## A Computation problems

1. (10 points) The table below shows a training set with 10 examples that is used for training a **3-nearest-neighbors** classifier that uses Manhattan distance, i.e., the distance between two points at coordinates p and q is |p-q|. The only attribute, X, is real-valued, and the label Y has two possible classes, 0 and 1. The first fold contains the first 5 examples, and the second fold contains that last 5 examples. In case of ties in distance, use the example with smallest X value as the neighbor. Please compute the 2-fold cross validation accuracy (percentage correct classification).

X	0	1	2	3	4	5	6	7	8	9
Υ	1	0	1	0	1	0	1	0	1	0

2. (10 points) You want to cluster 7 points into 3 clusters using the k-means clustering algorithm. Suppose after the first iteration, clusters  $C_1$ ,  $C_2$  and  $C_3$  contain the following two-dimensional points:

 $C_1$  contains the 2 points:  $\{(0,6),(6,0)\}$ 

 $C_2$  contains the 3 points:  $\{(2,2),(4,4),(6,6)\}$ 

 $C_3$  contains the 2 points:  $\{(5,5),(7,7)\}$ 

Please compute the coordinates of cluster centers for these 3 clusters.

3. (20 points) The following dataset as in the table is provided to build a naive Bayes classifier, where  $\{x_1, x_2, x_3, x_4\}$  and l are the features and the label, respectively. Please give the process of building the classifier and predict the label of the unknown instance  $\mathbf{x} = [1, 0, 1, 1]^T$ .

$$\begin{bmatrix} x_1 & x_2 & x_3 & x_4 & l \\ 0 & 1 & 0 & 1 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 1 & 1 & 1 & 0 & 0 \\ 1 & 0 & 1 & 0 & 1 \end{bmatrix}$$

## B Essay questions

4. (20 points) Perceptron is a function that maps input  $\boldsymbol{x}$  to a label as follows

$$f(\mathbf{x}) = \begin{cases} 1, & w \cdot x + b > 0 \\ 0, & \text{otherwise} \end{cases}$$

Now consider solving the logical **OR** and logical **XOR** problems (as shown in two tables) with the perceptron model.

$$y = f(\mathbf{x}) = \begin{cases} 1, & w_1 x_1 + w_2 x_2 + b > 0 \\ 0, & \text{otherwise} \end{cases}$$

Table 1: Logical OR

	- 0		 -
$x_1$	$x_2$	y	
0	1	1	
1	1	1	
1	0	1	
0	0	0	

Table 2: Logical XOR

$x_1$	$x_2$	y
0	1	1
1	1	0
1	0	1
0	0	0

- 1) (4 points) Please draw all datapoints of the tables in the two-dimensional space for logical OR and logical XOR problems, respectively, where different classes are marked with different shapes.
- 2) (16 points) Please explain separately whether the perceptron can mimic the output of logical OR and logical XOR or not. If so, please give an example of function f(x); if not, please prove that there is no such function f(x).