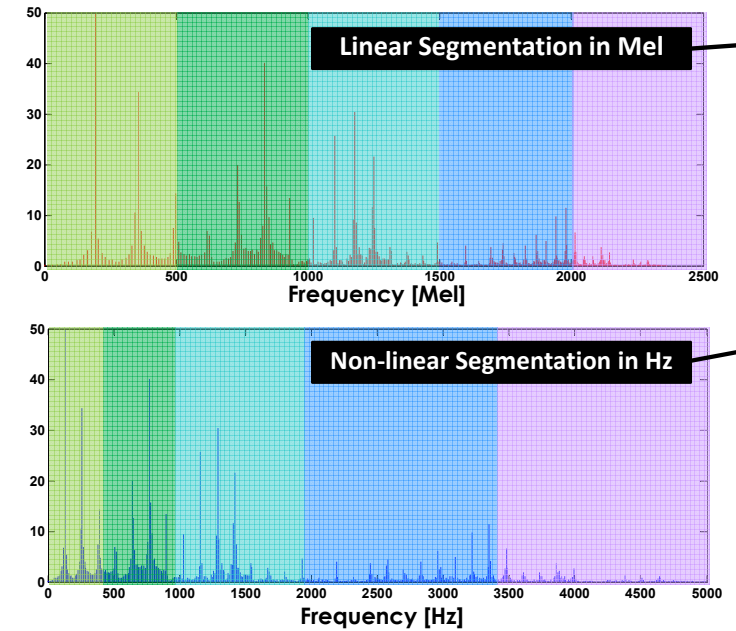
Mel-Scale



Mel-Scale



Mel-Scale

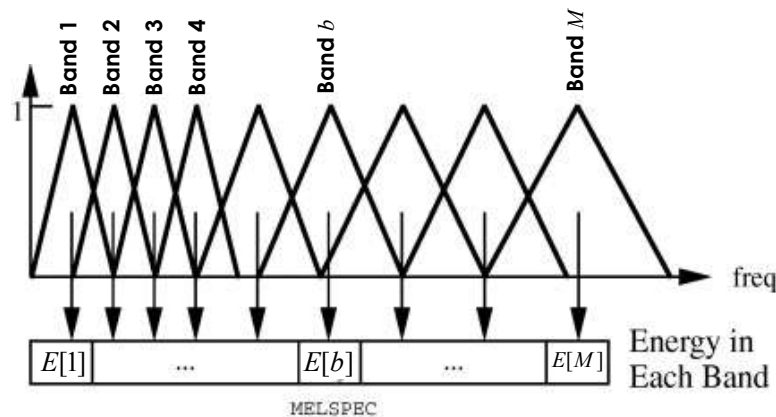


Mel-Scale Filter Bank

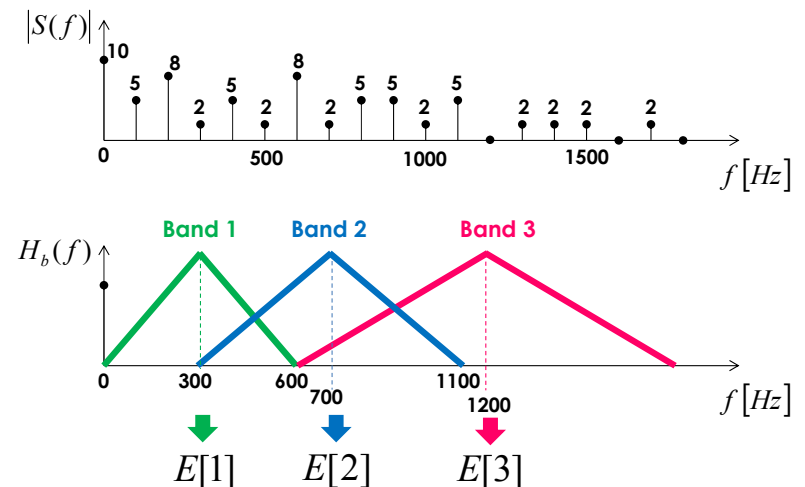
$$E[b] = \sum_{f \in \text{Band}[b]} |S(f)| H_b(f)$$

$E[b]$: Energy in Band b

$H_b(f)$: Freq. Response of Filter for Band b

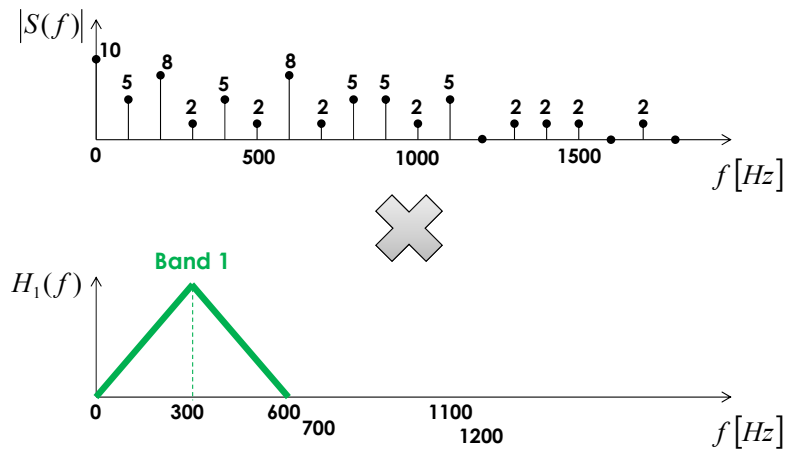


Mel-Scale Filter Bank



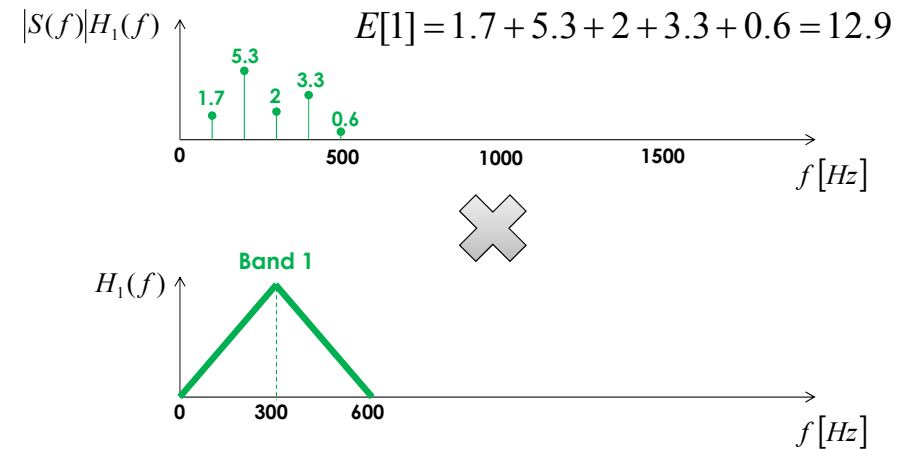
Mel-Scale Filter Bank

$$E[1] = \sum_{f \in \text{Band}[1]} |S(f)| H_1(f)$$



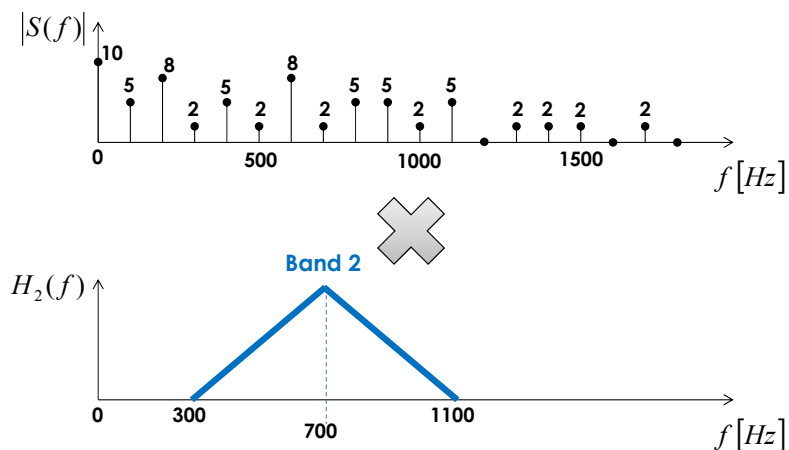
Mel-Scale Filter Bank

$$E[1] = \sum_{f \in \text{Band}[1]} |S(f)| H_1(f)$$



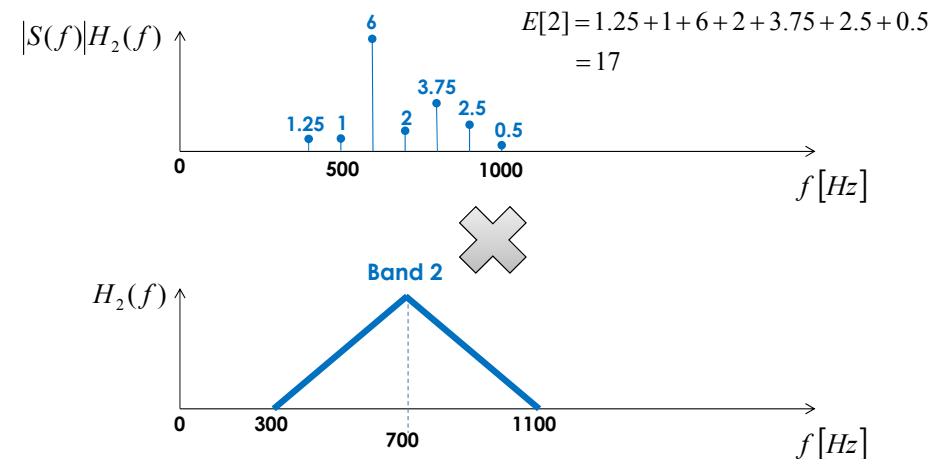
Mel-Scale Filter Bank

$$E[2] = \sum_{f \in \text{Band}[2]} |S(f)| H_2(f)$$



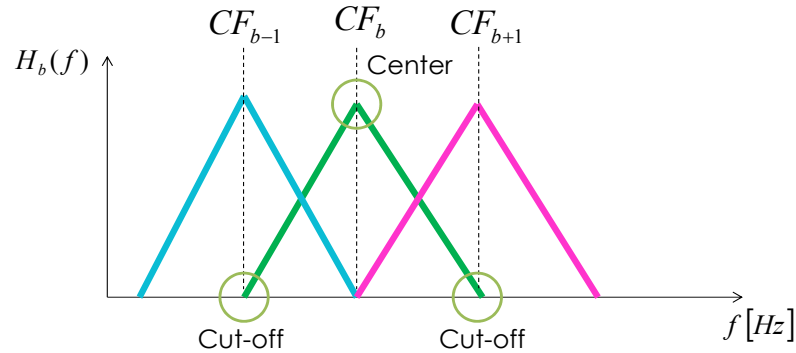
Mel-Scale Filter Bank

$$E[2] = \sum_{f \in \text{Band}[2]} |S(f)| H_2(f)$$



Mel-Scale Filter Bank

- Cut-off frequency of filter in the current band determined by the center frequencies of the two adjacent filters.



Mel-Scale Filter Bank

- Triangular Filter

$$H_b(f) = \begin{cases} \frac{f - CF_{b-1}}{CF_b - CF_{b-1}}; & CF_{b-1} < f < CF_b \\ \frac{f - CF_{b+1}}{CF_b - CF_{b+1}}; & CF_b \leq f < CF_{b+1} \\ 0; & \text{otherwise} \end{cases}$$

CF_b = Center Frequency of Band b [Hz]

Mel-Scale Filter Bank

- Center Frequency

$$CF_b = F_{\min} + b \cdot \frac{F_{\max} - F_{\min}}{M + 1} \quad \text{in [mel]}$$

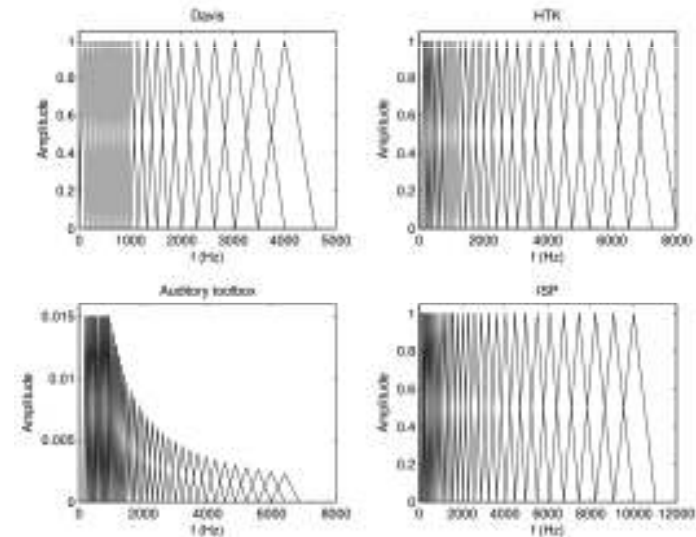


CF_b in [Hz]

M = Number of Bands

$F_{\min} \sim F_{\max}$ = Frequency Range

Mel-Scale Filter Bank



Discrete Cosine Transform [DCT]

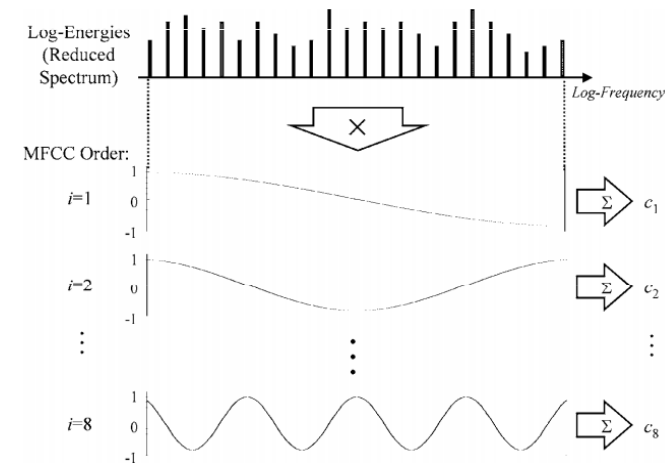
$$c[i] = \sum_{b=1}^M \ln(E[b]) \cos\left(i\left(b - \frac{1}{2}\right)\frac{\pi}{M}\right)$$

$c[i]$ = Mel Frequency Cepstrum Coefficient

i = Order of MFCC

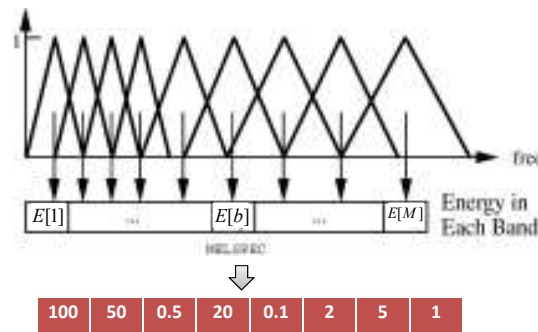
M = Number of Frequency Bands

Discrete Cosine Transform [DCT]



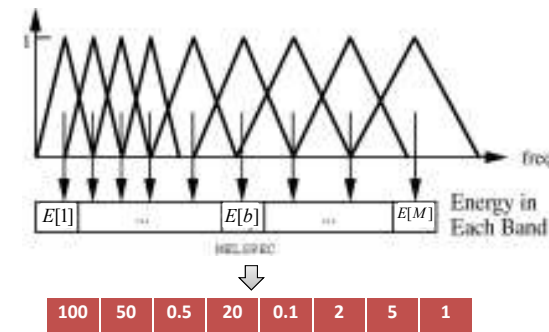
MPEG-7 Audio and Beyond. Audio Content Indexing and Retrieval. Hyoung-Gook Kim, et. al.

Discrete Cosine Transform [DCT]

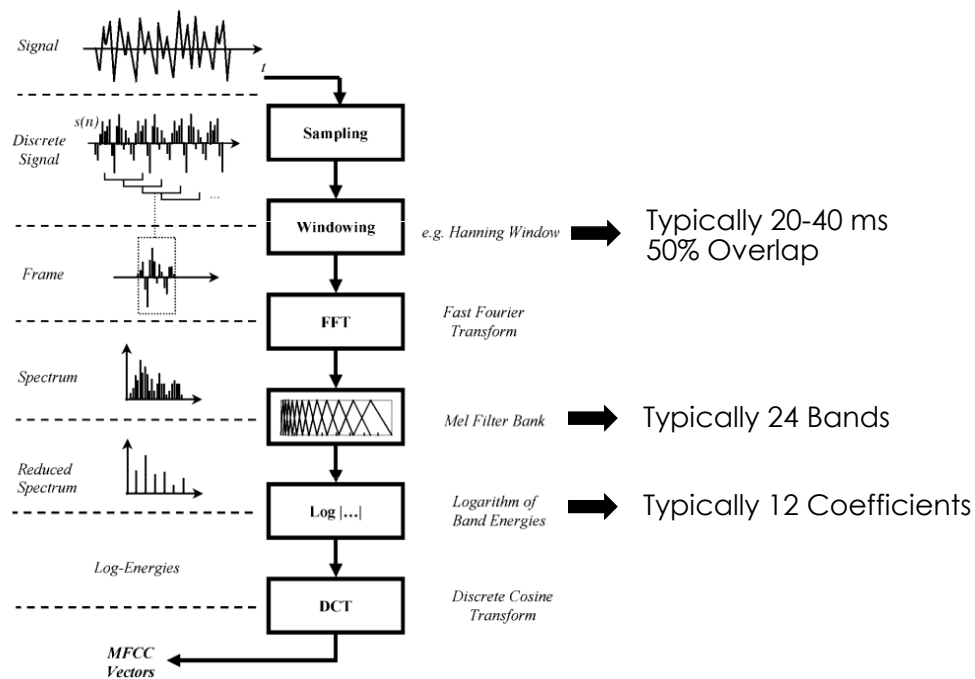


$$\begin{aligned} c[1] &= \sum_{b=1}^8 \ln(E[b]) \cos\left(\left(b - \frac{1}{2}\right)\frac{\pi}{8}\right) \\ &= \ln(100)\cos\left(\frac{\pi}{16}\right) + \ln(50)\cos\left(\frac{3\pi}{16}\right) + \ln(0.5)\cos\left(\frac{5\pi}{16}\right) + \dots + \ln(1)\cos\left(\frac{15\pi}{16}\right) \\ &= 6.6947 \end{aligned}$$

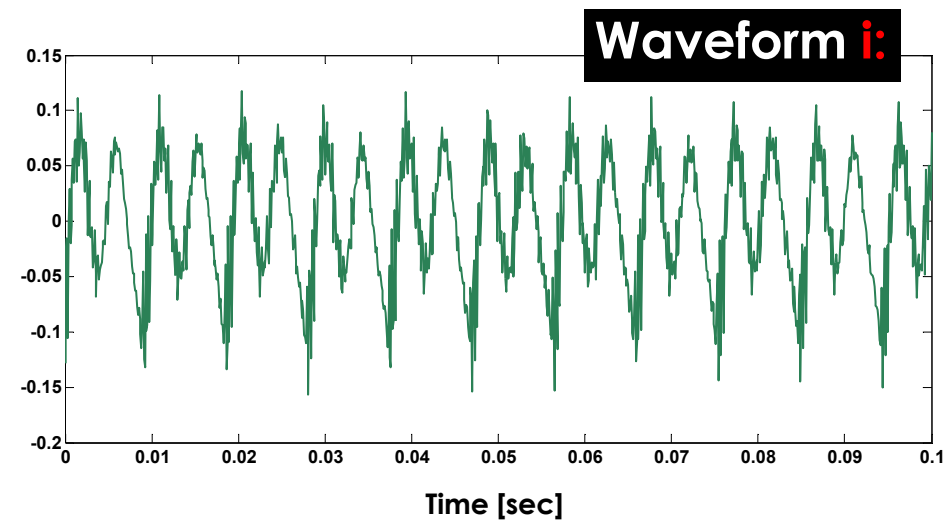
Discrete Cosine Transform [DCT]



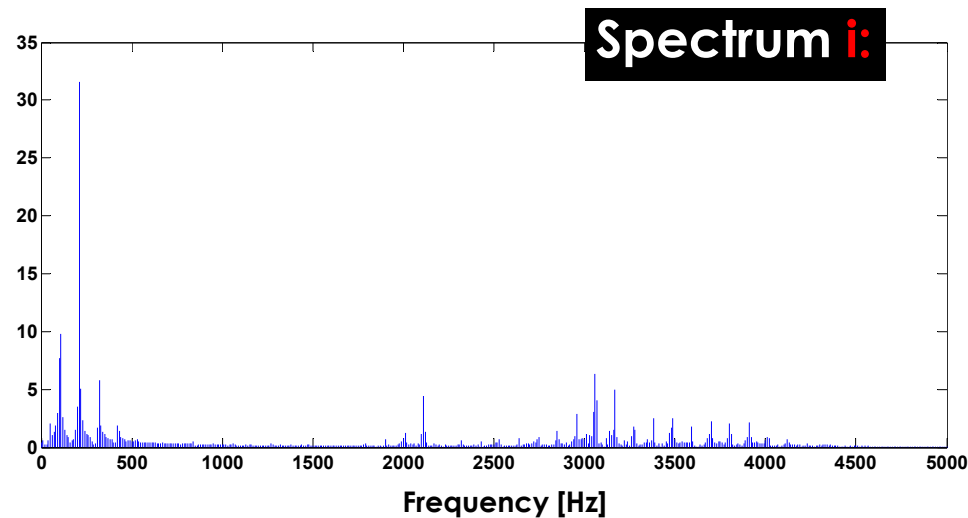
$$\begin{aligned} c[2] &= \sum_{b=1}^8 \ln(E[b]) \cos\left(2\left(b - \frac{1}{2}\right)\frac{\pi}{8}\right) \\ &= \ln(100)\cos\left(\frac{\pi}{8}\right) + \ln(50)\cos\left(\frac{3\pi}{8}\right) + \ln(0.5)\cos\left(\frac{5\pi}{8}\right) + \dots + \ln(1)\cos\left(\frac{15\pi}{8}\right) \\ &= 5.7272 \end{aligned}$$



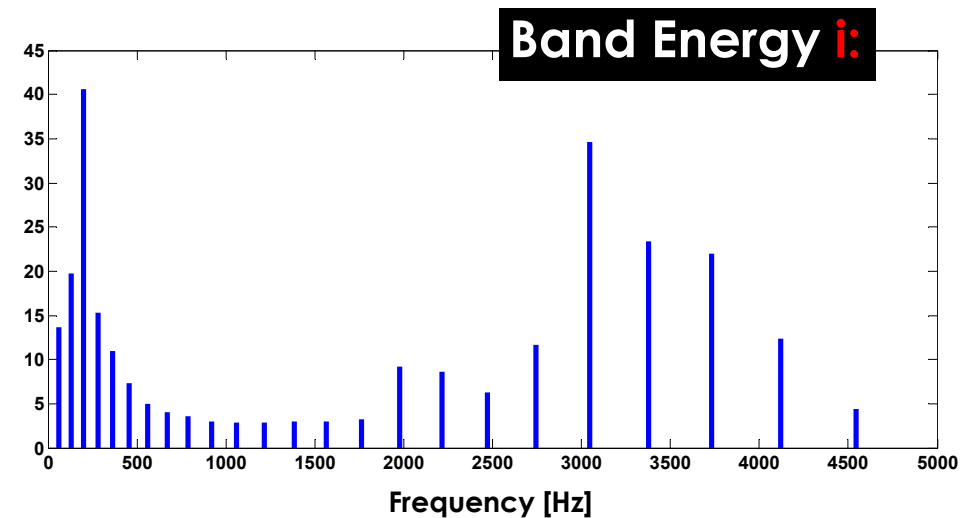
Mel-Frequency Cepstrum Coefficient



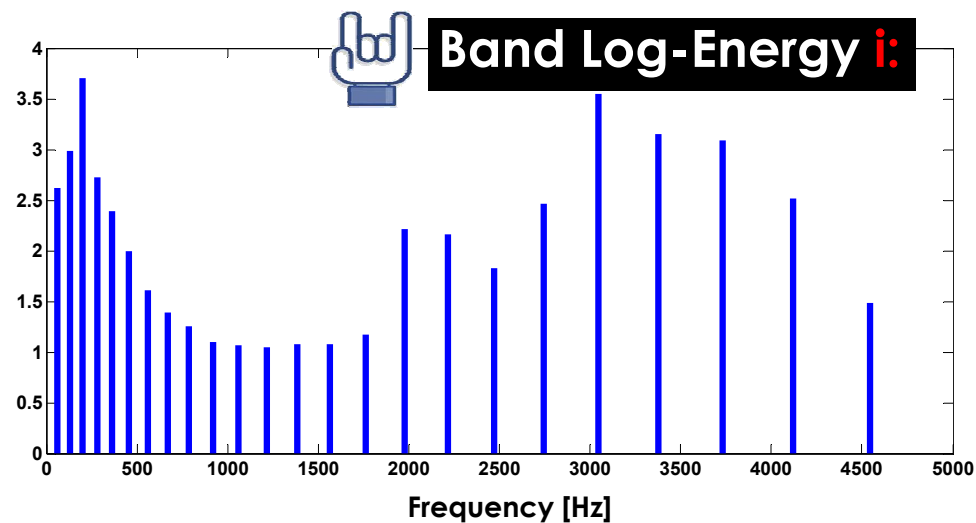
Mel-Frequency Cepstrum Coefficient



Mel-Frequency Cepstrum Coefficient



Mel-Frequency Cepstrum Coefficient



Mel-Frequency Cepstrum Coefficient

