Chapter 4 solution

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- 4.1-1 FIND-MAXIMUM-SUBARRAY returns the largest negative number in A.
- 4.1-2 Pseudocode for brute-force solution for maximum-subarray problem.

```
brute_force_maximum_subarray(A):
best_sum = -inifinity
best_low = -1
best_high = -1
for int i = 0 \dots A.size - 1:
    sum = A[i]
    if sum > best_sum:
        best_sum = sum
        best_low = i
        best_high = i
    for int j = i+1 \dots A.size - 1:
        sum += A[j]
        if sum > best_sum:
            best_sum = sum
            best_low = i
            best_high = j
return best_low, best_high, best_sum
```

- 4.1-3 The crossover point is somewhere between 850 and 875. I don't think there is much point to find out exactly what n is since the performance measurements has too many noises when it comes to tiny differences.
 - Replacing the base case of recursive algorithm makes the crossover point lower. In other words, the modified recursive algorithms runs faster on smaller problem size n. See maximum_subarray.cpp for more details.
- 4.1-4 Change the initial sum of sub array search to 0 and a special value pair for low and high indicating it's an empty sub array.
- 4.1-5 Suppose we know the maximum sub array of A[0] to A[j] and we know the maximum sub array that ends at A[j] of A[0] to A[j]. For j+1, compute the following in constant time
 - maximum sub array of A[0] to A[j]
 - maximum sub array ending at A[j] + A[j+1]
 - A[j + 1]

From these, we can easily compute the maximum sub array of A[0] to A[j+1] and the maximum sub array of A[0] to A[j+1] that ends at A[j+1]. Use induction and iterate until we get the maximum sub array of A.