

## List of Selected Problems along with links to Problem Statements:

No.	Problem ID	Title	Rating	Tags	Problem Link
1	2114F	Small Operations	2000	binary search, brute force, dfs and similar, dp, math, number theory, sortings	<a href="#">Link</a>
2	2107F1	Cycling (Easy Version)	2300	binary search, brute force, dp, greedy	<a href="#">Link</a>
3	2110F	Faculty	2400	brute force, greedy, math, number theory	<a href="#">Link</a>
4	603A	Alternative Thinking	1600	dp, greedy, math	<a href="#">Link</a>
5	2107C	Maximum Subarray Sum	1500	binary search, constructive algorithms, dp, implementation, math	<a href="#">Link</a>
6	571A	Lengthening Sticks	2100	combinatorics, implementation, math	<a href="#">Link</a>
7	2093C	Simple Repetition	1000	math, number theory	<a href="#">Link</a>
8	2104C	Card Game	1100	brute force, constructive algorithms, games, greedy, math	<a href="#">Link</a>
9	2094E	Boneca Ambalabu	1200	bitmasks	<a href="#">Link</a>
10	2109B	Slice to Survive	1200	bitmasks, greedy	<a href="#">Link</a>

## Detailed Approach Explanation for above Problems:

### Advanced Problem-Solving Techniques:

#### 1. 2114F : Small Operations

- My solution approaches the problem by first breaking it into : "transforming 2 numbers (x and y) into their GCD through multiplication operations with factors  $\leq k$ "
- First, it checks if x and y are equal, outputting 0 if true.
- For unequal numbers, it computes their GCD (g) and then determines the minimal steps required to reduce both x/g and y/g to 1, using valid factors.

- The calc function employs BFS on the divisors of the number, exploring valid transitions (multiplications) while ensuring that factors are  $\leq k$  and the largest prime factor of the number is  $\leq k$ .
- If either transformation is impossible, then it outputs -1; otherwise, it sums the steps for both transformations.

**Techniques Utilized:** *prime factorization, divisor enumeration, and BFS for shortest path calculation.*

## 2. 2107F1 : Cycling (Easy Version)

- My approach is to use DP to efficiently compute the minimum cost of processing elements in reverse order.
- The key observation is that for each position  $i$ , we need to find the next smallest element ( $p$ ) in the remaining array, as this minimizes the cost of swaps and overtakes.
- The DP array  $dp[i]$  stores the minimum cost to process elements from  $i$  to  $n$ . For each  $i$ , we iterate through all possible positions  $j$  starting from  $p$  to  $n$ , calculating the cost of swapping (swapCost), overtaking (overCost), and backtracking (backtrack).
- The total cost for  $i$  is derived by combining these costs with the precomputed cost  $dp[j]$ .
- This approach ensures optimal substructure and overlapping subproblems are handled efficiently, resulting in an  $O(n^2)$  solution per testcase.
- The main function reads input, processes each testcase, and outputs the result by calling **solveCase**.

## 3. 2110F : Faculty

- The approach is to maintain a running maximum (**mx**) and optimizing calculations by recognizing two key scenarios:
  1. When encountering an element at least twice as large as **mx**, it fully compares this element with all previous elements since it could yield higher values for **f(x, y)**.
  2. For smaller updates to **mx**, it simplifies the calculation knowing the maximum possible value of **f(x, y)** at that point is the new **mx** itself.
- This approach balances thoroughness with efficiency by minimizing unnecessary computations while ensuring all potential maxima are considered.

## Dynamic Programming (DP):

## 4. 603A : Alternative Thinking

- In this question using the DP approach would be **less efficient** than the greedy approach that I found to be simpler.
- The DP approach would be  $O(n^2)$ , whereas the greedy approach will only be  $O(n)$ .
- The approach involves counting the initial number of distinct adjacent segments (**res**) in the string.

- For example, the string "0011" has 2 segments ("00" and "11"), so **res** = 2.
- We can see that each operation can reduce the number of segments by at most 2 (by merging adjacent segments).
- Thus, the maximum possible reduction is **res** + 2, but it cannot exceed the string length **n**.
- The final result is the minimum of these 2 values, ensuring efficiency with a single pass through the string.

## 5. 2107C : Maximum Subarray Sum

- The approach is to use Kadane's Algorithm to calculate the Maximum Subarray Sum, and check if it exceeds **k** or if adjustment isn't possible (no '0' in the string).
- If valid, then calculate the maximum possible sums to the left (**R**) and right (**L**) of the first '0' position.
- Then, the value at this position is set to **k - L - R**, ensuring the maximum subarray sum equals **k**.

## Mathematics and Number Theory:

### 6. 571A : Lengthening Sticks

- The approach involves calculating the total possible ways to distribute **I** increments (combinations with repetitions) and subtracting the invalid cases where triangle inequality fails.
- The **count\_invalid** function efficiently checks invalid combinations by iterating over possible increments for one side and calculating invalid distributions for the remaining sides using Arithmetic Progression.
- The main function aggregates invalid counts for all three sides and subtracts them from total possibilities, ensuring optimal performance with combinatorial mathematics.

### 7. 2093C : Simple Repetition

- The approach is to first check the edge cases: if **n** is 1, etc.
- For **k=1**, it simply checks if **n** itself is prime using a helper function **isPrime()**, which efficiently tests primality up to the square root of **n**.
- For other cases, the code quickly outputs "NO" if **n** is even (and not 2) or if both **n>1** and **k>1**, so that it is optimized for specific scenarios.
- The main logic in **solve()** handles targeted conditions, while the primality test ensures correctness for the base case when **k=1**.

## Implementation and Greedy Strategies:

### 8. 2104C : Card Game

- The key insight is in checking if there exists any 'A' (Alice's move) that cannot be "beaten" by any 'B' (Bob's move) based on their positions.
- The **beats** function defines the winning condition: position **x** beats **y** if **x** is 0 and **y** is **n-1**, or **x** is **n-1** and **y** isn't 0, or **x** is greater than **y** in normal cases.
- The **solve** function iterates through each 'A' and checks if no 'B' can beat it.
- If such an 'A' exists, Alice wins; otherwise, Bob wins.

## Bitmasking and Optimization:

### 9. 2094E : Boneca Ambalabu

- For each bit position (0 to 29), count how many numbers have that bit set (**cnt[j]**).
- For each element, calculate the sum of XORs with all other elements by leveraging these counts: if the bit is set, it contributes  $(n - \text{cnt}[j]) \cdot (1 \ll j)$  (since unset bits will produce a set bit in XOR), and if unset, it contributes  $\text{cnt}[j] \cdot (1 \ll j)$ .
- The maximum of these sums across all elements is the answer.
- This approach efficiently reduces the  $O(n^2)$  brute-force problem to  $O(n \cdot 30)$  per test case by preprocessing bit counts.

### 10. 2109B : Slice to Survive

- The approach is to use two strategies: cutting rows first or cutting columns first.
- For each strategy, it computes the cost by considering the logarithmic ceiling of the remaining segments after each cut, which represents the number of binary cuts needed.
- The **compute\_log\_ceiling** function efficiently calculates this using bitwise operations (**\_builtin\_clz**).
- Then compare the costs of both strategies and selecting the minimum one.