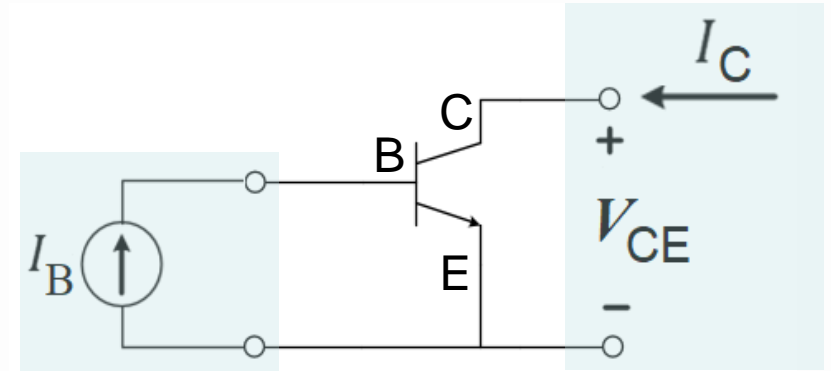
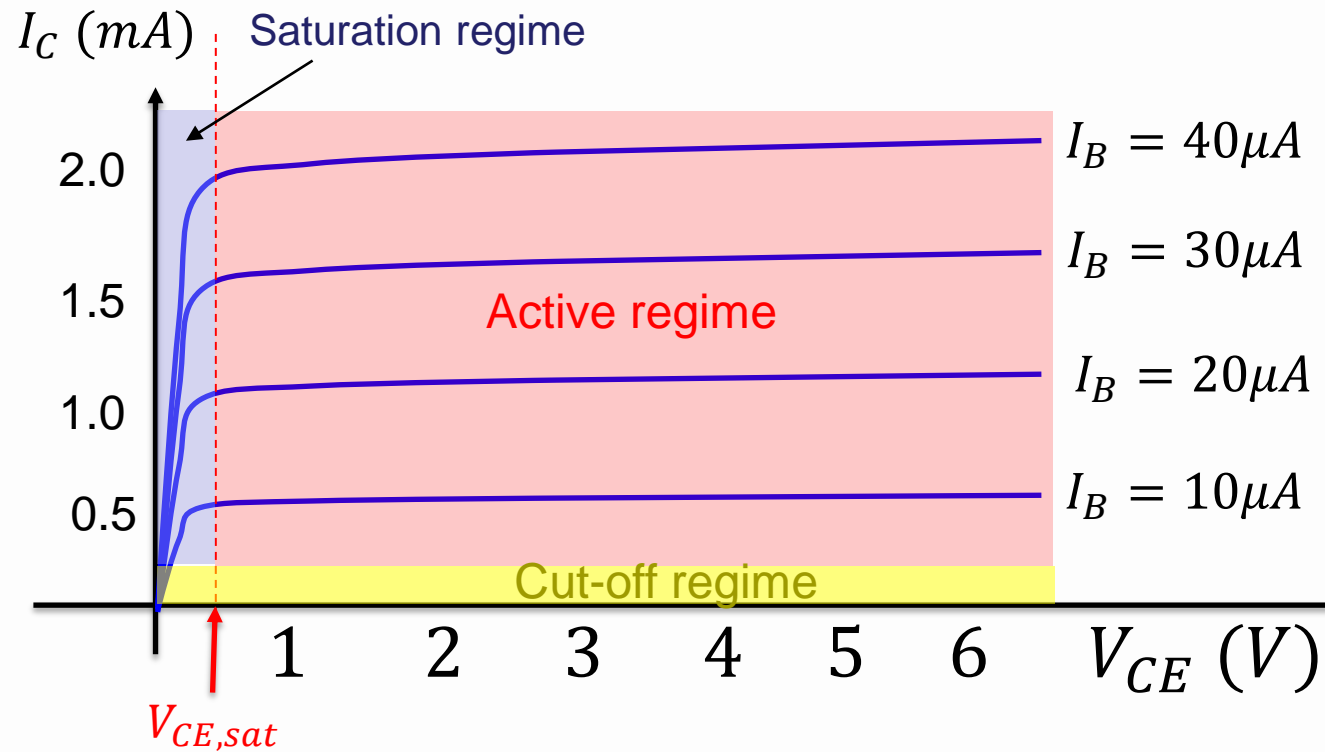


# Lecture 20: BJT IV Characteristics

- Interpreting CE junction IV curves for transistor parameters
- Interpreting load line IV curves
- Analysis of IV curves for the (I,V) operating point
- Explore the saturation condition
- Solving transistor-regime problems

## I-V curves of BJT



### 1. Cut-off regime

When  $V_{BE} < V_{on}$ , thus  $I_C \approx 0$

### 2. Active regime

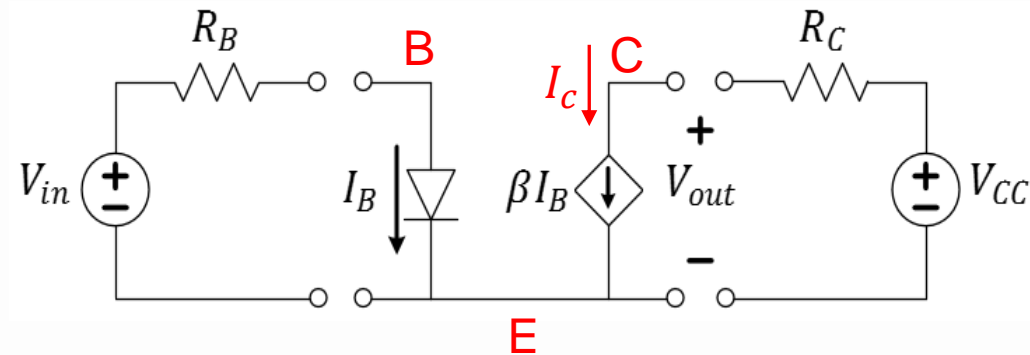
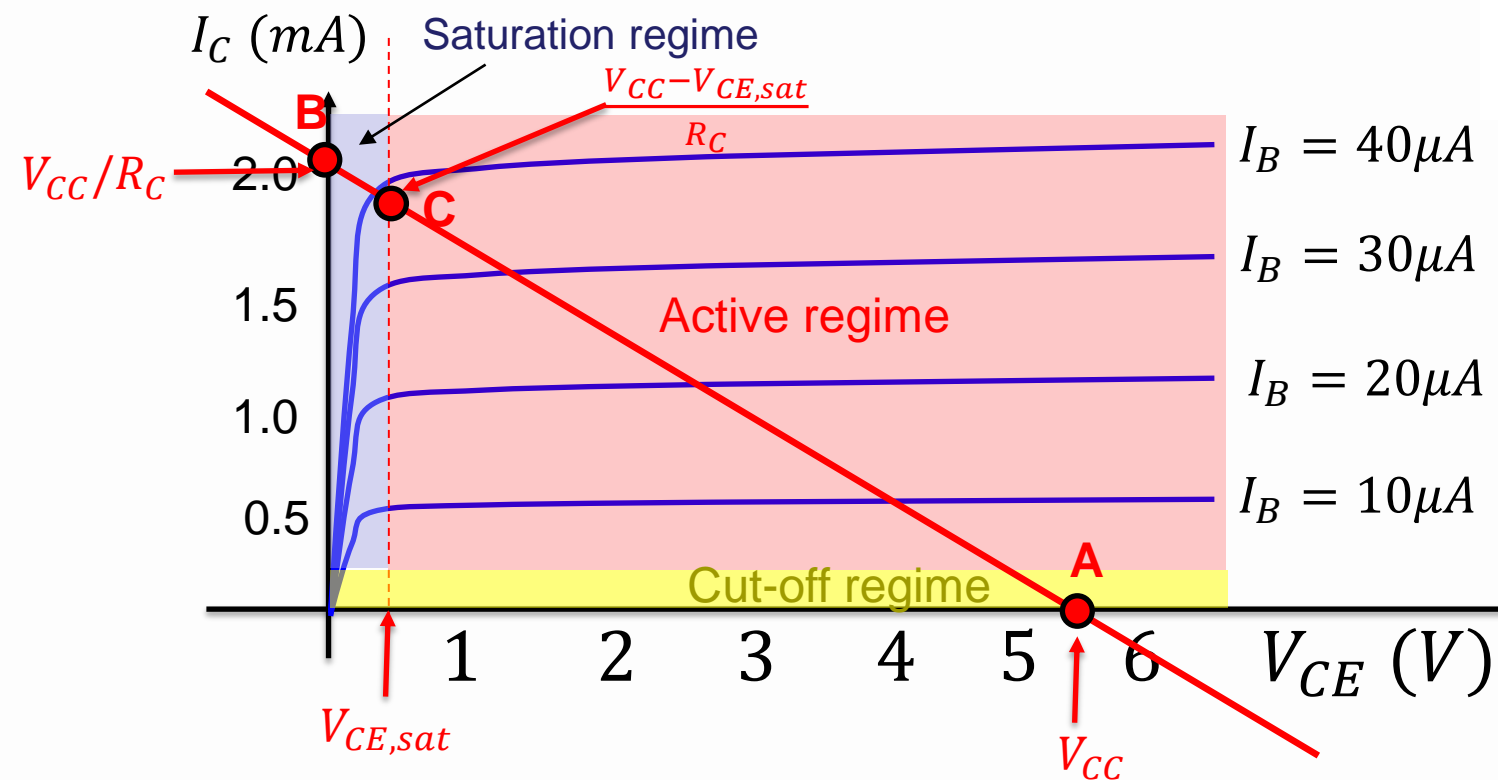
When  $V_{BE} \geq V_{on}$ , thus  $I_C = \beta I_B$

### 3. Saturation regime

When  $V_{BE} \geq V_{on}$ , and  $V_C < V_B$

Thus  $V_{CE} = V_{on,sat}$ , typically 0.3 V

## I-V curves of BJT & load line



IV formula for load

$$I_C = \frac{V_{CC} - V_{CE}}{R_C}$$

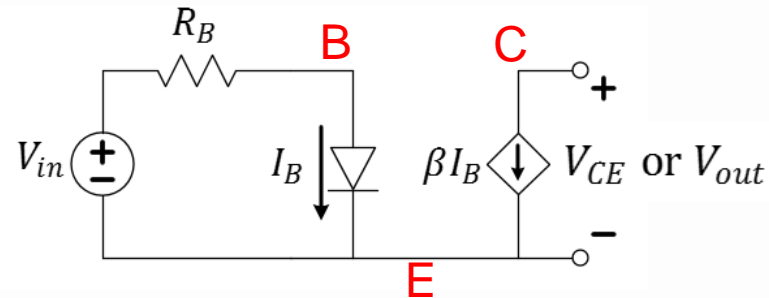
$$A = (V_{CC}, 0)$$

$$B = (0, V_{CC}/R_C)$$

$$C = (V_{CE,sat}, (V_{CC} - V_{CE,sat})/R_C)$$

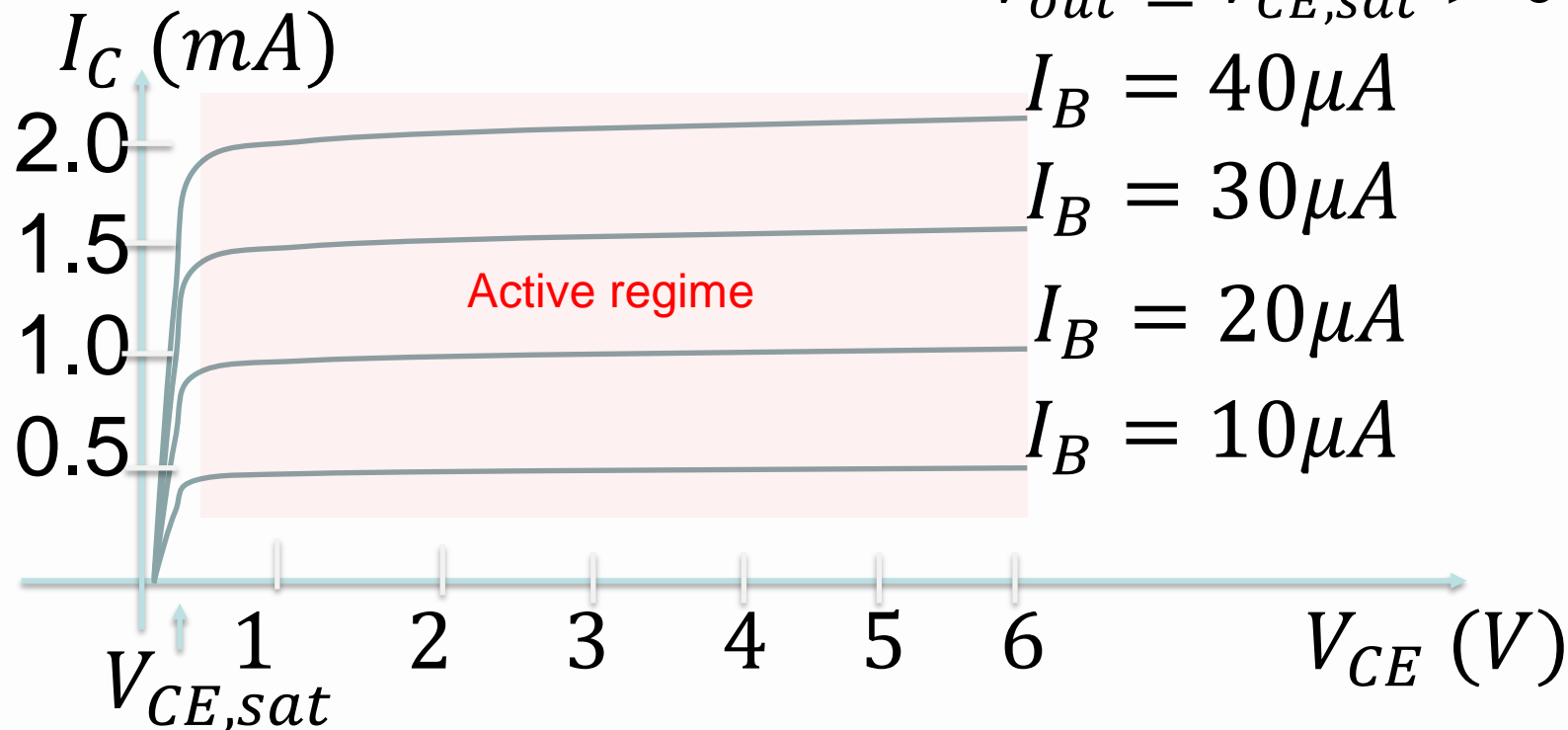
$$I_{C,sat} = \frac{V_{CC} - V_{CE,sat}}{R_C}$$

# BJT IV curves of the CE junction



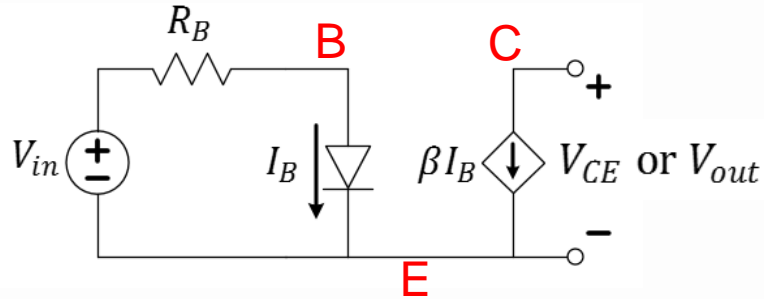
Constraints: In active regime

- $0 \leq \beta I_B \leq I_{C,sat}$
- $V_{out} \geq V_{CE,sat} > 0$



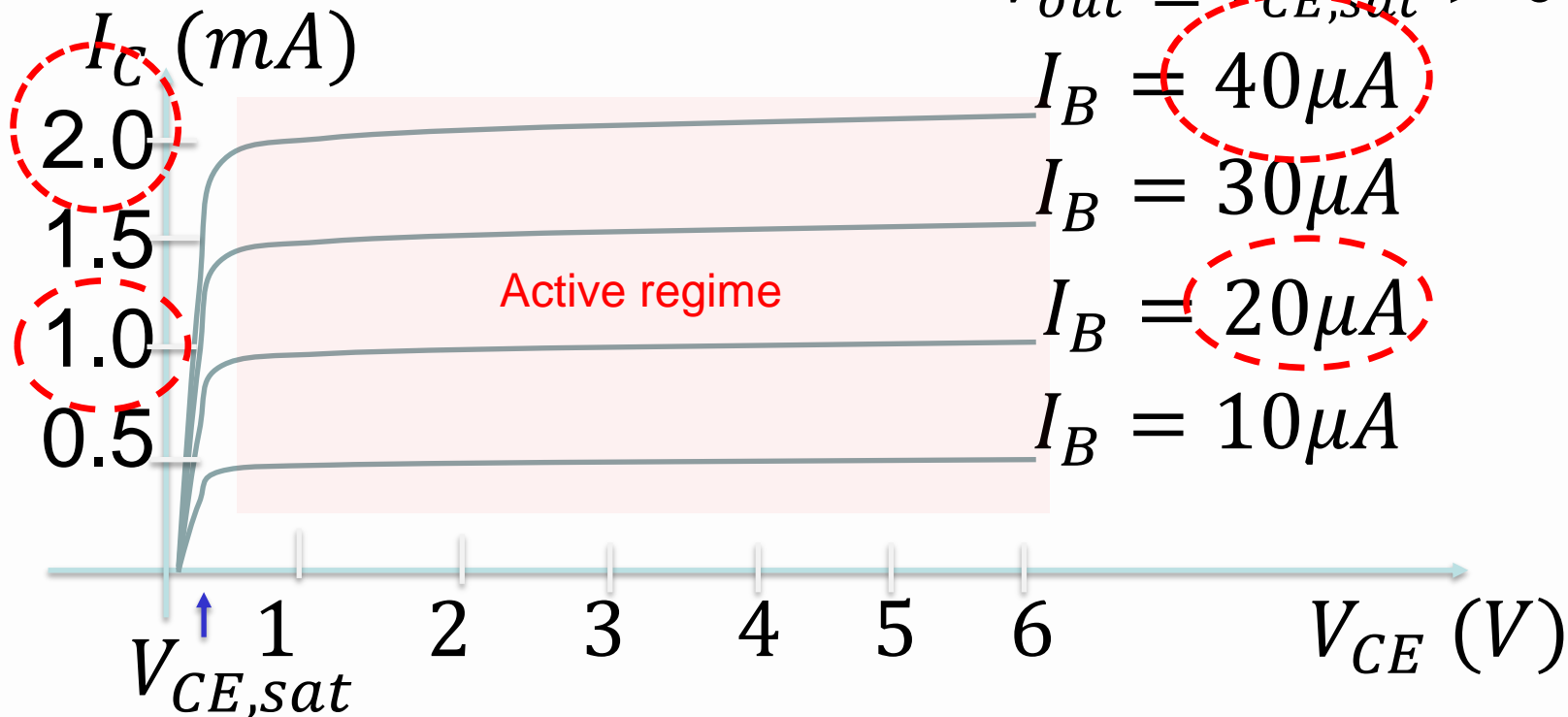
L20Q1: Use the IV plots above to estimate the value of  $\beta$ .

# BJT IV curves of the CE junction



Constraints:

- $0 \leq \beta I_B \leq I_{C,sat}$
- $V_{out} \geq V_{CE,sat} > 0$



$$\beta = \frac{I_C}{I_B} = \frac{2m}{40\mu}$$

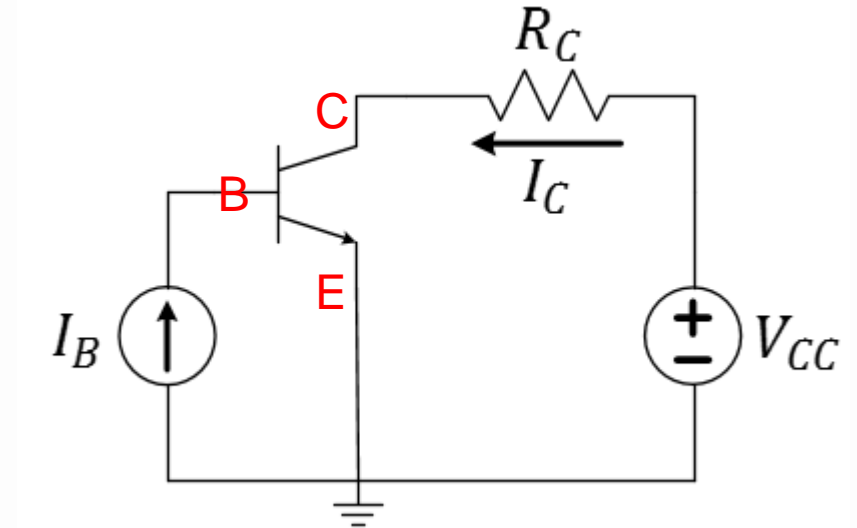
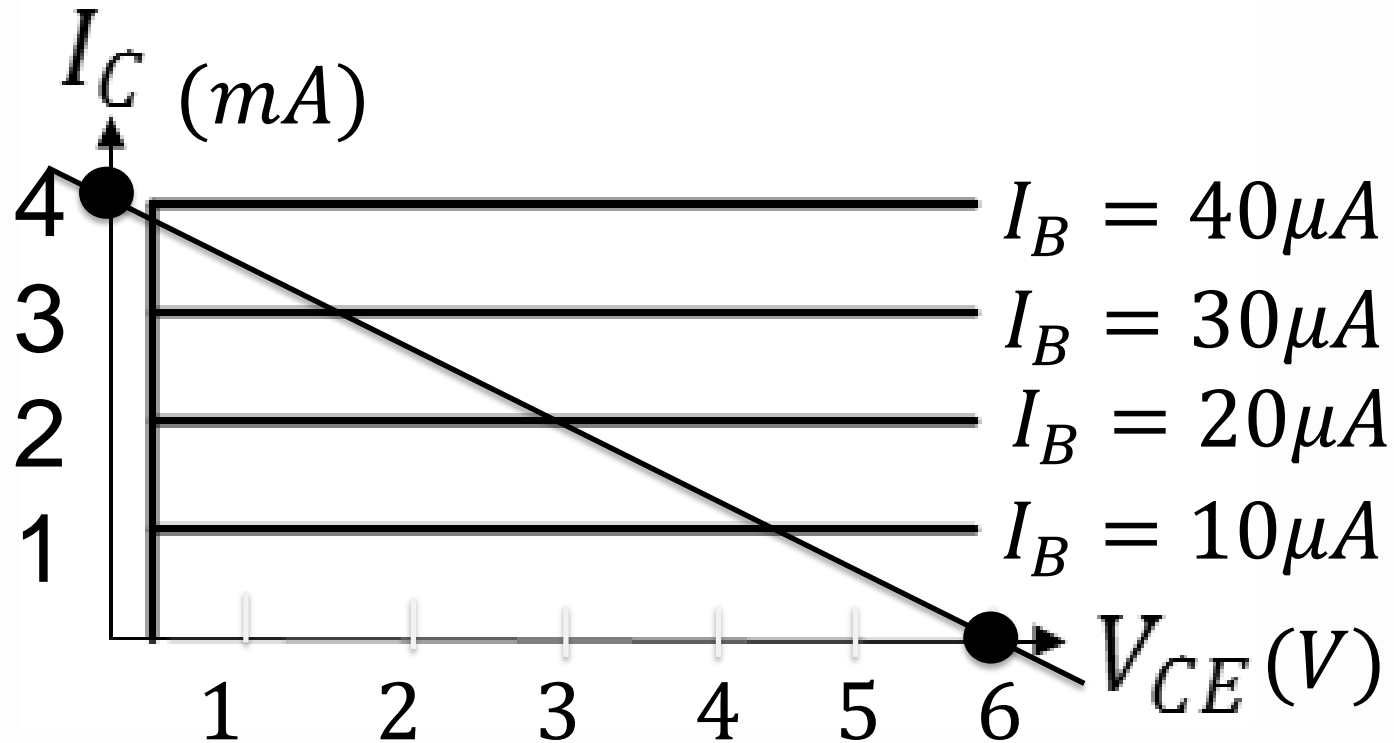
$$\beta = 50$$

$$\beta = \frac{I_C}{I_B} = \frac{1m}{20\mu}$$

$$\beta = 50$$

L20Q1: Use the IV plots above to estimate the value of  $\beta$ .

# Extracting information from the IV curve(s)



L20Q2: What is  $\beta$  and  $V_{CE,sat}$ ?

L20Q3: What is  $V_{CC}$ ?

L20Q4: What is  $R_C$ ?

L20Q5: What is  $I_{C,sat}$ ?

L20Q6: Which  $I_B$  results in saturation?

Q6:

A.  $I_B = 40 \mu A$

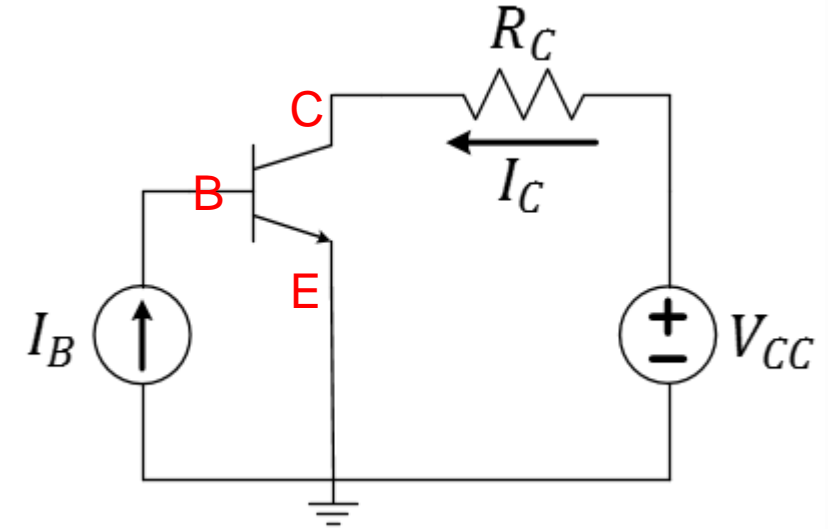
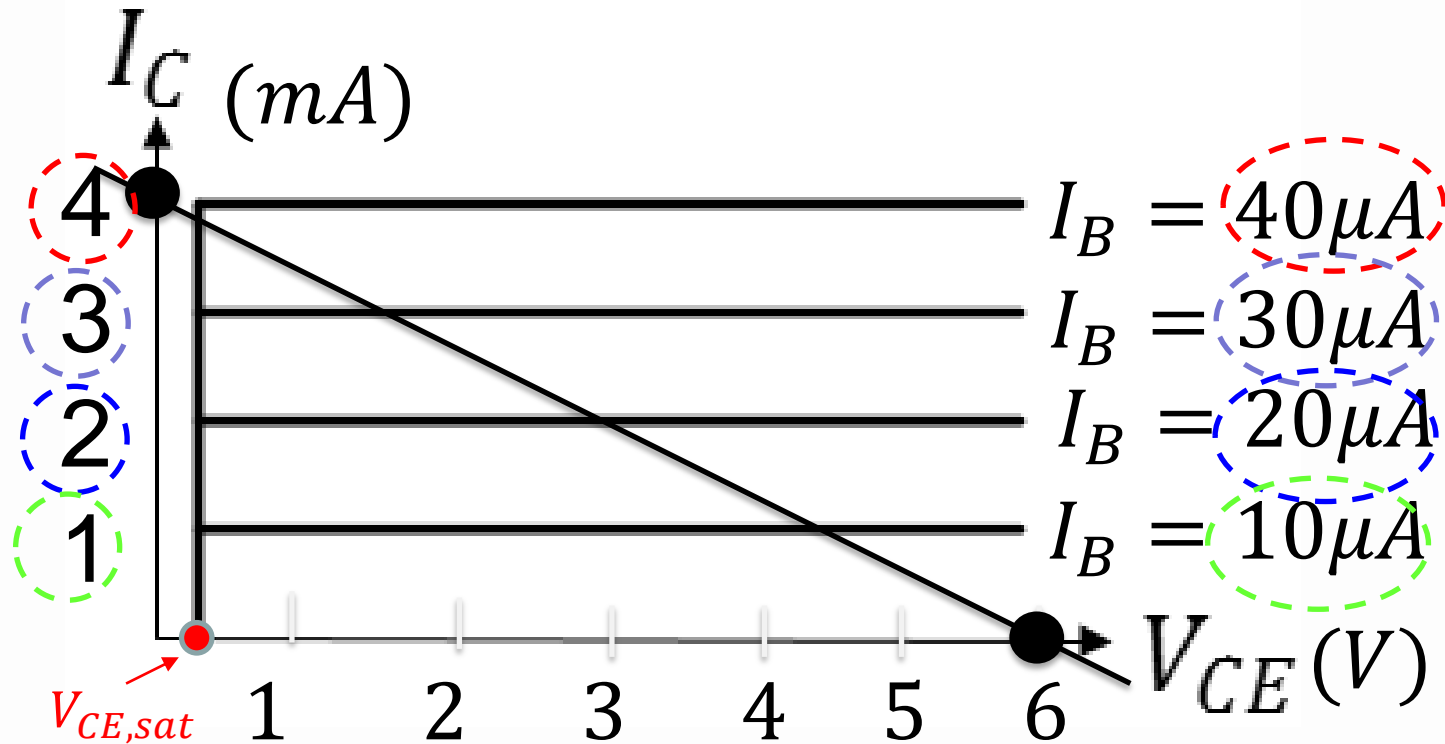
B.  $I_B = 30 \mu A$

C.  $I_B = 20 \mu A$

D.  $I_B = 10 \mu A$

E.  $I_B = 0 \mu A$

# Extracting information from the IV curve(s)



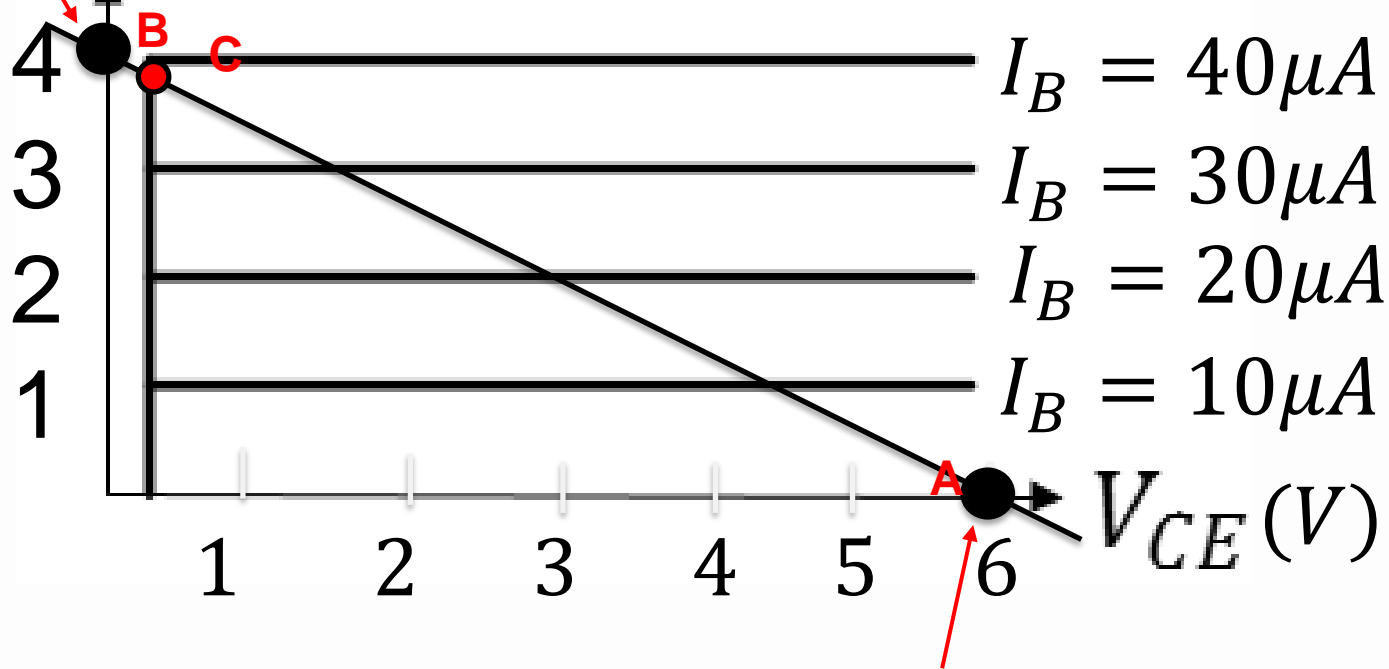
$$\beta = \frac{I_C}{I_B} = \frac{4m}{40\mu} = 100$$

$$V_{CE,sat} \approx 0.3V$$

L20Q2: What is  $\beta$  and  $V_{CE,sat}$ ?

# Extracting information from the IV curve(s)

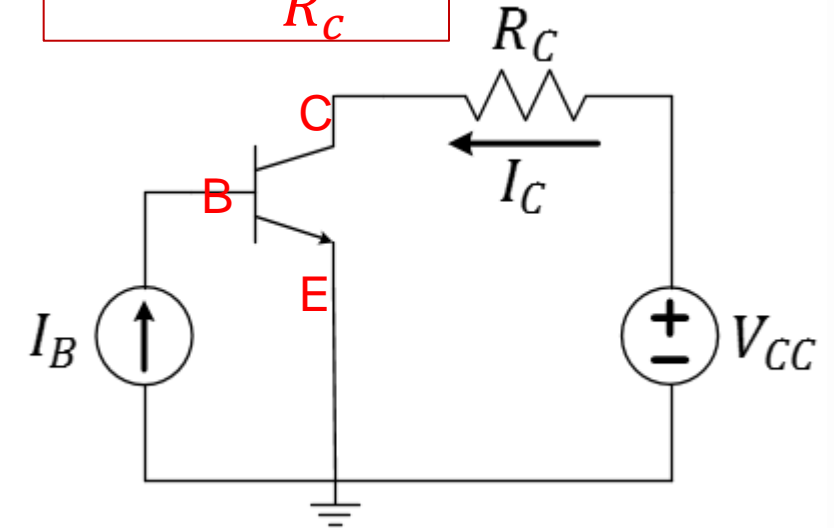
$$I_C = \frac{V_{CC}}{R_C} \rightarrow R_C = \frac{V_{CC}}{I_C} = \frac{6V}{4mA} = 1.5k\Omega$$



L20Q3: What is  $V_{CC}$ ?  
 L20Q4: What is  $R_C$ ?  
 L20Q5: What is  $I_{C,sat}$ ?

When  $V_{CE} = V_{CC}$ ,  $I_C = 0$

$$I_C = \frac{V_{CC} - V_{CE}}{R_C}$$



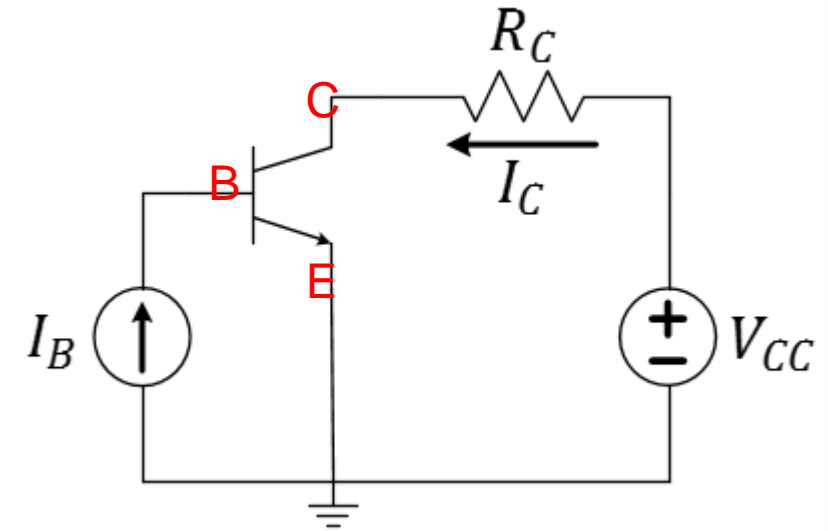
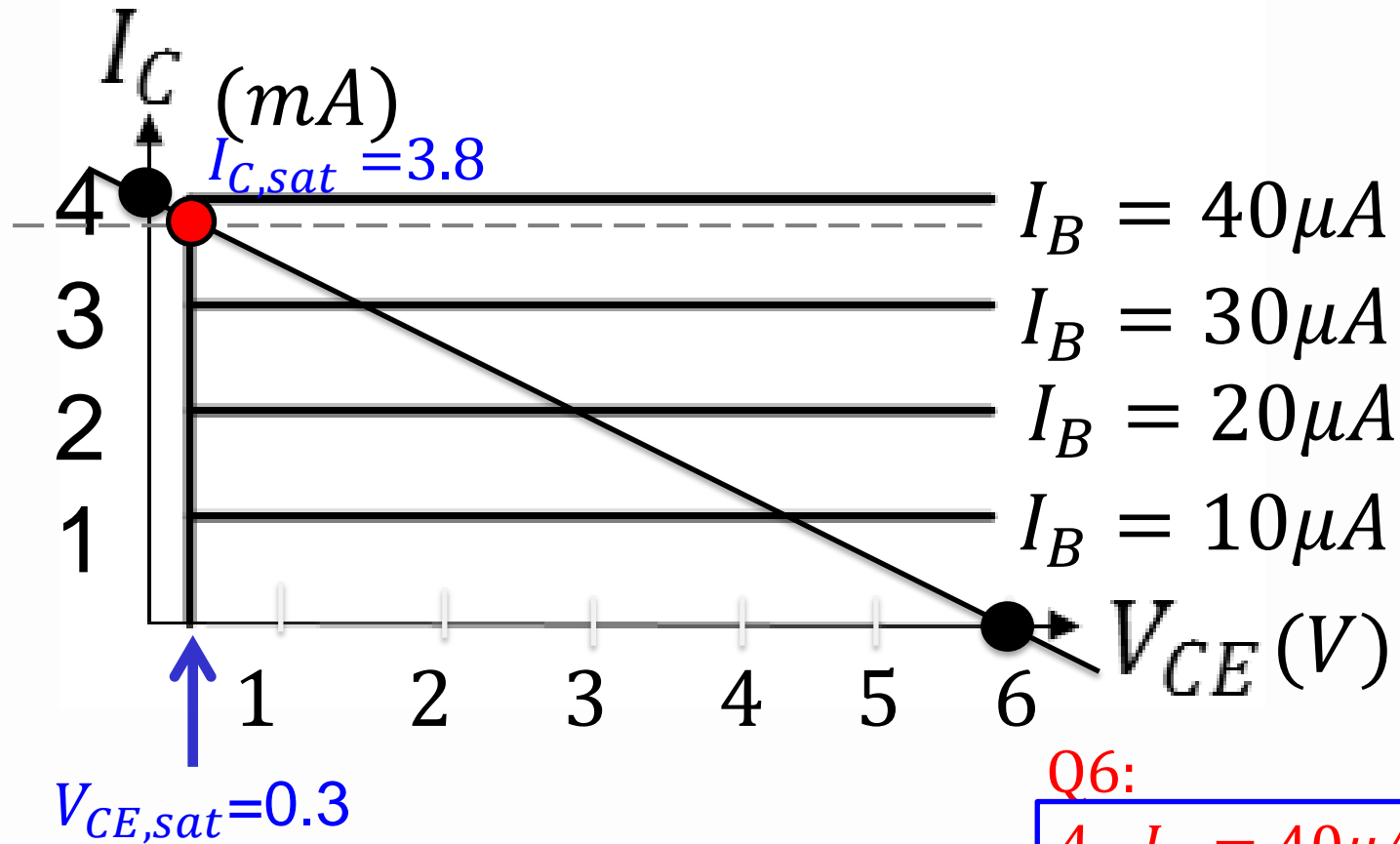
$$V_{CC} = 6V$$

$$R_C = 1.5k\Omega$$

$$I_{C,sat} = \frac{V_{CC} - V_{CE,sat}}{R_C} = \frac{6 - 0.3}{1.5k} = 3.8mA$$



# Extracting information from the IV curve(s)



● (3.8mA, 0.3V)

Q6:

A.  $I_B = 40\mu A$

B.  $I_B = 30\mu A$

C.  $I_B = 20\mu A$

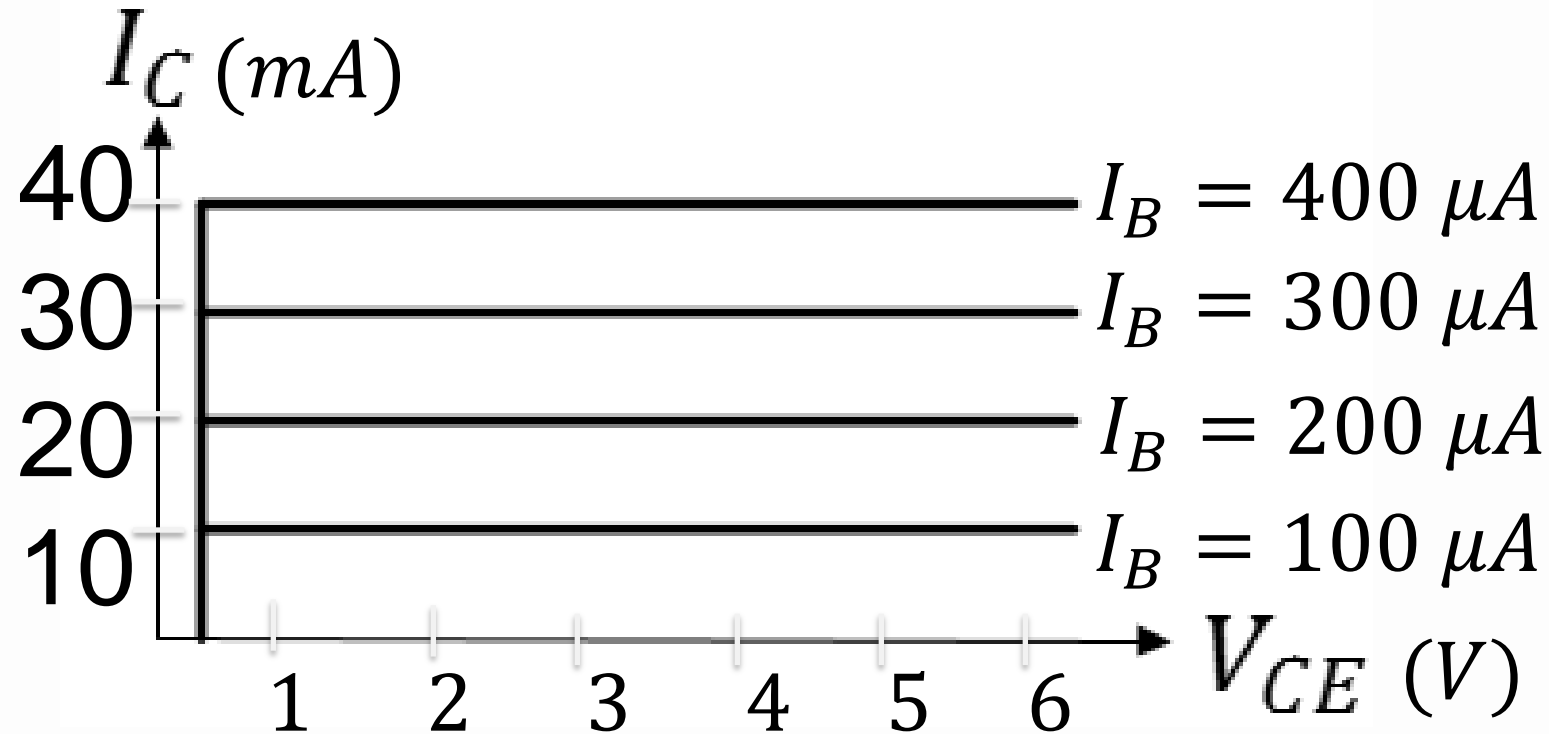
D.  $I_B = 10\mu A$

E.  $I_B = 0\mu A$

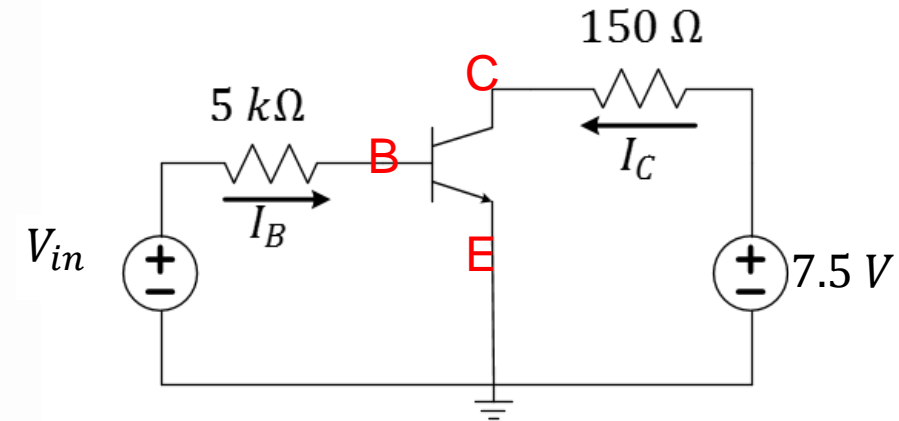
L20Q6: Which  $I_B$  results in saturation?

$$I_{B,sat} \approx \frac{I_{C,sat}}{\beta} = \frac{3.8\text{ mA}}{100} = 38\mu A$$

# BJT Exercise



$$V_{BE,on} = 0.7 V$$



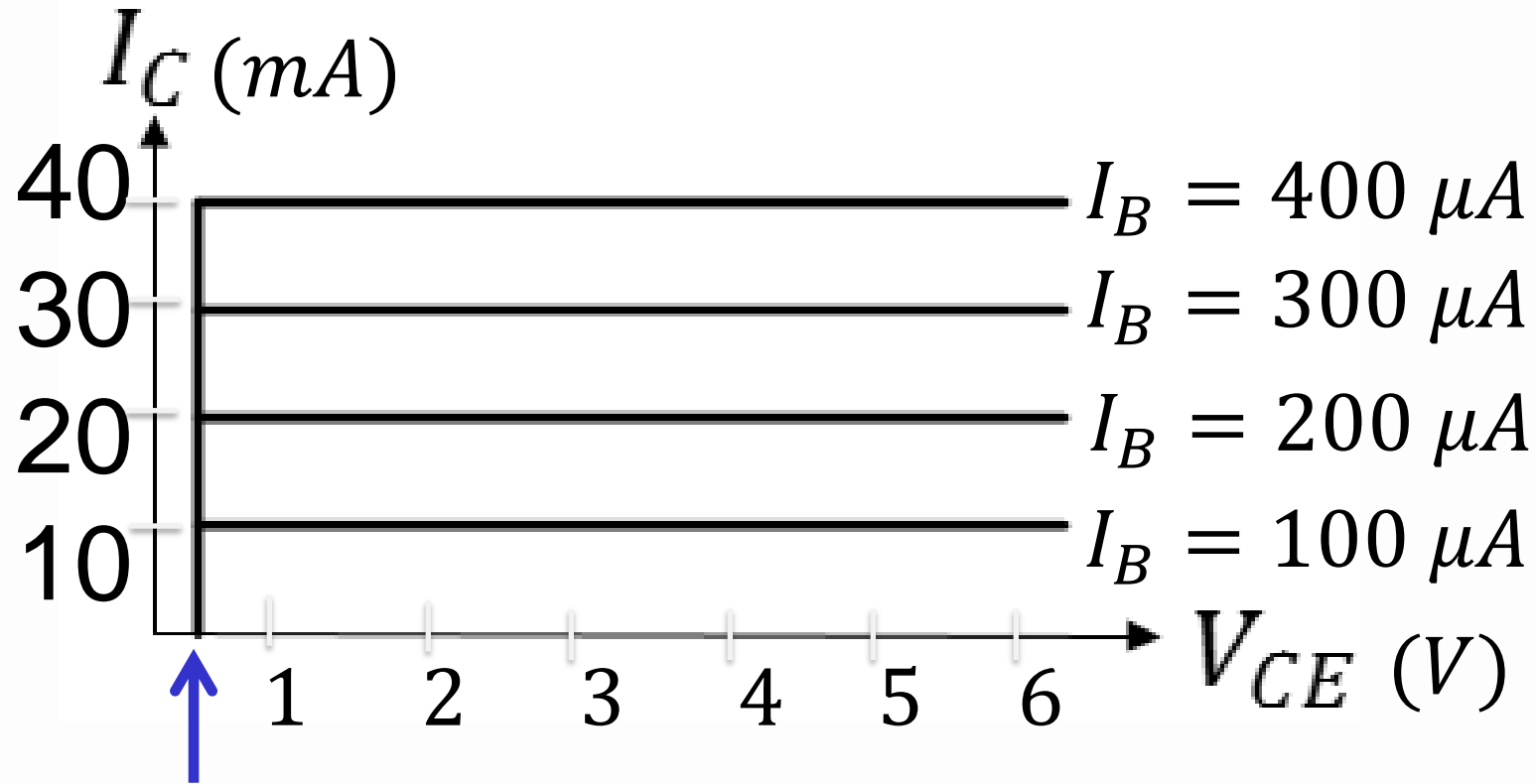
L20Q7: Estimate the operating point ( $I_C, V_{CE}$ ) when  $V_{in} = 1.7 V$ .

L20Q8: What value of  $V_{in}$  would drive the transistor to the edge of saturation?

# Method 1--Analytical

## BJT Exercise

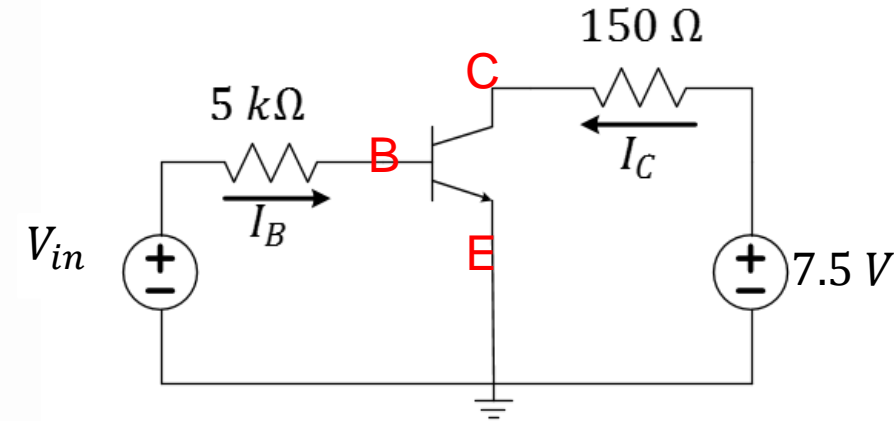
$$V_{BE,on} = 0.7 \text{ V}$$



$$V_{CE,sat} = 0.3$$

L20Q7: Estimate the operating point ( $I_C, V_{CE}$ ) when  $V_{in} = 1.7 \text{ V}$ .

Operating point ( $I_C, V_{CE}$ ) = (20mA, 4.5V)



$V_{in} > V_{BE,on}$ , active or saturation

$$\beta = \frac{I_C}{I_B} = \frac{40 \text{ mA}}{400 \mu\text{A}} = 100$$

$$I_B = \frac{V_{in} - V_{BE,on}}{5 \text{ k}\Omega} = \frac{1.7 \text{ V} - 0.7 \text{ V}}{5 \text{ k}\Omega} = 200 \mu\text{A}$$

$$I_C = \beta I_B = 20 \text{ mA}$$

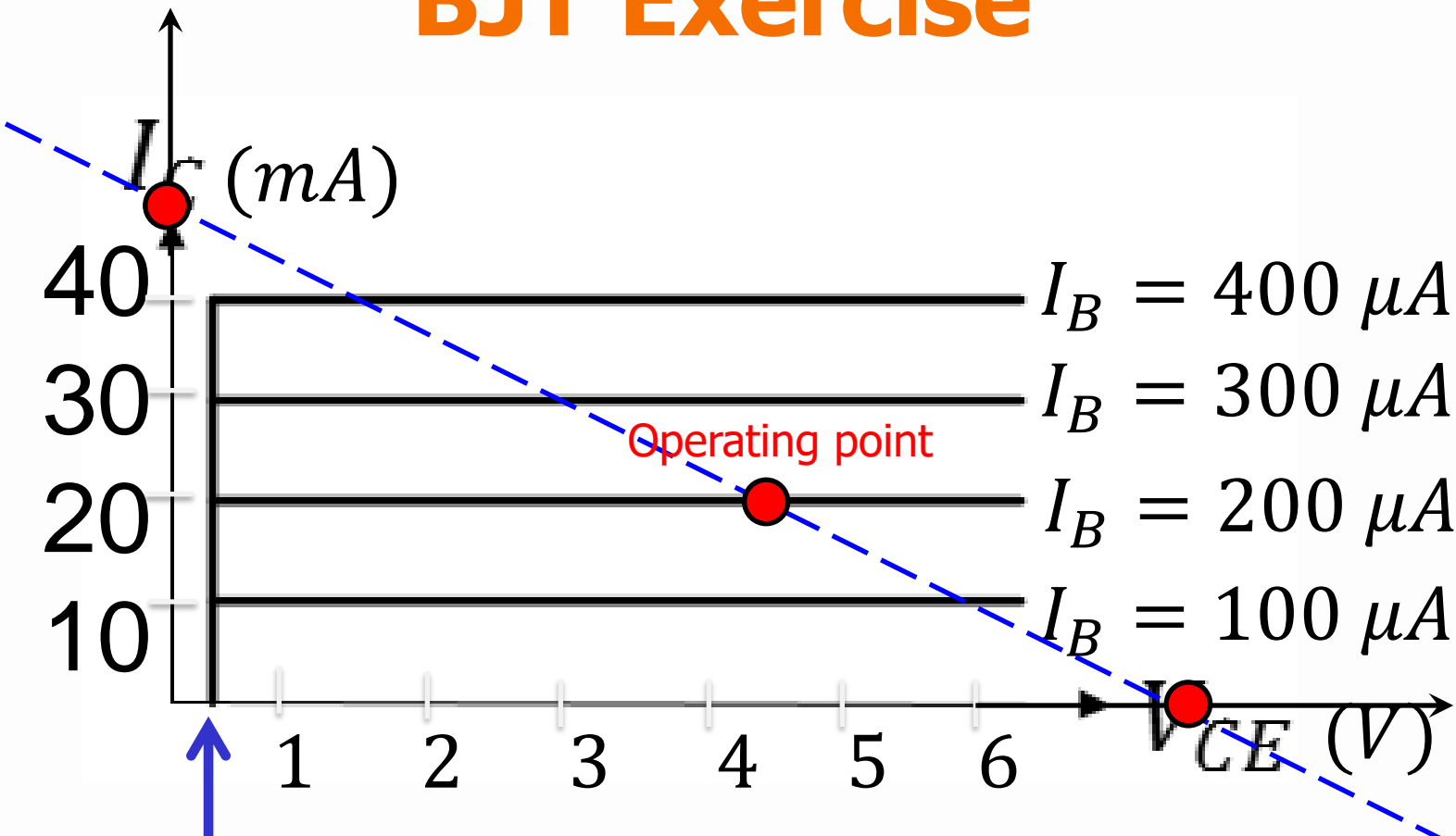
$$V_{CE} = 7.5 \text{ V} - 150 \Omega \times I_C = 4.5 \text{ V}$$

$$V_{CE} > V_{CE,sat}, \text{ active regime}$$

# Method 2--Graphic

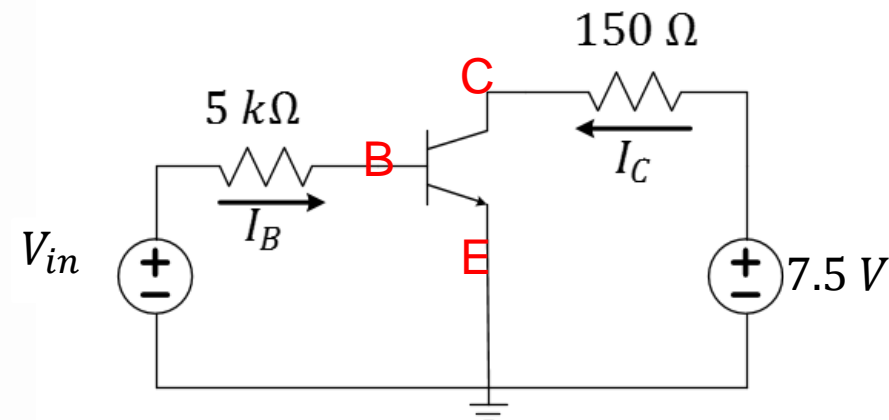
## BJT Exercise

$$V_{BE,on} = 0.7 \text{ V}$$



$$V_{CE,sat} = 0.3$$

L20Q7: Estimate the operating point  $(I_C, V_{CE})$  when  $V_{in} = 1.7 \text{ V}$ .



$$I_B = \frac{V_{in} - V_{BE,on}}{5 \text{ k}\Omega} = \frac{1.7 \text{ V} - 0.7 \text{ V}}{5 \text{ k}\Omega} = 200 \mu A$$

$$I_C = \frac{7.5 - V_{CE}}{150}$$

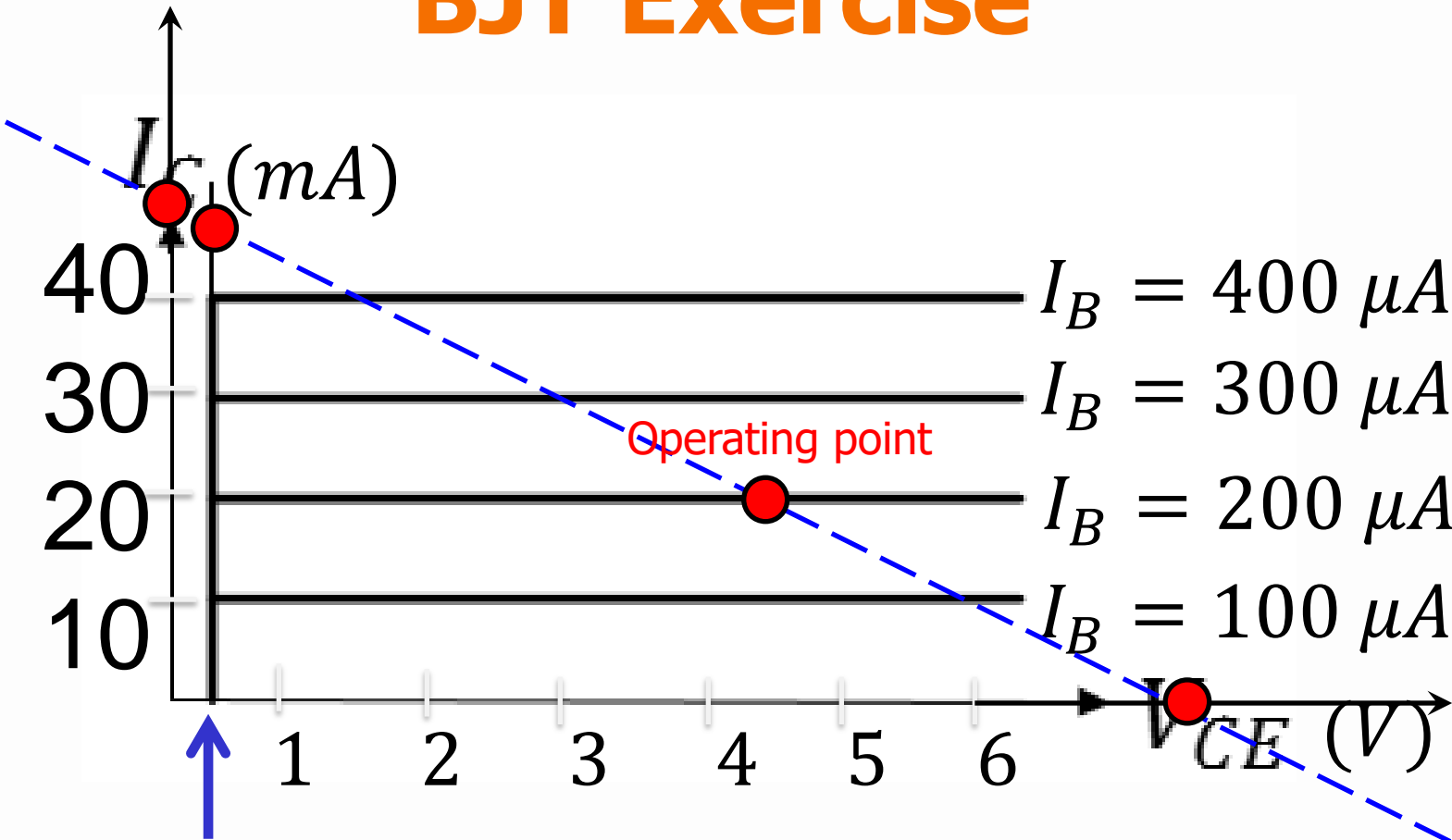
$$V_{CE} = 7.5 - 150 \times I_C$$

Operating point  $(I_C, V_{CE}) = (20 \text{ mA}, 4.5 \text{ V})$

# Method 2--Graphic

## BJT Exercise

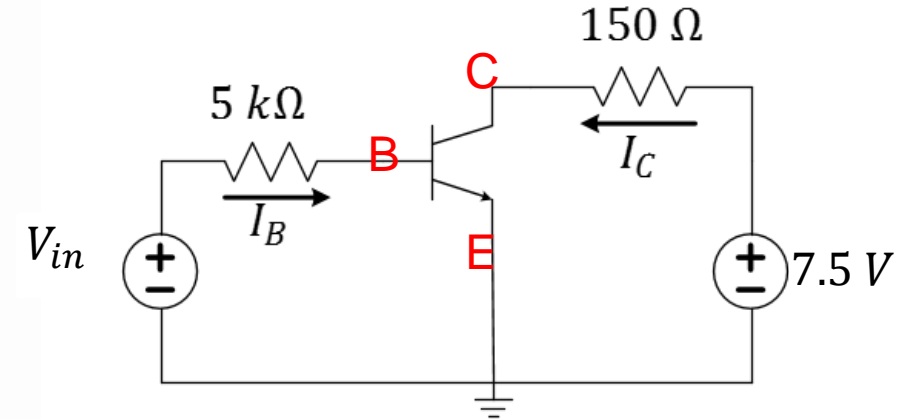
$$V_{BE,on} = 0.7 \text{ V}$$



$$V_{CE,sat} = 0.3$$

L20Q8: What value of  $V_{in}$  would drive the transistor to the edge of saturation?

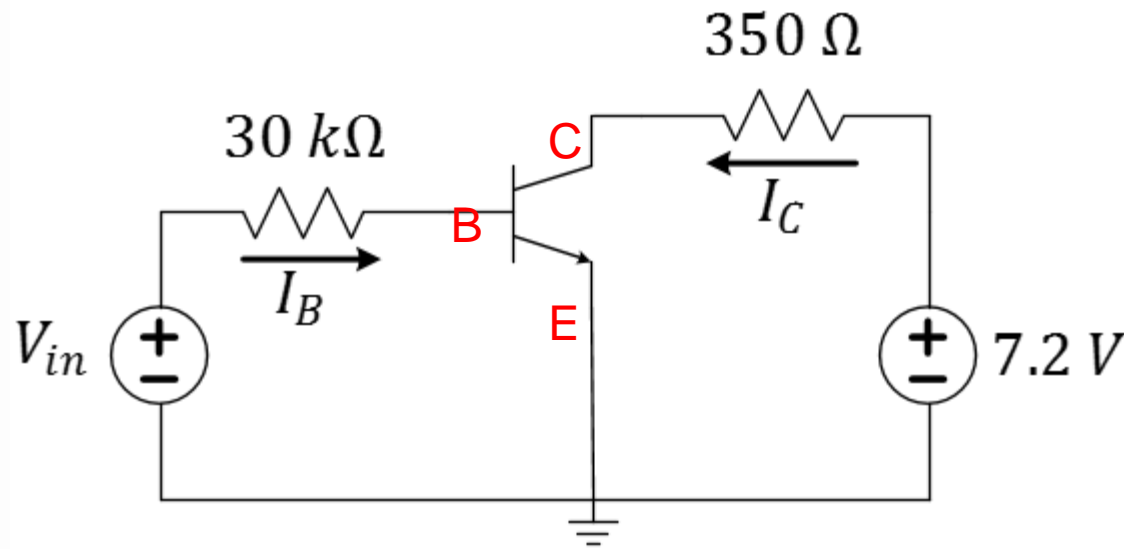
$$I_{C,sat} = (7.5 - 0.3)/150 = 48 \text{ mA} \quad V_{in} = \frac{48 \text{ mA}}{\beta} \times 5 \text{ k}\Omega + 0.7 = 3.1 \text{ V}$$



$$I_B = \frac{V_{in} - V_{BE,on}}{5 \text{ k}\Omega} = \frac{1.7 \text{ V} - 0.7 \text{ V}}{5 \text{ k}\Omega} = 200 \mu A$$

$$I_C = \frac{7.5 - V_{CE}}{150}$$

# BJT Exercise



BJT datasheet parameters:

- $\beta = 100$
- $V_{BE,on} = 0.7 \text{ V}$
- $V_{CE,sat} = 0.2 \text{ V}$

L20Q9: What value of  $V_{in}$  would drive the transistor to the edge of saturation?

L20Q10: How does your answer change if  $30 \text{ k}\Omega$  were replaced with  $60 \text{ k}\Omega$ ?

L20Q11: How does your answer change if, instead,  $350 \Omega \rightarrow 700 \Omega$ ?

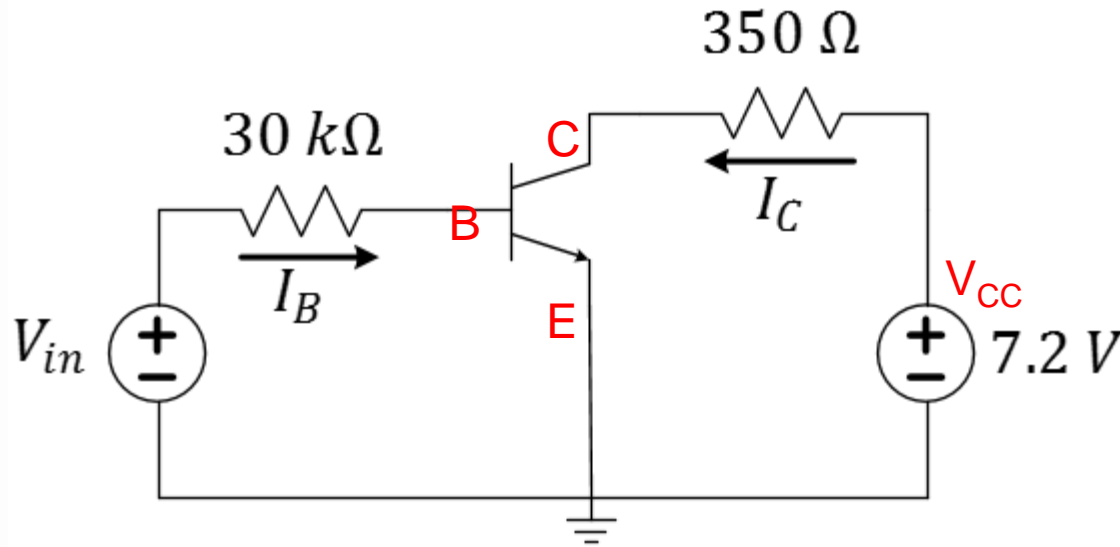
Q10:

- A.  $V_{in@sat}$  goes up
- B.  $V_{in@sat}$  goes down
- C.  $V_{in@sat}$  stays the same

Q11:

- A.  $V_{in@sat}$  goes up
- B.  $V_{in@sat}$  goes down
- C.  $V_{in@sat}$  stays the same

**L20Q9: What value of  $V_{in}$  would drive the transistor to the edge of saturation?**



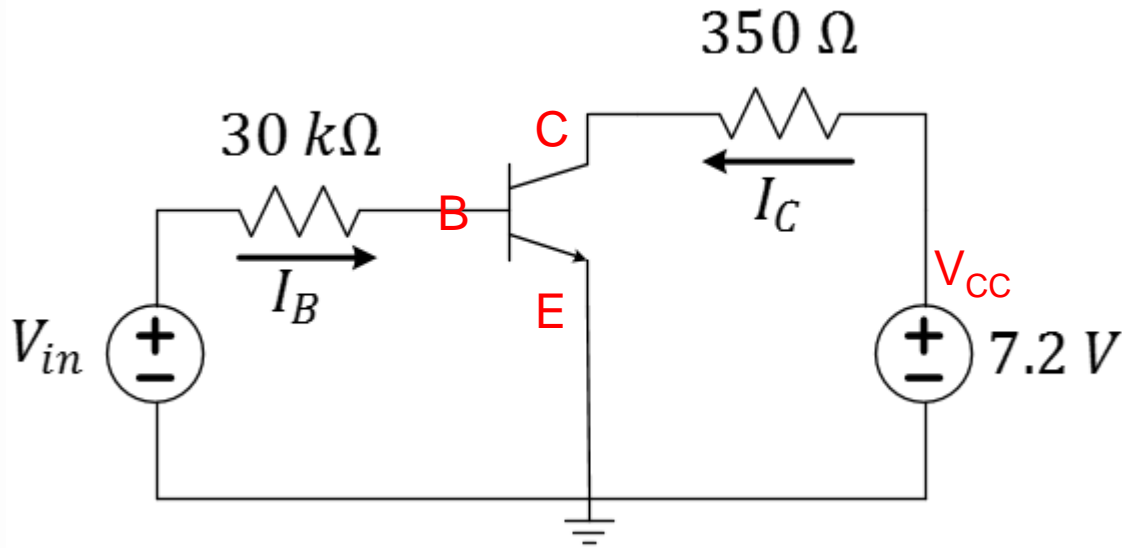
BJT datasheet parameters:

- $\beta = 100$
- $V_{BE,on} = 0.7 V$
- $V_{CE,sat} = 0.2 V$

$$I_{C,sat} = (V_{CC} - V_{CE,sat})/350 = (7.2 - 0.2)/350 = 20mA$$

$$I_{B,sat} = I_{C,sat}/\beta = 200\mu A$$

$$V_{in} = 30k \times I_{B,sat} + V_{BE,on} = 30k \times 200\mu + 0.7 = 6.7V$$



BJT datasheet parameters:

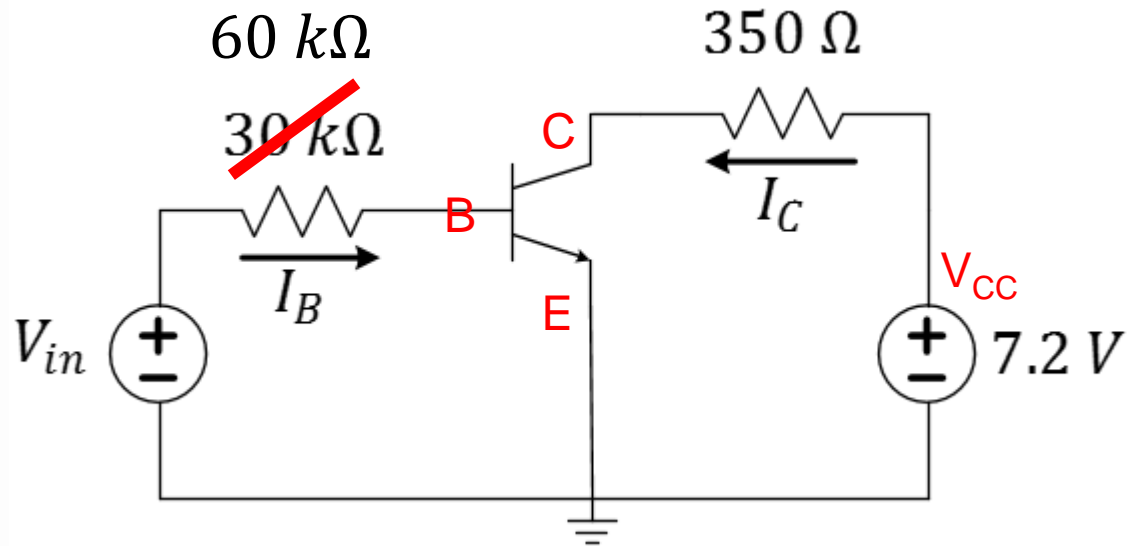
- $\beta = 100$
- $V_{BE,on} = 0.7 V$
- $V_{CE,sat} = 0.2 V$

L20Q10: How does your answer change if  $30 k\Omega$  were replaced with  $60 k\Omega$ ?

Q10:

- A.  $V_{in@sat}$  goes up
- B.  $V_{in@sat}$  goes down
- C.  $V_{in@sat}$  stays the same





BJT datasheet parameters:

- $\beta = 100$
- $V_{BE,on} = 0.7 V$
- $V_{CE,sat} = 0.2 V$

L20Q10: How does your answer change if  $30 k\Omega$  were replaced with  $60 k\Omega$ ?

( $V_{in} - V_{BE,sat}$  has to be double)

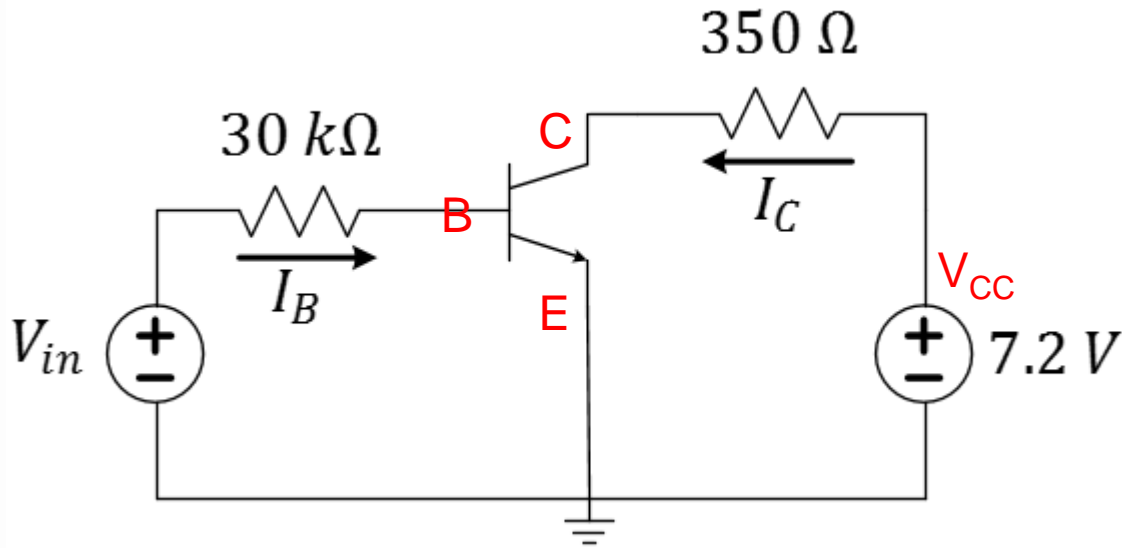
Q10:

- A.  $V_{in@sat}$  goes up
- B.  $V_{in@sat}$  goes down
- C.  $V_{in@sat}$  stays the same

$$I_{C,sat} = (7.2 - 0.2)/350 = 20mA$$

$$I_{B,sat} = I_{C,sat}/\beta = 200\mu A$$

$$V_{in} = 60k \times 200\mu + 0.7 = 12.7V$$



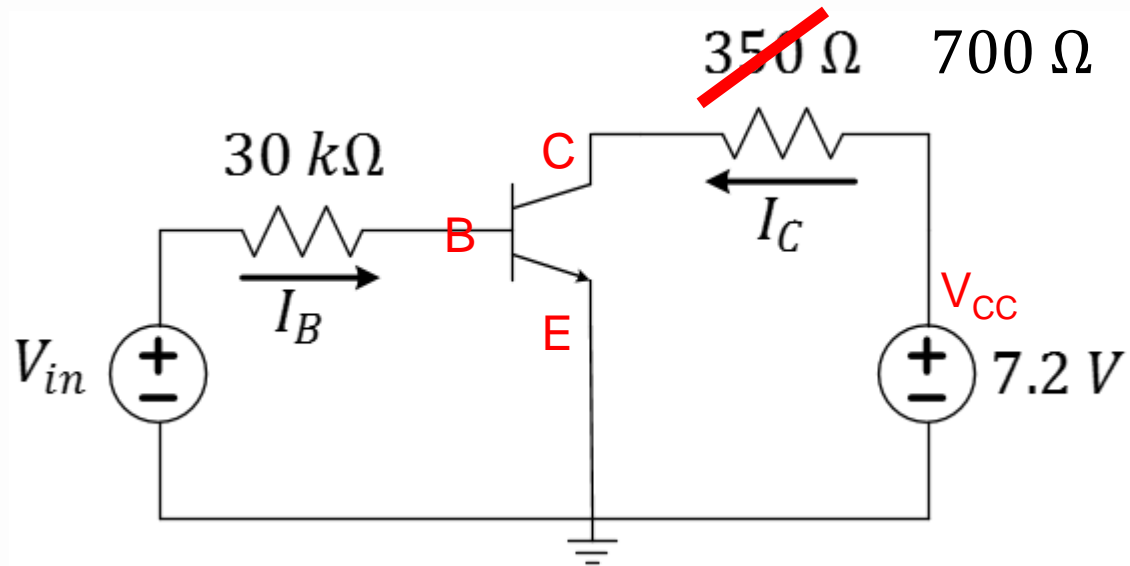
BJT datasheet parameters:

- $\beta = 100$
- $V_{BE,on} = 0.7 V$
- $V_{CE,sat} = 0.2 V$

L20Q11: How does your answer change if, instead,  $350 \Omega \rightarrow 700 \Omega$ ?

Q11:

- A.  $V_{in@sat}$  goes up
- B.  $V_{in@sat}$  goes down
- C.  $V_{in@sat}$  stays the same



BJT datasheet parameters:

- $\beta = 100$
- $V_{BE,on} = 0.7 V$
- $V_{CE,sat} = 0.2 V$

L20Q11: How does your answer change if, instead,  $350 \Omega \rightarrow 700 \Omega$ ?

( $V_{in} - V_{BE,sat}$  has to be half)

Q11:

A.  $V_{in@sat}$  goes up

B.  $V_{in@sat}$  goes down

C.  $V_{in@sat}$  stays the same

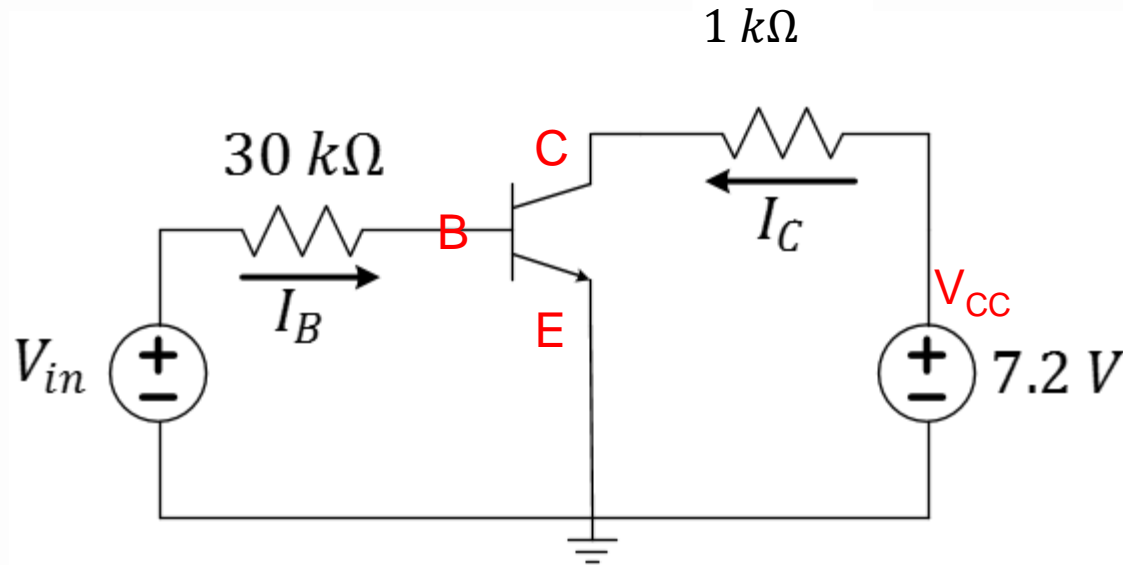
$$I_{C,sat} = (7.2 - 0.2)/700 = 10mA$$

$$I_{B,sat} = I_{C,sat}/\beta = 100\mu A$$

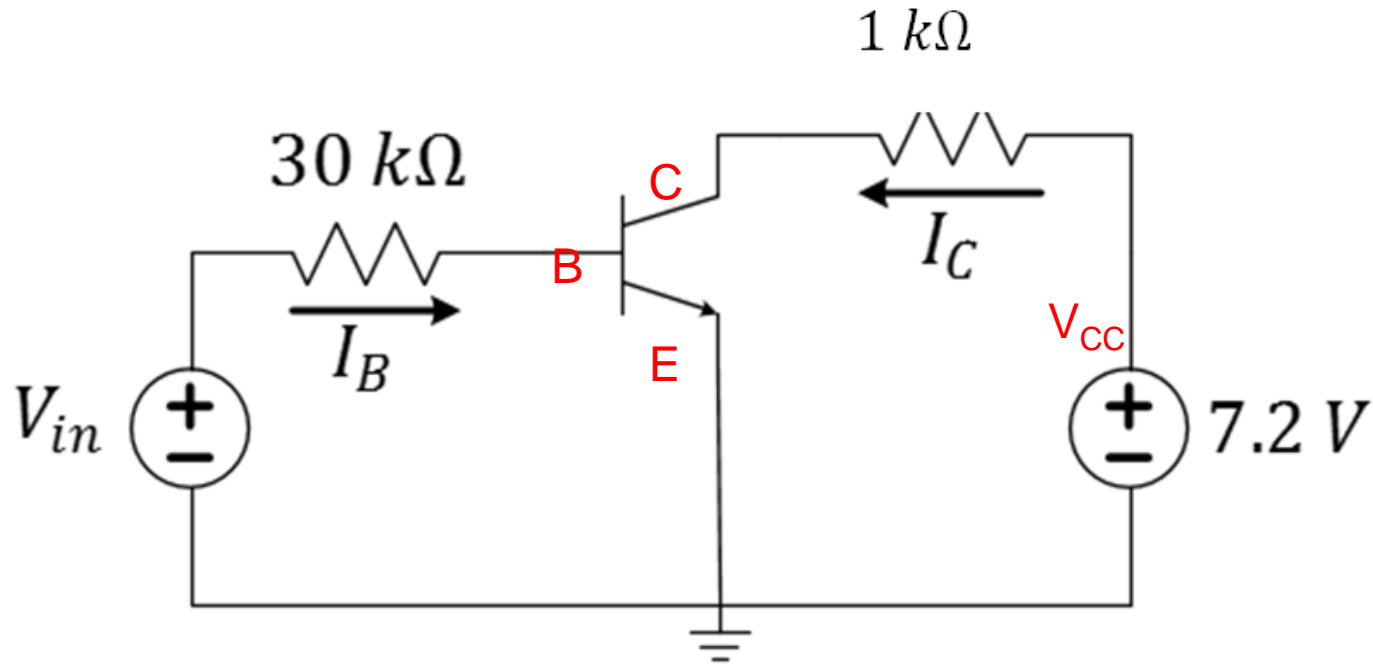
$$V_{in} = 30k \times 100\mu + 0.7 = 3.7V$$

# BJT circuit analysis: working back to $V_{in}$

BJT Datasheet:  $\beta = 100$ ,  $V_{BEon} = 0.7V$ ,  $V_{CE,sat} = 0.2V$



L20Q12: Find  $V_{in}$  such that  $V_{CE} = 3\text{ V}$

**L20Q12: Find  $V_{in}$  such that  $V_{CE} = 3 V$** 

BJT Datasheet:

- $\beta = 100$ ,
- $V_{BEon} = 0.7 V$
- $V_{CE,sat} = 0.2 V$

$V_{CE} > V_{BE,on}$ , working in active regime

$$I_C = (7.2 - 3)/1k = 4.2mA$$

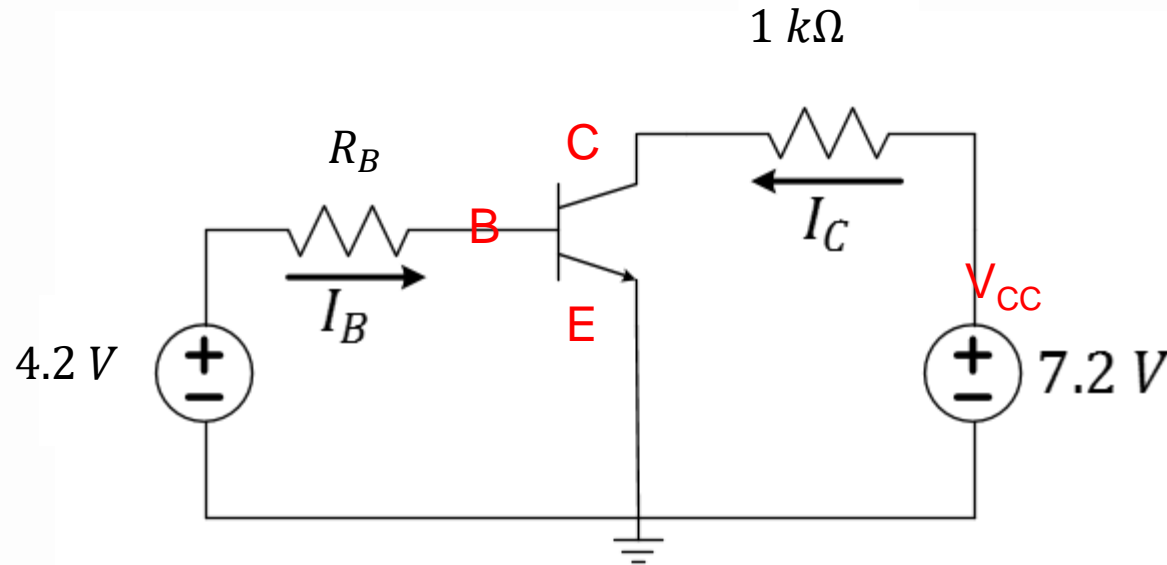
$$I_B = I_C / \beta = 42\mu A$$

$$V_{in} = 30k \times 42\mu + 0.7 = 1.96V$$

# BJT circuit analysis

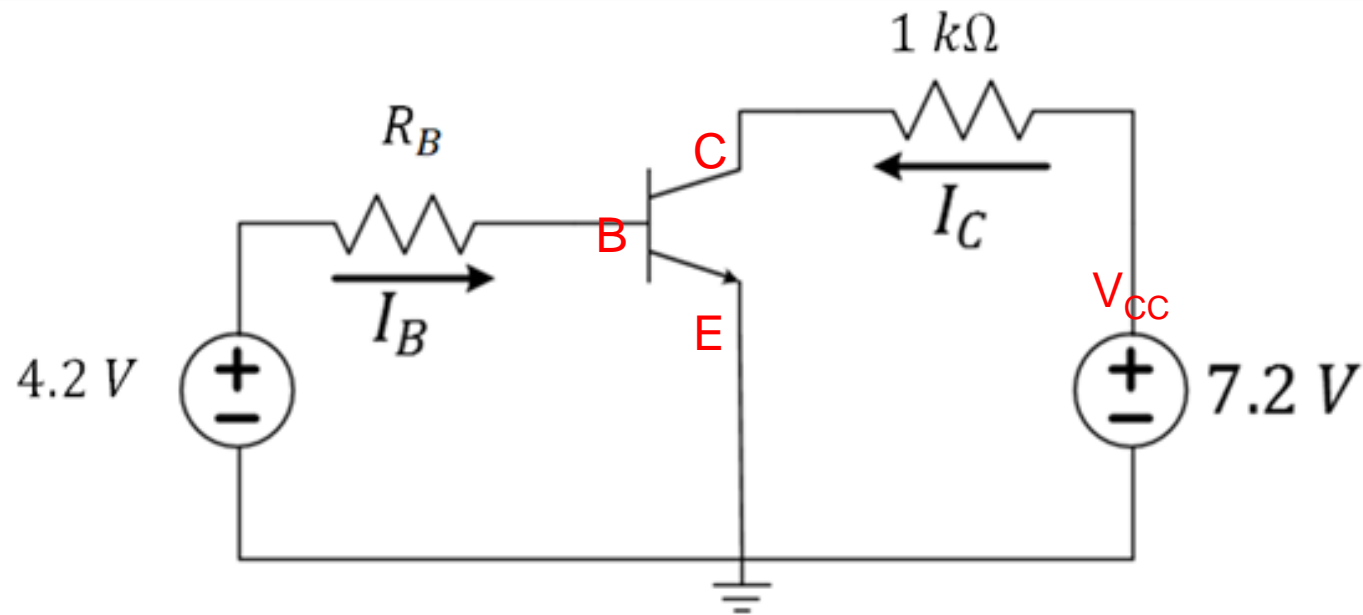
BJT Datasheet:

- $\beta = 100$ ,
- $V_{BEon} = 0.7 \text{ V}$
- $V_{CE,sat} = 0.2 \text{ V}$



L20Q13: Choose  $R_B$  such that the BJT is driven to the edge of saturation.

**L20Q13: Choose  $R_B$  such that the BJT is driven to the edge of saturation.**



BJT Datasheet:

- $\beta = 100$ ,
- $V_{BEon} = 0.7\text{ V}$
- $V_{CE,sat} = 0.2\text{ V}$

$$I_{C,sat} = (7.2 - 0.2)/1k = 7mA$$

$$I_B = I_{C,sat}/\beta = 70\mu A$$

$$R_B = \frac{V_{in} - V_{BEon}}{I_B} = \frac{4.2 - 0.7}{70\mu} = 50k\Omega$$

## L20 Learning Objectives

- a. Find  $\beta$  and  $V_{CE,sat}$  for a given BJT IV characteristic
- b. Find  $V_{CC}$  and  $R_C$  from the IV characteristic of the load line
- c. Compute  $I_{C,sat}$  from  $V_{CC}$ ,  $V_{CE,sat}$ , and  $R_C$
- d. Identify the BJT CE operating point given IV characteristics
- e. Solve numerically for unknown parameters among  $\{V_{in}, R_B, I_B, \beta, V_{BE,on}, V_{CE,sat}, I_C, R_C, V_{CC}, I_{C,sat}\}$  when given some or all of the other values
- f. Determine settings to drive transistor into a desired regime