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  basic
```

1.1 default

```
#include <bits/stdc++.h>
using namespace std;
#define masterspark ios::sync_with_stdio(0), cin.tie(0)
    ,cout.tie(0),cin.exceptions(cin.failbit);
#define int long long
#define pp pair<int, int>
#define ff first
#define ss second
```

```
#define forr(i,n) for(int i = 1; i <= n;++i)
#define rep(i,j,n) for(int i = j; i < n;++i)</pre>
#define PB push_back
#define PF push_front
#define EB emplace_back
#define all(v) (v).begin(), (v).end()
#define FZ(x) memset(x, 0, sizeof(x)) //fill zero
#define SZ(x) ((int)x.size())
using i128 = __int128_t;
using i64 = __int64_t;
using i32 = __int32_t;
    // freopen("stdin","r",stdin);
// freopen("stdout","w",stdout);
#pragma GCC optimize("03,unroll-loops")
#pragma GCC target("avx2,bmi,bmi2,lzcnt,popcnt")
mt19937 mt(chrono::steady_clock::now().time_since_epoch
int randint(int 1, int r){
    uniform_int_distribution >> dis(l, r); return dis(mt
g++ ac.cpp -o ac.exe
g++ wa.cpp -o wa.exe
   python gen.py > input
   ac.exe < input > ac
   wa.exe < input > wa
   set /a num=num+1
if not errorlevel 1 goto loop
    python gen.py > in
    ./ac < in > ac.out
     ./wa < in > wa.out
```

binarysearch

int bsearch_1(int l, int r)

int mid = $l + r \gg 1$; if (check(mid)) r = mid;

else l = mid + 1;

while (l < r)

return 1;

2.1 二分搜

{

};

```
}
// ......0000000000
int bsearch_2(int 1, int r)
{
   while (l < r)
   {
       int mid = l + r + 1 >> 1;
       if (check(mid)) l = mid;
       else r = mid - 1;
   return 1:
// 000000000.....
int m = *ranges::partition_point(views::iota(0LL,(int)1
   e9+9),[&](int a){
   return check(a) > k;
   });
//[begin,last)
//1111111000000000000
//搜左邊數過來第一個 0
//都是 1 會回傳 last
```

3 dataStructure

3.1 DSU

```
struct STRUCT_DSU {
      vector<int> f, sz;
      void init(int n) {
            f.resize(n), sz.resize(n);
for (int i = 0; i < n; i++) {</pre>
                  \tilde{f}[i] = i;
                  sz[\bar{i}] = 1;
            }
      int find(int x) {
    if (x == f[x]) return x;
    f[x] = find(f[x]);
            return find(f[x]);
      void merge(int x, int y) {
            x = find(x), y = find(y);
if (x == y) return;
if (sz[x] < sz[y])</pre>
            swap(x, y);
sz[x] += sz[y];
            f[y] = x;
      bool same(int a, int b) {
            return (find(a) == find(b));
};
```

3.2 fenwickTree

3.3 segTree

```
#define cl(x) (x << 1)
#define cr(x)(x \ll 1) + 1
struct segTree {
#define MXN 200500
    int n;
    // vector<int> seg;
// vector<int> arr, tag;
    int seg[MXN], arr[MXN], tag[MXN];
    void init(int a) {
         n = a;
         // seg.resize(4 * (n + 5), 0);
// tag.resize(4 * (n + 5), 0);
// arr.resize(n + 5, 0);
         for (int i = 0; i < n + 5; i++)
              arr[i] = 0;
         for (int i = 0; i < 4 * (n + 5); i++)
              seg[i] = tag[i] = 0;
     void push(int id, int l, int r) {
         if (tag[id] != 0) {
              seg[id] += tag[id] * (r - l + 1);
              if (l != r) {
                   tag[cl(id)] += tag[id];
                   tag[cr(id)] += tag[id];
              tag[id] = 0;
    void pull(int id, int l, int r) {
         int mid = (l + r) \gg 1;
         push(cl(id), l, mid);
         push(cr(id), mid + 1, r);
int a = seg[cl(id)];
         int b = seg[cr(id)];
         seg[id] = a + b;
    void build(int id, int l, int r) {
         if (l == r) {
    seg[id] = arr[l];
              return;
         int mid = (l + r) \gg 1;
         build(cl(id), l, mid);'
build(cr(id), mid + 1, r);
pull(id, l, r);
    void update(int id, int l, int r, int ql, int qr,
         push(id, l, r);
if (ql <= l && r <= qr) {</pre>
              tag[id] += v;
              return;
         int mid = (l + r) \gg 1;
         if (ql <= mid)</pre>
              update(cl(id), l, mid, ql, qr, v);
         if (qr > mid)
              update(cr(id), mid + 1, r, ql, qr, v);
         pull(id, l, r);
    int query(int id, int l, int r, int ql, int qr) {
         push(id, l, r);
if (ql <= l && r <= qr) {</pre>
              return seg[id];
         int mid = (l + r) >> 1;
int ans1, ans2;
         bool f1 = 0, f2 = 0;
         if (ql <= mid) {
              ans1 = query(cl(id), l, mid, ql, qr);
              f1 = 1:
         if (qr > mid) {
              ans2 = query(cr(id), mid + 1, r, ql, qr);
              f2 = 1;
         if (f1 && f2)
```

```
return ans1 + ans2;
if (f1)
        return ans1;
return ans2;
}
void build() { build(1, 1, n); }
int query(int ql, int qr) { return query(1, 1, n, ql, qr); }
void update(int ql, int qr, int val) { update(1, 1, n, ql, qr, val); }
};
```

4 dp

4.1 digit

4.2 p median

```
void p_Median(){
     for (int i=1; i<=N; ++i)
for (int j=i; j<=N; ++j){
    m = (i+j)/2,d[i][j] = 0;
                                                          // m是中位
                數, d[i][j]為距離的總和
for (int k=i; k<=j; ++k) d[i][j] += abs(arr
                     [k] - arr[m]);
     for (int p=1; p<=P; ++p)</pre>
          for (int n=1; n<=N; ++n){</pre>
               dp[p][n] = 1e9;
for (int k=p; k<=n; ++k)</pre>
                     if (dp[p-1][k-1] + d[k][n] < dp[p][n]){
                          dp[p][n] = dp[p-1][k-1] + d[k][n];
                          r[p][n] = k;
                                              // 從 第 k 個 位 置 往 右
                                到第 j個 位置
                     }
          }
}
```

4.3 sosdp

```
// 求子集和 或超集和 -> !(mask & (1 << i))
for(int i = 0; i <(1<<N); ++i) F[i] = A[i]; //預處理 狀態權重

for(int i = 0; i < N; ++i)
for (int s = 0; s < (1<<N); ++s)
    if (s & (1 << i))
    F[s] += F[s ^ (1 << i)];
```

5 flow

5.1 Dinic

```
struct Dinic{
   struct Edge{ int v,f,re; };
   int n,s,t,level[MXN];
   vector<Edge> E[MXN];
   void init(int _n, int _s, int _t){
      n = _n; s = _s; t = _t;
      for (int i=0; i<n; i++) E[i].clear();
   }
   void add_edge(int u, int v, int f){</pre>
```

```
E[u].PB({v,f,SZ(E[v])})
    E[v].PB({u,0,SZ(E[u])-1});
  bool BFS(){
    for (int i=0; i<n; i++) level[i] = -1;</pre>
    queue<int> que;
    que.push(s);
    level[s] = 0;
    while (!que.empty()){
       int u = que.front(); que.pop();
       for (auto it : E[u]){
         if (it.f > 0 && level[it.v] == -1){
          level[it.v] = level[u]+1;
          que.push(it.v);
    } } }
    return level[t] != -1;
  int DFS(int u, int nf){
    if (u == t) return nf;
     int res = 0;
     for (auto &it : E[u]){
       if (it.f > 0 && level[it.v] == level[u]+1){
        int tf = DFS(it.v, min(nf,it.f));
         res += tf; nf -= tf; it.f -= tf;
        E[it.v][it.re].f += tf;
        if (nf == 0) return res;
    if (!res) level[u] = -1;
    return res;
  int flow(int res=0){
    while ( BFS() )
      res += DFS(s,2147483647);
     return res;
} }flow;
```

5.2 isap

```
struct Maxflow {
  static const int MAXV = 20010;
  static const int INF = 1000000;
  struct Edge {
    int v, c, r;
Edge(int _v, int _c, int _r):
       v(_v), c(_c), r(_r) {}
  int s, t;
  vector<Edge> G[MAXV*2];
  int iter[MAXV*2], d[MAXV*2], gap[MAXV*2], tot;
  void init(int x) {
     tot = x+2;
    s = x+1, t = x+2;
for(int i = 0; i <= tot; i++) {
   G[i].clear();</pre>
       iter[i] = d[i] = gap[i] = 0;
  void addEdge(int u, int v, int c) {
    G[u].push_back(Edge(v, c, SZ(G[v]) ));
G[v].push_back(Edge(u, 0, SZ(G[u]) - 1));
  int dfs(int p, int flow) {
     if(p == t) return flow;
     for(int &i = iter[p]; i < SZ(G[p]); i++) {</pre>
       Edge &e = G[p][i];
       if(e.c > 0 \& d[p] == d[e.v]+1) {
         int f = dfs(e.v, min(flow, e.c));
         if(f) {
           e.c -= f;
           G[e.v][e.r].c += f;
            return f;
    if( (--gap[d[p]]) == 0) d[s] = tot;
else {
       d[p]++;
iter[p] = 0;
       ++gap[d[p]];
    return 0;
  int solve() {
    int res = 0;
     gap[0] = tot;
```

```
for(res = 0; d[s] < tot; res += dfs(s, INF));
                                                                          void addEdge(int a, int b, int cap, Tcost w){
     return res;
                                                                            g[a].push_back(Edge(b, cap, w, (int)g[b].size()));
g[b].push_back(Edge(a, 0, -w, (int)g[a].size()-1));
  void reset() {
     for(int i=0;i<=tot;i++) {</pre>
       iter[i]=d[i]=gap[i]=0;
                                                                          Tcost d[MAXV];
                                                                          int id[MAXV], mom[MAXV];
} } flow;
                                                                          bool inqu[MAXV];
                                                                          queue<int> q;
5.3 KM
                                                                         pair<int,Tcost> solve(){
  int mxf = 0; Tcost mnc = 0;
struct KM{ // max weight, for min negate the weights
  int n, mx[MXN], my[MXN], pa[MXN];
                                                                            while(1){
  11 g[MXN][MXN], lx[MXN], ly[MXN], sy[MXN];
                                                                               fill(d, d+1+V, INFc);
  bool vx[MXN], vy[MXN];
void init(int _n) { // 1-based, N個節點
                                                                               fill(inqu, inqu+1+V, 0);
                                                                               fill(mom, mom+1+V, -1);
                                                                              mom[s] = s;
     for(int i=1; i<=n; i++) fill(g[i], g[i]+n+1, 0);</pre>
                                                                              d[s] = 0;
                                                                               q.push(s); inqu[s] = 1;
  void addEdge(int x, int y, ll w) {g[x][y] = w;} //左
邊的集合節點x連邊右邊集合節點y權重為w
                                                                               while(q.size()){
                                                                                 int u = q.front(); q.pop();
                                                                                 inqu[u] = 0;
  void augment(int y) {
     for(int x, z; y; y = z)
x=pa[y], z=mx[x], my[y]=x, mx[x]=y;
                                                                                 for(int i = 0; i < (int) g[u].size(); i++){</pre>
                                                                                   Edge &e = g[u][i];
                                                                                    int v = e.v
  void bfs(int st) {
                                                                                   if(e.cap > 0 \& d[v] > d[u]+e.w){
     for(int i=1; i<=n; ++i) sy[i]=INF, vx[i]=vy[i]=0;</pre>
                                                                                      d[v] = d[u] + e.w;
     queue<int> q; q.push(st);
                                                                                      mom[v] = u;
                                                                                      id[v] = i;
     for(;;) {
       while(q.size()) {
                                                                                      if(!inqu[v]) q.push(v), inqu[v] = 1;
          int x=q.front(); q.pop(); vx[x]=1;
                                                                              } } }
          for(int y=1; y<=n; ++y) if(!vy[y]){
    ll t = lx[x]+ly[y]-g[x][y];</pre>
                                                                               if(mom[t] == -1) break;
                                                                               int df = INFf;
                                                                              for(int u = t; u != s; u = mom[u])
  df = min(df, g[mom[u]][id[u]].cap);
for(int u = t; u != s; u = mom[u]){
            if(t==0){
               pa[y]=x
               if(!my[y]){augment(y); return;}
               vy[y]=1, q.push(my[y]);
                                                                                 Edge &e = g[mom[u]][id[u]];
            }else if(sy[y]>t) pa[y]=x,sy[y]=t;
                                                                                 e.cap
       } }
                                                                                 g[e.v][e.rev].cap += df;
       il cut = INF;
for(int y=1; y<=n; ++y)
    if(!vy[y]&&cut>sy[y]) cut=sy[y];
                                                                              mxf += df;
                                                                              mnc += df*d[t];
       for(int j=1; j<=n; ++j){
  if(vx[j]) lx[j] -= cut;
  if(vy[j]) ly[j] += cut;</pre>
                                                                            return {mxf,mnc};
                                                                       } }flow;
          else sy[j] -= cut;
                                                                       5.5 最小花費最大流 SPFA
       for(int y=1; y<=n; ++y) if(!vy[y]&&sy[y]==0){
  if(!my[y]){augment(y);return;}</pre>
                                                                       struct zkwflow{
                                                                         static const int maxN=10000;
struct Edge{ int v,f,re; ll w;};
int n,s,t,ptr[maxN]; bool vis[maxN]; ll dis[maxN];
          vy[y]=1, q.push(my[y]);
  } } }
  ll solve(){ // 回傳值為完美匹配下的最大總權重
     fill(mx, mx+n+1, 0); fill(my, my+n+1, 0); fill(ly, ly+n+1, 0); fill(lx, lx+n+1, -INF);
                                                                          vector<Edge> E[maxN];
                                                                          void init(int _n,int _s,int _t){
     for(int x=1; x<=n; ++x) for(int y=1; y<=n; ++y) //
                                                                            n=_n,s=_s,t=_t;
                                                                            for(int i=0;i<n;i++) E[i].clear();</pre>
          1-base
       lx[x] = max(lx[x], g[x][y]);
     for(int x=1; x<=n; ++x) bfs(x);</pre>
                                                                          void addEdge(int u,int v,int f,ll w){
     11 \text{ ans} = 0;
                                                                            E[u].push_back(\{v,f,(int)E[v].size(),w\});
     for(int y=1; y<=n; ++y) ans += g[my[y]][y];
                                                                            E[v].push_back({u,0,(int)E[u].size()-1,-w});
     return ans;
} }graph;
                                                                          bool SPFA(){
                                                                            fill_n(dis,n,LLONG_MAX); fill_n(vis,n,false);
queue<int> q; q.push(s); dis[s]=0;
5.4 最小花費最大流 dijkstra 不能負值
                                                                            while (!q.empty()){
                                                                              int u=q.front(); q.pop(); vis[u]=false;
for(auto &it:E[u]){
struct MinCostMaxFlow{
typedef int Tcost;
  static const int MAXV = 20010;
                                                                                 if(it.f>0&&dis[it.v]>dis[u]+it.w){
  static const int INFf = 1000000;
static const Tcost INFc = 1e9;
                                                                                   dis[it.v]=dis[u]+it.w;
                                                                                   if(!vis[it.v]){
  struct Edge{
                                                                                      vis[it.v]=true; q.push(it.v);
     int v, cap;
                                                                            } } } }
     Tcost w;
                                                                            return dis[t]!=LLONG_MAX;
     int rev
                                                                          int DFS(int u,int nf){
     Edge(){}
     Edge(int t2, int t3, Tcost t4, int t5)
                                                                            if(u==t) return nf;
                                                                            int res=0; vis[u]=true;
     : v(t2), cap(t3), w(t4), rev(t5) {}
                                                                            for(int &i=ptr[u];i<(int)E[u].size();i++){</pre>
  int V, s, t;
                                                                               auto &it=E[u][i]
  vector<Edge> g[MAXV];
                                                                               if(it.f>0&&dis[it.v]==dis[u]+it.w&&!vis[it.v]){
  void init(int n, int _s, int _t){
                                                                                 int tf=DFS(it.v,min(nf,it.f));
     V = n; S = _S; t = _t;
for(int i = 0; i <= V; i++) g[i].clear();
                                                                                 res+=tf,nf-=tf,it.f-=tf;
```

E[it.v][it.re].f+=tf;

```
if(nf==0){ vis[u]=false; break; }
}
return res;
}
pair<int,ll> flow(){
  int flow=0; ll cost=0;
  while (SPFA()){
    fill_n(ptr,n,0);
    int f=DFS(s,INT_MAX);
    flow+=f; cost+=dis[t]*f;
  }
  return{ flow,cost };
} // reset: do nothing
} flow;
```

6 geometry

6.1 Point

```
using ld = long double;
template<class T>
struct pt{
  T x,y;
pt(T _x,T _y):x(_x),y(_y){}
  pt():x(0),y(0){}
 pt operator * (T c){ return pt(x*c,y*c);}
pt operator / (T c){ return pt(x/c,y/c);}
 pt operator + (pt a){ return pt(x+a.x,y+a.y);}
pt operator - (pt a){ return pt(x-a.x,y-a.y);}
T operator * (pt a){ return x*a.x + y*a.y;}
T operator ^ (pt a){ return x*a.y - y*a.x;}
  auto operator<=>(pt o) const { return (x != o.x) ? x
       <=> 0.x : y <=> 0.y; }
  bool operator < (pt a) const { return x < a.x || (x
       == a.x && y < a.y);};
  bool operator== (pt a) const { return x == a.x and y
       == a.y;;
  friend T ori(pt a, pt b, pt c) { return (b - a) ^ (c
        - a); }
  friend T abs2(pt a) { return a * a; }
  friend int dcmp(ld x) { return (x > -eps) - (x < eps)
  friend ld abs(pt a) { return sqrt(a * a); }
using numbers::pi;
const ld eps = 1e-8L;
using Pt = pt<ld>;
istream &operator>>(istream &s, Pt &a) { return s >> a.
     x \gg a.y;
ostream &operator<<(ostream &s, Pt &a) { return s << "(" << a.x << ", " << a.y << ")";}
ld pointToSeg(Pt a,Pt b,Pt o){ //distance of ab segment
      and point o
     if((o-b) * (a-b) < 0) return abs((o-b));
if((o-a) * (b-a) < 0) return abs((o-a));</pre>
     return abs(((b-a)^(o-a))/abs(b-a));
bool collinearity(const PT& a, const PT& b, const PT& c
     ) { // 是否三點共線
     return ((b - a) \wedge (c - a)) == 0;
```

6.2 Line

```
struct Line {
    Pt a, b;
    Pt dir() const { return b - a; }
};
int PtSide(Pt p, Line L) {
    return sgn(ori(L.a, L.b, p) / abs(L.a - L.b));
}
bool PtOnSeg(Pt p, Line L) {
    return PtSide(p, L) == 0 and sgn((p - L.a) * (p - L.a)) <= 0;
}</pre>
```

```
Pt proj(Pt p, Line l) {
   Pt dir = unit(l.b - l.a);
   return l.a + dir * (dir * (p - l.a));
}
```

6.3 Circle

```
struct Cir {
   Pt o;
   ld r;
};
bool disjunct(const Cir &a, const Cir &b) {
   return sgn(abs(a.o - b.o) - a.r - b.r) >= 0;
}
bool contain(const Cir &a, const Cir &b) {
   return sgn(a.r - b.r - abs(a.o - b.o)) >= 0;
}
```

6.4 ConvexHull

```
vector<Pt> Hull(vector<Pt> P){
   sort(all(P));
   P.erase(unique(all(P)),P.end());
   P.insert(P.end(),P.rbegin()+1,P.rend());
   vector<Pt> stk;
   for(auto p:P){
      auto it = stk.rbegin();
      while(stk.rend() - it >= 2 and \
      ori(*next(it),*it,p) <= 0L and \
      ((*next(it) < *it) == (*it < p))) ++it;
      stk.resize(stk.rend() - it);
      stk.PB(p);
   }
   stk.pop_back();
   return stk;
}</pre>
```

6.5 Hulltrick

```
struct Convex {
    int n:
    vector<Pt> A, V, L, U;
    Convex(const vector<Pt> &_A) : A(_A), n(_A.size())
         \{ // n >= 3
        auto it = max_element(all(A));
        L.assign(A.begin(), it + 1);
U.assign(it, A.end()), U.push_back(A[0]);
        for (int i = 0; i < n; i++) {
             V.push_back(A[(i + 1) % n] - A[i]);
    int inside(Pt p, const vector<Pt> &h, auto f) {
        auto it = lower_bound(all(h), p, f);
        if (it == h.end()) return 0;
        if (it == h.begin()) return p == *it;
        return 1 - sgn(ori(*prev(it), p, *it));
    // 0: out, 1: on, 2: in int inside(Pt p) {
        return min(inside(p, L, less{}), inside(p, U,
             greater{}));
    static bool cmp(Pt a, Pt b) { return sgn(a ^ b) >
        0; }
    // A[í] is a far/closer tangent point
    int tangent(Pt v, bool close = true) {
        assert(v != Pt{});
        auto l = V.begin(), r = V.begin() + L.size() -
        if (v < Pt{}) l = r, r = V.end();
        if (close) return (lower_bound(l, r, v, cmp) -
             V.begin()) % n;
        return (upper_bound(l, r, v, cmp) - V.begin())
             % n;
    // closer tangent point
    array<int, 2> tangent2(Pt p) {
        array<int, 2> t{-1, -1};
if (inside(p) == 2) return t;
        if (auto it = lower_bound(all(L), p); it != L.
             end() and p == *it) {
```

int s = it - L.begin();

```
return \{(s + 1) \% n, (s - 1 + n) \% n\};
         if (auto it = lower_bound(all(U), p, greater{})
             ; it != U.end() and p == *it) {
int s = it - U.begin() + L.size() - 1;
             return \{(s + 1) \% n, (s - 1 + n) \% n\};
         for (int i = 0; i != t[0]; i = tangent((A[t[0]
         = i] - p), 0));
for (int i = 0; i != t[1]; i = tangent((p - A[t
              [1] = i], 1);
         return t:
     int find(int 1, int r, Line L) {
         if (r < 1) r += n;
         int s = PtSide(A[1 % n], L);
         return *ranges::partition_point(views::iota(l,
              [&](int m) {
                  return PtSide(A[m % n], L) == s;
             }) - 1;
    };
// Line A_x A_x+1 interset with L
    vector<int> intersect(Line L) {
         int l = tangent(L.a - L.b), r = tangent(L.b - L
              .a);
         if (PtSide(A[1], L) * PtSide(A[r], L) >= 0)
              return {};
         return {find(l, r, L) % n, find(r, l, L) % n};
};
```

6.6 complex

```
//趕時間抄這份 (只要3行)
template<class T> ostream &operator<<(ostream &s, const
     complex<T> &v) { return s << "(" << v.real() << " " << v.imag() << ")";}
template<class T> istream & operator>>(istream & cin,
    complex<T> &a) \{T_x,y; cin >> x >> y; a.real(x),a.
    imag(y); return cin; }
typedef complex<double> P;//polar abs arg conj
#define X real()
#define Y imag()
#define pi acos(-1)
template<class T> inline constexpr T inf =
    numeric_limits<T>::max() / 2;
void solve(){
 P a = \{1,0\}, b = \{0,1\};
  a.imag(1),a.real(0); //設值
  // a = |a|e^xi = |a|(isinx + cosx)
  //a*b = |a||b|e^(x+y)i
  //polar(p,t) = 長度p且與+x夾t的向量
  a *= polar(1.0,pi/2); //旋轉 pi/2 rad
  auto prd = (conj(a)*b).X;// a dot b
 auto crs = (conj(a)*b).Y;// a cross b
auto dis = abs(a-b); // la-bl
auto theta = arg(a); // 輻角 (a 跟 +x 夾角)
```

6.7 basic

```
int operator^(const PT& a) const { // 計算幾何程式
         碼中外積通常用^表示
        return x * a.y - y * a.x;
    int length2() { return x * x + y * y; }
                                                        //
         回傳距離平方
    double length() { return sqrt(x * x + y * y); } //
          回傳距離
    bool operator<(const PT& a) const { // 判斷兩點座
         標先比x再比y
        return x < a.x | | (x == a.x \& y < a.y);
    friend int cross(const PT& o, const PT& a, const PT
        & b) {
        PT lhs = o - a, rhs = o - b;
        return lhs.x * rhs.y - lhs.y * rhs.x;
struct CIRCLE { // 圓心, 半徑
    PT o;
    ld r;
};
struct LINE { // 點, 向量
    PT p, v;
int judge(ld a, ld b) { // 判斷浮點數大小 // 等於回傳0, 小於回傳-1, 大於回傳1
    if (fabs(a - b) < eps)
        return 0;
    if (a < b)
        return -1;
    return 1;
PT zhixianjiaodian(LINE a, LINE b) { // 求兩直線交點
    PT u = a.p - b.p;
    ld t = (b.v \wedge u) / (a.v \wedge b.v);
    return a.p + (a.v * t);
PT zhuanzhuan(PT a, ld angle) { // 向量旋轉 return {a.x * cos(angle) + a.y * sin(angle)
             -a.x * sin(angle) + a.y * cos(angle)};
LINE bisector(PT a, PT b) { // 中垂線
    PT p = (a + b)^{'}/2;
    PT v = zhuanzhuan(b - a, PI / 2);
    return {p, v};
CIRCLE getcircle(PT a, PT b, PT c) { // 三點求外接圓
    auto n = bisector(a, b), m = bisector(a, c);
PT o = zhixianjiaodian(n, m);
    ld r = (o - a).length();
    return {o, r};
bool collinearity(const PT& a, const PT& b, const PT& c
    ) { // 是否三點共線
return ((b - a) ^ (c - a)) == 0;
bool inLine(const PT& p, const LINE& li) { // 是否在線
    PT st, ed;
    st = li.p, ed = st + li.v;
    return collinearity(st, ed, p) && (st - p) * (ed -
        p) < 0;
int dcmp(ld x) {
    if (abs(x) < eps)
        return 0;
        return x < 0 ? -1 : 1;
Pt LLIntersect(Line a, Line b) {
    Pt p1 = a.s, p2 = a.e, q1 = b.s, q2 = b.e;
    1d f1 = (p2 - p1) \wedge (q1 - p1), f2 = (p2 - p1) \wedge (p1)
          - q2), f;
    if (dcmp(f = f1 + f2) == 0)
        return dcmp(f1) ? Pt(NAN, NAN) : Pt(INFINITY,
            INFINITY)
    return q1 * (f2 / f) + q2 * (f1 / f);
int ori(const Pt& o, const Pt& a, const Pt& b) {
    LL ret = (a - o) ^ (b - o);
    return (ret > 0) - (ret < 0);</pre>
```

```
j = (j + 1) \% nn;
                                                                                                                          ret = max(ret, (a - tubao[j]).length2());
ret = max(ret, (b - tubao[j]).length2());
// p1 == p2 || q1 == q2 need to be handled
bool banana(const Pt& p1, const Pt& p2, const Pt& q1,
        const Pt& q2) {
        if (((p2 - p1) \land (q2 - q1)) == 0) \{ // parallel
                                                                                                                   return ret;
               if (ori(p1, p2, q1))
               return false;

return ((p1 - q1) * (p2 - q1)) <= 0 || ((p1 - q2) * (p2 - q2)) <= 0 || ((q1 - p1) * (q2 - p1)) <= 0 || ((q1 - p1) * (q2 - p1)) <= 0 || ((q1 - p1) * (q2 - p1)) <= 0 || ((q1 - q1) * (q2 - p1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q1) * (q2 - q1)) <= 0 || ((q1 - q
                                                                                                           6.11 Minkowski
                                                                                                           // P, Q, R(return) are counterclockwise order convex
                                   p2) * (q2 - p2)) <= 0;
                                                                                                                   polygon
                                                                                                           vector<Pt> Minkowski(vector<Pt> P, vector<Pt> Q) {
        return (ori(p1, p2, q1) * ori(p1, p2, q2) <= 0) && (ori(q1, q2, p1) * ori(q1, q2, p2) <= 0);
                                                                                                                   auto cmp = [\&](Pt a, Pt b) {
                                                                                                                          return Pt{a.y, a.x} < Pt{b.y, b.x};
}
                                                                                                                   auto reorder = [&](vector<Pt> &R) {
                                                                                                                          rotate(R.begin(), min_element(all(R), cmp), R.
6.8 MEC
                                                                                                                                  end());
                                                                                                                          R.push_back(R[0]), R.push_back(R[1]);
PT arr[MXN];
                                                                                                                  };
int n = 10;
                                                                                                                   const int n = P.size(), m = Q.size();
double checky(double x, double y) {
       double cmax = 0;
                                                                                                                   reorder(P), reorder(Q);
                                                                                                                   vector<Pt> R;
        for (int i = 0; i < n; i++) { // 過程中回傳距離^2
                                                                                                                   for (int i = 0, j = 0, s; i < n or j < m; ) {
    R.push_back(P[i] + Q[j]);
                避免不必要的根號運算
               s = sgn((P[i + 1] - P[i]) \wedge (Q[j + 1] - Q[j]));
                                                                                                                          if (s >= 0) i++;
                                                                                                                          if (s <= 0) j++;
        return cmax;
double checkx(double x) {
                                                                                                                   return R;
       double yl = -1e9, yr = 1e9;
while (yr - yl > EPS) {
               double ml = (yl + yl + yr) / 3, mr = (yl + yr +
                                                                                                                    graph
               if (checky(x, ml) < checky(x, mr))</pre>
                                                                                                           7.1 BCC
                      yr = mr;
               else
                                                                                                           #define REP(i, n) for (int i = 0; i < n; i++)
                      yl = ml;
                                                                                                           struct BccVertex {
                                                                                                                  int n, nScc, step, dfn[MXN], low[MXN];
vector<int> E[MXN], sccv[MXN];
       }
                                                                                                                   int top, stk[MXN];
signed main() {
        double xl = -1e9, xr = 1e9;
                                                                                                                   void init(int _n) {
        while (xr - xl > EPS) {
                                                                                                                          n = _n;
               double ml = (xl + xl + xr) / 3, mr = (xl + xr +
                                                                                                                          nScc = step = 0;
                        xr) / 3;
                                                                                                                          for (int i = 0; i < n; i++) E[i].clear();</pre>
               if (checkx(ml) < checkx(mr))</pre>
                                                                                                                   void addEdge(int u, int v) {
                      xr = mr;
               else
                                                                                                                          E[u].PB(v);
                      xl = ml;
                                                                                                                          E[v].PB(u);
        }
                                                                                                                   void DFS(int u, int f) {
}
                                                                                                                          dfn[u] = low[u] = step++;
6.9 sortbyangle
                                                                                                                          stk[top++] = u;
                                                                                                                          for (auto v : E[u]) {
   if (v == f) continue;
bool cmp(const Pt& lhs, const Pt rhs){
                                                                                                                                  if (dfn[v] == -1) {
        return atan2(lhs.y, lhs.x) < atan2(rhs.y, rhs.x);</pre>
                                                                                                                                        DFS(v, u);
low[u] = min(low[u], low[v]);
sort(P.begin(), P.end(), cmp);
                                                                                                                                         if (low[v] >= dfn[u]) {
bool cmp(const Pt& lhs, const Pt rhs){
   if((lhs < Pt(0, 0)) ^ (rhs < Pt(0, 0)))</pre>
                                                                                                                                                int z
                                                                                                                                                sccv[nScc].clear();
        return (lhs < Pt(0, 0)) < (rhs < Pt(0, 0));
return (lhs ^ rhs) > 0;
                                                                                                                                                do {
                                                                                                                                                        z = stk[--top];
                                                                                                                                                        sccv[nScc].PB(z);
} // 從 270 度開始逆時針排序
                                                                                                                                                } while (z != v);
                                                                                                                                                sccv[nScc++].PB(u);
sort(P.begin(), P.end(), cmp);
                                                                                                                                 } else
6.10 旋轉卡尺
                                                                                                                                         low[u] = min(low[u], dfn[v]);
int RoatingCalipers(vector<PT> &tubao) { // 最遠點對 回
                                                                                                                   vector<vector<int>> solve() {
         傳距離平方
        int nn = tubao.size();
                                                                                                                          vector<vector<int>> res;
                                                                                                                          for (int i = 0; i < n; i++) dfn[i] = low[i] =</pre>
        int ret = 0;
        if (tubao.size() <= 2) {</pre>
                                                                                                                                  -1;
                                                                                                                          for (int i = 0; i < n; i++)
               return (tubao[0] - tubao[1]).length2();
                                                                                                                                  if (dfn[i] == -1) {
        for (int i = 0, j = 2; i < nn; i++) {
    PT a = tubao[i], b = tubao[(i + 1) % nn];
                                                                                                                                        top = 0;
DFS(i, i);
               while (((a - tubao[j]) ^ (b - tubao[j])) <</pre>
```

REP(i, nScc) res.PB(sccv[i]);

return res;

((a - tubao[(j + 1) % nn]) ^ (b - tubao [(j + 1) % nn]))

```
[i, 1, n) {
idom[i] = par[i] = dfn[i] = nfd[i] = 0;
                                                                            REP(i, 1,
} graph;
                                                                                 cov[i].clear();
7.2 SCC
                                                                                mom[i] = mn[i] = sdom[i] = i;
struct Scc{
                                                                            dfs(s);
  int n, nScc, vst[MXN], bln[MXN];
vector<int> E[MXN], rE[MXN], vec;
                                                                            REPD(i, n, 2) {
                                                                                int u = nfd[i];
                                                                                if (u == 0) continue;
for (int v : pred[u])
    if (dfn[v]) {
  void init(int _n){
    n = _n;
for (int i=0; i<= n; i++)</pre>
       E[i].clear(), rE[i].clear();
                                                                                          eval(v)
                                                                                          if (cmp(sdom[mn[v]], sdom[u])) sdom
  void addEdge(int u, int v){
                                                                                               [u] = sdom[mn[v]];
    E[u].PB(v); rE[v].PB(u);
                                                                                cov[sdom[u]].push_back(u);
                                                                                mom[u] = par[u];
for (int w : cov[par[u]]) {
  void DFS(int u){
    vst[u]=1;
     for (auto v : E[u]) if (!vst[v]) DFS(v);
                                                                                     eval(w);
    vec.PB(u);
                                                                                     if (cmp(sdom[mn[w]], par[u]))
                                                                                          idom[w] = mn[w];
  void rDFS(int u){
                                                                                          idom[w] = par[u];
    vst[u] = 1; bln[u] = nScc;
     for (auto v : rE[u]) if (!vst[v]) rDFS(v);
                                                                                cov[par[u]].clear();
  void solve(){
                                                                            REP(i, 2, n) {
    nScc = 0;
    vec.clear();
                                                                                int u = nfd[i];
    fill(vst, vst+n+1, 0);
for (int i=0; i<=n; i++)
  if (!vst[i]) DFS(i);</pre>
                                                                                 if (u == 0) continue;
                                                                                 if (idom[u] != sdom[u]) idom[u] = idom[idom
     reverse(vec.begin(),vec.end());
                                                                            }
    fill(vst, vst+n+1, 0);
for (auto v : vec)
                                                                       }
                                                                  } domT;
       if (!vst[v]){
                                                                          最大團
         rDFS(v); nScc++;
                                                                  7.4
                                                                  struct MaxClique { // 0-base
  }
                                                                       typedef bitset<MXN> Int;
};
                                                                       Int linkto[MXN], v[MXN];
7.3
       支配樹
                                                                       int n:
                                                                       void init(int _n) {
#define REP(i, s, e) for (int i = (s); i \leftarrow (e); i \leftrightarrow
                                                                            n = _n;
#define REPD(i, s, e) for (int i = (s); i >= (e); i--)
struct DominatorTree { // O(N) 1-base
                                                                            for (int i = 0; i < n; i++) {</pre>
                                                                                linkto[i].reset();
    int n, s;
                                                                                v[i].reset();
    vector<int> g[MAXN], pred[MAXN];
                                                                            }
    vector<int> cov[MAXN];
    int dfn[MAXN], nfd[MAXN], ts;
int par[MAXN]; // idom[u] s到u的最後一個必經點
int sdom[MAXN], idom[MAXN];
                                                                       void addEdge(int a, int b) { v[a][b] = v[b][a] = 1;
                                                                       int popcount(const Int& val) { return val.count();
     int mom[MAXN], mn[MAXN];
     inline bool cmp(int u, int v) { return dfn[u] < dfn</pre>
                                                                       int lowbit(const Int& val) { return val._Find_first
                                                                            (); }
         [v]; }
    int eval(int u) {
                                                                       int ans, stk[MXN];
         if (mom[u] == u) return u;
                                                                       int id[MXN], di[MXN], deg[MXN];
         int res = eval(mom[u]):
                                                                       Int cans;
         if (cmp(sdom[mn[mom[u]]], sdom[mn[u]])) mn[u] =
                                                                       void maxclique(int elem_num, Int candi) {
               mn[mom[u]];
                                                                            if (elem_num > ans) {
         return mom[u] = res;
                                                                                ans = elem num:
                                                                                 cans.reset();
                                                                                for (int i = 0; i < elem_num; i++) cans[id[
    stk[i]]] = 1;</pre>
     void init(int _n, int _s) {
         ts = 0;
         n = _n;
                                                                            int potential = elem_num + popcount(candi);
         REP(i, 1, n) g[i].clear(), pred[i].clear();
                                                                            if (potential <= ans) return;</pre>
                                                                            int pivot = lowbit(candi);
     void addEdge(int u, int v) {
                                                                            Int smaller_candi = candi & (~linkto[pivot]);
         g[u].push_back(v)
                                                                            while (smaller_candi.count() && potential > ans
         pred[v].push_back(u);
                                                                                 int next = lowbit(smaller_candi);
     void dfs(int u) {
                                                                                 candi[next] = !candi[next];
                                                                                 smaller_candi[next] = !smaller_candi[next];
         ts++;
         dfn[\dot{u}] = ts;
                                                                                 potential--;
         nfd[ts] = u;
                                                                                 if (next == pivot || (smaller_candi &
         for (int v : g[u])
                                                                                     linkto[next]).count()) {
              if (dfn[v] == 0) {
                                                                                     stk[elem_num] = next;
                  par[v] = u;
                                                                                     maxclique(elem_num + 1, candi & linkto[
                  dfs(v);
                                                                                          next]);
```

}

}

}

void build() {

```
int solve() {
    for (int i = 0; i < n; i++) {</pre>
                 id[i] = i;
                 deg[i] = v[i].count();
           sort(id, id + n, [&](int id1, int id2) { return
    deg[id1] > deg[id2]; });
for (int i = 0; i < n; i++) di[id[i]] = i;</pre>
           for (int i = 0; i < n; i++)
                 for (int j = 0; j < n; j++)
    if (v[i][j]) linkto[di[i]][di[j]] = 1;</pre>
           Int cand:
           cand.reset();
           for (int i = 0; i < n; i++) cand[i] = 1;
           ans = 1:
           cans.reset();
           cans[0] = 1;
           maxclique(0, cand);
           return ans;
} solver;
7.5 最小圈
```

```
/* minimum mean cycle O(VE) */
struct MMC{
#define E 101010
#define V 1021
#define inf 1e9
#define eps 1e-6
  struct Edge { int v,u; double c; };
  int n, m, prv[V][V], prve[V][V], vst[V];
  Edge e[E];
  vector<int> edgeID, cycle, rho;
  double d[V][V];
  void init( int _n )
  { n = _n; m = 0; }
// WARNING: TYPE matters
  void addEdge( int vi , int ui , double ci )
  { e[ m ++ ] = { vi , ui , ci }; } void bellman_ford() {
    for(int j=0; j<m; j++) {
  int v = e[j].v, u = e[j].u;
  if(d[i][v]<inf && d[i+1][u]>d[i][v]+e[j].c) {
           d[i+1][u] = d[i][v]+e[j].c;
           prv[i+1][u] = v
           prve[i+1][u] = j;
  double solve(){
    // returns inf if no cycle, mmc otherwise
    double mmc=inf;
    int st = -1;
    bellman_ford();
    for(int i=0; i<n; i++) {</pre>
      double avg=-inf;
       for(int k=0; k<n; k++) {</pre>
         if(d[n][i]<inf-eps) avg=max(avg,(d[n][i]-d[k][i</pre>
             ])/(n-k));
        else avg=max(avg,inf);
      if (avg < mmc) tie(mmc, st) = tie(avg, i);</pre>
    fill(vst,0); edgeID.clear(); cycle.clear(); rho.
         clear();
    for (int i=n; !vst[st]; st=prv[i--][st]) {
      vst[st]++
      edgeID.PB(prve[i][st]);
      rho.PB(st);
    while (vst[st] != 2) {
      if(rho.empty()) return inf;
      int v = rho.back(); rho.pop_back();
      cycle.PB(v);
      vst[v]++;
    reverse(ALL(edgeID));
    edgeID.resize(SZ(cycle));
    return mmc;
} }mmc;
```

8 math

8.1 DiscreteSqrt

```
void calcH(i64 &t, i64 &h, const i64 p) {
   i64 tmp=p-1; for(t=0;(tmp&1)==0;tmp/=2) t++; h=tmp;
// solve equation x^2 \mod p = a
//!!!! (a != 0) !!!!!
bool solve(i64 a, i64 p, i64 &x, i64 &y) {
  if(p == 2) { x = y = 1; return true; }
  int p2 = p / 2, tmp = mypow(a, p2, p);
   if (tmp == p - 1) return false;
if ((p + 1) % 4 == 0) {
     x=mypow(a,(p+1)/4,p); y=p-x; return true;
   } else {
     i64 t, h, b, pb; calcH(t, h, p); if (t >= 2) {
        do \{b = rand() \% (p - 2) + 2;
        } while (mypow(b, p / 2, p) != p - 1);
     pb = mypow(b, h, p);

} int s = mypow(a, h / 2, p);

for (int step = 2; step <= t; step++) {

int ss = (((i64)(s * s) % p) * a) % p;
         for(int i=0;i<t-step;i++) ss=mul(ss,ss,p);</pre>
        if (ss + 1 == p) s = (s * pb) % p;
              pb = ((i64)pb * pb) % p;
     x = ((i64)s * a) % p; y = p - x;
   } return true;
```

```
8.2 excrt
typedef __int128 ll;
void exgcd(ll a,ll b,ll &g,ll &x,ll &y) {
    if (b == 0) {
        g = a;
        x = 1;
        y = 0;
        return;
    exgcd(b,a\%b,g,y,x);
    y=(a/b)*x;
bool flag = false;
ll a1,a2,n1,n2;
ll abs(ll x) {
    return x>0?x:-x;
void china() {
    ll d = a2 - a1;
    ll g,x,y;
    exgcd(n1,n2,g,x,y);
    if (d \% g == 0) {
        x = ((x*d/g)\%(n2/g)+(n2/g))\%(n2/g);
        a1 = x*n1 + a1;
        n1 = (n1*n2)/q
    else
        flag = true;
int n;
long long as[100001]; //算式答案 x
long long ns[100001]; //模數 MOD
ll realchina() {
    a1 = as[0];
    n1 = ns[0];
    for (ll i = 1;i<n;i++) {
        a2 = as[i];
        n2 = ns[i];
        china():
        if (flag)
             return -1;
    return a1;
int main() {
    cin>>n;
    flag = false;
    for (ll i = 0;i<n;i++)</pre>
        cin>>ns[i]>>as[i];
    cout<<(long long)realchina()<<endl;</pre>
```

|}

```
8.3 exgcd
```

```
int exgcd(int a,int b,int&x,int&y){
    if(b==0)return x=1,y=0,a;
    int d = exgcd(b,a%b,y,x);
    y-=a/b*x;
    return d;
}
```

8.4 FFT

```
const int MAXN = 262144;
// (must be 2^k)
// before any usage, run pre_fft() first
typedef long double ld;
typedef complex<ld> cplx; //real() ,imag()
const ld PI = acosl(-1);
const cplx I(0, 1);
cplx omega[MAXN+1]
void pre_fft(){
  for(int i=0; i<=MAXN; i++)
  omega[i] = exp(i * 2 * PI / MAXN * I);</pre>
// n must be 2^k
void fft(int n, cplx a[], bool inv=false){
  int basic = MAXN / n;
  int theta = basic;
  for (int m = n; m >= 2; m >>= 1) {
    int mh = m >> 1;
for (int i = 0; i < mh; i++) {</pre>
       cplx w = omega[inv ? MAXN-(i*theta%MAXN)
                             : i*theta%MAXN];
       for (int j = i; j < n; j += m) {
         int k = j + mh;
         cplx x = a[j] - a[k];
         a[j] += a[k];

a[k] = w * x;
    } }
     theta = (theta * 2) % MAXN;
  int i = 0;
  for (int j = 1; j < n - 1; j++) {
  for (int k = n >> 1; k > (i ^= k); k >>= 1);
    if (j < i) swap(a[i], a[j]);
  if(inv) for (i = 0; i < n; i++) a[i] /= n;
cplx arr[MAXN+1];
inline void mul(int _n,i64 a[],int _m,i64 b[],i64 ans
    ]([]
  int n=1, sum=_n+_m-1;
  while(n<sum)</pre>
    n <<=1;
  for(int i=0;i<n;i++) {</pre>
    double x=(i<_n?a[i]:0), y=(i<_m?b[i]:0);
    arr[i]=complex<double>(x+y,x-y);
  fft(n,arr);
  for(int i=0;i<n;i++)</pre>
    arr[i]=arr[i]*arr[i];
  fft(n,arr,true);
  for(int i=0;i<sum;i++)</pre>
    ans[i]=(i64)(arr[i].real()/4+0.5);
```

8.5 josephus

```
int josephus(int n, int m){ //n人每m次
  int ans = 0;
  for (int i=1; i<=n; ++i)
      ans = (ans + m) % i;
  return ans;
}</pre>
```

8.6 Theorem

- Lucas's Theorem : For $n,m\in\mathbb{Z}^*$ and prime P, $C(m,n)\mod P=\Pi(C(m_i,n_i))$ where m_i is the i-th digit of m in base P.
- Stirling approximation : $n! \approx \sqrt{2\pi n} (\frac{n}{e})^n e^{\frac{1}{12n}}$

```
• Stirling Numbers(permutation |P|=n with k cycles): S(n,k)= coefficient of x^k in \prod_{i=0}^{n-1}(x+i)
```

- Stirling Numbers(Partition n elements into k non-empty set): $S(n,k)=\frac{1}{k!}\sum_{j=0}^k (-1)^{k-j} {k \choose j} j^n$
- Pick's Theorem : A=i+b/2-1 A: Area, i: grid number in the inner, b: grid number on the side

```
 \begin{array}{l} \bullet \quad \text{Catalan number} \ : \ C_n = {2n \choose n}/(n+1) \\ C_n^{n+m} - C_{n+1}^{n+m} = (m+n)! \frac{n-m+1}{n+1} \quad for \quad n \geq m \\ C_n = \frac{1}{n+1} {2n \choose n} = \frac{(2n)!}{(n+1)!n!} \\ C_0 = 1 \quad and \quad C_{n+1} = 2(\frac{2n+1}{n+2})C_n \\ C_0 = 1 \quad and \quad C_{n+1} = \sum_{i=0}^n C_i C_{n-i} \quad for \quad n \geq 0 \end{array}
```

• Euler Characteristic: planar graph: V-E+F-C=1 convex polyhedron: V-E+F=2 V,E,F,C: number of vertices, edges, faces(regions), and components

• Kirchhoff's theorem : $A_{ii}=deg(i), A_{ij}=(i,j)\in E$?-1:0, Deleting any one row, one column, and cal the det(A)

- Polya' theorem (c is number of color, m is the number of cycle size): $(\sum_{i=1}^m c^{gcd(i,m)})/m$

• Burnside lemma: $|X/G| = \frac{1}{|G|} \sum_{g \in G} |X^g|$

• 錯排公式: (n 個人中, 每個人皆不再原來位置的組合數): dp[0] = 1; dp[1] = 0; dp[i] = <math>(i-1)*(dp[i-1]+dp[i-2]);

• Bell 數 (有 n 個人, 把他們拆組的方法總數) : $B_0 = 1$ $B_n = \sum_{k=0}^n s(n,k)$ (second – stirling) $B_{n+1} = \sum_{k=0}^n \binom{n}{k} B_k$

• Wilson's theorem : $(p-1)! \equiv -1 (mod \ p)$

• Fermat's little theorem : $a^p \equiv a (mod\ p)$

• Euler's totient function: $A^{B^{\,C}}\,mod\ p = pow(A,pow(B,C,p-1))mod\ p$

• 歐拉函數降冪公式: $A^B \mod C = A^B \mod \phi(c) + \phi(c) \mod C$

• 6 的倍數: $(a-1)^3 + (a+1)^3 + (-a)^3 + (-a)^3 = 6a$

8.7 Primes

```
Root
Prime
                    Prime
                                   Root
                    167772161
7681
             17
12289
             11
                     104857601
40961
                    985661441
65537
                    998244353
786433
             10
                    1107296257
5767169
             3
                    2013265921
                                   31
7340033
             3
                    2810183681
                                  11
23068673
                    2885681153
469762049
                    605028353
```

8.8 millerrabin

```
// n < 4,759,123,141
// n < 1,122,004,669,633
// n < 3,474,749,660,383
                                  3 : 2, 7, 61
4 : 2, 13, 23, 1662803
6 : pirmes <= 13
// n < 2^64
// 2, 325, 9375, 28178, 450775, 9780504, 1795265022
// Make sure testing integer is in range [2, n-2] if
// you want to use magic.
bool witness(i64 a,i64 n,i64 u,int t){
  if(!a) return 0;
  i64 x=mypow(a,u,n);
  for(int i=0;i<t;i++) {</pre>
     i64 nx=mul(x,x,n);
     if(nx==1&&x!=1&&x!=n-1) return 1;
     x=nx;
  return x!=1;
bool mii64er_rabin(i64 n) {
  int s = 7;
```

```
// iterate s times of witness on n
if(n<2) return 0;
if(!(n&1)) return n == 2;
i64 u=n-1; int t=0;
// n-1 = u*2^t
while(!(u&1)) u>>=1, t++;
while(s--){
    i64 a=magic[s]%n;
    if(witness(a,n,u,t)) return 0;
}
return 1;
}
```

8.9 phi

8.10 pollardrho

```
// does not work when n is prime O(n^(1/4))
i64 f(i64 x, i64 c, i64 mod){ return add(mul(x,x,mod),c
    ,mod); }
i64 poi64ard_rho(i64 n) {
    i64 c = 1, x = 0, y = 0, p = 2, q, t = 0;
    while (t++ % 128 or gcd(p, n) == 1) {
        if (x == y) c++, y = f(x = 2, c, n);
        if (q = mul(p, abs(x-y), n)) p = q;
        x = f(x, c, n); y = f(f(y, c, n), c, n);
    }
    return gcd(p, n);
}
```

8.11 primes

```
/* 12721, 13331, 14341, 75577, 123457, 222557, 556679 * 999983, 1097774749, 1076767633, 100102021, 999997771
* 1001010013, 1000512343, 987654361, 999991231
* 999888733, 98789101, 987777733, 999991921, 1010101333
* 1010102101, 1000000000039, 100000000000037
* 2305843009213693951, 4611686018427387847
* 9223372036854775783, 18446744073709551557 */
int mu[ N ] , p_tbl[ N ];
vector<int> primes;
void sieve() {
  mu[ 1 ] = p_tbl[ 1 ] = 1;
for( int i = 2 ; i < N ; i ++ ){
   if( !p_tbl[ i ] ){</pre>
        p_tbl[ i ] = i;
        primes.push_back( i );
        mu[i] = -\overline{1};
     for( int p : primes ){
  int x = i * p;
  if( x >= M ) break;
        p_tbl[ x ] = p;
mu[ x ] = -mu[ i ];
        if( i % p == 0 ){
  mu[ x ] = 0;
           break;
vector<int> factor( int x ){
  vector<int> fac{ 1 };
  while(x > 1){
      int fn = SZ(fac), p = p_tbl[x], pos = 0;
     while( x \% p == 0 ){
        x /= p;
for( int i = 0 ; i < fn ; i ++ )
fac.PB( fac[ pos ++ ] * p );
  } }
   return fac;
```

8.12 Euler

```
int Euler(int n){
  int now = n;
  for (int i = 2; i * i <= n; i++)
    if (n % i == 0){
      now = now - now / i;
      while (n % i == 0) n = n / i;
      }
  if (n > 1) now = now - now / n;
    return now;
}
```

8.13 quickeuler

```
vector<int> pri;
bool not_prime[MXN + 10];
int phi[MXN + 10];
void quick_euler(int n) {
    phi[1] = 1;
     for (int i = 2; i <= n; i++) {
         if (!not_prime[i]) {
             pri.push_back(i);
             phi[i] = i - 1;
         for (int pri_j : pri) {
             if (i * pri_j > n)
                  break
             not_prime[i * pri_j] = true;
if (i % pri_j == 0) {
                  phi[i * pri_j] = phi[i] * pri_j;
                  break:
             phi[i * pri_j] = phi[i] * phi[pri_j];
         }
    }
}
```

8.14 sieve

9 string

9.1 KMP

```
vector<int> prefunc(const string& s){
  int n = s.size();
  vector<int> pi(n);
  for(int i=1, j=0; i < n; ++i){</pre>
    j = pi[i-1];
    while(j && s[j] != s[i]) j = pi[j-1]; //取次小LCP
    if(s[j] == s[i]) ++j;
    pi[i] = j;
  }
  return pi;
vector<int> kmp(string str, string s, vector<int>& nxt)
    vector<int> ans;
for (int i = 0, j = 0; i < SZ(str); i++) {
        while (j && str[i] != s[j]) j = nxt[j - 1];
         if (str[i] == s[j]) j++;
         if (j == SZ(s)) {
             ans.push_back(i - SZ(s) + 1);
             j = nxt[j - 1];
    }
    return ans;
}
```

9.2 minRotation

```
// rotate(begin(s),begin(s)+minRotation(s),end(s))
#define rep(i, s, e) for (int i = (s); i < (e); i++)
int minRotation(string s) {
   int a = 0, N = s.size();
   s += s;
   rep(b, 0, N) rep(k, 0, N) {
      if (a + k == b || s[a + k] < s[b + k]) {
            b += max(0LL, k - 1);
            break;
      }
   if (s[a + k] > s[b + k]) {
            a = b;
            break;
      }
   return a;
}
```

9.3 PalindromeTree

```
// len[s]是對應的回文長度
// num[s] 是 有 幾 個 回 文 後 綴
// cnt[s]是這個回文子字串在整個字串中的出現次數
// fail[s]是他長度次長的回文後綴, aba的fail是a
// fail[s] -> s 建邊是顆樹
const int MXN = 1000010;
struct PalT{
  int nxt[MXN][26],fail[MXN],len[MXN];
  int tot,lst,n,state[MXN],cnt[MXN],num[MXN];
int diff[MXN],sfail[MXN],fac[MXN],dp[MXN];
  char s[MXN] = \{-1\}
  int newNode(int 1,int f){
    len[tot]=1,fail[tot]=f,cnt[tot]=num[tot]=0;
    memset(nxt[tot],0,sizeof(nxt[tot]));
diff[tot]=(l>0?1-len[f]:0);
    sfail[tot]=(l>0&&diff[tot]==diff[f]?sfail[f]:f);
    return tot++;
  int getfail(int x){
    while(s[n-len[x]-1]!=s[n]) x=fail[x];
    return x;
  int getmin(int v){
    dp[v]=fac[n-len[sfail[v]]-diff[v]];
    if(diff[v]==diff[fail[v]])
        dp[v]=min(dp[v],dp[fail[v]]);
    return dp[v]+1;
 }
  int push(){
    int c=s[n]-'a',np=getfail(lst);
    if(!(lst=nxt[np][c])){
      lst=newNode(len[np]+2,nxt[getfail(fail[np])][c]);
      nxt[np][c]=lst; num[lst]=num[fail[lst]]+1;
    fac[n]=n;
    for(int v=lst;len[v]>0;v=sfail[v])
        fac[n]=min(fac[n],getmin(v));
    return ++cnt[lst],lst;
  void init(const char *_s){
    tot=lst=n=0;
    newNode(0,1), newNode(-1,1);
    for(;_s[n];) s[n+1]=_s[n],++n,state[n-1]=push();
    for(int i=tot-1;i>1;i--) cnt[fail[i]]+=cnt[i];
}palt;
```

9.4 RollingHash

```
struct RollingHash{
#define psz 2
    vector<ll> primes={17, 75577};
    vector<ll> MOD={998244353, 10000000007};
    vector<array<ll, psz>> hash, base;
    void init(const string &s){
        hash.clear(); hash.resize(s.size());
        base.clear(); base.resize(s.size());
        for(int i=0;i<psz;i++){
            hash[0][i] = s[0];
            base[0][i] = 1;</pre>
```

9.5 SuffixArray

```
const int N = 300010;
struct SA{
#define REP(i,n) for ( int i=0; i<int(n); i++ )</pre>
#define REP1(i,a,b) for ( int i=(a); i <= int(b); i++)
      bool _t[N*2];
      int _s[N*2], _sa[N*2], _c[N*2], x[N], _p[N], _q[N*2],
    hei[N], r[N];
     int operator [] (int i){ return _sa[i]; }
void build(int *s, int n, int m){
           memcpy(_s, s, sizeof(int) * n);
            sais(_s, _sa, _p, _q, _t, _c, n, m);
           mkhei(n);
      void mkhei(int n){
           REP(i,n) r[_sa[i]] = i;
            hei[0] = 0;
           REP(i,n) if(r[i]) {
  int ans = i>0 ? max(hei[r[i-1]] - 1, 0) : 0;
                  while(_s[i+ans] == _s[_sa[r[i]-1]+ans]) ans++;
                 hei[r[i]] = ans;
           }
      void sais(int *s, int *sa, int *p, int *q, bool *t,
                  int *c, int n, int z){
           bool uniq = t[n-1] = true, neq;
int nn = 0, nmxz = -1, *nsa = sa + n, *ns = s + n,
                        lst = -1;
#define MSO(x,n) memset((x),0,n*sizeof(*(x)))
#define MAGIC(XD) MSO(sa, n); \
memcpy(x, c, sizeof(int) * z); \
           XD;
           memcpy(x + 1, c, sizeof(int) * (z - 1)); \
REP(i,n) if(sa[i] && !t[sa[i]-1]) sa[x[s[sa[i
                        ]-1]]++] = sa[i]-1; \setminus
           memcpy(x, c, sizeof(int) * z); \
for(int i = n - 1; i >= 0; i--) if(sa[i] && t[sa[i
                         MSO(c, z);
            REP(i,n) uniq \&= ++c[s[i]] < 2;
            REP(i,z-1) c[i+1] += c[i];
           if (uniq) { REP(i,n) sa[--c[s[i]]] = i; return; }
for(int i = n - 2; i >= 0; i--) t[i] = (s[i]==s[i +1] ? t[i+1] : s[i]<s[i+1]);</pre>
           MAGIC(REP1(i,1,n-1) if(t[i] && !t[i-1]) sa[--x[s[i]]]=p[q[i]=nn++]=i);
REP(i, n) if (sa[i] && t[sa[i]] && !t[sa[i]-1]) {
                 neq=lst<0||memcmp(s+sa[i],s+lst,(p[q[sa[i]]+1]-sa[i])||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||sa[i]||s
                              [i])*sizeof(int));
                 ns[q[lst=sa[i]]]=nmxz+=neq;
            sais(ns, nsa, p + nn, q + n, t + n, c + z, nn, nmxz
                           + 1);
           MAGIC(for(int i = nn - 1; i >= 0; i--) sa[--x[s[p[
                        nsa[i]]]] = p[nsa[i]]);
     }
}sa;
// H [i] 第 i 跟前面的最大共同前綴// SA[i] 第 i 小是從第幾個字元開始
```

```
int H[ N ], SA[ N ];
void suffix_array(int* ip, int len) {
                                                               int ans[MXN], color[MXN], son[MXN];
                                                              map<int, int> mp[MXN];
  // should padding a zero in the back
                                                               void dfs(int x, int f){
  // ip is int array, len is array length
                                                                   if(son[x]){
  // ip[0..n-1] != 0, and ip[len] = 0
                                                                       dfs(son[x], x);
swap(mp[x], mp[son[x]]);
  ip[len++] = 0;
  sa.build(ip, len, 128); // 注意字元個數 for (int i=0; i<len; i++) {
                                                                       ans[x] = ans[son[x]];
    H[i] = sa.hei[i + 1];
                                                                   mp[x][color[x]]++;
    SA[i] = sa.\_sa[i + 1];
                                                                   ans[x] = max(ans[x], mp[x][color[x]]);
                                                                   for(int i : edge[x]){
  // resulting height, sa array \in [0,len)
                                                                       if(i == f | i == son[x])
                                                                                                       continue:
                                                                       dfs(i, x);
                                                                       for(auto j : mp[i]){
    mp[x][j.first] += j.second;
9.6
      trie
                                                                            ans[x] = max(ans[x], mp[x][j.first]);
//01 bitwise trie
                                                                   }
struct trie{
    trie *nxt[2]; // 差別
int cnt: //紀錄有多少個數字以此節點結尾
                                                              }
                                                               10.2
                                                                      EularTour
                 //有多少數字的前級包括此節點
    int sz;
    trie():cnt(0),sz(0){
                                                               int timing=0;
        memset(nxt,0,sizeof(nxt));
                                                               int in[N],out[N];
                                                               void dfs(int u){
};
//創建新的字典樹
                                                                   in[u] = ++timing;//這時進入u
                                                                   for(int nxt : g[u]){//跑過所有孩子
trie *root;
                                                                       dfs(nxt);
void insert(int x){
    trie *now = root;
                        // 每次從根節點開始
                                                                   out[u] = timing;//這時離開u 不會++
    for(int i=22;i>=ó;i--){ // 從最高位元開始往低位元走
        now->sz++;
         //cout<<(x>>i&1)<<endl;
         if(now->nxt[x>>i&1] == NULL){ //判斷當前第 i 個
                                                               10.3 LCA
             位元是 0 還是 1
             now->nxt[x>>i&1] = new trie();
                                                               int n, q;
        }
                                                               int anc[MAXN][25], in[MAXN], out[MAXN];
        now = now->nxt[x>>i&1]; //走到下一個位元
                                                               vector<int> edge[MAXN];
                                                               int timing = 1;
    now->cnt++;
                                                               void dfs(int_cur, int fa) {
    now->sz++;
                                                                   anc[cur][0] = fa;
                                                                   in[cur] = timing++;
                                                                   for (int nex : edge[cur]) {
9.7 Z-algorithm
                                                                       if (nex == fa) continue;
                                                                       dfs(nex, cur);
vector<int> zfunc(string &s){ //求 s 跟 s[i..n-1] 的最
     長真共同前綴長度 z[0] = 0
                                                                   out[cur] = timing++;
  int n = s.size();
  vector<int> z(n);
                                                               void init() {
  for(int i = 1, l = 0, r = 0; i < n; ++i){
                                                                   dfs(1, 0);
    if(i <= r && z[i - l] < r - i + 1) z[i] = z[i - l];
                                                                   for (int i = 1; i < 25; i++) {
                                                                       for (int cur = 1; cur <= n; cur++) {</pre>
      z[i] = \max(0LL, r - i + 1);
                                                                            anc[cur][i] = anc[anc[cur][i - 1]][i - 1];
      while(i + z[i] < n && s[z[i]] == s[i + z[i]]) ++z
           Γi];
                                                                   }
    if(i + z[i] - 1 > r) l = i, r = i + z[i] - 1;
                                                               bool isanc(int u, int v) { return (in[u] <= in[v] &&</pre>
  }
                                                                   out[v] <= out[u]); }</pre>
  return z;
                                                               int lca(int a, int b) {
                                                                   if (isanc(a, b)) return a;
                                                                   if (isanc(b, a)) return b;
      馬拉車
9.8
                                                                   for (int i = 24; i >= 0; i--) {
    if (anc[a][i] == 0) continue;
                                                                       if (!isanc(anc[a][i], b)) a = anc[a][i];
void z_value_pal(char* s, int len, int* z) {
    len = (len << 1) + 1;
for (int i = len - 1; i >= 0; i--)
        s[i] = i \& 1 ? s[i >> 1] : '@';
                                                                   return anc[a][0];
    z[0] = 1;
    for (int i = 1, l = 0, r = 0; i < len; i++) {
z[i] = i < r ? min(z[l + l - i], r - i) : 1;
while (i - z[i] >= 0 \&\& i + z[i] < len \&\& s[i - i]
                                                               10.4 treehash
              z[i] == s[i + z[i]]
                                                              i64 dfs(int u){
             ++z[i];
                                                                   vector<i64> h;
                                                                   subtree_sz[u] = 1;
for(i64 child : edge[u]){
        if (i + z[i] > r)
             l = i, r = i + z[i];
                                                                       h.push_back(dfs(child));
    }
                                                                       subtree_sz[u] += subtree_sz[child];
                                                                   sort(h.begin(), h.end());
10
      tree
                                                                   i64 ret = subtree_sz[u];
```

10.1 DSUONTREE

for(i64 v : h){
 ret = (ret * base + v) % MOD;

}
return ret;
}



















