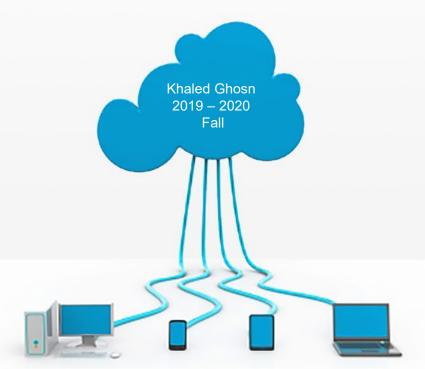


Types of Linked Lists

Singly, Doubly, and Circular Linked Lists



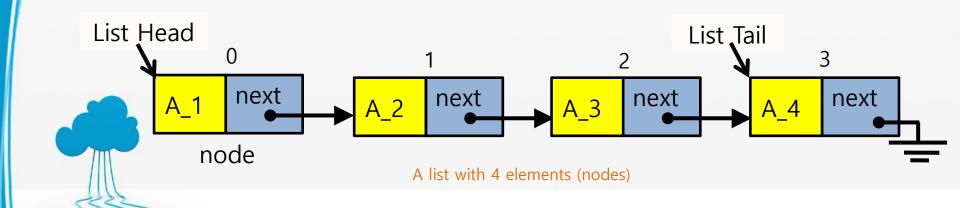
Definition

- A linked list is a <u>dynamic</u> data structure where each element is a separate element
 - Dynamically allocate space for each element as needed
 - ✓ Flexible space use
 - Each element of a list is called a Node
 - Nodes are NOT contiguous but are scattered in the memory
- Linked list consists of one or more nodes
 - The number of nodes in a list is not fixed and can grow and shrink
 - Any application which has to deal with an unknown number of objects will need to use a linked list
- Linked Lists addresses some of the limitations of arrays



Nodes

- Each node contains some data
- A Node class must store reference/s to other nodes (pointer/s to another nodes)



Head & Tail Nodes

- Need to know the location of the first node
 - the entry point into a linked list
- The first node is called the **Head** (**Front / First-Node**) of the list
 - The head is not a separate node, just the reference to the first node
 - If you want to access a particular item then you have to start at the head and follow the references until you get to that item
 - If the list is empty then the head is a null reference
 - Initially NULL
- The last node is known as Tail (Back / Last-Node) of the list
 - has a reference to <u>NULL</u>



Disadvantages

- One disadvantage of a linked list against an array is that it does not allow direct access to the individual elements.
- Another disadvantage is that a linked list uses more memory compare with an array



Types

- 1. Singly Linked List
- 2. Doubly Linked List

is a list that has two references:

- a) next node
- b) previous node
- 3. Singly Circular Linked List

where last node of the list points back to the first node (head)

4. Doubly Circular Linked List

where last node of the list points back to the first node (head), and the first node of the list points to the last node (tail)



Array-List vs. Linked List

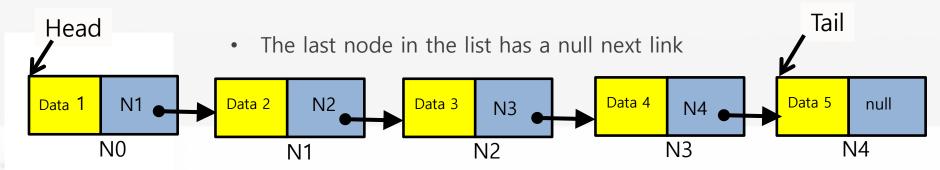
Types

- Accessing elements are faster with Array-List (because it is index based)
- Accessing is difficult with Linked List. It is slow access. This is to access any element, you need to navigate through the elements one by one
- Insertion and deletion is much faster with Linked List, because if you know the node, just change the pointers before or after nodes
- Insertion and deletion is slow with Array-List, this is because, during these operations Array-List need to adjust the indexes according to deletion or insertion if you are performing on middle indexes.

 Means, an Array-List having 10 elements, if you are inserting at index 5, then you need to shift the indexes above 5 to one more



- The basic linked list consists of a collection of connected dynamically allocated nodes
- In a singly linked list, each node consists of:
 - 1. Data element (value)
 - 2. One Link (reference) to the next node in the list



SLL-Node operations

SLL Node

Data

Next



SLLNode

- Anytype Data
- SLLNode Next
- + SLLNode ()
- + **SLLNode** (*Anytype* Data)
- + **SLLNode** (*Anytype* Data, *SLLNode* next)
- + Anytype getData ()
- + void setData (Anytype Data)
- + SLLNode getNext ()
- + *void* **setNext** (*SLLNode* next)

Singly Linked List SLL operations Head Size = 3

- SLLNode Head
- SLLNode Tail
- int Size
- + **SLL** ()
- + **SLL** (*Anytype* value)
- + **SLL** (*SLLNode* FirstNode)
- + boolean isEmpty ()
- + void makeEmpty ()
- + int Length ()
- + SLLNode getHead ()
- + SLLNode getTail ()
- + *void* **addFirst** (*Anytype* value)
- + *void* addLast (*Anytype* value)
- + *Anytype* removeFirst ()
- + Anytype removeLast ()
- + void Print ()

isEmpty ()

✓ Check if Head is null

Head → null

public boolean isEmpty()
{

return this.Head == null;

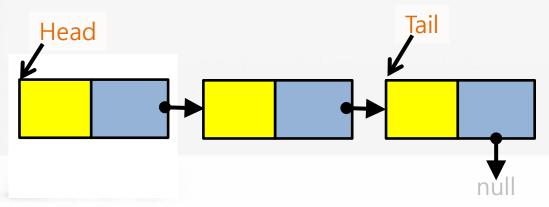
- SLLNode Head
- SLLNOGC 13
- + **SLL** ()
- + **SLL** (*Anytype* value)
- + **SLL** (*SLLNode* FirstNode)
- + boolean isEmpty ()
- + void makeEmpty ()
- + int Length ()
- + SLLNode getHead ()
- + SLLNode getTail ()
- + *void* addFirst (*Anytype* value) + *void* addLast (*Anytype* value)
- + Anytype removeFirst ()
- + Anytype removeLast ()
- + void Print ()

Singly Linked List makeEmpty () ✓ Let Head be null Head null Size = 0public void makeEmpty() this.Head = null;

- SLLNode Head
- SLLNode Tai
- int Size
- + **SLL** ()
- + **SLL** (*Anytype* value)
- + **SLL** (*SLLNode* FirstNode)
- + boolean isEmpty ()
- + void makeEmpty ()
- + int Length ()
- + SLLNode getHead ()
- + SLLNode getTail ()
- + *void* addFirst (*Anytype* value)
- + *void* addLast (*Anytype* value)
- + *Anytype* removeFirst ()
- + Anytype removeLast ()
- + void Print ()

Length ()

- ✓ Count Nodes
 - 1. Start from Head (check if null to stop)
 - 2. Count and move to next node
 - 3. Stop when reaching the tail (its "next node" is null)



- SLLNode Head
- SLLNode Tail
- int Siz
- + **SLL** ()
- + **SLL** (*Anytype* value)
- + **SLL** (*SLLNode* FirstNode)
- + boolean isEmpty ()
- + *void* makeEmpty ()
- + int Length ()
- + SLLNode getHead ()
- + SLLNode getTail ()
- + void addFirst (Anytype value)
- + *void* addLast (*Anytype* value)
- + *Anytype* removeFirst ()
- + Anytype removeLast ()
- + void Print ()

```
Length () - Iterative
public int Length()
  if (isEmpty())
     return 0;
  SLLNode currentNode = this.Head;
  int counter=1;
  while(currentNode.getNext()!=null)
     currentNode=currentNode.getNext();
     counter++;
  return counter;
```



```
Length () - Recursive
```

```
public int Length(SLLNode start)
{
    if (start == null)
        return 0;
    else
        return 1 + Length(start.getNext());
}
```

- - Move to next node

Head

Stop when reaching the node having a NULL next node (its "next node" is null)

getTail () ✓ Find Last Node -Tail-**Start from Head (if List is not empty)**

- SLLNode Head

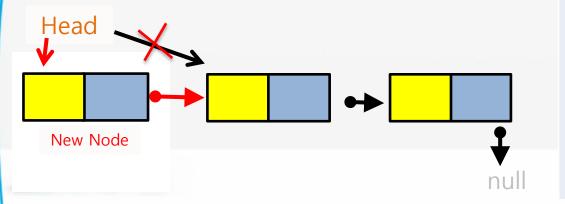
- + **SLL**()
- + **SLL** (*Anytype* value)
- + **SLL** (*SLLNode* FirstNode)
- + boolean isEmpty ()
- + void makeEmpty ()
- + int Length ()
- + SLLNode getHead ()
- + SLLNode getTail ()
- + *void* addFirst (*Anytype* value)
- + *void* addLast (*Anytype* value)
- + Anytype removeFirst ()
- + Anytype removeLast ()
- + void Print ()

```
getTail ( ) - Iterative
public SLLNode getTail()
  if (this.isEmpty())
     return null;
  SLLNode currentNode = this.Head;
  while (currentNode.getNext() != null)
     currentNode = currentNode.getNext();
  return currentNode;
```

```
getTail ( ) - Recursive
public SLLNode getTail(SLLNode start)
    if (start == null)
        return null;
    if (start.getNext() == null)
        return start;
    else
        return getTail(start.getNext());
```

addFirst (value)

- 1. Create a new node
- 2. Let the "next node" of the new node be the "Head" node (unless if the list is empty)
- 3. Let "Head" refer to the new node



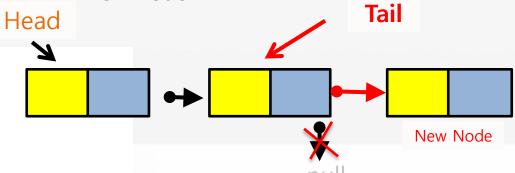
- SLLNode Head
- SLLNode Tail
- int Size
- + **SLL**()
- + **SLL** (*Anytype* value)
- + **SLL** (*SLLNode* FirstNode)
- + boolean isEmpty ()
- + *void* makeEmpty ()
- + int Length ()
- + SLLNode getHead ()
- + SLLNode getTail ()
- + *void* addFirst (*Anytype* value)
- + *void* addLast (*Anytype* value)
- + *Anytype* removeFirst ()
- + Anytype removeLast ()
- + void Print ()

addFirst (value)

```
public void addFirst(Anytype value)
{
    //if ( isEmpty() )
    // this.Head = new SLLNode(value);
    // else
        this.Head = new SLLNode (value, this.Head);
}
```

addLast (value)

- 1. Check if the List is not empty (if empty, just set the Head to be the new node)
- 2. Create a new node
- 3. Find the last node (getTail())
- 4. Set the Tail's "next node" to refer to the new node



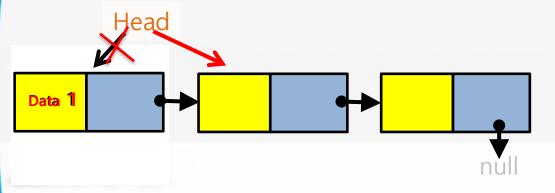
- SLLNode Head
- SLLNode Tail
- int Size
- + **SLL** ()
- + **SLL** (*Anytype* value)
- + **SLL** (*SLLNode* FirstNode)
- + boolean isEmpty ()
- + void makeEmpty ()
- + int Length ()
- + SLLNode getHead ()
- + SLLNode getTail ()
- + *void* addFirst (*Anytype* value)
- + *void* addLast (*Anytype* value)
- + *Anytype* removeFirst ()
- + *Anytype* removeLast ()
- + void Print ()

```
addLast (value)
public void addLast (value)
    if (this.isEmpty())
      this.addFirst(value);
    else
      SLLNode newNode = new SLLNode (value);
      SLLNode currentNode = this.getTail();
       currentNode.setNext(newNode);
```



removeFirst ()

- 1. Check if the List is not empty (if empty, stop here)
- 2. Get the data stored in the Head
- 3. Let the Head refers to the "next node" of the Head node
- 4. Return the stored data



- SLLNode Head
- SLLNode Tai
- int Size
- + **SLL** ()
- + **SLL** (*Anytype* value)
- + **SLL** (*SLLNode* FirstNode)
- + boolean isEmpty ()
- + void makeEmpty ()
- + int Length ()
- + SLLNode getHead ()
- + SLLNode getTail ()
- + *void* addFirst (*Anytype* value)
- + *void* addLast (*Anytype* value)
- + Anytype removeFirst ()
- + Anytype removeLast ()
- + void Print ()

```
removeFirst ( )
public Anytype removeFirst()
    if (this.isEmpty())
        return null;
    Anytype removedValue = this.Head.getData();
    this.Head = this.Head.getNext();
    return removedValue;
```



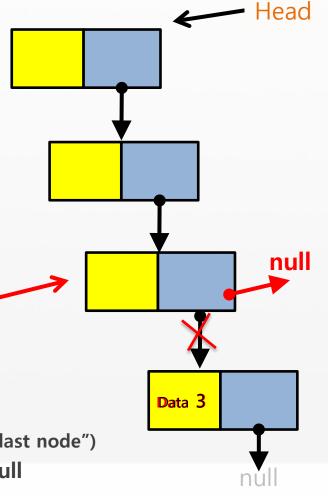
removeLast ()

- SLLNode Head
- SLLNode Tail
- int Siz
- + **SLL** ()
- + **SLL** (*Anytype* value)
- + **SLL** (*SLLNode* FirstNode)
- + boolean isEmpty () + void makeEmpty ()
- + int Length ()
- + SLLNode getHead ()
- + SLLNode getTail ()
- + *void* addFirst (*Anytype* value)
- + *void* addLast (*Anytype* value)
- + Anytype removeFirst ()
- + Anytype removeLast ()
- + void Print ()



removeLast ()

- 1. Check if the List is not empty (if empty, stop here)
- 2. Check if the List has only one node, if so:
 - a) Get the data stored in the Head
 - b) Let the Head refers to null
 - c) Return the stored data (& stop here)
- 3. If more than a node exits:
 - a) Find the "before last node": the node having its "next node" is the Tail itself (i.e. the node having its "next node" has a null "next node")
 - b) Get the data stored in the Tail (next of "before last node")
 - c) Set the "before last node" next node to be null
 - d) Return the stored data



```
removeLast ()
public Anytype removeLast() {
   if (this.isEmpty())
                                             // Size = 0
      return null;
   Anytype removedValue;
                                             // Size = 1
   if (Head.getNext() == null) {
      removedValue = Head.getData();
      Head = null; }
                                             // Size > 1
   else {
      SLLNode<Anytype> currentNode=this.Head;
      while (currentNode.getNext().getNext() != null)
              currentNode = currentNode.getNext();
      removedValue = currentNode.getNext().getData();
```

currentNode.setNext(null); }

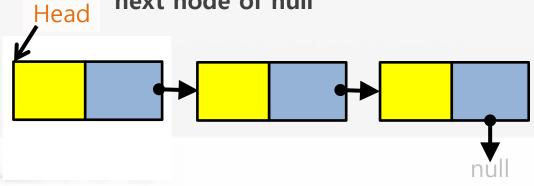
return removedValue; }



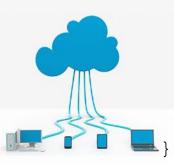
Print ()

- 1. Check if List is not empty (if empty, stop here)
- 2. Starting from Head node:
- 3. Print the Data stored in the node
- 4. Go to next node
- 5. Repeat step 3 & 4 until you reach a next node of null

- SLLNode Head
- SLLNode Tai
- int Size
- + **SLL** ()
- + **SLL** (*Anytype* value)
- + **SLL** (*SLLNode* FirstNode)
- + boolean isEmpty ()
- + void makeEmpty ()
- + int Length ()
- + SLLNode getHead ()
- + SLLNode getTail ()
- + *void* addFirst (*Anytype* value)
- + *void* addLast (*Anytype* value)
- + Anytype removeFirst ()
- + Anytype removeLast ()
- + void Print ()



```
Print ()
public void Print() {
  if (this.isEmpty())
     System.out.println("The list is empty.");
  else
     SLLNode currentNode = this.Head;
     while (currentNode != null)
        System.out.print(currentNode.getData() + " --> ");
        currentNode = currentNode.getNext();
     System.out.println("");
```



Exercise 1

- a) Write the appropriate implementations for all of the class operations marked in <u>red</u> taking into consideration that the class has only 2 attributes:
 - SLLNode **Head**;
 - SLLNode Tail;
- b) What is the complexity (in the form of Big-*Oh* notation) for each operation



SLLNode Head

- SLLNode **Tail**
- + **SLL**()
- + **SLL** (*Anytype* value)
- + **SLL** (*SLLNode* FirstNode)
- + boolean isEmpty ()
- + void makeEmpty ()
- + int Length ()
- + SLLNode getHead ()
- + SLLNode getTail ()
- + *void* addFirst (*Anytype* value)
- + *void* addLast (*Anytype* value)
- + *Anytype* removeFirst ()
- + Anytype removeLast ()
- + void Print ()



Exercise 2

- a) Write the appropriate implementations for all of the class operations marked in <u>red</u> taking into consideration that the class has only 2 attributes:
 - SLLNode **Head**;
 - int Size;

b) What is the complexity (in the form of Big-*Oh* notation) for each operation



- SLLNode Head
- *int* Size
- + **SLL** ()
- + **SLL** (*Anytype* value)
- + **SLL** (*SLLNode* FirstNode)
- + boolean isEmpty ()
- + void makeEmpty ()
- + int Length ()
- + SLLNode getHead ()
- + SLLNode getTail ()
- + *void* addFirst (*Anytype* value)
- + *void* addLast (*Anytype* value)
- + Anytype removeFirst ()
- + Anytype removeLast ()
- + void Print ()



DLL

Head

null

- The basic linked list consists of a collection of connected dynamically allocated nodes
- In a *doubly linked list*, each node consists of:
 - 1. Data element (value)
 - 2. One Link (reference) to the next node in the list

Tail

- 3. Another link to the previous node in the list
- The last node in the list has a null next link



DLL-Node operations

DLL Node

Prev Data

Next



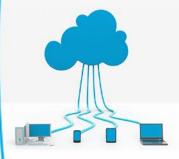
DLLNode

- Anytype Data
- DLLNode Prev
- DLLNode Next
- + DLLNode ()
- + **DLLNode** (*Anytype* Data)
- + Anytype getData ()
- + *void* **setData** (*Anytype* Data)
- + DLLNode getPrev ()
- + *void* **setPrev** (*DLLNode* prevNode)
- + DLLNode getNext ()
- + *void* **setNext** (*DLLNode* nextNode)

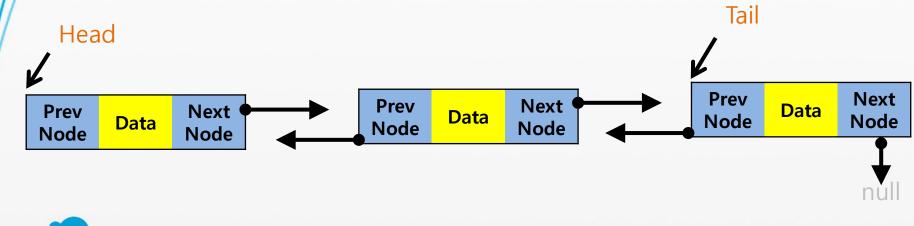
DLL operations

DLL

- DLLNode Head
- DLLNode Tail int Size
- + **DLL**()
- + **DLL** (*Anytype* value)
- + **DLL** (*DLLNode* FirstNode)
- + boolean isEmpty ()
- + void makeEmpty () + int Length ()
- + DLLNode getHead ()
- + DLLNode getTail ()
- + *void* addFirst (*Anytype* value)
- + *void* addLast (*Anytype* value)
- + Anytype removeFirst ()
- + Anytype removeLast ()
- + void Print ()



DLL operations





Size = 3

✓ Check if Head is null.

Same as SLL

isEmpty ()

DLL

- DLLNode Head
- *DLLNode* **Tail**
- + **DLL**()
- + **DLL** (*Anytype* value)
- + **DLL** (*SLLNode* FirstNode)
- + boolean isEmpty ()
- + void makeEmpty ()
- + int Length ()
- + DLLNode getHead ()
- + DLLNode getTail ()
- + void addFirst (Anytype value)
- + *void* addLast (*Anytype* value)
- + Anytype removeFirst ()
- + Anytype removeLast ()
- + void Print ()

makeEmpty ()

✓ Let Head be null

Same as SLL

- DLLNode **Head**
- -DLLNode Tail
- *int* Size
- + **DLL** ()
- + **DLL** (*Anytype* value) + **DLL** (*SLLNode* FirstNode)
- + boolean isEmpty ()
- + void makeEmpty ()
- + int Length ()
- + DLLNode getHead ()
- + DLLNode getTail ()
- + *void* addFirst (*Anytype* value)
- + *void* addLast (*Anytype* value)
- + Anytype removeFirst ()
- + *Anytype* removeLast ()
- + void Print ()



Length ()

✓ Count Nodes

Same as SLL



- DLLNode **Head**
- -DLLNode Tail
- . DII ()
- + **DLL** ()
- + **DLL** (*Anytype* value) + **DLL** (*SLLNode* FirstNode)
- + boolean isEmpty ()
- + void makeEmpty ()
- + int Length ()
- + DLLNode getHead ()
- + DLLNode getTail ()
- + void addFirst (Anytype value)
- + *void* addLast (*Anytype* value)
- + Anytype removeFirst ()
- + Anytype removeLast ()
- null + *void* **Print** ()

getTail ()

✓ Find Last Node -Tail-

Same as SLL

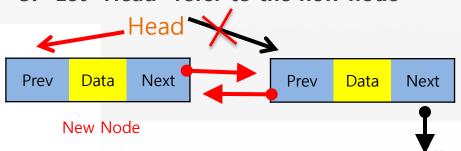


- DLLNode **Head**
- -DLLNode Tail
- int Size
- + **DLL**()
- + **DLL** (*Anytype* value)
- + **DLL** (*SLLNode* FirstNode)
- + boolean isEmpty ()
- + void makeEmpty ()
- + int Length ()
- + DLLNode getHead ()
- + DLLNode getTail ()
- + *void* addFirst (*Anytype* value)
- + *void* addLast (*Anytype* value)
- + Anytype removeFirst ()
- + Anytype removeLast ()
- + void Print ()



addFirst (value)

- 1. Create a new node
- 2. Check if the List is not empty (if empty, just set the Head to be the new node)
- 3. Let the "next node" of the new node be the "Head" node
- 4. Let the "prev node" of the Head be the new node
- 5. Let "Head" refer to the new node



- DLLNode **Head**
- DLLNode Tail
- int Size
- + **DLL**()
- + **DLL** (*Anytype* value)
- + **DLL** (*SLLNode* FirstNode)
- + boolean isEmpty ()
- + void makeEmpty ()
- + int Length ()
- + DLLNode getHead ()
- + DLLNode getTail ()
- + *void* addFirst (*Anytype* value)
- + *void* addLast (*Anytype* value)
- + *Anytype* removeFirst ()
- + Anytype removeLast ()
- + void Print ()

```
addFirst (value)
```

addLast (value)

1. Create a new node

Head

- 2. Check if the List is not empty (if empty, just set the Head to be the new node)
- 3. Find the last node (getTail)
- 4. Let the "next node" of the last node be the new node
- 5. Let the "prev node" of the new node be the last node

Prev Data Next Prev Data Next New Node

- DLLNode **Head**
- DLLNode Tail
- *int* Size
- + **DLL**()
- + **DLL** (*Anytype* value)
- + **DLL** (*SLLNode* FirstNode)
- + boolean isEmpty ()
- + void makeEmpty ()
- + int Length ()
- + DLLNode getHead ()
- + DLLNode getTail ()
- + *void* addFirst (*Anytype* value)
- + *void* **addLast** (*Anytype* value)
- + *Anytype* removeFirst ()
- + Anytype removeLast ()
- + void Print ()

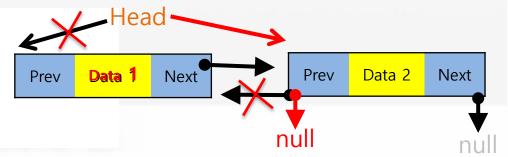
```
addLast (value)
```

```
public void addLast(Anytype value)
   if (this.isEmpty())
     this.addFirst(value);
   else
   DLLNode<Anytype> newNode = new DLLNode<Anytype>(value);
      DLLNode<Anytype> Tail = this.getTail();
      Tail.setNext(newNode);
      newNode.setPrev(Tail);
```



removeFirst ()

- 1. Check if the List is not empty (if empty, stop here)
- 2. Get the data stored in the Head
- 3. Let the Head refers to the "next node" of the Head node
- 4. Set the previous node of the <u>new</u> Head to be null
- 5. Return the stored data



- DLLNode **Head**
- *DLLNode* Tail
- *int* Size
- + **DLL** ()
- + **DLL** (*Anytype* value)
- + **DLL** (*SLLNode* FirstNode)
- + boolean isEmpty ()
- + void makeEmpty ()
- + int Length ()
- + DLLNode getHead ()
- + DLLNode getTail ()
- + void addFirst (Anytype value)
- + *void* addLast (*Anytype* value)
- + Anytype removeFirst ()
- + Anytype removeLast ()
- + void Print ()

```
removeFirst ()
public Anytype removeFirst()
   if (this.isEmpty())
       return null;
   Anytype removedValue = this.Head.getData();
   if (Head.getNext() == null)
     Head = null;
else {
      this.Head = this.Head.getNext();
      this.Head.setPrev(null);
   return removedValue;
```

removeLast ()

- DLLNode Head
- -DLLNode Tail
- int Size
- + **DLL** ()
- + **DLL** (*Anytype* value)
- + **DLL** (*SLLNode* FirstNode)
- + boolean isEmpty ()
- + void makeEmpty ()
- + int Length ()
- + DLLNode getHead ()
- + DLLNode getTail ()
- + *void* addFirst (*Anytype* value)
- + *void* addLast (*Anytype* value)
- + Anytype removeFirst ()
- + Anytype removeLast ()
- + void Print ()



removeLast ()

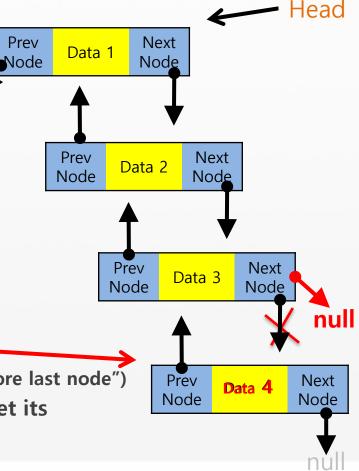
- 1. Check if the List is not empty (if empty, stop here)
- 2. Check if the List has only one node, if so:
 - a) Get the data stored in the Head
 - b) Let the Head refers to null
 - c) Return the stored data (& stop here)
- 3. If more than a node exits:
 - a) Get the "last node" (Tail)
 - b) Get the data stored in the Tail (next of "before last node")

null

c) Catch the previous node of the tail, then set its

"Next Node" to be null

d) Return the stored data



```
removeLast ()
public Anytype removeLast() {
   if (this.isEmpty())
                                             // Size = 0
      return null;
   Anytype removedValue;
                                             // Size = 1
   if (Head.getNext() == null) {
      removedValue = Head.getData();
      Head = null; }
                                             // Size > 1
   else {
      DLLNode<Anytype> currentNode=getTail();
      removedValue = currentNode.getData();
      currentNode.getPrev().setNext(null);
```



Print ()

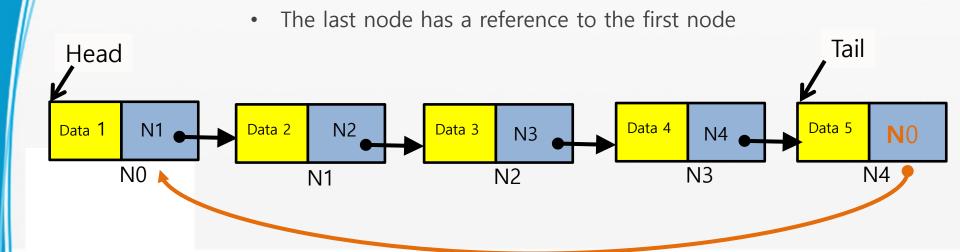
Same as SLL

- DLLNode **Head**
- -DLLNode Tail
- + **DLL** ()
- + **DLL** (*Anytype* value)
- + **DLL** (*SLLNode* FirstNode)
- + boolean isEmpty ()
- + *void* makeEmpty () + *int* Length ()
- + DLLNode getHead ()
- + DLLNode getTail ()
- + *void* addFirst (*Anytype* value)
- + *void* addLast (*Anytype* value)
- + Anytype removeFirst ()
- + Anytype removeLast ()
- + void Print ()



Singly Circular Linked List

• It's a Singly Linked List



Doubly Circular Linked List

- It's a Doubly Linked List
- The last node has a reference to the first node
- The first node has a reference to the last node

