



S&DS 265 / 565  
Introductory Machine Learning

# Word Embeddings and Review

October 12

ADV

ADJ

NOUN

VERB

PROPN

Yale

# Plan for today

- Reminders
- Recap of word embeddings
- Demo notebook
- Review–AMA

# Reminders

- Assn 3 is out; due October 26
- Quiz 3 posted today; open at 1pm, closes Friday at 6pm—discriminative vs. generative models, trees, bias/variance, SGD – good review for midterm!
- Midterm Tuesday, October 17, in class
- “Closed book, notes, computer...”
- $8\frac{1}{2} \times 11$  sheet of notes, handwritten double-sided
- Practice midterms posted on Canvas (with solutions)

# Review sessions

Regina: Thursday, October 12, 8-9pm

Hannah: Friday, October 13, 5-6pm

Kaylee: Saturday, October 14, 5-6pm

Awni: Sunday, October 15, 2-3pm

Held in Kline Tower (KT) 211 and Zoom (see announcements)

# Language models

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- By the basic rules of conditional probability we can factor this as

$$p(w_1, \dots, w_n) = p(w_1)p(w_2 | w_1) \dots p(w_n | w_1, \dots, w_{n-1})$$

# Modern language models

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↑  
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Can convert this to a language model by the “softmax” operation:

$$p(w \mid w_1, \dots, w_n) = \frac{\exp(s(w; w_1, \dots, w_n))}{\sum_{v \in V} \exp(s(v; w_1, \dots, w_n))}$$



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In ChatGPT, the function  $s(v; w_{1:n})$  is learned on large amounts of text (unsupervised) using a type of deep neural network called a *transformer*.

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# Key intuition

- Similar words will appear with similar words
- Self-referential notion of similarity

# Constructing embeddings

Language model is

$$p(w_2 | w_1) = \frac{\exp(\phi(w_2)^T \phi(w_1))}{\sum_w \exp(\phi(w)^T \phi(w_1))}.$$

Carry out stochastic gradient descent over the embedding vectors  $\phi \in \mathbb{R}^d$  (where  $d \approx 50$ – $500$  is chosen by hand)

This is what Mikolov et al. (2014, 2015) did at Google. With a couple of twists:

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Heuristics used:

- Skip-gram: predict surrounding words from current word, rather than the next word.
- This leads to a model of nearby words  $p_{\text{near}}(w_2 | w_1)$ .
- Second is computational, to avoid bottleneck in computing the denominator in the softmax.

# GloVe

Shortly after, a group at Stanford group introduced a variant called “GloVe”

- Based on a type of regression model
- More scalable with SGD

# Using PCA

A closely related approach is to use PCA of pointwise mutual information (PMI):

- Form  $V \times V$  matrix of pointwise mutual information values

$$\log \left( \frac{p_{\text{near}}(w_1, w_2)}{p(w_1)p(w_2)} \right)$$

- Compute top  $k$  eigenvectors  $\phi_1, \dots, \phi_k$
- For each word  $w$ , define embedding as

$$\phi(w) \equiv (\phi_{1w}, \phi_{2w}, \dots, \phi_{kw})^T$$

# Analogies

Leads to vector representations of words with interesting properties.

For example, analogies:

`king is to man as ? is to woman`

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$$\phi(\text{king}) - \phi(\text{man}) \stackrel{?}{\approx} \phi(\text{queen}) - \phi(\text{woman})$$

$$\hat{w} = \arg \min_w \|\phi(\text{king}) - \phi(\text{man}) + \phi(\text{woman}) - \phi(w)\|^2$$

Does  $\hat{w} = \text{queen}$ ?

# Learned Analogies

Table 8: *Examples of the word pair relationships, using the best word vectors from Table 4 (Skip-gram model trained on 783M words with 300 dimensionality).*

Relationship	Example 1	Example 2	Example 3
France - Paris	Italy: Rome	Japan: Tokyo	Florida: Tallahassee
big - bigger	small: larger	cold: colder	quick: quicker
Miami - Florida	Baltimore: Maryland	Dallas: Texas	Kona: Hawaii
Einstein - scientist	Messi: midfielder	Mozart: violinist	Picasso: painter
Sarkozy - France	Berlusconi: Italy	Merkel: Germany	Koizumi: Japan
copper - Cu	zinc: Zn	gold: Au	uranium: plutonium
Berlusconi - Silvio	Sarkozy: Nicolas	Putin: Medvedev	Obama: Barack
Microsoft - Windows	Google: Android	IBM: Linux	Apple: iPhone
Microsoft - Ballmer	Google: Yahoo	IBM: McNealy	Apple: Jobs
Japan - sushi	Germany: bratwurst	France: tapas	USA: pizza

# Evaluation Analogies

Type of relationship	Word Pair 1		Word Pair 2	
Common capital city	Athens	Greece	Oslo	Norway
All capital cities	Astana	Kazakhstan	Harare	Zimbabwe
Currency	Angola	kwanza	Iran	rial
City-in-state	Chicago	Illinois	Stockton	California
Man-Woman	brother	sister	grandson	granddaughter
Adjective to adverb	apparent	apparently	rapid	rapidly
Opposite	possibly	impossibly	ethical	unethical
Comparative	great	greater	tough	tougher
Superlative	easy	easiest	lucky	luckiest
Present Participle	think	thinking	read	reading
Nationality adjective	Switzerland	Swiss	Cambodia	Cambodian
Past tense	walking	walked	swimming	swam
Plural nouns	mouse	mice	dollar	dollars
Plural verbs	work	works	speak	speaks



# Notebook

Let's go to the Python notebook!

# Embedding / Visualization Examples

[WebVectors](#)[Similar words](#)[Visualizations](#)[Calculator](#)[2D text](#)[Miscellaneous](#)[Models](#)[About](#)

## WebVectors: word embeddings online

"You shall know a word by the company it keeps." (Firth 1957)

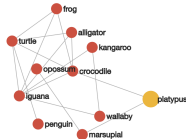
Enter a word to produce a list of its 10 nearest semantic associates.  
English Wikipedia model will be used; for other models, visit [Similar Words](#) tab.

### Semantic associates for **platypus** (computed on [English Wikipedia](#))

Word frequency

☒ High ☒ Medium ☐ Low

1. marsupial 0.642
2. crocodile 0.605
3. kangaroo 0.595
4. turtle 0.595
5. iguana 0.589
6. frog 0.573
7. penguin 0.572
8. wallaby 0.570
9. alligator 0.569
10. opossum 0.568



Similarity threshold ☐ Show tags

• We show only the associates of the same part of speech as your query. All associates can be found at the [Similar Words](#) tab.

<http://vectors.nlp1.eu/explore/embeddings/en/>

# Many uses

## species2vec: A novel method for species representation

 Boyan Angelov

**doi:** <https://doi.org/10.1101/461996>

This article is a preprint and has not been certified by peer review [what does this mean?].

**Abstract**

Full Text

Info/History

Metrics

 Preview PDF

### Abstract

Word embeddings are omnipresent in Natural Language Processing (NLP) tasks. The same technology which defines words by their context can also define biological species. This study showcases this new method - species embedding (species2vec). By proximity sorting of 6761594 mammal observations from the whole world (2862 different species), we are able to create a training corpus for the skip-gram model. The resulting species embeddings are tested in an environmental classification task. The classifier performance confirms the utility of those embeddings in preserving the relationships between species, and also being representative of species consortia in an environment.

## Visualisation

```
In [10]: m = gensim.models.KeyedVectors.load_word2vec_format('reptilia.vec')
```

```
In [11]: len(m.vocab)
```

```
Out[11]: 7397
```

```
In [15]: m.most_similar(u'Alligator_mississippiensis')
```

```
Out[15]: [(u'Sternotherus_bonevalleyensis', 0.8425856828689575),  
(u'Apalone_ferox', 0.8147842884063721),  
(u'Macrochelys_suwanniensis', 0.8063992261886597),  
(u'Deirochelys_reticularia', 0.7871163487434387),  
(u'Terrapene_putnami', 0.7841686010360718),  
(u'Chelydra_floridana', 0.7829421758651733),  
(u'Alligator_mefferdi', 0.7742743492126465),  
(u'Macrochelys_temminckii', 0.7682404518127441),  
(u'Trachemys_inflata', 0.7563525438308716),  
(u'Deirochelys_carri', 0.755811333656311)]
```

```
In [16]: %matplotlib inline
```

```
def tsne_plot(model):  
    "Creates and TSNE model and plots it"  
    labels = []
```

# Summary: Word embeddings

- Word embeddings are vector representations of words, learned from cooccurrence statistics
- The models can be built using language modeling (or regression or PCA)
- Surprising semantic relations are encoded in linear relations—for example, analogies
- Embeddings are the “ground floor” representations in ChatGPT

Week	Dates	Topics	Demos & Tutorials	Lecture Slides	Readings and Notes	Assignments & Exams
1	Aug 31	Course overview		Thu: <a href="#">Course overview</a>		
2	Sept 5, 7	Python and background concepts	<a href="#">Python elements</a> <a href="#">Covid trends</a>	Tue: <a href="#">Python elements</a> Thu: <a href="#">Pandas and linear regression</a>	Data8 Chapters 3, 4, 5	<a href="#">Quiz 1</a> <a href="#">Assn 1 out</a>
3	Sept 12, 14	Linear regression and classification	<a href="#">Covid trends (revisited)</a> <a href="#">Classification examples</a>	Tue: <a href="#">Regression concepts</a> Thu: <a href="#">Classification</a>	ISL Sections 3.1, 3.2, 3.5 Notes on <a href="#">regression</a> ISL Sections 4.3, 4.4 Notes on <a href="#">classification</a>	
4	Sept 19, 21	Stochastic gradient descent	<a href="#">SGD examples</a>	Tue: <a href="#">Classification (continued)</a> Thu: <a href="#">Stochastic gradient descent</a>	ISL Section 6.2.2 ISL Section 10.7.2	Assn 1 in <a href="#">Assn 2 out</a>
5	Sept 26, 28	Bias and variance, cross-validation	<a href="#">Bias-variance tradeoff</a> <a href="#">Covid trends (revisited)</a> <a href="#">California housing</a>	Tue: <a href="#">Bias and variance</a> Thu: <a href="#">Cross-validation</a>	ISL Section 2.2 ISL Section 5.1	<a href="#">Quiz 2</a>
6	Oct 3, 5	Tree-based methods and principal components	<a href="#">Trees and forests</a> <a href="#">Visualizing trees</a> <a href="#">PCA examples</a>	Tue: <a href="#">Trees and Forests</a> Thu: <a href="#">PCA</a>	ISL Sections 8.1, 8.2 ISL Section 12.2	Assn 2 in <a href="#">Assn 3 out</a>
7	Oct 10, 12	PCA and dimension reduction	<a href="#">PCA revisited</a> <a href="#">Used for dimension reduction</a> <a href="#">Word embeddings</a>	Tue: <a href="#">PCA and word embeddings</a> Thu: <a href="#">Review</a>	ISL Section 12.2	<a href="#">Quiz 3</a>

**“Ask Me Anything” (AMA)**