

Problem 1 Cryptic Connection

Describe what `func1` and `func2` do in the following Python program, what the value of the last expression in the program is, and why we might be interested in that value. (*Hint:* It may be helpful to copy this code into a notebook cell and run it, modifying it or putting in `print()` statements to see how it works. To do that, you'd need to generate your own test tables `t1` and `t2` with some made-up data.)

```
def func1(t, c, v):
    for i in np.arange(t.num_rows):
        rv = t[c][i]
        if rv == v:
            return t.rows[i]
    return False

def func2(t1, c1, t2, c2):
    cs = t1.column_labels + t2.column_labels
    ics = [[]]*len(cs)
    t = Table(ics, cs)
    for i in np.arange(t1.num_rows):
        v = t1[c1][i]
        r1 = t1.rows[i]
        r2 = func1(t2, c2, v)
        if r2 is not False:
            t.append(r1 + r2)
    return t

# Has 2 columns: 'date' and 'number of ice cream cones sold'
t1 = Table.read_table('ice_cream_sales.csv')
# Has 2 columns: 'the date' and 'peak temperature (celcius)'
t2 = Table.read_table('weather.csv')
func2(t1, 'date', t2, 'the date')
```

Problem 2 Bernoulli Ballots

A polling organization reports that 42% of voters in a state will vote for Candidate A. Assume that their report is based on a random sample of 1500 voters in the state, and that the method of sampling is essentially equivalent to sampling with replacement. Construct an approximate 90%-confidence interval for the percent of the state's voters who will vote for Candidate A.

Problem 3 Fickle Functions

Imagine that you have two Python functions, `f` and `g`, each taking a single real (floating-point) number as its argument and returning a real number. For example, you could imagine that `f` is the function `math.exp` and `g` is the function `math.sin`. Say that you would like to know how dissimilar `f` and `g` are – the “distance” between them, in some sense.

There are lots of ways to measure distance between functions, but one simple way is to ask: Across a range of possible inputs `x` to `f` and `g`, what is the maximum difference between `f` and `g`? In other words,

what is the biggest value of $|f(x) - g(x)|$ across a range of possible values of x ? This notion of distance between functions is called the *Chebyshev distance* (yes, that Chebyshev!) or more commonly today the max-norm distance. The Kolmogorov-Smirnov distance between two distributions is just the max-norm distance between their CDFs, so you already computed a max-norm distance in lab 7. In this problem and the two after it, we'll explore that a bit more, starting with something simple. First, *describe the following functions*:

- (a)

```
def what(an_array, a_number):
    return np.count_nonzero(an_array <= a_number) / len(an_array)
```
- (b)

```
def hmm(an_array):
    def result_func(input):
        return what(an_array, input)
    return result_func
```

Problem 4 More Max-Norms

This problem continues the previous problem. Describe the following functions. In each case, assume that an argument with a name like `func<something>` is a function that takes a floating-point number as its argument and returns a floating-point number. Any other argument is a floating-point number. *Hint*: Once you figure out a function's purpose, it may be useful to give it a more informative name and substitute that name where the function appears later. *Hints II: Afterhints*: If you're confused about how defining a function inside another function (and returning that function) works, try it out yourself. Start with a very simple function, define another function inside it, and convince yourself that nothing breaks.

- ```
def something(func1, func2):
 def result_func(input):
 return func1(input) - func2(input)
 return result_func
```
- ```
def something_else(func):
    def result_func(input):
        return abs(func(input))
    return result_func
```
- ```
def another_thing(func, lowest_input, highest_input):
 NUM_TICKS = 100000
 tick_length = (highest_input - lowest_input) / NUM_TICKS
 values = []
 for input in np.arange(lowest_input, highest_input, tick_length):
 values.append(func(input))
 return max(values)
```
- ```
def final_thing(func1, func2, lowest_input, highest_input):
    return another_thing(something_else(something(func1, func2)), \
        lowest_input, highest_input)
```
- Write Python code that defines a function named `approximate_ks_distance`. It takes two arguments, each one an array of numbers forming a dataset, and returns the approximate KS distance between the empirical distributions of those two datasets. *Hint*: You may want to use one or several of the

functions defined above in the previous problem or this problem. *The Hint: Part II:* Those functions are pretty powerful tools. The staff solutions were only a few lines long.

Problem 5 Groovy Graphs

Draw the graphs that appear when the following code is run. (Feel free to investigate plotting in general on your computer, but please don't just copy this exact code into a notebook and draw what you see. That's lame.) Parts of this problem use code from the previous two problems. *Assume that the function definitions in the previous two problems have been executed before this code runs.*

Note: We've seen `plots.xlabel(<some string>)` and `plots.ylabel(<some string>)` before, but for reference: When you call them, they modify the most recent plot you created, putting the *string* you pass as an argument as a label on the x or y axis, respectively.

```
1.  def f(x):
        return 2*x
    ticks = np.arange(-1.0, 2.0, 0.1)
    t = Table([ticks], ['x'])
    t['f(x)'] = t.apply(f, 'x')
    t.plot('x')
    plots.xlabel('x')
    plots.ylabel('f(x)')

2.  t['something_else(f)(x)'] = t.apply(something_else(f), 'x')
    t.select(['something_else(f)(x)', 'x']).plot('x')
    plots.xlabel('x')
    plots.ylabel('something_else(f)(x)')
```

Problem 6 Buggy Bootstrap?

A wise old man wants to know the average length of the hairs in his long beard. To measure them, he has to pluck them out, so he wants to measure only a few. Being a good statistician, he carefully takes a simple random sample of 100 hairs (you can assume they're taken with replacement), plucks them, measures them, and places the lengths in a *column* named `length` in a *table* called `hair`. However, his Python is a little rusty (in the last few years he has jumped on the Scala bandwagon), and he runs the following code to estimate a 99.2% confidence interval for the average length of hairs in his beard. He intends for the last line of code to evaluate to a two-element list, where the 0th element is the left side of the 99.2% confidence interval, and the 1st element is the right side of that interval. Find as many bugs as you can in the code, and describe how you would fix each one.

```
REPETITIONS = 10000
actual_mean = np.mean(hair)
bootstrap_means = []
for rep in REPETITIONS:
    resample = hair.sample()
    resample_mean = np.mean(resample)
    bootstrap_means.append(resample_mean)
left_side_index = int((1 - .992)*REPETITIONS)
right_side_index = int(.992*REPETITIONS)
[bootstrap_means[left_side_index], bootstrap_means[right_side_index]]
```

Problem 7 Pessimistic Polling

Suppose you are going to conduct an opinion poll based on a sampling scheme that is approximately the same as sampling at random with replacement. What is the minimum sample size that will ensure that 95%-confidence intervals for population proportions will have a total width of 0.04 or less? *Hint:* Yes, you can answer this question.

STAT/CS 94 Fall 2015 Adhikari

HW09, Due: 11/4/15

NAME:

SID:

Problem 1 Cryptic Connection

Problem 2 Bernoulli Ballots

Problem 3 Fickle Functions

(a)

(b)

Problem 4 More Max-Norms

(a)

(b)

(c)

(d)

(e) `def approximate_ks_distance(dataset1, dataset2):`

Problem 5 Groovy Graphs

(a)

(b)

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Problem 7 Pessimistic Polling