

Student Number: 1226909816

Name: Wei Hng Yeo

CSE450 Assignment 1

- 1) In ascending order, $f_1(n)$, $f_6(n)$, $f_4(n)$, $f_3(n)$, $f_2(n)$, $f_7(n)$, $f_5(n)$, $f_8(n)$
- 2) (a) $O(3n^2 + 5) = O(3n^2) = O(n^2)$ as constant multiples or additions can be omitted in the order of growth computation. Thus since $O(n^2) \notin O(n)$ as $O(n^2)$ exceeds the upper bound $O(n)$, so $O(3n^2 + 5) \notin O(n)$.

(b) Since $O(n^{1.1})$ cannot be simplified such that it becomes $O(kn)$ where k is a constant multiple, so $O(n^{1.1})$ exceeds the upper bound $O(n)$, $O(n^{1.1}) \notin O(n)$.

(c) Since the $\Omega(n^2 \log(n))$ tells us the lower bound runtime of $n^2 \log(n)$ while $O(n^2 \log(n))$ tells us the upper bound runtime of $n^2 \log(n)$. But in this case, the big theta must be $\Theta(n^2 \log(n))$ as big theta definition is to find the tightest bound between big ohmega and big O. Thus $\Theta(n^2 \log(n)) \notin \Theta(n^2)$ as the $n^2 \log(n)$ exceeds the tightest bound of n^2 .

(d) Since 2^n does not exceed the upper bound of $n!$ except only at small n values such as when $n = 2$, thus $2^n \in O(n!)$.

(e) $O(n^4) + \Theta(n^3)$ can be simplified to $O(n^4)$, and since $O(n^4)$ gives the upper bound, while $\Theta(n^4)$ gives the tight bound. $O(n^4) + \Theta(n^3) \in \Theta(n^4)$.
- 3) (a) $f(n) = O(f(n)^2)$ is false for $0 < f(n) < 1$, since big O describes the upper bound for a certain function. If for a particular n , $0 < f(n) < 1$, $f(n)^2$ would be smaller than $f(n)$ which contradicts the definition of big O describing the upper bound.

(b) $f(n) = \Theta(\max(f(n), g(n)))$ is not true when $g(n) > f(n)$. Since the definition of big theta is that it gives the tightest bound of function $f(n)$, the tightest bound of function $f(n)$ should be itself. But when $g(n)$ is greater than $f(n)$, big theta would be $g(n)$ which is incorrect unless $g(n) = f(n)$ for all values of n .

(c) "If $f(n) = \Omega(g(n))$, then $f(n) = O(g(n))$ " is not true. Say if $g(n) = n$ and $f(n) = n^2$, $g(n)$ is indeed the lower bound of $f(n)$ but it is not the upper bound of $f(n)$ since $n < n^2$ for $n > 1$.

(d) If $f(n) = O(g(n))$, then $2^{f(n)} = O(2^{g(n)})$ is true. Since $f(n) \leq g(n)$, so $2^{f(n)} \leq 2^{g(n)}$.
- 4) Operation per second = 10^{10} operations/second
Total operations in 1 hours = $10^{10} \times (60 \times 60) = 3.6 \times 10^{13}$ operations
 - (a) Largest $n = 6000000$
 - (b) Largest $n = 33019$
 - (c) Largest $n = 600000$

(d) Largest $n = 1.29095 \times 10^{12}$

(e) Largest $n = 45$