S&DS	123
Spring	2019

YData: An Introduction to Data Science

FINAL

INSTRUCTIONS

- You have three hours to complete the exam.
- The exam is closed book, closed notes, closed computer, closed phone, and closed calculator, except one handwritten 8.5" × 11" crib sheet of your own creation and the official study guide provided with the exam.
- Mark your answers **on the exam itself**. We will *not* grade answers written on scratch paper.

First name	
Last name (Surname)	
NetID	

Name:

This page was intentionally left blank.

2

Problem	Score	Out of
1		10
2		14
3		6
4		14
5		4
6		8
7		10
8		8
9		14
10		2
Total		90

Name:

1. Tables (10 points)

Each row of the trips table describes a single bicycle rental in the San Francisco area. Durations are integers representing times in seconds. The first three rows out of 338,343 appear below.

start	end	duration
Ferry Building	SF Caltrain	765
San Antonio Shopping Center	Mountain View City Hall	1036
Post at Kearny	2nd at South Park	307

Write Python expressions that compute each of the following values. You may use up to two lines and introduce variables, and assume numpy is imported as np.

(a)) The	average	duration	of	a	renta
-----	-------	---------	----------	----	---	-------

(c)	The	number	of rer	tale th	at sta	rted a	at the	SF	Caltrain	station
10	, ine	пиппрег	OI TEL	иань и	iau suc	นเยนล	it the	oг		. Statitoi

- (d) The average duration for rentals that started and ended at the same station
- (e) The name of the station where the most rentals ended (assume no ties)

2. Hypothesis testing (14 points)

- (a) Following the analysis of a well-designed completely randomized experiment it was reported that the observed effect had a p-value of 1% and the researchers rejected the null hypothesis. Which of the following statements best explains the conclusion of the researchers? Circle all correct answers.
 - i. The observed result made sense to the experimenter since it was what they hoped would happen.
 - ii. The observed effect happened because the experiment was properly designed and carried out without bias.
 - iii. The experimenter carefully employed the basic principles of experimental design in conducting the study.
 - iv. The laws of probability say that this observed result would be expected to happen by chance.
 - v. The observed effect was sufficiently large so that it would rarely occur simply by chance.

Name:	5

- (b) A hypothesis test is going to be carried out by researchers, and they have decided to use a p-value cutoff of 8%. If the null hypothesis is actually true, what is the probability that the test reaches the correct conclusion? Circle all correct answers and explain your choice(s).
 - i. 0%
 - ii. 4%
 - iii. 8%
 - iv. 92%
 - v. 96%
 - vi. 100%
 - vii. None of the above.

Explanation:

(c) A study on the effect of caffeine involved asking subjects to take a memory test 20 minutes after drinking cola. The memory test had a total of 25 items on it. Some subjects were randomly assigned to drink caffeine-free cola, and some to drink regular cola (with caffeine). For each subjects, a test score (the number of items recalled correctly) was recorded. The subjects were not told which type of cola they had been given. Each row of the table **cola** contains the **Type** and **Test score** for a subject in the study. The first four rows out of 120 appear below.

Type	Test Score
Caffeine-free	20
Regular	12
Regular	21
Regular	15

• The researchers would like to carry-out a hypothesis test using these data. Suppose the researchers think the regular cola (with caffeine) group will perform better on the memory test. State an appropriate null and alternative hypothesis.

• What is an appropriate test statistic to use in this setting? Explain. (You can write your solution as Python code or as an equation.)

6

Name:

(b) If you reject the null hypothesis H_0 : mean = x_0 vs. the alternative H_1 : mean $\neq x_0$ with a p-value cutoff of 0.05, then x_0 would fall in the 90% confidence interval for the mean. (True or False or Not Enough Information)

Answer:

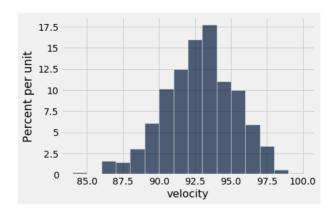
(c) The confidence interval for a population mean is narrower for smaller confidence level C with everything else the same. (True or False or Not Enough Information)

Answer:

4. Sampling (14 points)

Data are collected on the average pitch velocities of all 700 Major League Baseball pitchers during the 2018 season. The first 10 rows of the data are shown below on the left; a histogram of all of the velocity data is shown on the right (the units are miles-per-hour).

index	player	velocity
1	Justin Verlander	94.6
2	Zack Greinke	89.2
3	J.A. Happ	91.9
4	Kevin Gausman	93.1
5	Mike Clevinger	93.5
6	Sean Newcomb	92.9
7	Jose Quintana	91.5
8	Luis Severino	97.3
9	Jon Lester	90.8
10	Max Scherzer	93.9



In the following questions, the 700 velocities are considered to be the true population.

- (a) Which of the following is the best estimate of the mean of the distribution? Circle your response.
 - i. 2.5
 - ii. 5
 - iii. 90
 - iv. 93
 - v. 95
- (b) Which of the following is the best estimate of the standard deviation of the distribution? Circle your response.
 - i. 1
 - ii. 2.5
 - iii. 5
 - iv. 10
 - v. 93

ne: _	
(c)	Does the distribution approximately have a normal distribution? Answer yes or no, and explain.
(d)	Suppose that you have a sample of 100 pitchers from this population and compute the average of their velocities to be 93 with a standard deviation of 2.5. Construct a 95% confidence interval for the average velocity of the population. Show your work.
(e)	Suppose that we have 100 random samples from this population, each containing 50 pitchers. A 95% confidence interval for the average population velocity is computed for each of these samples. We expect that the true average of the population will fall into how many of these intervals? Circle your response.
	 i. 0 ii. all of them iii. 95 iv. 97.5 v. It is impossible to predict given the available information
(f)	Suppose that we have 100 random samples from this population, each containing 50 pitchers. A 95% confidence interval for the average population velocity is computed for each of these samples. We expect that the sample average will fall into how many of these intervals? Circle your response. i. 0 ii. all of them iii. 95 iv. 97.5 v. It is impossible to predict given the available information
(g)	Suppose that we have 100 random samples from this population, each containing 50 pitchers. A 95% confidence interval for the average population velocity is computed for each of these samples. We expect that the average velocity of the population of pitchers from the 2019 season (the season after the season where the data were collected) will fall into how many of these intervals? Circle your response. i. 0 ii. all of them iii. 95

iv. 97.5

v. It is impossible to predict given the available information

Name:	
Nome of	9
Name:	ч

5. Sample size (4 points)

(a) To assess the accuracy of a laboratory scale, a standard weight that is known to weigh exactly 1 gram is repeatedly weighed a total of n times and the sample mean \bar{x} is computed. Suppose the scale readings are normally distributed with unknown population mean μ and population standard deviation $\sigma = 0.01$ g. How large should n be so that a 95% confidence interval for the mean is no wider than 0.0002?

- (b) Suppose that we wish to estimate the fraction p of the vote that a political candidate has obtained, by counting a random sample of the ballots that have been cast. Which of the following constraints on the sample size ensure that a 95% confidence interval constructed from the random sample will have a width no larger than one-half of one percent (0.005)? Circle each statement that is true.
 - i. Sample size smaller than 2000
 - ii. Sample size at least 1600
 - iii. Sample size at least 2000
 - iv. Sample size at least 400
 - v. No sample size will guarantee this

6. Causality (8 points)

Measles was declared eliminated in the United States in 2000 but the highly contagious disease has returned in recent years in communities with low vaccination rates. Outbreaks have been largely confined to regions with low immunization rates. A non-profit organization decides to perform a public service experiment. They compile a list of all adults in the greater New York region and send a mailing offering for free a new measles vaccine to the first 1,000 respondents. Those that respond and receive the vaccine form the treatment group. The second 1,000 respondents form a control group, and do not receive the vaccine. A year later the non-profit contacts both the treatment and control groups to ask whether measles was contracted. The results are used to estimate the effectiveness of the vaccine.

Circle True or False for each of the following statements. Justify each answer.

(a)	True or	False:	This i	s a	randomized	controlled	experiment.

Explain:

(b) True or False: Due to the design of the study, confounding factors will make it impossible to determine whether the new vaccine is effective.

Explain:

Name:

Subsequently, the non-profit decides to perform another experiment. This time they compile a list of all adults in the U.S., and they now choose a *random subset* of 1,000 adults from this list and mail them an offer for a free measles vaccine. Those that respond and receive the vaccine form the treatment group. Another random set of 1,000 adults is chosen as a control group, and do not receive the vaccine. A year later the non-profit contacts both the treatment and control groups to ask whether measles was contracted. The results are used to estimate the effectiveness of the vaccine.

10

Circle True or False for each of the following statements. Justify each answer.

(c) True or False: This is a randomized controlled experiment.

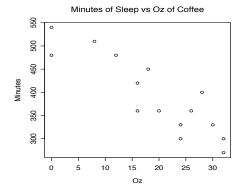
Explain:

(d) True or False: Due to the design of the study, confounding factors will make it impossible to determine whether the new vaccine is effective.

Explain:

7. Regression (10 points)

- (a) The least-squares regression line is
 - i. the line that makes the sum of the squares of the vertical distances of the data points to the line as small as possible
 - ii. the line that best splits the data in half, with half of the points above the line and half below the line.
 - iii. the line that makes the square of the correlation in the data as large as possible.
 - iv. all of the above
 - v. i and ii
 - vi. i and iii
 - vii. ii and iii
 - viii. None of the above
- (b) The following scatterplot represents the relationship between the number of ounces of coffee consumed and the number of minutes of sleep per day.

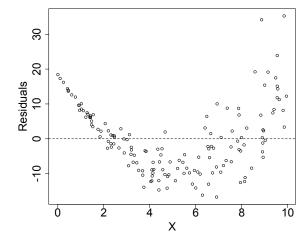


Variable	Mean	Stand. Deviation
Ounces of coffee	$\bar{x} = 19.07$	$s_x = 10.53$
Minutes of sleep	$\bar{y} = 392.67$	$s_y = 83.7$

• Given $r^2 = 0.7756$ (the estimated correlation squared) and the summary information in the table above, find the Least Squares regression Line for predicting the amount of sleep in minutes using ounces of coffee consumed.

• One of the points on the scatterplot has the coordinates (12 oz, 480 min.), calculate the residual value at 12 oz for this observation.

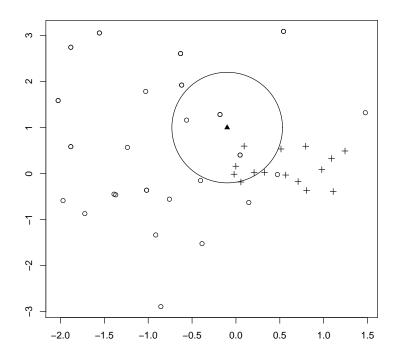
(c) Suppose a Least-squares line was fit on explanatory variable X and response variable Y, with the residuals plotted in the figure below against X. Which linear model assumptions, if any, appear to be violated given the residual plot below?



(d) You roll a fair 6-sided die 10 times. What is the chance that every roll is less than or equal to 5?

Nan	ne: _	
9.	The Step	ssification (14 points) k -nearest neighbor classifier can be described as a 2-step procedure. The first step is as follows. 1: To classify test point p , first find the k training points that are closest to p , and determine their classes. What is the second step, in words?
	Here	e is the template of code to implement the k -nearest neighbor classifier, where $\mathtt{step2}$ implements the second :
	def	<pre>classify(training, p, k): kclosest = closest(training, p, k) topkclasses = kclosest.select('Class') return step2(topkclasses)</pre>
	(b)	Write Python code to implement the second step.
		<pre>def step2(topkclasses):</pre>

(c) The following figure shows a training data set.



The solid triangle in the center of the circle is the test point p, which is not contained in the training data. The circles are the training points labeled '0' and the plus signs are the training points labeled '1'.

i. What is the 1-nearest neighbor prediction for the class of p ('0' or '1')?

ii. What is the 3-nearest neighbor prediction for the class of p ('0' or '1')?

iii. What is the 7-nearest neighbor prediction for the class of p ('0' or '1')?

Name:	15
-------	----

- (d) When a k-nearest neighbor classifier is applied to an independent set of test points, the error rate generally satisfies which of the following:
 - A. The test error is higher than the error rate of the classifier on the training data
 - B. The test error is about the same as the error rate of the classifier on the training data
 - C. The test error is lower than the error rate of the classifier on the training data

Circle the correct answer above, and explain your answer below.

Explain:

10. Distributions (2 points)

A city has 500,000 households. The annual incomes of these households have an average of \$65,000 and an SD of \$45,000. The distribution of the incomes: **Circle your response.**

- (a) is roughly normal because the number of households is large.
- (b) is not close to normal.
- (c) may be close to normal, or not; we can't tell from the information given.