Cheese Model (A simple version)

$$\forall ij := \log Q_{ij}$$
, $\times ij := \log P_{ij}$, $P_{ii} := \log Q_{i}$

2. The Model

clenoted by n is the total number of shops, it's a large enough number - so we can obtain No:3 and Vo:3 directly from ols solutions.

3. Inference

3. | Posteria

$$\propto \lambda^{\frac{mn}{2}} \exp\left\{-\frac{\lambda}{2} \sum_{j=1}^{n} \sum_{j=1}^{m} (y_{ij} - \beta_{0i} - \beta_{ij} \nabla \hat{y} - \beta_{2i} \times ij - \beta_{ij} \nabla \hat{y})^{2}\right\}$$

$$-\exp\{-\frac{1}{2V_{0}}\sum_{i=1}^{N}(\beta_{0i}-\mu_{0})^{2}\}\cdot\exp\{-\frac{1}{2V_{i}}\sum_{i=1}^{N}(\beta_{ii}-\mu_{i})^{2}\}$$

3.2 Full conditionals.

$$Y_{0i} = \left(\frac{1}{v_0} + m \cdot \lambda\right)^{-1}, \quad \psi_{0i} = Y_{0i} \cdot \left[\lambda \sum_{j=1}^{m} (y_{ij} - \beta_{ij} \nabla y_{ij} - \beta_{ji} \nabla y_{ij} - \beta_{ji} \nabla y_{ij} + \frac{\mu_0}{v_0^2}\right]$$

$$Y_{ii} = \left(\frac{1}{V_{i}^{2}} + \lambda \cdot \sum_{j=1}^{m} \mathcal{D}_{ij}^{*}\right)^{-1}, \quad Q_{ii} = Y_{ii} \cdot \left[\lambda \sum_{j=1}^{m} \mathcal{D}_{ij}^{*}\left(y_{ij} - \beta_{0i} - (\beta_{2i} + \beta_{2i}) \times ij\right) + \frac{\mu_{i}}{V_{i}^{2}}\right]$$

$$(2)$$

$$Y_{2i} = \left(\frac{1}{\sqrt{2}} + \lambda \sum_{j=1}^{n} \times \hat{y}\right)^{-1}, \quad Q_{ij} = Y_{2i} \cdot \left[\lambda \sum_{j} \times \hat{y}(y_{ij} - \beta_{0i} - Q_{ii}D_{ij} - \beta_{0i} \times \hat{y}D_{ij}) + \frac{Q_{ij}}{\sqrt{2}}\right]$$
(3)

•
$$f(\lambda) = Ga(\lambda | \lambda a, \lambda b)$$
 where

$$\lambda \alpha = \frac{mn}{2} + \frac{1}{2}, \quad \lambda_b = \frac{1}{2} \sum_{i,j} \left(y_{ij} - \beta_{0i} - \beta_{ij} D_{ij} - \beta_{2i} X_{ij} - \beta_{3i} X_{ij} D_{ij} \right)^2$$
 (5)

4. The Gibbs Sampler

- 1- Start;
- a. Run ols of model on the data, initialize Bo, B, B, B, (Mo, Vo), (M, V,), (M2, V2) and (M3, V3);
- 3. Initialize >;
- 4. While (chain does not converge) do =
- 5. Sample Bo from f(Ooi | ...), i=1,..., n, (Eq(1))
- 6. Sample B1 from f(Biil ...), i=1,..., n, (Eq. Q1);
- 7. Sample B from f(Bi) ...), 1=1,..., 1, (Eq. (3));
- 8. Sample B from f(Bi)...), i=1,..., n, (Eq(6));
- 9. Sample A from f(x/~), (Eg(s));
- 10. End While;
- 11. End.

(4)