```
HASKEL
greet :: String -> String
-- greet :: [Char] -> [Char]
greet name = "Hello " ++ name
howLong :: [a] -> Integer
howLona \Gamma1 = 0
howLong(x:xs) = 1 + howLongxs
-- UNION TYPES
-- 'Food' => Type Constructor
-- 'Fruit', 'Dairy', ... => Data Constructors
data Food = Fruit | Dairy | Fishb | MetaData
-- PRODUCT TYPES
data Point2D a = Point2D a a
manhattanDistance
    (Point2D x0 v0)
    (Point2D x1 v1) = (x1 - x0) + (v1 - v0)
p1 = Point2D 0 0
p2 = Point2D 1 1
data Point2D' a = Point2D' {pointX, pointY :: a}
p3 = Point2D' 1 2
-- It gives us two 'selector functions':
-- pointX p3 -> 1
-- pointY p3 -> 2
showJustX (Point2D' x1 y1) = pointX (Point2D' x1
v1)
getJustX Point2D' {pointX = x} = x
-- RECURSIVE TYPES
data Tree a = Leaf a | Branch (Tree a) (Tree a)
mvTree = Branch (Leaf "a")
                (Branch (Leaf "b") (Leaf "c"))
-- SYNONYM TYPES
type MyString = [Char]
name :: MyString
name = "Yuliva"
lst :: [Integer]
lst = (1 : (2 : (3 : [])))
-- Partial functions
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add1 = (1 +)
double = (2 *)
mvList = [1,2,3,4,5]
comp = add1 . double
-- map (add1 . double) myList => [3,5,7,9,11]
-- functions are applied from RIGHT to LEFT:
-- map (double . add1) myList => [4,6,8,10,12]
-- LET for local scope variables
cvlinderArea r h =
  let sideArea = 2 * pi * r * h
      topArea = pi * r ^ 2
   in sideArea + 2 * topArea
-- sum $ map (\x -> double x) myList
-- sum (map (\xspace x) = double x) myList)
-- '@' DESTRUCTURING in pattern matching
-- it keeps the reference to the whole list,
-- the head, and the rest.
showMyList lst@(x : xs) =
    "Head: " ++ show x
    ++ " Rest: " ++ show xs
    ++ " List: " ++ show lst
infList = [1 ..]
finiteList = [1, 3 .. 15]
take5 = take 5 infList
-- List comprehension
evenNums = [x * 2 | x < -[0 ..]]
-- a<sup>2</sup> + b<sup>2</sup> = c<sup>2</sup>
pytagorianTriples = [(a, b, c)
    c <- [1 ..],
    b <- [1 .. c].
    a \leftarrow [1 .. b],
    a ^ 2 + b ^ 2 == c ^ 2]
-- ZIP : takes in parallel one element from each
of two lists
-- and makes a pair out of them
-- zip [1, 2, 3, 4, 5] "ciao"
-- [(1,'c'),(2,'i'),(3,'a'),(4,'o')]
-- BOOLEAN GUARD
calcBMI weight height
     bmi <= underweight = "Underweight"
      bmi < normal = "Normal"</pre>
      bmi < overweight = "Overweight"</pre>
      otherwise = "Obese"
    where
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bmi = weight / height ^ 2
       -- using pattern matching for assignment
       (underweight, normal, overweight) =
(18.5, 25.0, 30.0)
initials firstName lastName = [f] ++ " " ++ [l]
   where
       (f) = head firstName
       (l) = head lastName
initials' firstName lastName = [f] ++ " " ++ [l]
       (f : _) = firstName
       (l : \_) = lastName
ifExample x = [1, if x > 2 then 999 else 0]
-- "CASE"
head' :: [a] -> a
head' [] = error "Empty list"
head'(x: _ ) = x
head'' lst = case lst of
   [] -> error "No head"
   (x : xs) \rightarrow x
-- Forces evaluation of x
-- seg x v -> v
-- myFunc :: Num a => a -> a -> a
-- class Equal a where
-- (==) :: a -> a -> Bool
      x /= y = not (x == y)
data Tree a = Empty | Leaf a | Branch (Tree a)
(Tree a) deriving (Eg. Show)
-- instance (Eq a) => Eq (Tree a) where
      Leaf a == Leaf b = a == b
      Branch l1 r1 == Branch l2 r2 = l1 == l2
&& r1 == r2
   == = False
-- SUBCLASSES can be defined as:
-- class Eq a => Ord a where
-- (<), (<=), (>), (>=) :: a -> a -> Bool
      min. max :: a -> a -> a
-- For custom SHOW create an instance
-- instance (Show a) => Show (Tree a) where
-- show (Leaf a) = show a
```

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show (Branch l r) = "<" ++ show l ++ "|"
++ show r ++ ">"
-- FOLDABLE
-- FOLD <br/>
--
treeFoldr f z Empty = z
treeFoldr f z (Leaf x) = f x z
treeFoldr f z (Branch l r) = treeFoldr f
(treeFoldr f z r) l
instance Foldable Tree where
           foldr :: (a -> b -> b) -> b -> Tree a -> b
           foldr = treeFoldr
-- `foldl` can be expressed in terms of `foldr`
-- as 'foldr' can work on infinite lists, while
-- `foldl` cannot.
foldl f a bs = foldr (\b g x -> g(f x b)) id bs
-- instance Foldable Maybe where
                 foldr _ z Nothing = z
                 foldr f z (Just x) = f x z
data Result a = Err | Ok a deriving (Eq. Ord,
Show)
safediv :: Int -> Int -> Result Int
safediv n m =
          if m == 0
                    then Err
                    else Ok (n 'div' m)
-- FUNCTOR
instance Functor Tree where
          fmap :: (a -> b) -> Tree a -> Tree b
          fmap Empty = Empty
          fmap f (Leaf x) = Leaf (f x)
          fmap f (Branch l r) = Branch (fmap f l)
(fmap f r)
instance Functor Result where
          fmap :: (a -> b) -> Result a -> Result b
          fmap _ Err = Err
          fmap f (0k x) = 0k (f x)
-- we can call fmap with an infix notation as "f
<$> t"
-- APPLICATIVE
instance Applicative Result where
           (<*>) :: Result (a -> b) -> Result a ->
          pure x = 0k x -- wraps an argument in our
structure
          <*> Err = Err
          Err <*> _ = Err
           (0k f) <*> (0k x) = 0k (f x)
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```
-- (0k f) <*> x = f <$> x
-- instance Applicative Tree where
      (<*>) :: Tree (a -> b) -> Tree a -> Tree
       pure x = Leaf x
       - <*> Empty = Empty
       Empty <*> = Empty
       (Leaf f) <*> (Leaf x) = Leaf (f x)
       (Leaf f) <*> (Branch l r) = Branch (Leaf
f <*> l) (Leaf f <*> r)
      (Branch f g) <*> (Leaf x) = Branch (f <*>
Leaf x) (\alpha < *> Leaf x)
-- (Branch f g) <*> (Branch l r) = Branch (f
<*> l) (q <*> r)
-- Tree concatenation
tconc Emptv t = t
tconc t Empty = t
tconc t1 t2 = Branch t1 t2
tconcat t = foldr tconc Empty t
tconcmap f t = tconcat (fmap f t)
-- for lists concatMap f l = concat (map f l)
instance Applicative Tree where
    pure x = Leaf x
    (<*>) :: Tree (a -> b) -> Tree a -> Tree b
    fs <*> xs = tconcmap (\f -> fmap f xs) fs
-- instance Applicative [] where
       pure x = [x]
       fs <*> xs = concatMap (\f -> map f xs) fs
APPLICATIVE RULES:
pure id <*> v = v
Identity
pure f <*> pure x = pure (f x)
Homomorphism
u < *> pure v = pure ($ v) < *> u
Interchange
pure (.) <*> u <*> v <*> w = u <*> (v <*> w) --
Composition
--}
data Result a = Ok a | Err deriving (Eq. Show)
data Expr = Val Int | Div Expr Expr deriving
(Eq. Show)
eval :: Expr -> Int
eval (Val n) = n
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eval (Div x y) = eval x 'div' eval y
ex1 = Div (Val 4) (Val 2)
ex2 = Div (Val 4) (Val 0)
safeDiv :: Int -> Int -> Result Int
safeDiv n m =
   if m == 0
       then Err
        else Ok (n 'div' m)
eval' :: Expr -> Result Int
eval' (Val n) = 0k n
eval'(Div x v) =
    case eval' x of
        Err -> Err
        Ok x -> case eval' v of
            Err -> Err
            Ok v -> safeDiv x v
-- eval' (Div x y) = eval x `safeDiv` eval y
bind :: Result Int -> (Int -> Result Int) ->
Result Int
m `bind` f = case m of
   Frr -> Frr
    0k x \rightarrow f x
eval'' :: Expr -> Result Int
eval'' (Val n) = 0k n
eval'' (Div x v) =
    eval'' x `bind` (\n -> eval'' v `bind` \m ->
safeDiv n m)
mEval :: Expr -> Result Int
mEval (Val n) = 0k n
mEval (Div x v) = do
    n <- mEval x
    m <- mEval v
    safeDiv n m
instance Functor Result where
    fmap f (0k x) = 0k (f x)
    fmap Err = Err
instance Applicative Result where
    pure = 0k
    _ <*> Err = Err
    Err <*> = Err
    0k f < *> 0k x = fmap f (0k x)
instance Monad Result where
   return = pure
   Err >>= _ = Err
    0k \times >>= f = f \times
1. LEFT IDENTITY: 'return x >>= f' == 'f x'
```

```
2. RIGHT IDENTITY: 'm >>= return' == 'm'
3. ASSOCIATIVITY: `(m >>= f) >>= g` ==
                  m >= (\x -> f x >= q)
--}
square x = x ^2
addOne x = x + 1
x = addOne (square 2)
data NumberWithLogs = NumberWithLogs
    number :: Int,
    logs :: [String]
    deriving (Eq. Show)
square1 :: Int -> NumberWithLogs
square1 x = NumberWithLogs (x^2) ["Squared" ++
show x ++ " to get " ++ show (x^2)]
square2 :: NumberWithLogs -> NumberWithLogs
square2 x = NumberWithLogs (number x ^ 2) $ logs
x ++ ["Squared " ++ show (number x) ++ " to get
" ++ show (number x ^ 2)]
addOne1 :: Int -> NumberWithLogs
addOne1 x = NumberWithLogs (x + 1) ["Added 1 to
" ++ show x ++ " to get " ++ show (x + 1)]
addOne2 :: NumberWithLogs -> NumberWithLogs
addOne2 x = NumberWithLogs (number <math>x + 1) (logs
x ++ ["Added 1 to " ++ show (number x) ++ " to
get " ++ show (number x + 1)])
wrapWithLogs :: Int -> NumberWithLogs
wrapWithLogs x = NumberWithLogs x []
runWithLogs :: NumberWithLogs -> (Int ->
NumberWithLogs) -> NumberWithLogs
runWithLogs input transform =
    let newNumberWithLogs = transform (number
input)
        in NumberWithLogs
            (number newNumberWithLogs)
            (logs input ++ logs
newNumberWithLogs)
a = wrapWithLogs 2
b = runWithLogs a square1
c = b `runWithLogs` addOne1
```