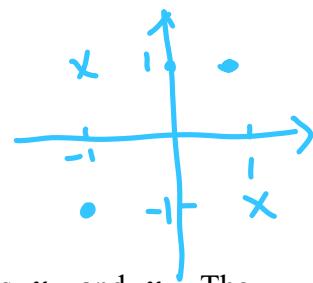


INT301 Bio-computation

Week 3 Tutorial



✓ Question 1

The following two Boolean functions take two Boolean features x_1 and x_2 . The features can take on the values -1 and $+1$, where -1 represents False and $+1$ represents True. The output y of the functions can also take on the values -1 and $+1$, with the same interpretation. For each of the functions below, either give weights for a perceptron such that the perceptron represents the function or argue that no such weights exist.

$$1) y = \begin{cases} +1, & \text{if } x_1 = x_2 \\ -1, & \text{otherwise} \end{cases}$$

No

"XOR"

$$2) y = \begin{cases} +1, & \text{if } x_1 = 1 \text{ and } x_2 = -1 \\ -1, & \text{otherwise} \end{cases}$$



✓ Question 2

You want to design a neural network with sigmoid units to predict a person's academic role from his webpage. Possible roles are "professor", "student", and "staff". However, each person can take any number (from 0 to all 3) of these roles at the same time. Briefly describe:

- (1) How you would represent the role label of a person in your training data. **vector**: $[0, 0, 0]$
- (2) Suggest a possible threshold value for the outputs. $\rightarrow [1, 1, 1]$

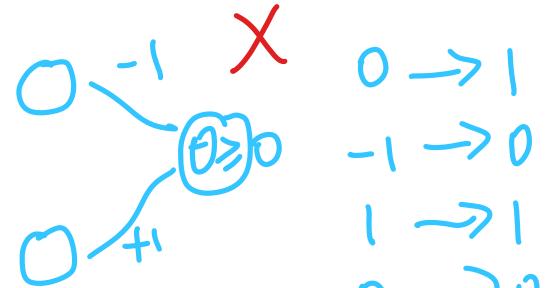
注意 preceptron 定义 $\theta > 0.5$

Question 3

Consider the following Boolean function:

存在 bias, $f_{CS} = \begin{cases} 1, & s \geq \theta \\ 0, & s < \theta \end{cases}$

| A | B | $A \vee B$ |
|---|---|------------|
| 1 | 1 | 1 |
| 1 | 0 | 0 |
| 0 | 1 | 1 |
| 0 | 0 | 0 |



Construct a perceptron that represents the function.

$$w_0 \geq \theta \quad \text{if } w_0 = 0 \Rightarrow \theta \geq 0 \nRightarrow w_2 \geq 0, w_1 < 0$$

$$w_1 = -1, w_2 = 1, \theta = 0, w_0 = 0 \quad w_1 + w_2 \geq 0$$

✓ Question 4 $\Rightarrow w_1 = -1, w_2 = 1, \theta = 0, w_0 = 0$
Consider a task involving "a three-input, one-output parity detector" which outputs a 1 if the number of "1" inputs is even; otherwise it outputs a 0. Can this function be represented by a perceptron? Explain.

$f_{Parity} = \sum_{i=1}^3 x_i = S$ $f_{CS} = \begin{cases} 1, & s \geq \theta \\ 0, & s < \theta \end{cases}$

$E(x'_1, x'_2, x'_3) \rightarrow (x'_1 + x'_2 + x'_3) \geq \theta$

$\Rightarrow \begin{cases} f + w_1 < 0 \\ f + 2w_1 \geq 0 \end{cases} \Rightarrow \begin{cases} f < 0 \\ f \geq -2w_1 \end{cases}$