

Notes: ‘n’ represents the dimension of the corresponding problem. ‘NI’ represents the total number of iterations. ‘NF’ represents the number of the function evaluation. ‘T’ represents the running time of the algorithm. ‘ $\|g^*\|$ ’ represents the gradient value for the solution. The values of ‘NI’, ‘NF’, ‘T’ and ‘ $\|g^*\|$ ’ are set as ‘NaN’ if and only if the number of iterations is greater than 3000.

| Table 1: Numerical results for Test 2 | | | | |
|---------------------------------------|---------------------------|---------------------------|---------------------------|---------------------------|
| Problem/n | SHCGMcC-MED | PRP | HS | LS |
| | NI/NF/T/ $\ g^*\ $ | NI/NF/T/ $\ g^*\ $ | NI/NF/T/ $\ g^*\ $ | NI/NF/T/ $\ g^*\ $ |
| cosine/600 | 43/100/0.028/5.46e-06 | 34/210/0.011/1.80e-06 | 73/298/0.013/7.31e-06 | 1269/5457/0.199/8.33e-06 |
| cosine/3000 | 65/132/0.021/9.48e-06 | 31/170/0.022/7.86e-06 | 66/214/0.029/9.86e-06 | 284/1406/0.180/3.30e-06 |
| cosine/10000 | 40/101/0.043/8.50e-06 | 41/236/0.089/7.37e-06 | NaN/NaN/NaN/NaN | NaN/NaN/NaN/NaN |
| dixmaana/6000 | 13/70/0.199/5.33e-06 | 34/214/0.634/3.98e-06 | 28/172/0.654/1.76e-06 | 31/178/0.549/5.57e-06 |
| dixmaana/9000 | 12/68/0.348/2.53e-06 | 28/151/0.682/4.91e-06 | 35/242/1.147/1.90e-06 | 29/156/0.803/7.07e-06 |
| dixmaanb/4800 | 15/75/0.238/5.60e-06 | 24/172/0.469/1.93e-06 | 28/162/0.257/8.34e-06 | 29/172/0.273/2.86e-06 |
| dixmaanb/24000 | 16/77/1.179/4.32e-06 | 36/220/3.079/7.74e-06 | 28/168/2.210/3.25e-06 | 51/330/4.175/4.84e-06 |
| dixmaanc/270 | 19/72/0.069/2.85e-06 | 38/233/0.048/3.19e-06 | 30/185/0.045/5.27e-06 | 44/299/0.051/5.04e-06 |
| dixmaanc/2700 | 48/111/0.112/7.66e-06 | 27/150/0.180/8.70e-06 | 24/129/0.112/9.41e-06 | 65/446/0.443/5.72e-06 |
| dixmaand/1200 | 17/73/0.069/2.75e-06 | 30/159/0.070/6.63e-06 | 28/112/0.048/8.83e-06 | 38/238/0.121/5.81e-06 |
| dixmaand/9000 | 17/76/0.246/5.80e-06 | 28/148/0.795/9.66e-06 | 29/148/0.700/4.52e-06 | 49/329/1.451/7.03e-06 |
| dixmaane/2400 | 420/478/0.501/8.23e-06 | 384/1383/1.257/9.68e-06 | 314/509/0.560/9.18e-06 | 366/1413/1.453/9.11e-06 |
| dixmaane/4800 | 478/550/0.840/9.45e-06 | 520/1876/2.761/7.62e-06 | 482/729/1.029/8.96e-06 | 651/2353/4.161/6.46e-06 |
| dixmaanf/6000 | 577/638/2.095/8.89e-06 | 582/2067/4.629/9.83e-06 | 344/581/1.217/7.78e-06 | 643/2274/4.997/7.28e-06 |
| dixmaanf/15000 | 1652/1885/15.316/8.60e-06 | 878/3146/26.141/8.00e-06 | 619/1011/8.856/6.21e-06 | 711/2435/21.005/7.87e-06 |
| dixmaang/6000 | 733/817/3.101/8.09e-06 | 490/1751/6.252/8.06e-06 | 293/483/1.631/8.90e-06 | 371/1394/5.341/9.77e-06 |
| dixmaang/12000 | 1380/1660/12.700/9.68e-06 | 526/2081/15.890/9.37e-06 | 560/894/6.799/5.08e-06 | 793/2745/20.309/9.51e-06 |
| dixmaanb/6000 | 1211/1518/5.802/8.12e-06 | 636/2485/9.202/7.24e-06 | 361/605/2.243/7.91e-06 | 567/1990/5.530/9.12e-06 |
| dixmaanb/15000 | 941/1014/9.153/9.84e-06 | 1111/4013/33.297/9.56e-06 | 527/837/6.907/6.06e-06 | 968/3620/28.352/7.48e-06 |
| dixmaani/360 | 1464/1520/0.412/8.69e-06 | 1436/5250/1.162/8.55e-06 | 1683/2659/0.825/7.91e-06 | 2786/9725/2.395/8.16e-06 |
| dixmaanj/3000 | 992/1104/1.162/8.57e-06 | 532/1971/2.152/5.50e-06 | 352/602/0.598/9.51e-06 | 523/1852/1.876/8.62e-06 |
| dixmaanj/15000 | 281/356/2.918/9.82e-06 | 749/2755/22.654/8.69e-06 | 465/750/6.140/9.30e-06 | 635/2242/19.455/9.45e-06 |
| dixmaank/6000 | 678/852/3.439/7.97e-06 | 369/1544/5.533/9.61e-06 | 354/570/1.186/9.84e-06 | 556/1904/7.437/9.56e-06 |
| dixmaank/12000 | 307/384/3.038/8.89e-06 | 461/1776/12.864/9.58e-06 | 416/684/5.199/7.54e-06 | 622/2152/14.803/8.99e-06 |
| dixmaanl/1200 | 2403/2504/1.165/9.99e-06 | 326/1327/0.526/9.48e-06 | 232/393/0.155/8.56e-06 | 1052/3890/1.666/9.54e-06 |
| dixmaanl/2400 | NaN/NaN/NaN/NaN | 456/1792/1.736/8.43e-06 | 286/470/0.362/8.51e-06 | 406/1643/1.259/8.33e-06 |
| dixon3dq/50 | 433/486/0.025/9.67e-06 | 572/2266/0.071/9.67e-06 | 399/620/0.021/9.83e-06 | 605/2128/0.069/8.57e-06 |
| dixon3dq/150 | 1194/1243/0.053/9.95e-06 | 2340/8491/0.366/8.73e-06 | 1441/2244/0.127/7.85e-06 | 2409/8417/0.444/8.31e-06 |
| dqdrtic/300 | 71/232/0.023/5.33e-06 | 151/743/0.045/3.11e-06 | 67/239/0.017/4.39e-06 | 104/496/0.024/4.56e-06 |
| dqdrtic/5000 | 44/148/0.215/2.99e-06 | 47/184/0.277/5.78e-06 | 56/197/0.272/6.46e-06 | 58/258/0.343/3.56e-06 |
| dqdrtic/9000 | 113/310/0.042/6.81e-06 | 95/505/0.057/2.42e-06 | 73/272/0.031/1.08e-06 | 127/673/0.070/7.74e-06 |
| edensch/500 | 43/101/0.026/6.31e-06 | 51/303/0.068/9.15e-06 | 43/156/0.043/7.43e-06 | 58/292/0.049/5.93e-06 |
| edensch/1000 | 46/113/0.067/9.91e-06 | 42/192/0.079/7.17e-06 | 46/156/0.069/9.40e-06 | 56/383/0.164/9.78e-06 |
| edensch/4000 | 76/177/0.316/7.86e-06 | 43/208/0.389/9.77e-06 | 207/1495/2.564/6.08e-06 | 39/168/0.302/7.97e-06 |
| eg2/100 | 156/458/0.049/2.57e-06 | 467/2311/0.079/9.80e-06 | 58/259/0.010/8.11e-06 | 166/1305/0.053/2.20e-06 |
| fletcher/100 | 47/117/0.026/9.38e-06 | 44/167/0.012/5.03e-06 | 40/115/0.008/8.69e-06 | 60/234/0.014/8.38e-06 |
| fletcher/500 | 92/376/0.027/5.08e-06 | 85/509/0.023/1.61e-06 | 46/147/0.005/5.93e-06 | 66/427/0.026/3.11e-06 |
| fletcher/2000 | 82/354/0.020/5.66e-06 | 81/641/0.048/5.93e-06 | 280/2021/0.214/7.06e-06 | 165/1428/0.124/8.43e-06 |
| freuroth/460 | 563/5098/0.262/9.92e-06 | 548/5041/0.324/1.95e-06 | NaN/NaN/NaN/NaN | 1670/17020/1.123/9.36e-06 |
| genrose/100 | 688/805/0.043/7.52e-06 | 1621/6073/0.250/6.95e-06 | 897/1487/0.063/4.96e-06 | 1354/5000/0.243/8.50e-06 |
| himmelbg/700 | 2/15/0.019/1.35e-29 | 2/15/0.002/1.68e-27 | 2/15/0.004/1.90e-27 | 2/15/0.004/1.68e-27 |
| himmelbg/2400 | 2/10/0.003/5.14e-20 | 2/10/0.003/3.91e-19 | 2/10/0.003/1.49e-18 | 2/10/0.004/3.91e-19 |
| liarwhd/6000 | 139/443/0.085/7.72e-06 | 121/701/0.063/7.69e-06 | 32/168/0.015/4.73e-06 | 82/572/0.046/6.15e-06 |
| liarwhd/3000 | 175/478/0.063/5.74e-06 | 106/637/0.055/1.35e-06 | 41/214/0.015/9.81e-06 | 77/574/0.068/1.81e-06 |
| penalty1/100 | 17/101/0.025/1.61e-06 | 13/83/0.005/7.77e-06 | NaN/NaN/NaN/NaN | 385/4209/0.314/1.00e-05 |
| penalty1/1000 | 29/199/0.199/3.29e-06 | 293/2088/1.986/7.18e-06 | NaN/NaN/NaN/NaN | 859/9417/9.115/9.90e-06 |
| quartc/4000 | 56/168/0.282/9.95e-06 | 58/263/0.456/6.27e-06 | 49/177/0.258/7.04e-06 | 68/299/0.487/9.49e-06 |
| quartc/8000 | 72/195/0.690/4.80e-06 | 63/259/0.815/6.66e-06 | 77/214/0.874/6.61e-07 | 67/260/1.089/4.00e-06 |
| quartc/50000 | 117/251/6.739/4.41e-06 | 97/408/10.214/5.31e-06 | 105/292/7.392/6.18e-06 | 102/397/9.692/8.18e-06 |
| tridia/300 | 604/671/0.051/8.70e-06 | 941/3522/0.164/8.19e-06 | 483/758/0.055/9.09e-06 | 882/3006/0.100/9.40e-06 |
| tridia/2000 | 1644/1720/0.164/8.81e-06 | 2538/9097/0.508/9.69e-06 | 2044/3166/0.237/8.47e-06 | 2748/9576/0.677/7.10e-06 |
| woods/1500 | 95/273/0.051/5.75e-06 | 447/2112/0.167/9.19e-06 | 174/518/0.027/5.09e-06 | 188/898/0.047/9.50e-06 |
| woods/2000 | 215/388/0.039/7.95e-06 | 517/2223/0.131/4.80e-06 | 177/510/0.036/7.84e-06 | 222/1042/0.065/9.12e-06 |
| bdexp/5000 | 2/11/0.033/4.40e-111 | 2/11/0.009/2.19e-79 | NaN/NaN/NaN/NaN | 2/11/0.017/2.19e-79 |
| bdexp/50000 | 2/16/0.153/3.49e-89 | 2/16/0.174/6.83e-37 | NaN/NaN/NaN/NaN | 2/16/0.076/6.83e-37 |
| bdexp/5000 | 2/11/0.006/4.40e-111 | 2/11/0.006/2.19e-79 | NaN/NaN/NaN/NaN | 2/11/0.008/2.19e-79 |
| exdenschnf/9000 | 46/117/0.046/7.00e-06 | 32/173/0.024/9.82e-06 | 32/179/0.025/9.00e-06 | 67/478/0.064/9.60e-06 |
| exdenschnf/2800 | 40/109/0.008/4.37e-06 | 39/212/0.013/3.33e-06 | 42/265/0.017/9.91e-06 | 69/563/0.043/7.23e-06 |
| exdenschnf/6000 | 36/103/0.021/6.08e-06 | 36/225/0.024/5.43e-06 | 31/139/0.014/7.86e-06 | 39/224/0.024/7.17e-06 |
| exdenschnb/3000 | 39/97/0.015/4.70e-06 | 38/199/0.013/8.90e-06 | 30/177/0.012/1.18e-06 | 34/247/0.019/9.53e-06 |
| exdenschnb/6000 | 17/75/0.009/5.65e-06 | 25/155/0.013/5.21e-06 | 26/146/0.012/9.55e-06 | 48/285/0.020/6.42e-06 |
| exdenschnb/24000 | 18/79/0.020/9.65e-06 | 26/162/0.034/4.79e-07 | 28/151/0.031/7.90e-06 | 47/296/0.060/9.92e-06 |
| genquartic/9000 | 28/88/0.027/4.99e-06 | 48/320/0.041/4.77e-06 | 88/445/0.058/9.63e-06 | 40/219/0.029/4.75e-06 |
| genquartic/9000 | 28/88/0.014/4.99e-06 | 48/320/0.039/4.77e-06 | 88/445/0.051/9.63e-06 | 40/219/0.025/4.75e-06 |
| genquartic/50000 | 19/82/0.047/3.41e-06 | 28/132/0.066/4.67e-06 | NaN/NaN/NaN/NaN | 54/326/0.157/7.97e-06 |
| biggsb1/300 | 1301/1358/0.065/8.12e-06 | 1723/6327/0.299/8.90e-06 | 1431/2198/0.132/8.51e-06 | 2702/9423/0.447/6.74e-06 |
| sine/500 | 189/388/0.056/5.49e-06 | NaN/NaN/NaN/NaN | NaN/NaN/NaN/NaN | NaN/NaN/NaN/NaN |
| sine/1000 | 57/143/0.017/9.61e-06 | 102/455/0.071/5.78e-06 | NaN/NaN/NaN/NaN | 36/210/0.045/6.79e-06 |
| sine/2000 | 193/474/0.096/9.15e-06 | 258/1041/0.310/3.68e-06 | NaN/NaN/NaN/NaN | 263/1324/0.428/9.53e-06 |
| fletchv3/100 | 2743/5765/0.537/9.73e-06 | 2737/6642/0.536/9.01e-06 | 2626/4741/0.433/6.90e-06 | 1015/2837/0.265/7.85e-06 |
| nonscomp/5000 | 168/263/0.091/9.79e-06 | 86/452/0.073/9.65e-06 | 481/1559/0.138/5.88e-06 | 87/375/0.029/9.90e-06 |
| nonscomp/8000 | 2004/2685/0.469/9.57e-06 | 64/261/0.029/6.88e-06 | 132/396/0.044/8.67e-06 | 75/350/0.036/8.88e-06 |
| power1/150 | 1558/1647/0.066/9.88e-06 | 2815/10480/0.468/5.88e-06 | 2519/3981/0.201/9.49e-06 | 2726/9301/0.407/9.27e-06 |
| raydan1/500 | 317/375/0.044/8.95e-06 | 261/1055/0.062/8.49e-06 | 175/315/0.016/7.03e-06 | 241/971/0.054/6.34e-06 |
| raydan1/1000 | NaN/NaN/NaN/NaN | 310/1076/0.130/9.48e-06 | 251/435/0.065/5.91e-06 | 363/1351/0.137/7.04e-06 |
| raydan2/1000 | 15/70/0.014/6.53e-06 | 21/151/0.011/1.43e-06 | NaN/NaN/NaN/NaN | 462/5057/0.598/8.71e-06 |
| raydan2/2000 | 12/63/0.010/5.09e-06 | 47/297/0.050/1.46e-06 | NaN/NaN/NaN/NaN | 662/7271/1.379/2.26e-06 |
| raydan2/5000 | 10/71/0.029/1.06e-06 | 13/86/0.025/8.16e-06 | NaN/NaN/NaN/NaN | 517/5674/1.680/5.33e-06 |
| diagonal1/800 | 658/4620/0.541/9.92e-06 | 683/5335/0.667/9.28e-06 | NaN/NaN/NaN/NaN | 1143/10423/1.310/7.70e-06 |
| diagonal1/2000 | 2996/29170/7.269/9.52e-06 | NaN/NaN/NaN/NaN | NaN/NaN/NaN/NaN | NaN/NaN/NaN/NaN |
| diagonal2/5000 | 400/618/0.308/9.35e-06 | 551/2169/1.069/8.59e-06 | NaN/NaN/NaN/NaN | 577/2029/0.779/7.45e-06 |
| diagonal2/10000 | 588/888/0.774/9.51e-06 | 781/2995/2.340/7.92e-06 | NaN/NaN/NaN/NaN | 998/3676/2.774/8.45e-06 |
| diagonal3/500 | 899/7222/0.580/9.47e-06 | 614/5099/0.364/9.50e-06 | 1303/10734/0.787/8.38e-06 | 1222/11448/0.808/6.46e-06 |
| diagonal3/1000 | 1140/9629/1.361/9.60e-06 | 1852/17580/2.189/8.53e-06 | NaN/NaN/NaN/NaN | NaN/NaN/NaN/NaN |
| diagonal3/2000 | 2069/18930/4.846/9.84e-06 | NaN/NaN/NaN/NaN | NaN/NaN/NaN/NaN | 2533/23863/5.842/7.55e-06 |
| osb2/11 | 410/741/0.135/6.78e-06 | 829/3002/0.268/6.94e-06 | 543/1172/0.137/8.77e-06 | 854/3319/0.326/7.93e-06 |
| ie/150 | 16/52/0.594/8.93e-06 | 33/193/2.309/4.64e-06 | 27/149/1.659/6.62e-06 | 41/223/2.412/9.21e-06 |
| ie/500 | 12/45/4.757/7.38e-06 | 37/232/24.227/9.21e-06 | 17/79/7.712/8.54e-06 | 30/202/20.399/6.62e-06 |
| singx/500 | 210/505/0.373/9.26e-06 | 238/1033/0.681/9.40e-06 | 239/968/0.563/1.64e-06 | 192/1020/0.553/8.84e-07 |
| singx/1000 | 375/878/2.159/9.07e-06 | 266/1299/3.952/7.38e-06 | 105/368/1.708/4.53e-06 | 284/1425/5.630/1.02e-06 |
| singx/2000 | 338/818/12.485/8.51e-06 | 431/1958/28.877/4.06e-06 | 173/755/12.428/7.34e-06 | 262/1273/21.566/1.94e-06 |
| lin/50 | 10/57/0.093/2.08e-06 | 11/73/0.019/3.44e-06 | 18/70/0.016/5.93e-06 | 75/719/0.138/1.53e-06 |
| lin/100 | 13/63/0.022/8.86e-07 | 12/85/0.029/6.73e-06 | 31/160/0.049/9.55e-06 | 72/671/0.198/6.92e-06 |
| pen1/200 | 183/954/0.093/9.34e-06 | NaN/NaN/NaN/NaN | 94/644/0.049/7.05e-07 | 122/910/0.070/7.53e-06 |
| pen1/1000 | 143/1045/11.946/6.41e-06 | NaN/NaN/NaN/NaN | 297/2355/7.952/8.98e-06 | 168/1254/4.498/9.15e-06 |
| pen2/160 | 298/943/0.117/9.90e-06 | NaN/NaN/NaN/NaN | NaN/NaN/NaN/NaN | NaN/NaN/NaN/NaN |
| rosex/500 | 79/299/0.220/9.24e-06 | 153/934/0.828/3.56e-06 | 44/236/0.182/9.70e-07 | 77/559/0.517/3.82e-06 |
| rosex/1000 | 83/296/1.725/2.64e-06 | 102/608/2.830/2.98e-06 | 43/204/1.914/3.95e-06 | 49/340/2.281/2.61e-06 |
| trid/400 | 151/206/0.179/7.95e-06 | 105/370/0.175/5.10e-06 | 75/174/0.092/7.55e-06 | 107/476/0.207/9.93e-06 |
| trid/800 | 127/182/0.389/8.68e-06 | 46/192/0.410/7.44e-06 | 48/147/0.357/7.39e-06 | 62/314/0.704/9.09e-06 |