

**INSTRUCTIONS**

- You have 50 minutes to complete the exam.
- The exam is closed book, closed notes, closed computer, closed phone, and closed calculator, except one hand-written 8.5" × 11" crib sheet of your own creation and the official study guide provided with the exam.
- Mark your answers **on the exam itself**. We will *not* grade answers written on scratch paper.

|                     |  |
|---------------------|--|
| First name          |  |
| Last name (Surname) |  |
| NetID               |  |

# 1. (12 points) Expressions

- (a) (10 pt) An array of integers named `ca` contains the (estimated) population of California every 10 years. It has 11 items. The first item is the population of California in 1900. The last is the population in 2000.

```
array([ 1485053,  2377549,  3426861, ..., 23667902, 29760021, 33871648])
```

Write a Python expression below each of the following descriptions that computes its value. The first one is provided as an example. Do not include numbers above (e.g., 1485053) in your solutions.

- The population in 1900.  
`ca.item(0)`
- The population change from 1940 to 1960, expressed as a number of persons (not a proportion).
- Whether the population ever grew by less than 500000 in a decade represented by `ca`. (**True** or **False**)
- The *annual* (yearly) growth rate from 1920 to 1930.
- The population in 1924, assuming a fixed exponential annual growth rate from 1920 to 1930.  
*You may use the name  $g$  for the annual growth rate from 1920 to 1930 (computed above).*
- The number of items in `ca` that are at least twice as large as the population in 1960.

- (b) (2 pt) You have 1000 different shirts in your huge closet, but only 2 of them are red. Each morning, you pick one uniformly at random, wear it, then put it back at night. Write a Python expression to compute the chance that, during a 30-day month, you *never* wear a red shirt.

**2. (10 points) Tables**

- (a) **(2 pt)** The table named `twins` has a row for each pair of twins that contains the height of each twin in inches. The following code computes the average absolute difference in heights among the twins.

```
def diff(height1, height2):
    return abs(height1 - height2)
diffs = Table(['Absolute Differences'])
for i in np.arange(twins.num_rows):
    diffs.append([diff(twins.column(0).item(i), twins.column(1).item(i))])
np.mean(diffs.column(0))
```

Complete the expression below to compute the same result **without calling diff or using a for statement**.

`np.mean(_____)`

- (b) **(8 pt)** Each row of the `trip` table from lecture describes a single bicycle rental in the San Francisco area. Durations are integers representing times in seconds. The first three rows out of 338343 appear below.

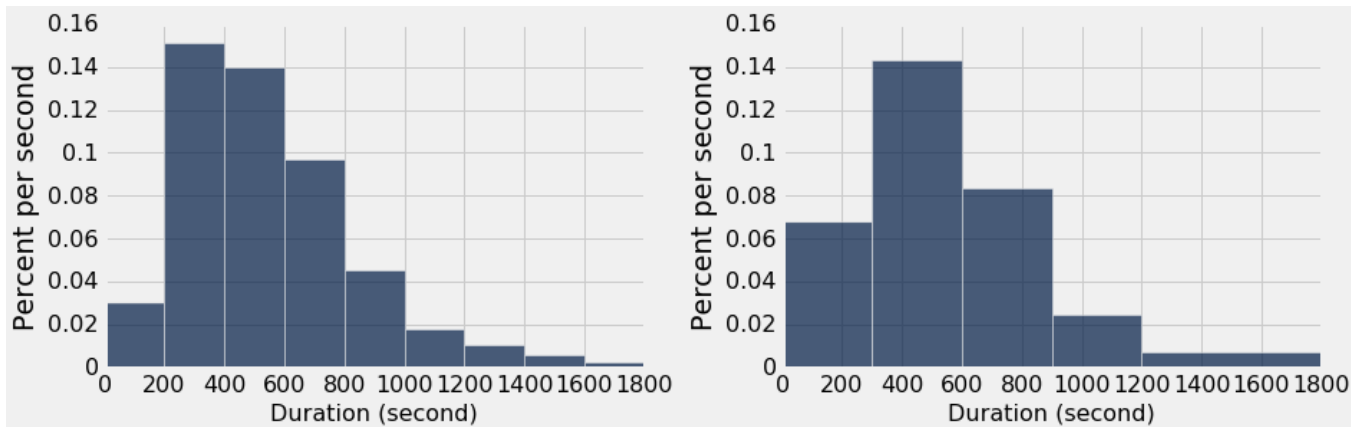
| Start                       | End                     | Duration |
|-----------------------------|-------------------------|----------|
| Ferry Building              | SF Caltrain             | 765      |
| San Antonio Shopping Center | Mountain View City Hall | 1036     |
| Post at Kearny              | 2nd at South Park       | 307      |

Write a Python expression below each of the following descriptions that computes its value. You *may* use up to two lines and introduce variables.

- The average duration of a rental that lasted more than 2 minutes.
- The number of rentals that started at the `SF Caltrain` station.
- The name of the station where the most rentals ended (assume no ties).
- The number of stations for which the average duration ending at that station was at least 300 seconds.

### 3. (11 points) Distributions

The two histograms of bike trip durations below were both generated by `trip.hist(...)` using different bins.



(a) (8 pt) Write the proportion of trips that fall into each range of durations below. *Show your work.* If it is not possible to tell from the histograms, instead write **Not enough information**.

- Between 200 (inclusive) and 400 (exclusive) seconds
  
- Between 300 (inclusive) and 900 (exclusive) seconds
  
- Between 400 (inclusive) and 900 (exclusive) seconds
  
- Between 200 (inclusive) and 300 (exclusive) seconds

(b) (3 pt) A study followed 369 people with cardiovascular disease, randomly selected from hospital patients. A year later, those who owned a dog were four times more likely to be alive than those who didn't.

- Circle *True* or *False*: This study is a randomized controlled experiment.
  
- Circle *True* or *False*: This study shows that dog owners live longer than cat owners on average.
  
- Circle *True* or *False*: This study shows that for someone with cardiovascular disease, adopting a dog will probably cause them to live longer.