全连接神经网络

在前面的作业中,你在CIFAR-10上实现了一个两层的全连接神经网络。那个实现很简单,但不是很模块化,因为损失和梯度计算在一个函数内。对于一个简单的两层网络来说,还可以人为处理,但是当我们使用更大的模型时,人工处理损失和梯度就变得不切实际了。理想情况下,我们希望使用更加模块化的设计来构建网络,这样我们就可以独立地实现不同类型的层,然后将它们整合到不同架构的模型中。

在本练习中,我们将使用更模块化的方法实现全连接网络。对于每一层,我们将实现一个 forward 和一个 backward 的函数。 forward 函数将接收输入、权重和其他参数,并返回一个输出和一个 cache 对象,存储反向传播所需的数据,如下所示:

```
def layer_forward(x, w):
  """ Receive inputs x and weights w """
  # Do some computations ...
  z = # ... some intermediate value
  # Do some more computations ...
  out = # the output
  cache = (x, w, z, out) # Values we need to compute gradients
  return out, cache
反向传播将接收上游的梯度和 cache 对象,并返回相对于输入和权重的梯度:
def layer_backward(dout, cache):
  Receive dout (derivative of loss with respect to outputs) and cache,
  and compute derivative with respect to inputs.
  # Unpack cache values
  x, w, z, out = cache
  # Use values in cache to compute derivatives
  dx = \# Derivative of loss with respect to x
  dw = # Derivative of loss with respect to w
  return dx, dw
```

以这种方式实现了一些层之后,我们能够轻松地将它们组合起来,以构建不同架构的分类器。

除了实现任意深度的全连接网络外,我们还将探索不同的优化更新规则,并引入Dropout作为正则化器和Batch/Layer归一化工具来更有效地优化网络。

```
In [1]: # As usual, a bit of setup
from __future__ import print_function
import time
import numpy as np
import matplotlib.pyplot as plt
from daseCV.classifiers.fc_net import *
from daseCV.data_utils import get_CIFAR10_data
from daseCV.gradient_check import eval_numerical_gradient, eval_numerical_gradient_array
from daseCV.solver import Solver

%matplotlib inline
plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
plt.rcParams['image.interpolation'] = 'nearest'
```

```
plt.rcParams['image.cmap'] = 'gray'
        # for auto-reloading external modules
        # see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipython
        %load ext autoreload
        %autoreload 2
        def rel error(x, y):
         """ returns relative error """
          return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
        c:\Users\75872\.conda\envs\dnn\lib\site-packages\tqdm\auto.py:22: TqdmWarning: IProgress
        not found. Please update jupyter and ipywidgets. See https://ipywidgets.readthedocs.io/e
        n/stable/user install.html
         from .autonotebook import tqdm as notebook tqdm
        run the following from the daseCV directory and try again:
        python setup.py build ext --inplace
        You may also need to restart your iPython kernel
In [2]: # Load the (preprocessed) CIFAR10 data.
        data = get CIFAR10 data()
        for k, v in list(data.items()):
         print(('%s: ' % k, v.shape))
        ('X train: ', (49000, 3, 32, 32))
        ('y train: ', (49000,))
```

```
('y_train: ', (49000,))
('X_val: ', (1000, 3, 32, 32))
('y_val: ', (1000,))
('X_test: ', (1000, 3, 32, 32))
('y_test: ', (1000,))
```

仿射层: 前向传播

打开 daseCV/layers.py 并实现 affine_forward 函数。

当你完成上述函数后, 你可以用下面的代码测试你的实现正确与否

```
In [3]: # Test the affine forward function
        num inputs = 2
        input shape = (4, 5, 6)
        output dim = 3
        input size = num inputs * np.prod(input shape)
        weight size = output dim * np.prod(input shape)
        x = np.linspace(-0.1, 0.5, num=input size).reshape(num inputs, *input shape)
        w = np.linspace(-0.2, 0.3, num=weight size).reshape(np.prod(input shape), output dim)
        b = np.linspace(-0.3, 0.1, num=output dim)
        out, = affine forward(x, w, b)
        correct_out = np.array([[ 1.49834967, 1.70660132, 1.91485297],
                                [ 3.25553199, 3.5141327,
                                                           3.7727334211)
        # Compare your output with ours. The error should be around e-9 or less.
        print('Testing affine forward function:')
        print('difference: ', rel error(out, correct out))
```

Testing affine_forward function: difference: 9.7698500479884e-10

仿射层: 反向传播

实现 affine_backwards 函数,并使用数值梯度检查测试你的实现。

```
In [4]: # Test the affine_backward function
       np.random.seed(114514)
       x = np.random.randn(10, 2, 3)
       w = np.random.randn(6, 5)
       b = np.random.randn(5)
        dout = np.random.randn(10, 5)
        dx num = eval numerical gradient array(lambda x: affine forward(x, w, b)[0], x, dout)
        dw_num = eval_numerical_gradient_array(lambda w: affine_forward(x, w, b)[0], w, dout)
        db num = eval numerical gradient array(lambda b: affine forward(x, w, b)[0], b, dout)
        , cache = affine forward(x, w, b)
       dx, dw, db = affine backward(dout, cache)
        # The error should be around e-10 or less
       print('Testing affine backward function:')
       print('dx error: ', rel error(dx num, dx))
       print('dw error: ', rel error(dw num, dw))
       print('db error: ', rel error(db num, db))
```

Testing affine_backward function: dx error: 2.455378219135173e-10 dw error: 2.98530465744813e-11 db error: 9.266941356636817e-12

ReLU 激活函数: 前向传播

在 relu forward 函数中实现ReLU激活函数的前向传播,并使用以下代码测试您的实现:

Testing relu_forward function: difference: 4.999999798022158e-08

ReLU 激活函数:反向传播

在 relu_back 函数中为ReLU激活函数实现反向传播,并使用数值梯度检查来测试你的实现

```
In [6]: np.random.seed(114514)
    x = np.random.randn(10, 10)
    dout = np.random.randn(*x.shape)

dx_num = eval_numerical_gradient_array(lambda x: relu_forward(x)[0], x, dout)
```

```
_, cache = relu_forward(x)
dx = relu_backward(dout, cache)

# The error should be on the order of e-12
print('Testing relu_backward function:')
print('dx error: ', rel_error(dx_num, dx))
```

Testing relu_backward function: dx error: 3.2756100345805755e-12

Inline Question 1:

作业中只要求你实现ReLU,但是神经网络可以使用很多不同的激活函数,每个都有它的优点和缺点。但是,激活函数的一个常见问题是在反向传播时出现零(或接近零)梯度流。下列哪个激活函数会有这个问题?如果在一维情况下考虑这些函数,什么样的输入将会发生这种现象?

- 1. Sigmoid
- 2. ReLU
- 3. Leaky ReLU

Answer:

- 1. 绝对值较大的值(基本上到6就没梯度了)
- 2. 负值和零值
- 3. 负值和零值, 如果leaky slope足够大, 则只有零值.

"三明治"层

在神经网络中有一些常用的层模式。例如,仿射层后面经常跟一个ReLU层。为了简化这些常见模式,我们在 文件 daseCV/layer_utils.py 中定义了几个常用的层

请查看 affine_relu_forward 和 affine_relu_backward 函数,并且运行下列代码进行数值梯度检查:

```
In [7]: from daseCV.layer_utils import affine_relu forward, affine relu backward
        np.random.seed(114514)
        x = np.random.randn(2, 3, 4)
        w = np.random.randn(12, 10)
        b = np.random.randn(10)
        dout = np.random.randn(2, 10)
        out, cache = affine relu forward(x, w, b)
        dx, dw, db = affine relu backward(dout, cache)
        dx num = eval numerical gradient array(lambda x: affine relu forward(x, w, b)[0], x, dou
        dw num = eval numerical gradient array(lambda w: affine relu forward(x, w, b)[0], w, dou
        db num = eval numerical gradient array(lambda b: affine relu forward(x, w, b)[0], b, dou
        # Relative error should be around e-10 or less
        print('Testing affine relu forward and affine relu backward:')
        print('dx error: ', rel error(dx num, dx))
       print('dw error: ', rel error(dw num, dw))
        print('db error: ', rel_error(db num, db))
```

Testing affine_relu_forward and affine_relu_backward: dx error: 1.4425080577469413e-10

dw error: 1.3004526350597686e-09
db error: 7.826683101713151e-12

损失层: Softmax and SVM

在上次作业中你已经实现了这些损失函数,所以这次作业就不用做了,免费送你了。当然,你仍然应该通过查看 daseCV/layers.py 其中的实现来确保理解它们是如何工作的。

你可以通过运行以下程序来确保实现是正确的:

```
In [8]: | np.random.seed(114514)
        num classes, num inputs = 10, 50
        x = 0.001 * np.random.randn(num inputs, num classes)
        y = np.random.randint(num classes, size=num inputs)
        dx num = eval numerical gradient(lambda x: svm loss(x, y)[0], x, verbose=False)
        loss, dx = svm loss(x, y)
        # Test svm loss function. Loss should be around 9 and dx error should be around the orde
        print('Testing svm loss:')
        print('loss: ', loss)
        print('dx error: ', rel error(dx num, dx))
        dx num = eval numerical gradient(lambda x: softmax loss(x, y)[0], x, verbose=False)
        loss, dx = softmax loss(x, y)
        # Test softmax loss function. Loss should be close to 2.3 and dx error should be around
        print('\nTesting softmax loss:')
        print('loss: ', loss)
       print('dx error: ', rel error(dx num, dx))
       Testing svm loss:
       loss: 9.000848412807304
       dx error: 3.038735505103329e-09
       Testing softmax loss:
       loss: 2.3026703950620897
       dx error: 8.280545539165663e-09
```

两层网络

在之前的作业中, 你已经实现了一个简单的两层神经网络。现在你已经模块化地实现了一些层, 你将使用这些模块重新实现两层网络。

打开文件 daseCV/classifiers/fc_net 。并完成 TwoLayerNet 类的实现。这个类将作为这个作业中其他 网络的模块,所以请通读它以确保你理解了这个API。 你可以运行下面的单元来测试您的实现。

```
In [9]: np.random.seed(114514)
N, D, H, C = 3, 5, 50, 7
X = np.random.randn(N, D)
y = np.random.randint(C, size=N)

std = 1e-3
model = TwoLayerNet(input_dim=D, hidden_dim=H, num_classes=C, weight_scale=std)

print('Testing initialization ... ')
W1_std = abs(model.params['W1'].std() - std)
b1 = model.params['b1']
W2 std = abs(model.params['W2'].std() - std)
```

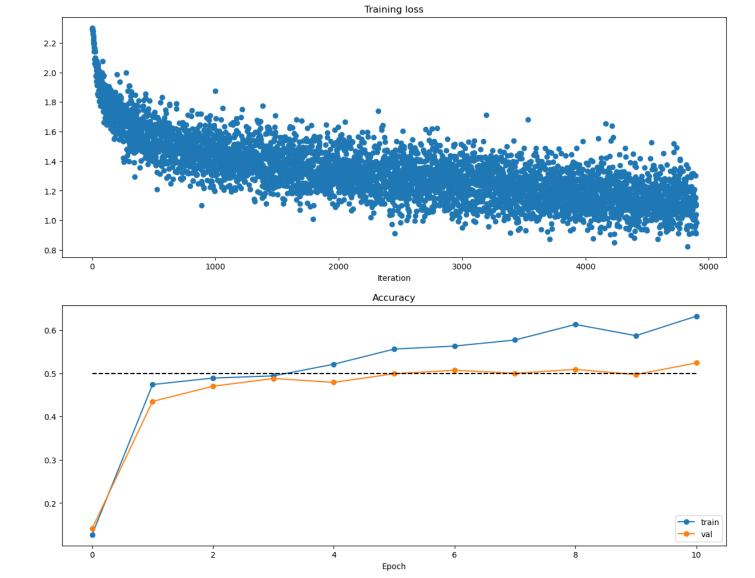
```
b2 = model.params['b2']
assert W1 std < std / 10, 'First layer weights do not seem right'
assert np.all(b1 == 0), 'First layer biases do not seem right'
assert W2 std < std / 10, 'Second layer weights do not seem right'
assert np.all(b2 == 0), 'Second layer biases do not seem right'
print('Testing test-time forward pass ... ')
model.params['W1'] = np.linspace(-0.7, 0.3, num=D*H).reshape(D, H)
model.params['b1'] = np.linspace(-0.1, 0.9, num=H)
model.params['W2'] = np.linspace(-0.3, 0.4, num=H*C).reshape(H, C)
model.params['b2'] = np.linspace(-0.9, 0.1, num=C)
X = np.linspace(-5.5, 4.5, num=N*D).reshape(D, N).T
scores = model.loss(X)
correct scores = np.asarray(
                              13.05181771, 13.81190102, 14.57198434, 15.33206765,
  [[11.53165108, 12.2917344,
   [12.05769098, 12.74614105, 13.43459113, 14.1230412, 14.81149128, 15.49994135,
   [12.58373087, 13.20054771, 13.81736455, 14.43418138, 15.05099822, 15.66781506,
scores diff = np.abs(scores - correct scores).sum()
assert scores diff < 1e-6, 'Problem with test-time forward pass'
print('Testing training loss (no regularization)')
y = np.asarray([0, 5, 1])
loss, grads = model.loss(X, y)
correct loss = 3.4702243556
assert abs(loss - correct loss) < 1e-10, 'Problem with training-time loss'</pre>
model.reg = 1.0
loss, grads = model.loss(X, y)
correct loss = 26.5948426952
assert abs(loss - correct loss) < 1e-10, 'Problem with regularization loss'</pre>
# Errors should be around e-7 or less
for reg in [0.0, 0.7]:
  print('Running numeric gradient check with reg = ', reg)
  model.reg = reg
  loss, grads = model.loss(X, y)
  for name in sorted(grads):
    f = lambda : model.loss(X, y)[0]
    grad num = eval numerical gradient(f, model.params[name], verbose=False)
    print('%s relative error: %.2e' % (name, rel_error(grad num, grads[name])))
Testing initialization ...
Testing test-time forward pass ...
Testing training loss (no regularization)
Running numeric gradient check with reg = 0.0
W1 relative error: 1.22e-08
W2 relative error: 3.17e-10
b1 relative error: 6.19e-09
b2 relative error: 4.33e-10
Running numeric gradient check with reg = 0.7
W1 relative error: 3.12e-07
W2 relative error: 7.98e-08
b1 relative error: 1.09e-09
b2 relative error: 7.76e-10
```

Solver

在之前的作业中,模型的训练逻辑与模型本身是耦合的。在这次作业中,按照更加模块化的设计,我们将模型的训练逻辑划分为单独的类。

打开文件 daseCV/solver ,通读一遍以熟悉API。然后使用一个 Sovler 实例来训练一个 TwoLayerNet ,它可以在验证集上达到至少 50% 的精度。

```
In [10]: model = TwoLayerNet(reg=0.01)
       # TODO: Use a Solver instance to train a TwoLayerNet that achieves at least #
       # 50% accuracy on the validation set.
       # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) *****
       solver = Solver(model, data, lr decay=0.95, optim config={'learning rate': 1e-3}, print
       solver.train()
       # *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
       END OF YOUR CODE
       (Iteration 1 / 4900) loss: 2.301112
       (Epoch 0 / 10) train acc: 0.127000; val acc: 0.141000
       (Epoch 1 / 10) train acc: 0.474000; val acc: 0.435000
       (Epoch 2 / 10) train acc: 0.489000; val acc: 0.470000
       (Epoch 3 / 10) train acc: 0.494000; val acc: 0.488000
       (Epoch 4 / 10) train acc: 0.521000; val acc: 0.479000
       (Epoch 5 / 10) train acc: 0.556000; val acc: 0.499000
       (Epoch 6 / 10) train acc: 0.563000; val acc: 0.507000
       (Epoch 7 / 10) train acc: 0.577000; val acc: 0.500000
       (Epoch 8 / 10) train acc: 0.613000; val acc: 0.509000
       (Epoch 9 / 10) train acc: 0.587000; val acc: 0.497000
       (Epoch 10 / 10) train acc: 0.632000; val acc: 0.524000
In [11]: # Run this cell to visualize training loss and train / val accuracy
       plt.subplot(2, 1, 1)
       plt.title('Training loss')
       plt.plot(solver.loss history, 'o')
       plt.xlabel('Iteration')
       plt.subplot(2, 1, 2)
       plt.title('Accuracy')
       plt.plot(solver.train acc history, '-o', label='train')
       plt.plot(solver.val acc history, '-o', label='val')
       plt.plot([0.5] * len(solver.val acc history), 'k--')
       plt.xlabel('Epoch')
       plt.legend(loc='lower right')
       plt.gcf().set size inches(15, 12)
       plt.show()
```



多层网络

接下来,请实现一个带有任意数量的隐层的全连接网络。

阅读 daseCV/classifiers/fc_net.py 中的 FullyConnectedNet 类。

实现初始化、前向传播和反向传播的函数,暂时不要考虑实现dropout或batch/layer normalization,我们将在后面添加上去。

初始化loss和梯度检查

刚开始要做完整性检查,运行以下代码来检查初始loss,并对有正则化和无正则化的网络进行梯度检查。请问初始的loss合理吗?

在梯度检查中,你应该期望得到1e-7或更少的errors。

```
In [12]: np.random.seed(114514)
N, D, H1, H2, C = 2, 15, 20, 30, 10
X = np.random.randn(N, D)
y = np.random.randint(C, size=(N,))

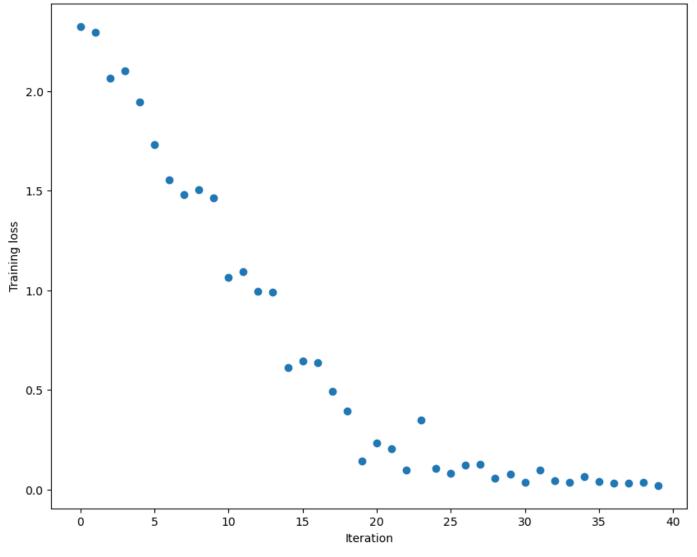
for reg in [0, 3.14]:
```

```
Running check with reg = 0
Initial loss: 2.3040446026497716
W1 relative error: 9.86e-07
W2 relative error: 1.95e-06
W3 relative error: 6.43e-08
b1 relative error: 1.14e-08
b2 relative error: 1.07e-08
b3 relative error: 1.23e-10
Running check with reg = 3.14
Initial loss: 6.0896278390251055
W1 relative error: 1.93e-08
W2 relative error: 1.81e-08
W3 relative error: 2.78e-07
b1 relative error: 9.82e-08
b2 relative error: 4.60e-08
b3 relative error: 2.69e-10
```

实现另一个完整性检查,请确保你可以过拟合50个图像的小数据集。首先,我们将尝试一个三层网络,每个隐藏层有100个单元。在接下来的代码中,调整learning rate和weight initialization scale以达到过拟合,在20 epoch内达到100%的训练精度。

```
# TODO: Use a three-layer Net to overfit 50 training examples by
In [13]:
         # tweaking just the learning rate and initialization scale.
         num train = 50
         small data = {
          'X train': data['X train'][:num train],
          'y train': data['y train'][:num train],
          'X val': data['X val'],
           'y val': data['y val'],
         weight scale = 1e-2  # Experiment with this!
         learning rate = 1e-2 # Experiment with this!
         model = FullyConnectedNet([100, 100],
                       weight scale=weight scale, dtype=np.float64)
         solver = Solver(model, small data,
                         print every=10, num epochs=20, batch size=25,
                         update rule='sgd',
                         optim config={
                           'learning rate': learning rate,
         solver.train()
         plt.plot(solver.loss history, 'o')
         plt.title('Training loss history')
         plt.xlabel('Iteration')
         plt.ylabel('Training loss')
         plt.show()
```

```
(Iteration 1 / 40) loss: 2.324442
(Epoch 0 / 20) train acc: 0.320000; val acc: 0.093000
(Epoch 1 / 20) train acc: 0.420000; val acc: 0.106000
(Epoch 2 / 20) train acc: 0.520000; val acc: 0.169000
(Epoch 3 / 20) train acc: 0.620000; val acc: 0.165000
(Epoch 4 / 20) train acc: 0.520000; val acc: 0.145000
(Epoch 5 / 20) train acc: 0.640000; val acc: 0.154000
(Iteration 11 / 40) loss: 1.063150
(Epoch 6 / 20) train acc: 0.680000; val acc: 0.144000
(Epoch 7 / 20) train acc: 0.840000; val acc: 0.156000
(Epoch 8 / 20) train acc: 0.820000; val acc: 0.187000
(Epoch 9 / 20) train acc: 0.880000; val acc: 0.146000
(Epoch 10 / 20) train acc: 0.920000; val acc: 0.189000
(Iteration 21 / 40) loss: 0.232994
(Epoch 11 / 20) train acc: 0.960000; val acc: 0.194000
(Epoch 12 / 20) train acc: 1.000000; val acc: 0.185000
(Epoch 13 / 20) train acc: 0.980000; val_acc: 0.191000
(Epoch 14 / 20) train acc: 0.940000; val acc: 0.190000
(Epoch 15 / 20) train acc: 0.960000; val acc: 0.202000
(Iteration 31 / 40) loss: 0.034993
(Epoch 16 / 20) train acc: 1.000000; val acc: 0.197000
(Epoch 17 / 20) train acc: 0.980000; val acc: 0.207000
(Epoch 18 / 20) train acc: 1.000000; val acc: 0.198000
(Epoch 19 / 20) train acc: 1.000000; val acc: 0.194000
(Epoch 20 / 20) train acc: 1.000000; val acc: 0.199000
                                      Training loss history
```



现在尝试使用一个五层的网络,每层100个单元,对50张图片进行训练。同样,你将调整learning rate和 weight initialization scale比例,你应该能够在20个epoch内实现100%的训练精度。

```
In [14]: # TODO: Use a five-layer Net to overfit 50 training examples by
         # tweaking just the learning rate and initialization scale.
         num train = 50
         small data = {
           'X train': data['X train'][:num train],
           'y train': data['y train'][:num train],
           'X val': data['X val'],
           'y val': data['y val'],
         weight scale = 1e-1 # Experiment with this!
         learning rate = 2e-3 # Experiment with this!
        model = FullyConnectedNet([100, 100, 100, 100],
                         weight scale=weight scale, dtype=np.float64)
         solver = Solver(model, small data,
                         print every=10, num epochs=20, batch size=25,
                         update rule='sgd',
                         optim config={
                           'learning rate': learning rate,
         solver.train()
        plt.plot(solver.loss history, 'o')
         plt.title('Training loss history')
         plt.xlabel('Iteration')
         plt.ylabel('Training loss')
         plt.show()
         (Iteration 1 / 40) loss: 130.521574
         (Epoch 0 / 20) train acc: 0.200000; val acc: 0.086000
         (Epoch 1 / 20) train acc: 0.120000; val acc: 0.149000
         (Epoch 2 / 20) train acc: 0.280000; val acc: 0.105000
         (Epoch 3 / 20) train acc: 0.400000; val acc: 0.134000
         (Epoch 4 / 20) train acc: 0.580000; val acc: 0.124000
         (Epoch 5 / 20) train acc: 0.720000; val acc: 0.112000
         (Iteration 11 / 40) loss: 2.887287
         (Epoch 6 / 20) train acc: 0.860000; val acc: 0.104000
         (Epoch 7 / 20) train acc: 0.760000; val acc: 0.114000
         (Epoch 8 / 20) train acc: 0.900000; val acc: 0.122000
         (Epoch 9 / 20) train acc: 0.960000; val acc: 0.133000
```

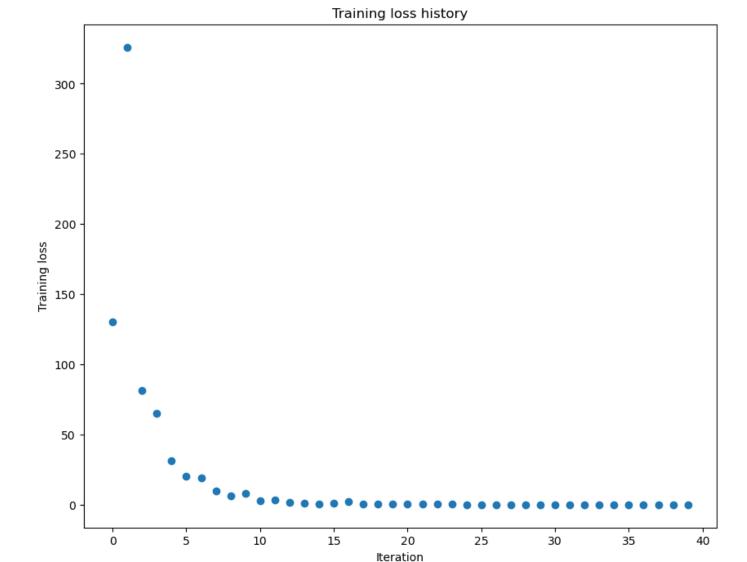
(Epoch 10 / 20) train acc: 0.940000; val acc: 0.137000

(Epoch 11 / 20) train acc: 0.960000; val_acc: 0.144000 (Epoch 12 / 20) train acc: 1.000000; val_acc: 0.148000 (Epoch 13 / 20) train acc: 1.000000; val_acc: 0.147000 (Epoch 14 / 20) train acc: 1.000000; val_acc: 0.147000 (Epoch 15 / 20) train acc: 1.000000; val_acc: 0.146000

(Epoch 16 / 20) train acc: 1.000000; val_acc: 0.147000 (Epoch 17 / 20) train acc: 1.000000; val_acc: 0.147000 (Epoch 18 / 20) train acc: 1.000000; val_acc: 0.147000 (Epoch 19 / 20) train acc: 1.000000; val_acc: 0.147000 (Epoch 20 / 20) train acc: 1.000000; val_acc: 0.147000

(Iteration 21 / 40) loss: 0.278804

(Iteration 31 / 40) loss: 0.000725



Inline Question 2:

你注意到训练三层网和训练五层网难度的区别了吗?根据你的经验,哪个网络对initalization scale更敏感?为什么会这样呢?

Answer:

更深的网络对初始化更加敏感.

网络更深时,对不同的输入,神经网络根据参数放大或者缩小中间层输出的分布范围.

当网络更深时,不加注意的初始化更容易导致病态的中间层输出,而这随着层数的加深变得更严重,导致梯度消失或者爆炸,使得模型更难训练.

更新规则

到目前为止,我们使用了普通的随机梯度下降法(SGD)作为我们的更新规则。更复杂的更新规则可以更容易地训练深度网络。我们将实现一些最常用的更新规则,并将它们与普通的SGD进行比较。

SGD+Momentum

带动量的随机梯度下降法是一种广泛使用的更新规则,它使深度网络的收敛速度快于普通的随机梯度下降法。更多信息参见http://cs231n.github.io/neural-networks-3/#sqd 动量更新部分。

打开文件 daseCV/optim ,并阅读该文件顶部的文档,以确保你理解了该API。在函数 sgd_momentum 中实现SGD+动量更新规则,并运行以下代码检查你的实现。你会看到errors小于e-8。

```
In [15]: from daseCV.optim import sgd momentum
       N, D = 4, 5
       w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
       dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
       v = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)
       config = {'learning rate': 1e-3, 'velocity': v}
       next w, = sgd momentum(w, dw, config=config)
       expected next w = np.asarray([
        [ 0.80849474, 0.87528421, 0.94207368, 1.00886316, 1.07565263],
        [ 1.14244211, 1.20923158, 1.27602105, 1.34281053, 1.4096 ]])
       expected velocity = np.asarray([
        [ 0.61138947,  0.62554737,  0.63970526,  0.65386316,  0.66802105],
         [ 0.68217895,  0.69633684,  0.71049474,  0.72465263,  0.73881053],
         [ 0.75296842, 0.76712632, 0.78128421, 0.79544211, 0.8096 ]])
       # Should see relative errors around e-8 or less
       print('next w error: ', rel error(next w, expected next w))
       print('velocity error: ', rel error(expected velocity, config['velocity']))
       next w error: 8.882347033505819e-09
```

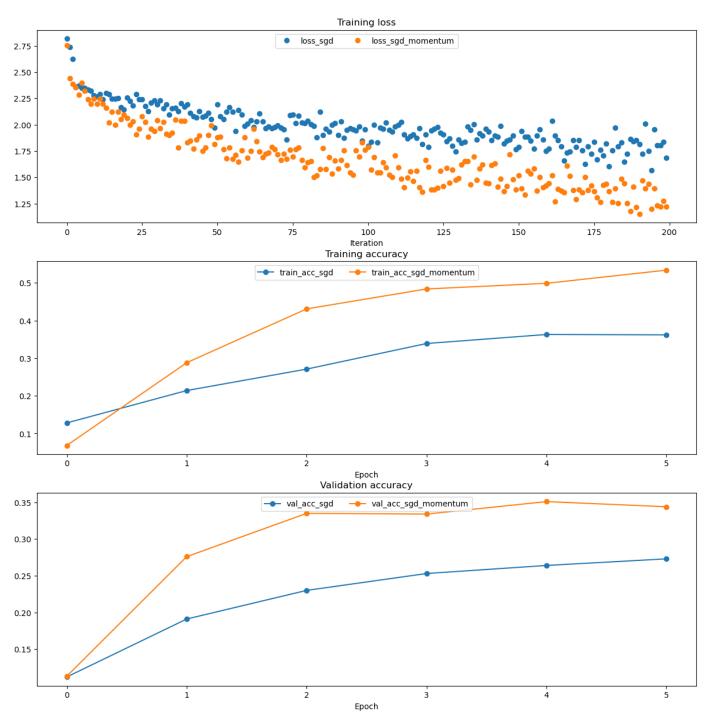
velocity error: 4.269287743278663e-09 当你完成了上面的步骤,运行以下代码来训练一个具有SGD和SGD+momentum的六层网络。你应该看到

SGD+momentum更新规则收敛得更快。

```
In [16]: num train = 4000
         small data = {
          'X_train': data['X_train'][:num_train],
          'y train': data['y train'][:num train],
          'X val': data['X val'],
          'y val': data['y val'],
         solvers = {}
         for update rule in ['sgd', 'sgd momentum']:
          print('running with ', update rule)
          model = FullyConnectedNet([100, 100, 100, 100, 100], weight scale=5e-2)
          solver = Solver(model, small data,
                           num epochs=5, batch size=100,
                           update rule=update rule,
                           optim config={
                             'learning rate': 5e-3,
                           verbose=True)
          solvers[update rule] = solver
           solver.train()
          print()
         plt.subplot(3, 1, 1)
```

```
plt.title('Training loss')
plt.xlabel('Iteration')
plt.subplot(3, 1, 2)
plt.title('Training accuracy')
plt.xlabel('Epoch')
plt.subplot(3, 1, 3)
plt.title('Validation accuracy')
plt.xlabel('Epoch')
for update rule, solver in solvers.items():
 plt.subplot(3, 1, 1)
 plt.plot(solver.loss history, 'o', label="loss %s" % update rule)
 plt.subplot(3, 1, 2)
 plt.plot(solver.train acc history, '-o', label="train acc %s" % update rule)
 plt.subplot(3, 1, 3)
 plt.plot(solver.val acc history, '-o', label="val acc %s" % update rule)
for i in [1, 2, 3]:
 plt.subplot(3, 1, i)
  plt.legend(loc='upper center', ncol=4)
plt.gcf().set size inches(15, 15)
plt.show()
running with sgd
(Iteration 1 / 200) loss: 2.816666
(Epoch 0 / 5) train acc: 0.128000; val acc: 0.112000
(Iteration 11 / 200) loss: 2.269594
(Iteration 21 / 200) loss: 2.254420
(Iteration 31 / 200) loss: 2.193956
(Epoch 1 / 5) train acc: 0.214000; val acc: 0.191000
(Iteration 41 / 200) loss: 2.190202
(Iteration 51 / 200) loss: 2.191721
(Iteration 61 / 200) loss: 2.008235
(Iteration 71 / 200) loss: 1.991281
(Epoch 2 / 5) train acc: 0.271000; val acc: 0.230000
(Iteration 81 / 200) loss: 2.034080
(Iteration 91 / 200) loss: 1.902123
(Iteration 101 / 200) loss: 1.795957
(Iteration 111 / 200) loss: 1.996119
(Epoch 3 / 5) train acc: 0.339000; val acc: 0.253000
(Iteration 121 / 200) loss: 1.785391
(Iteration 131 / 200) loss: 1.855856
(Iteration 141 / 200) loss: 1.934352
(Iteration 151 / 200) loss: 1.786561
(Epoch 4 / 5) train acc: 0.363000; val acc: 0.264000
(Iteration 161 / 200) loss: 1.771611
(Iteration 171 / 200) loss: 1.849872
(Iteration 181 / 200) loss: 1.606331
(Iteration 191 / 200) loss: 1.815892
(Epoch 5 / 5) train acc: 0.362000; val acc: 0.273000
running with sgd momentum
(Iteration 1 / 200) loss: 2.754268
(Epoch 0 / 5) train acc: 0.068000; val acc: 0.113000
(Iteration 11 / 200) loss: 2.197175
(Iteration 21 / 200) loss: 2.063424
(Iteration 31 / 200) loss: 2.039988
(Epoch 1 / 5) train acc: 0.288000; val acc: 0.276000
(Iteration 41 / 200) loss: 1.830932
(Iteration 51 / 200) loss: 1.879851
(Iteration 61 / 200) loss: 1.687092
(Iteration 71 / 200) loss: 1.715726
```

```
(Epoch 2 / 5) train acc: 0.431000; val acc: 0.335000
(Iteration 81 / 200) loss: 1.643061
(Iteration 91 / 200) loss: 1.584446
(Iteration 101 / 200) loss: 1.787894
(Iteration 111 / 200) loss: 1.594990
(Epoch 3 / 5) train acc: 0.484000; val acc: 0.334000
(Iteration 121 / 200) loss: 1.598701
(Iteration 131 / 200) loss: 1.491945
(Iteration 141 / 200) loss: 1.441724
(Iteration 151 / 200) loss: 1.516655
(Epoch 4 / 5) train acc: 0.499000; val acc: 0.351000
(Iteration 161 / 200) loss: 1.442543
(Iteration 171 / 200) loss: 1.381633
(Iteration 181 / 200) loss: 1.367549
(Iteration 191 / 200) loss: 1.151507
(Epoch 5 / 5) train acc: 0.534000; val acc: 0.344000
```



RMSProp and Adam

RMSProp [1] 和Adam [2] 是另外两个更新规则,它们通过使用梯度的二阶矩平均值来设置每个参数的学习速 率。

在文件 daseCV/optim 中实现 RMSProp 函数和 Adam 函数,并使用下面的代码来检查您的实现。

- [1] Tijmen Tieleman and Geoffrey Hinton. "Lecture 6.5-rmsprop: Divide the gradient by a running average of its recent magnitude." COURSERA: Neural Networks for Machine Learning 4 (2012).
- [2] Diederik Kingma and Jimmy Ba, "Adam: A Method for Stochastic Optimization", ICLR 2015.

```
In [17]: # Test RMSProp implementation
        from daseCV.optim import rmsprop
        N, D = 4, 5
        w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
        dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
        cache = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)
        config = {'learning rate': 1e-2, 'cache': cache}
        next w, = rmsprop(w, dw, config=config)
        expected next w = np.asarray([
         [-0.39223849, -0.34037513, -0.28849239, -0.23659121, -0.18467247],
         [-0.132737, -0.08078555, -0.02881884, 0.02316247, 0.07515774],
         [ 0.12716641, 0.17918792, 0.23122175, 0.28326742, 0.33532447],
         [ 0.38739248, 0.43947102, 0.49155973, 0.54365823, 0.59576619]])
        expected cache = np.asarray([
         [ 0.67329252, 0.68859723, 0.70395734, 0.71937285, 0.73484377],
         [0.75037008, 0.7659518, 0.78158892, 0.79728144, 0.81302936],
          [ 0.82883269,  0.84469141,  0.86060554,  0.87657507,  0.8926  ]])
        # You should see relative errors around e-7 or less
        print('next w error: ', rel error(expected next w, next w))
        print('cache error: ', rel error(expected cache, config['cache']))
        next w error: 9.524687511038133e-08
```

cache error: 2.647795492281335e-09

```
In [18]: # Test Adam implementation
       from daseCV.optim import adam
       N, D = 4, 5
       w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
       dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
       m = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)
       v = np.linspace(0.7, 0.5, num=N*D).reshape(N, D)
       config = {'learning rate': 1e-2, 'm': m, 'v': v, 't': 5}
       next w, = adam(w, dw, config=config)
       expected next w = np.asarray([
         [-0.40094747, -0.34836187, -0.29577703, -0.24319299, -0.19060977],
         [-0.1380274, -0.08544591, -0.03286534, 0.01971428, 0.0722929],
        [0.1248705, 0.17744702, 0.23002243, 0.28259667, 0.33516969],
        [ 0.38774145,  0.44031188,  0.49288093,  0.54544852,  0.59801459]])
       expected v = np.asarray([
        [0.64683452, 0.63628604, 0.6257431, 0.61520571, 0.60467385,],
         [0.59414753, 0.58362676, 0.57311152, 0.56260183, 0.55209767,],
         [ 0.54159906, 0.53110598, 0.52061845, 0.51013645, 0.49966, ]])
       expected m = np.asarray([
```

```
[ 0.57736842, 0.59684211, 0.61631579, 0.63578947, 0.65526316],
[ 0.67473684, 0.69421053, 0.71368421, 0.73315789, 0.75263158],
[ 0.77210526, 0.79157895, 0.81105263, 0.83052632, 0.85 ]])

# You should see relative errors around e-7 or less
print('next_w error: ', rel_error(expected_next_w, next_w))
print('v error: ', rel_error(expected_v, config['v']))
print('m error: ', rel_error(expected_m, config['m']))

next_w error: 1.1395691798535431e-07
v error: 4.208314038113071e-09
m error: 4.214963193114416e-09
```

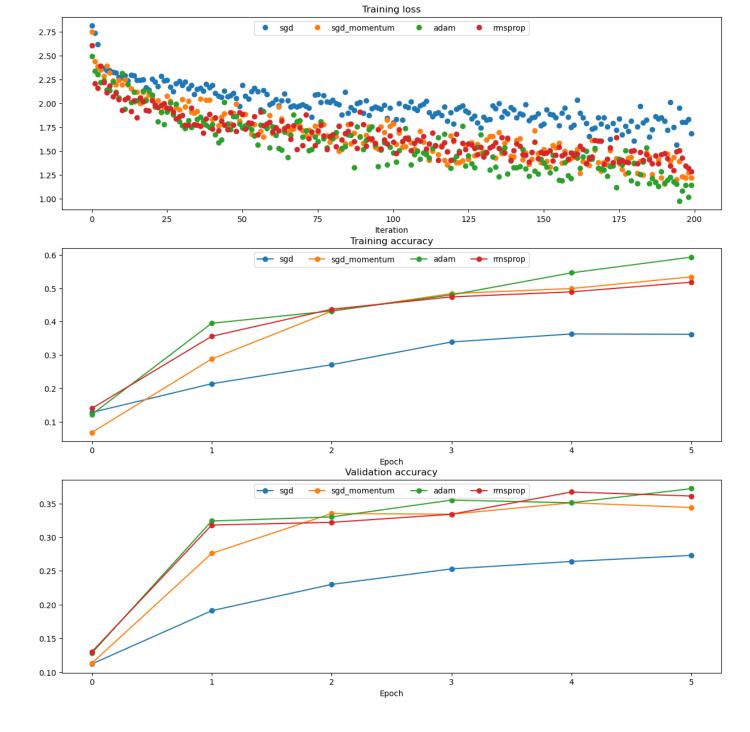
当你完成了上面RMSProp和Adam函数后,运行下面的代码训练一对网络,其中分别使用了上述两个方法

```
In [19]: learning_rates = {'rmsprop': 1e-4, 'adam': 1e-3}
         for update rule in ['adam', 'rmsprop']:
           print('running with ', update rule)
           model = FullyConnectedNet([100, 100, 100, 100, 100], weight scale=5e-2)
           solver = Solver(model, small data,
                           num epochs=5, batch size=100,
                           update rule=update rule,
                           optim config={
                             'learning rate': learning rates[update rule]
                           verbose=True)
           solvers[update rule] = solver
           solver.train()
          print()
         plt.subplot(3, 1, 1)
         plt.title('Training loss')
         plt.xlabel('Iteration')
         plt.subplot(3, 1, 2)
         plt.title('Training accuracy')
         plt.xlabel('Epoch')
         plt.subplot(3, 1, 3)
         plt.title('Validation accuracy')
         plt.xlabel('Epoch')
         for update rule, solver in list(solvers.items()):
          plt.subplot(3, 1, 1)
          plt.plot(solver.loss history, 'o', label=update rule)
          plt.subplot(3, 1, 2)
          plt.plot(solver.train acc history, '-o', label=update rule)
           plt.subplot(3, 1, 3)
          plt.plot(solver.val acc history, '-o', label=update rule)
         for i in [1, 2, 3]:
           plt.subplot(3, 1, i)
          plt.legend(loc='upper center', ncol=4)
         plt.gcf().set size inches(15, 15)
         plt.show()
         running with adam
         (Iteration 1 / 200) loss: 2.495259
         (Epoch 0 / 5) train acc: 0.122000; val acc: 0.128000
         (Iteration 11 / 200) loss: 2.317346
         (Iteration 21 / 200) loss: 2.092152
```

(Iteration 31 / 200) loss: 1.769410

(Epoch 1 / 5) train acc: 0.395000; val acc: 0.324000

```
(Iteration 41 / 200) loss: 1.779823
(Iteration 51 / 200) loss: 1.745313
(Iteration 61 / 200) loss: 1.754007
(Iteration 71 / 200) loss: 1.651215
(Epoch 2 / 5) train acc: 0.432000; val acc: 0.330000
(Iteration 81 / 200) loss: 1.633240
(Iteration 91 / 200) loss: 1.519306
(Iteration 101 / 200) loss: 1.479580
(Iteration 111 / 200) loss: 1.481148
(Epoch 3 / 5) train acc: 0.480000; val acc: 0.355000
(Iteration 121 / 200) loss: 1.412316
(Iteration 131 / 200) loss: 1.474755
(Iteration 141 / 200) loss: 1.328829
(Iteration 151 / 200) loss: 1.373671
(Epoch 4 / 5) train acc: 0.546000; val acc: 0.351000
(Iteration 161 / 200) loss: 1.474406
(Iteration 171 / 200) loss: 1.304476
(Iteration 181 / 200) loss: 1.372967
(Iteration 191 / 200) loss: 1.167323
(Epoch 5 / 5) train acc: 0.593000; val acc: 0.372000
running with rmsprop
(Iteration 1 / 200) loss: 2.606104
(Epoch 0 / 5) train acc: 0.140000; val acc: 0.130000
(Iteration 11 / 200) loss: 1.930949
(Iteration 21 / 200) loss: 2.029422
(Iteration 31 / 200) loss: 1.872671
(Epoch 1 / 5) train acc: 0.356000; val acc: 0.318000
(Iteration 41 / 200) loss: 1.730048
(Iteration 51 / 200) loss: 1.884917
(Iteration 61 / 200) loss: 1.699826
(Iteration 71 / 200) loss: 1.559276
(Epoch 2 / 5) train acc: 0.437000; val acc: 0.322000
(Iteration 81 / 200) loss: 1.670811
(Iteration 91 / 200) loss: 1.779277
(Iteration 101 / 200) loss: 1.593992
(Iteration 111 / 200) loss: 1.657953
(Epoch 3 / 5) train acc: 0.474000; val acc: 0.334000
(Iteration 121 / 200) loss: 1.615274
(Iteration 131 / 200) loss: 1.442173
(Iteration 141 / 200) loss: 1.507020
(Iteration 151 / 200) loss: 1.474433
(Epoch 4 / 5) train acc: 0.489000; val acc: 0.367000
(Iteration 161 / 200) loss: 1.452065
(Iteration 171 / 200) loss: 1.364858
(Iteration 181 / 200) loss: 1.506351
(Iteration 191 / 200) loss: 1.473888
(Epoch 5 / 5) train acc: 0.518000; val acc: 0.361000
```



Inline Question 3:

AdaGrad,类似于Adam,是一个per-parameter优化方法,它使用以下更新规则:

```
cache += dw**2
w += - learning_rate * dw / (np.sqrt(cache) + eps)
```

当使用AdaGrad训练一个网络时,更新的值会变得非常小,而且他的网络学习的非常慢。利用你对AdaGrad更新规则的了解,解释为什么更新的值会变得非常小? Adam会有同样的问题吗?

Answer:

因为dw**2非负, cache随迭代单调递增.

因此, 更新时学习率会越来越小. Adam没有这样的问题, 因为它采取了动量更新缩放参数的方法, 如果dw都很小时, 分母会逐渐减小, 学习率会逐渐增加.

训练一个效果足够好的模型!

(Iteration 1301 / 2450) loss: 1.427256 (Iteration 1401 / 2450) loss: 1.451936

在CIFAR-10上尽可能训练最好的全连接模型,将最好的模型存储在 best_model 变量中。我们要求你在验证集上获得至少50%的准确性。

如果你细心的话,应该是有可能得到55%以上精度的,但我们不苛求你达到这么高的精度。在后面的作业上,我们会要求你们在CIFAR-10上训练最好的卷积神经网络,我们希望你们把精力放在卷积网络上,而不是全连接网络上。

在做这部分之前完成 BatchNormalization.ipynb 和 Dropout.ipynb 可能会对你有帮助,因为这些技术可以帮助你训练强大的模型。

```
In [26]: best_model = None
       # TODO: Train the best FullyConnectedNet that you can on CIFAR-10. You might #
       # find batch/layer normalization and dropout useful. Store your best model in #
       # the best model variable.
       # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) *****
       model = FullyConnectedNet([100, 100], weight scale=1.2e-02, reg=3.7e-2, normalization='b
       # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
       solver = Solver(model, data, update rule='adam', optim config={'learning rate': 1.245e-0
          print every=100, num epochs=10, batch size=200)
       solver.train()
       solver = Solver(model, data, update rule='sgd momentum', optim config={'learning rate':
          print every=100, num epochs=20, batch size=200)
       solver.train()
       best model = model
       # *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
       END OF YOUR CODE
       (Iteration 1 / 2450) loss: 3.209108
       (Epoch 0 / 10) train acc: 0.116000; val acc: 0.118000
       (Iteration 101 / 2450) loss: 2.304769
       (Iteration 201 / 2450) loss: 2.120514
       (Epoch 1 / 10) train acc: 0.468000; val acc: 0.445000
       (Iteration 301 / 2450) loss: 2.042426
       (Iteration 401 / 2450) loss: 1.976509
       (Epoch 2 / 10) train acc: 0.504000; val acc: 0.494000
       (Iteration 501 / 2450) loss: 1.677764
       (Iteration 601 / 2450) loss: 1.744640
       (Iteration 701 / 2450) loss: 1.575542
       (Epoch 3 / 10) train acc: 0.523000; val acc: 0.497000
       (Iteration 801 / 2450) loss: 1.679396
       (Iteration 901 / 2450) loss: 1.440741
       (Epoch 4 / 10) train acc: 0.528000; val acc: 0.498000
       (Iteration 1001 / 2450) loss: 1.603155
       (Iteration 1101 / 2450) loss: 1.377467
       (Iteration 1201 / 2450) loss: 1.500870
       (Epoch 5 / 10) train acc: 0.536000; val acc: 0.505000
```

```
(Epoch 6 / 10) train acc: 0.568000; val acc: 0.502000
(Iteration 1501 / 2450) loss: 1.545511
(Iteration 1601 / 2450) loss: 1.380931
(Iteration 1701 / 2450) loss: 1.500689
(Epoch 7 / 10) train acc: 0.571000; val acc: 0.540000
(Iteration 1801 / 2450) loss: 1.376559
(Iteration 1901 / 2450) loss: 1.325783
(Epoch 8 / 10) train acc: 0.581000; val acc: 0.532000
(Iteration 2001 / 2450) loss: 1.266508
(Iteration 2101 / 2450) loss: 1.352303
(Iteration 2201 / 2450) loss: 1.313391
(Epoch 9 / 10) train acc: 0.581000; val acc: 0.542000
(Iteration 2301 / 2450) loss: 1.397033
(Iteration 2401 / 2450) loss: 1.285815
(Epoch 10 / 10) train acc: 0.598000; val acc: 0.528000
(Iteration 1 / 4900) loss: 1.330950
(Epoch 0 / 20) train acc: 0.596000; val acc: 0.542000
(Iteration 101 / 4900) loss: 1.285027
(Iteration 201 / 4900) loss: 1.217762
(Epoch 1 / 20) train acc: 0.596000; val acc: 0.553000
(Iteration 301 / 4900) loss: 1.259255
(Iteration 401 / 4900) loss: 1.259039
(Epoch 2 / 20) train acc: 0.630000; val acc: 0.555000
(Iteration 501 / 4900) loss: 1.378480
(Iteration 601 / 4900) loss: 1.213960
(Iteration 701 / 4900) loss: 1.332126
(Epoch 3 / 20) train acc: 0.612000; val acc: 0.553000
(Iteration 801 / 4900) loss: 1.411395
(Iteration 901 / 4900) loss: 1.331909
(Epoch 4 / 20) train acc: 0.614000; val acc: 0.550000
(Iteration 1001 / 4900) loss: 1.458855
(Iteration 1101 / 4900) loss: 1.358654
(Iteration 1201 / 4900) loss: 1.290443
(Epoch 5 / 20) train acc: 0.600000; val acc: 0.549000
(Iteration 1301 / 4900) loss: 1.411681
(Iteration 1401 / 4900) loss: 1.308292
(Epoch 6 / 20) train acc: 0.608000; val acc: 0.552000
(Iteration 1501 / 4900) loss: 1.307554
(Iteration 1601 / 4900) loss: 1.269824
(Iteration 1701 / 4900) loss: 1.260238
(Epoch 7 / 20) train acc: 0.608000; val acc: 0.550000
(Iteration 1801 / 4900) loss: 1.174878
(Iteration 1901 / 4900) loss: 1.311515
(Epoch 8 / 20) train acc: 0.614000; val acc: 0.549000
(Iteration 2001 / 4900) loss: 1.359453
(Iteration 2101 / 4900) loss: 1.309900
(Iteration 2201 / 4900) loss: 1.330742
(Epoch 9 / 20) train acc: 0.622000; val acc: 0.549000
(Iteration 2301 / 4900) loss: 1.312524
(Iteration 2401 / 4900) loss: 1.137829
(Epoch 10 / 20) train acc: 0.640000; val acc: 0.550000
(Iteration 2501 / 4900) loss: 1.254197
(Iteration 2601 / 4900) loss: 1.193829
(Epoch 11 / 20) train acc: 0.625000; val acc: 0.552000
(Iteration 2701 / 4900) loss: 1.288601
(Iteration 2801 / 4900) loss: 1.320550
(Iteration 2901 / 4900) loss: 1.236324
(Epoch 12 / 20) train acc: 0.606000; val acc: 0.551000
(Iteration 3001 / 4900) loss: 1.119956
(Iteration 3101 / 4900) loss: 1.310999
(Epoch 13 / 20) train acc: 0.627000; val acc: 0.552000
(Iteration 3201 / 4900) loss: 1.290168
(Iteration 3301 / 4900) loss: 1.155471
(Iteration 3401 / 4900) loss: 1.405335
(Epoch 14 / 20) train acc: 0.640000; val acc: 0.549000
(Iteration 3501 / 4900) loss: 1.273778
```

```
(Iteration 3601 / 4900) loss: 1.260513
(Epoch 15 / 20) train acc: 0.609000; val acc: 0.551000
(Iteration 3701 / 4900) loss: 1.316917
(Iteration 3801 / 4900) loss: 1.244228
(Iteration 3901 / 4900) loss: 1.307020
(Epoch 16 / 20) train acc: 0.634000; val acc: 0.545000
(Iteration 4001 / 4900) loss: 1.430306
(Iteration 4101 / 4900) loss: 1.235945
(Epoch 17 / 20) train acc: 0.604000; val acc: 0.545000
(Iteration 4201 / 4900) loss: 1.295875
(Iteration 4301 / 4900) loss: 1.516959
(Iteration 4401 / 4900) loss: 1.273916
(Epoch 18 / 20) train acc: 0.594000; val acc: 0.547000
(Iteration 4501 / 4900) loss: 1.298765
(Iteration 4601 / 4900) loss: 1.369611
(Epoch 19 / 20) train acc: 0.620000; val acc: 0.547000
(Iteration 4701 / 4900) loss: 1.267463
(Iteration 4801 / 4900) loss: 1.336636
(Epoch 20 / 20) train acc: 0.622000; val acc: 0.546000
```

测试你的模型!

在验证和测试集上运行您的最佳模型。验证集的准确率应达到50%以上。

```
In [27]: y_test_pred = np.argmax(best_model.loss(data['X_test']), axis=1)
    y_val_pred = np.argmax(best_model.loss(data['X_val']), axis=1)
    print('Validation set accuracy: ', (y_val_pred == data['y_val']).mean())
    print('Test set accuracy: ', (y_test_pred == data['y_test']).mean())

Validation set accuracy: 0.555
Test set accuracy: 0.522
```

Data for leaderboard

这里额外提供了一组未给标签的测试集X,用于leaderborad上的竞赛。

提示: 该题的目的是鼓励同学们探索能够提升模型性能的方法。

提醒:运行完下面代码之后,点击下面的submit,然后去leaderboard上查看你的成绩。本模型对应的成绩在phase1的leaderboard中。

```
In [29]: import os
#输出格式
def output_file(preds, phase_id=1):
    path=os.getcwd()
```

```
if not os.path.exists(path + '/output/phase {}'.format(phase id)):
        os.mkdir(path + '/output/phase {}'.format(phase id))
    path=path + '/output/phase {}/prediction.npy'.format(phase id)
   np.save(path,preds)
def zip fun(phase id=1):
   path=os.getcwd()
   output path = path + '/output'
    files = os.listdir(output path)
    for file in files:
        if file.find('zip') != -1:
           os.remove(output path + '/' + file)
    newpath=path+'/output/phase {}'.format(phase id)
    os.chdir(newpath)
    cmd = 'zip ../prediction phase {}.zip prediction.npy'.format(phase id)
    os.system(cmd)
    os.chdir(path)
output file(preds)
zip fun()
```