Report

Exercise 01:

Computing of Matrix Multiplication using C++

Group: ex01_group02

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1. Objectives:

Objective of this report is to implement a matrix-matrix multiplication $C = A \times B$, where A is a M X K matrix, B is a K X N matrix, and C is aM X N matrix.

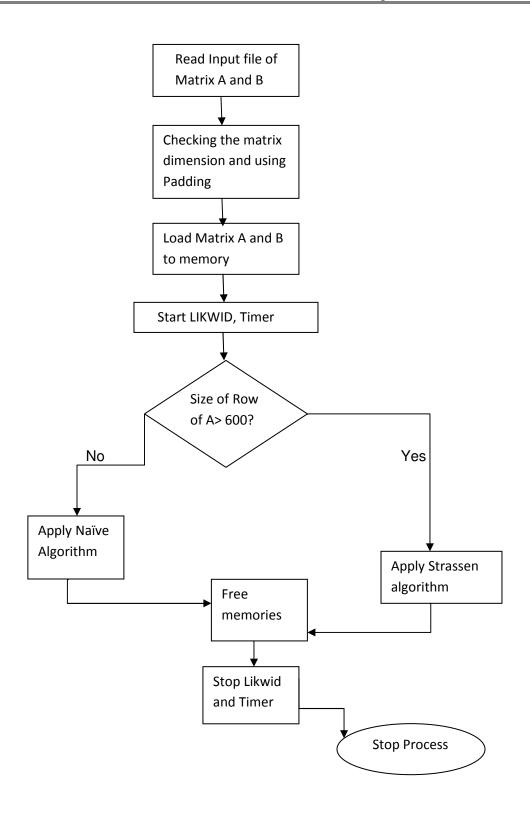
2. Description of the task:

Refer to the file ex01.pdf

3. Design/Flowchart:

Following diagram is the flow chart of the implemented C++ program.

Start Process



4. Methodologies:

These are the key points used in the implementation.

- 1. A separate class "matrix" (implemented in matrix.hpp) is used for all the basic operations and properties of a Matrix. It is kind of a wrapper class around the native double array. It also handles access to sub blocks of the matrix.
- 2. For the transposition a blocking size of 128 is used.
- 3. All the matrix rows are padded by 64 to avoid cache threshing.
- 4. Advanced Vector Extensions (AVX) Instruction set (a new 256 bit Instruction set features provided by Intel processor) is used while fetching data from memory in matrix multiplication operation both in naïve and Strassen modules.
- 5. In naïve multiplication, block size of 4 X 4 is considered.
- 6. AVX methodologies like mm256 blend pd(), mm256 hadd pd(), _mm256_permute2f128_pd() and _mm256_add_pd() are used for the addition of multiplied components of A with B.
- 7. More optimized recursive Strassen algorithm is implemented to measure the multiplication of matrix size more than 600.
- 8. Compare.cpp is written to compare the output matrix of the program to the standard output files. It will confirm us about the correctness of the result.
- 9. The program is compiled with a Makefile.
- 10. Double precision floating-point operations are used for the multiplication.
- 11. 5 stages of optimization techniques as opt1, opt2, opt3, opt4, opt5 has been done. Opt5 is the final version.

5. Optimization stages:

All stages include optimizations of previous stages.

Naïve: Basic implementation of matrix matrix multiplication.

Opt1: Transpose B before doing matrix multiplication to have better memory layout for B.

Opt2: Using AVX instructions to increase performance of naïve matrix matrix multiplication.

Opt3: Loop unrolling for naïve multiplication.

Opt4: Introduced blocking in matrix transposition.

Op5: Implementation of Strassen algorithm.

6. Source Code:

Refer to the following cpp files.

- 1. Matmult.cpp
- 2. compare.cpp
- 3. matrix.hpp

7. Discussion on the Result and Graphical **Representations:**

Performance and result of the implementation has been measured in all the optXX versions. And the results attached in the Package.

Following is the table for the final opt5 version which will give the different likwid measurement of time taken by the program. It is taking only 0.781054 sec for 2048 X 2048 matrix multiplication. All the time measurements are lesser than the tutor implementation except for 32 X 32 implementation.

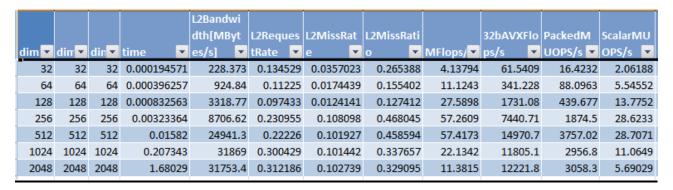
Opt 5 Results:

				L2Bandwi							
				dth[MByt	L2Reques	L2MissRa	L2MissRat		AVXFlops	PackedM	ScalarMU
dim1	dim2	dim3	time	es/s]	tRate	te	io	MFlops/s	/s	UOPS/s	OPS/s
32	32	32	4.12E-05	346.805	0.186532	0.0542	0.290567	4.29474	69.3809	18.4194	2.14638
64	64	64	8.41E-05	1072.01	0.140917	0.038137	0.270631	14.3908	470.286	121.169	7.1954
128	128	128	0.000356	3364.93	0.110735	0.028097	0.253733	37.4148	2455.4	623.199	18.7175
256	256	256	0.002151	10817.6	0.151221	0.048412	0.320139	47.7533	6298.87	1586.65	23.8918
512	512	512	0.015691	24061.5	0.171358	0.048412	0.28252	52.822	14044.5	3524.34	26.4128
1024	1024	1024	0.111356	26653.6	0.180665	0.056845	0.314642	64.9698	17279.2	4336.03	32.4875
2048	2048	2048	0.781054	27568.4	0.183776	0.057751	0.314248	65.5946	17559.6	4406.31	32.7972

Opt 4 Results:

									32b	Packe	
				L2Bandwi					AVX	dMU	
				dth[MByt	L2Request		L2MissRat		MFlo	OPS/	ScalarM
din	din🔽	dim3 🔽	time 🔽	es/s]	Rate 🔽	L2MissRate 💌	io 💌	MFlops	ps/:▼	s 🔻	UOPS.
32	32	32	0.000181351	390.851	0.0325097	0.00819859	0.252189	155.456	0	0	0
64	64	64	0.000429757	1090.72	0.0163535	0.00232315	0.142059	598.818	0	0	0
128	128	128	0.00209118	4917.15	0.0331493	0.00143158	0.043186	1116.67	0	0	0
256	256	256	0.0142631	7351.06	0.056958	0.0185848	0.326289	1922.7	0	0	0
512	512	512	0.111144	10074.8	0.0556738	0.0182398	0.327619	1740.58	0	0	0
1024	1024	1024	0.958655	7239.13	0.0739376	0.0229468	0.310354	2281.75	0	0	0
2048	2048	2048	8.17724	9050.51	0.0832589	0.0253613	0.304608	2165.75	0	0	0

Opt 3 Results:



Opt2 Result:



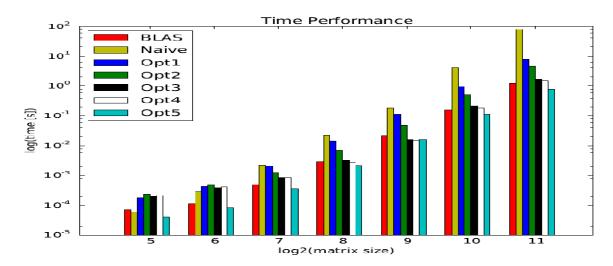
Opt 1 Result:

				L2Bandw					32b AVX	Packe	
dim					L2Reques	L2MissRat	L2MissR				ScalarM
1 🔽	din 🔽	din	time 🔽	ytes/s]	tRate 💌	e 🔽	atio 🔽	s 🔻	/s 🔻	PS/s ▼	UOPS
32	32	32	0.000181351	390.851	0.0325097	0.0081986	0.252189	155.456	0	0	0
64	64	64	0.000429757	1090.72	0.0163535	0.0023232	0.142059	598.818	0	0	0
128	128	128	0.00209118	4917.15	0.0331493	0.0014316	0.043186	1116.67	0	0	0
256	256	256	0.0142631	7351.06	0.056958	0.0185848	0.326289	1922.7	0	0	0
512	512	512	0.111144	10074.8	0.0556738	0.0182398	0.327619	1740.58	0	0	0
1024	1024	1024	0.958655	7239.13	0.0739376	0.0229468	0.310354	2281.75	0	0	0
2048	2048	2048	8.17724	9050.51	0.0832589	0.0253613	0.304608	2165.75	0	0	0

Naïve Result:

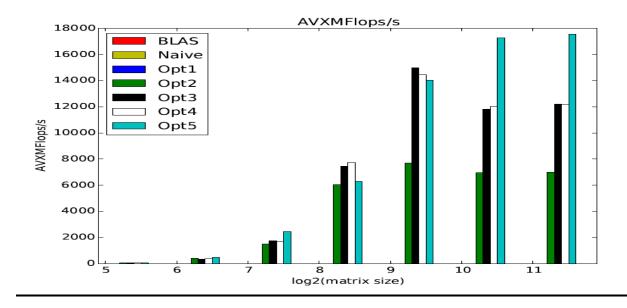


Plot:Time Performance:



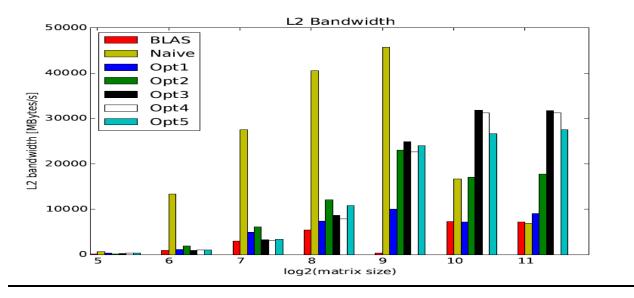
From the above diagram it is clear that for the final opt5 version, time taken is always lesser than BLAS irrespective of the matrix size.

Plot of AVXMFlops/

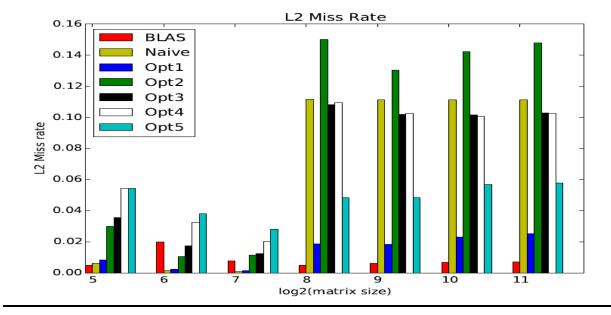


You can clearly see the introduction of AVX instructions in Opt2. BLAS seems to not use AVX instructions at all.

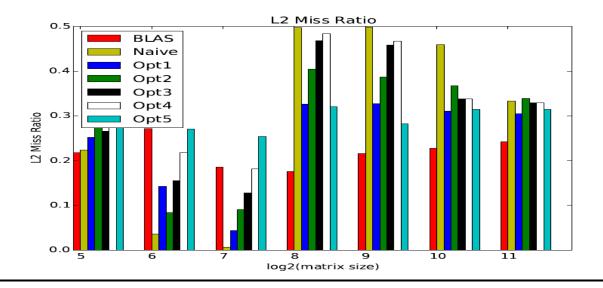
Plot: L2 Bandwidth:



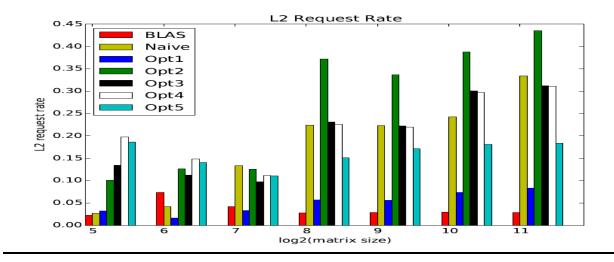
Plot: L2 Miss Rate:



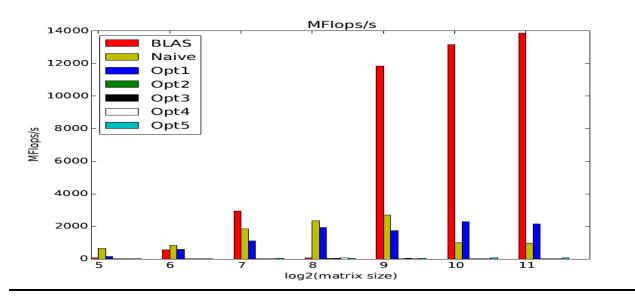
Plot: L2 Miss Ratio:



Plot: L2RequestRate:



Plot:MFlops:



Plot: PackedMUOPSs:

