Midsen 2019 CS 215 Solutions

OI) The reg. log likelihood is
$$L(\{x_i\}_{i=1}^n | P) = \frac{1}{n} \sum_{i=1}^{n} (x_i - P)^2 / 26^2$$

$$\rightarrow \hat{p} = \sum_{i} x_{i}/n$$

a)
$$v = ap + b \rightarrow p = (v - b)/a$$

 $= \frac{1}{2} \left(\frac{(2xi3)}{v} \right)^{2} = \frac{1}{2} \left(\frac{(2xi - v - b)}{a} \right)^{2} / \frac{26^{2}}{a}$
 $= \frac{1}{2} \left(\frac{(2xi3)}{v} \right)^{2} = \frac{1}{2} \left(\frac{(2xi - v - b)}{a} \right)^{2} / \frac{26^{2}}{a}$

$$\therefore \partial L/\partial v = -\frac{1}{h} \sum_{i=1}^{n} 2(x_i - \frac{y-b}{a})(-\frac{1}{a}) = 0$$

$$\therefore \mathcal{L}\left(\left(\frac{1}{2}\right)^{2}\right)^{2} = \frac{1}{n} \frac{1}{2} \left(\frac{1}{2}\right)^{2} = \frac{1}{n} \frac{1}{2} \left(\frac{1}{2}\right)^{2} = \frac{1}{n} \left(\frac{1}{2}\right)^{2} = \frac{1}{n} \left(\frac{1}{2}\right)^{2} = \frac{1}{n} \left(\frac{1}{2}\right)^{2} + \frac{1}{n} \left(\frac{1}{2}\right)^$$

$$E(\hat{v}) = aE(\hat{p}) + b = ap + b = g(p).$$

So this is an unbiased estimator

$$\mathcal{L}(\{xi\}) \mathcal{V}) = \frac{1}{n} i = 1$$

$$\frac{1}{2} \mathcal{L}(xi - v^{1/3}) + \frac{1}{2} \mathcal{V}^{3} = 0$$

$$\frac{1}{2} \mathcal{L}(xi - v^{1/3}) + \frac{1}{2} \mathcal{L}(xi - v^{1/3}) + \frac{1}{2} \mathcal{L}(xi - v^{1/3}) = 0$$

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As
$$v \neq 0$$
, $\hat{v} = \left(\frac{1}{n} \sum_{i=1}^{n} x_i\right)^3 = \hat{V}^3 = g(\hat{V})$

$$E(\hat{p}^{3}) = ? \quad E(\hat{p}) = p, E[\hat{p}^{2}] = Var(\hat{p}) - (E(\hat{p}))^{2} (2)$$

$$E[(\hat{p}-p)^{3}] = 0 \quad \text{as} \quad \hat{p} \text{ is Gaussian distribute}$$

$$E[(\hat{p}^{3}-p^{3}+3\hat{p}p^{2}-3\hat{p}^{2}p)] = 0$$

$$E[(\hat{p}^{3})] - p^{3} + 3p^{2}p - 3p E[(\hat{p}^{2})] = 0$$

$$E[(\hat{p}^{3})] + 2p^{3} - 3p[Var((\hat{p})) + p^{2}] = 0$$

$$E[(\hat{p}^{3})] + 2p^{3} - 3p[Var((\hat{p})) + p^{2}] = 0$$

$$E[(\hat{p}^{3})] = p^{3} + 3p^{6} + p^{3} = 0$$

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So this to not an unbiased estimator

For values of x such that P(A|x) = P(B|x), 3 make it is impossible to classify using conditionals on x alone. This is for $\frac{-(x-1)^2/2}{e} = \frac{-(x-2)^2/4}{8}$ $\rightarrow -\frac{(\chi-1)^2}{2} = -\frac{(\chi-2)^2}{4} + \ln\sqrt{2}$ $\frac{-3(x-2)^{2}-2(x-1)^{2}}{4}=\frac{7}{4}\ln\sqrt{2}$ $\rightarrow + \chi^2 = + (2 - 4 \ln S_2)$ Take only positive root, as x > 6. Q3) See class lecture slides Q(4) Y = 1/x $P(Y \le y) = P(x \ge 1/y) = 1 - P(x < 1/y)$ $= 1 - F_{x}(1/y)$ $= 1 - F_{x}(1/y)$ $\therefore f_{y}(y) = + f_{x}(\frac{1}{y})(\frac{1}{y^{2}}) \blacksquare$

$$f_{x}(x) = \begin{cases} \frac{1}{b-a} & 0 \le x \le b \\ 0 & \text{otherwise} \end{cases}$$

$$\therefore f_{y}(y) = \begin{cases} \frac{1}{y^{2}(b-a)} & \text{if } b \le y \le a \\ 0 & \text{otherwise} \end{cases}$$

$$0 & \text{otherwise}$$

$$F_{y}(y) = 1 - F_{x}(\frac{1}{y})$$

$$= 1 - \frac{1}{b-a} = \frac{b-\frac{1}{y}}{b-a} = \frac{b-\frac{1}{y}}{b-a}$$

$$E(Y) = \int_{y^{2}(b-a)}^{1/a} \frac{1}{b-a} dy = \frac{\ln y}{1/b}$$

$$= \frac{\log(1/a) - \log(1/b)}{b-a} = \frac{\ln b - \ln a}{b-a}$$

$$= \frac{b-a}{b-a}$$

$$F_{Y}(y) = 1/2 \rightarrow y \text{ is median}$$

$$\frac{b - 1/y}{b - a} = \frac{1}{2} \rightarrow y = \frac{2}{a + b}$$

$$Van(Y) = E(Y^{2}) - (E(Y))^{2}$$

$$E(Y^{2}) = \sqrt{\frac{1}{y^{2}}} \frac{1}{b-a} = \frac{1}{a^{2}} \frac{1}{b-a} = \frac{1}{ab} = \frac{1}{ab}$$

$$Van (Y) = \frac{1}{ab} - \left(\frac{hb - ha}{b - a}\right)^{2}$$

$$= \frac{1}{ab} - \left(\frac{hb - ha}{b - a}\right)^{2}$$

$$= \frac{1}{b} - \frac{hb}{b - a}$$

$$= \frac{1}{$$

For the second inequality, we have
$$G$$

$$P(X \leq \Lambda - x) = P(e^{tX} \leq e^{t(\Lambda - x)})$$

$$= P(e^{t(\Lambda - x - x)} \geq 1)$$

$$= P(e^{t(\Lambda - x - x)}) \text{ by } \text{Markov's}$$

$$= E[e^{t(\Lambda - x)} \in (e^{tx})]$$

$$= e^{t(\Lambda - x)} \in (e^{tx})$$

$$= e^{t(\Lambda - x)} = P(e^{tx})$$

$$= e^{t(\Lambda - x)} = P(e^{tx})$$

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$$\begin{aligned}
& \sum_{i \in S_{1}} \left[\frac{(\chi_{i} - \mu_{i})^{2}}{26^{2}} + \log 6 \right] \\
& + \sum_{i \in S_{2}} \left[\frac{(\chi_{i} - \mu_{i})^{2}}{26^{2}} + \log 6 \right] + \dots + \sum_{i \in S_{K}} \frac{(\chi_{i} - \mu_{K})^{2}}{26^{2}} + \log 8 \right] \\
& \gamma = 6^{2} \\
& \frac{\partial NJLL}{\partial \delta} = \sum_{i \in S_{1}} \frac{(\chi_{i} - \mu_{i})^{2}(-2)}{2 + \dots + \sum_{i \in S_{K}} \frac{(\chi_{i} - \mu_{K})^{2}(-2)}{26^{2}} + \dots + \sum_{i \in S_{K}} \frac{(\chi_{i} - \mu_{K})^{2}(-2)}{26^{2}} \\
& + \frac{(\eta_{1} + \eta_{2} + \dots + \eta_{K})}{6} = 0
\end{aligned}$$

$$\sum_{i \in S_{1}} \frac{(\chi_{i} - \mu_{i})^{2}}{6^{2}} + \dots + \sum_{i \in S_{K}} \frac{(\chi_{i} - \mu_{K})^{2}}{6^{2}} = \frac{\eta_{1}}{1}$$

$$\vdots \quad 6^{2} = \prod_{i \in S_{1}} \frac{\sum_{i \in S_{1}} (\chi_{i} - \mu_{i})^{2} + \dots + \sum_{i \in S_{K}} (\chi_{i} - \mu_{K})^{2}}{1 + \dots + \sum_{i \in S_{K}} (\chi_{i} - \mu_{K})^{2}}$$

$$As \quad \mu_{1}, \dots \mu_{K} \quad \text{ax unknown we have}$$

$$\hat{\delta}^{2} = \prod_{i \in S_{1}} \frac{\sum_{i \in S_{1}} (\chi_{i} - \chi_{i})^{2} + \dots + \sum_{i \in S_{K}} (\chi_{i} - \chi_{k})^{2}}{1 + \dots + \sum_{i \in S_{K}} (\chi_{i} - \chi_{k})^{2}}$$

$$\hat{\delta}^{2} = \prod_{i \in S_{1}} \frac{\sum_{i \in S_{1}} (\chi_{i} - \chi_{i})^{2} + \dots + \sum_{i \in S_{K}} (\chi_{i} - \chi_{k})^{2}}{1 + \dots + \sum_{i \in S_{K}} (\chi_{i} - \chi_{k})^{2}}$$

$$E\left[\frac{\lambda(z)}{\lambda(z)}\right] = E\left[\frac{\lambda(z)}{\lambda(z)} + \frac{\lambda(z)}{\lambda(z)}\right]$$

$$= n_1(p_1^2 + 6^2) + np_1^2 + \frac{6n}{n} - 2np_1$$

$$E\left[\sum_{i \in S_{1}} (x_{i} - \overline{x_{i}})^{2}\right]$$

$$= E\left[\sum_{i \in S_{1}} (x_{i}^{2} + \overline{x_{i}}^{2} - 2x_{i}\overline{x_{i}})\right]$$

$$= n_{1} (p_{1}^{2} + \delta^{2}) + n_{1} E(\overline{x_{i}}^{2}) - 2 \cdot E(\overline{x_{i}} \sum_{i \in S_{i}} x_{i})$$

$$= n_{1} (p_{1}^{2} + \delta^{2}) + n_{1} \left[p_{1}^{2} + \frac{\delta^{2}}{n_{1}}\right] - 2n_{1} E(\overline{x_{i}}^{2})$$

$$= n_{1} (p_{1}^{2} + \delta^{2}) + n_{1} (p_{1}^{2} + \frac{\delta^{2}}{n_{1}})$$

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 $\beta^{2} = \frac{1}{h} \left(\sum_{l=1}^{k-2} \sum_{i \in S_{k}-1} (x_{i} - \mu_{k})^{2} + \sum_{i \in S_{k}-1} (x_{i} - \mu_{k})^{2} + \sum_{i \in S_{k}} (x_{i} - \mu_{k})^{2} \right)$

$$E(\hat{\delta}^2) = \frac{1}{n} \delta^2 \left[n_1 + n_2 + \dots + n_k - 2 \right]$$
This is still a biased estimate. $\Rightarrow 2$

To correct $\textcircled{1}_{N^0}$ we multiply

$$E(\hat{\delta}^2) \text{ with } \underbrace{n}_{n_1 + n_2 + \dots + n_k - k}$$

To correct $\textcircled{2}$ for bias, we multiply

$$E(\hat{\delta}^2) \text{ with } \underbrace{n}_{n_1 + n_2 + \dots + n_k - k}$$

$$E(\hat{\delta}^2) \text{ with } \underbrace{n}_{n_1 + n_2 + \dots + n_k - k}$$

$$= \frac{1}{n} \sum_{n_1 + n_2 + \dots + n_k - k} E(1(X_i \le x))$$

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$$MSE = F(x)(1 - F(x))/n$$

(10)

b) By
$$CI$$

$$P(|F_n(x) - F(x)| \ge k 6) \le \frac{1}{k^2} 6 = std.$$

$$\therefore P(|F_n(x) - F(x)| \ge \epsilon) \le \frac{\delta^2}{\epsilon^2}$$

$$= F(x)(1-F(x))/n\varepsilon^2 \text{ Note } \overline{F(x)} = F(x)$$

CLT
$$P\left(\frac{|F_n(x) - F(x)|}{|F(x)(1 - F(x)/n)} > E\right) \leq \frac{2e}{4\sqrt{2\pi}}$$
by tail bounds for $N(0,1)$

Here we have
$$\frac{-nE^2}{2F(x)(1 - F(x))} = \frac{-nE^2}{2F(x)(1 - F(x))}$$

Here we have
$$P(|F_n(x) - F(x)| \ge \epsilon) \le \frac{-n\epsilon^2}{2F(x)(1-F(x))} F(x)(1-F(x))$$

$$P(|F_n(x) - F(x)| \ge \epsilon) \le \frac{2e}{\sqrt{n}} \sqrt{2\pi}$$
(\epsilon is being replaced by \(\epsilon/6\))

e) We have
$$P\left(\max_{x} |F_{n}(x) - F(x)| \ge \varepsilon\right) \le 2e^{2n\varepsilon^{2}} \text{ by } DKW$$

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$$P(X > z) = \int_{0}^{\infty} \frac{1}{6\sqrt{2\pi}} e^{-\frac{t^{2}}{26^{2}}} e^{-\frac{t^{2}}{26^{2}}} dt$$

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