

MOAA Guest Lecture



# Radiative Processes

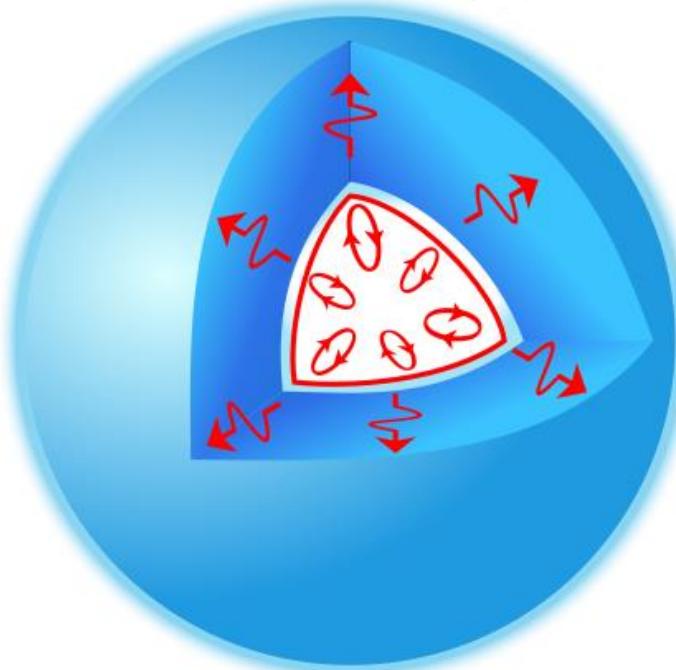
2025.03.22 | Yen-Hsing Lin (UCSD)

# Why do we care about radiative processes?

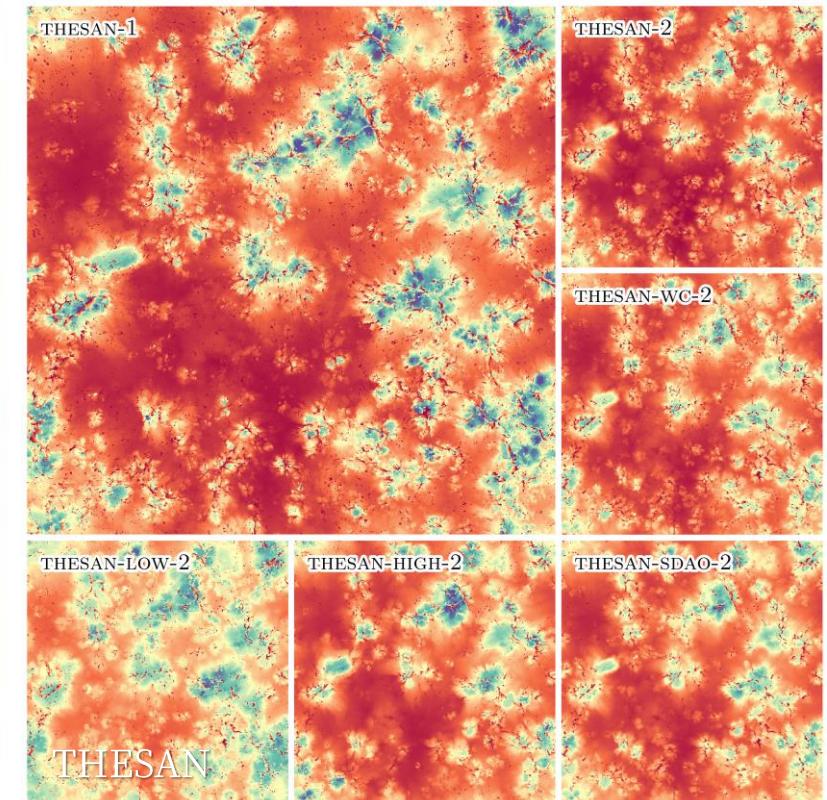
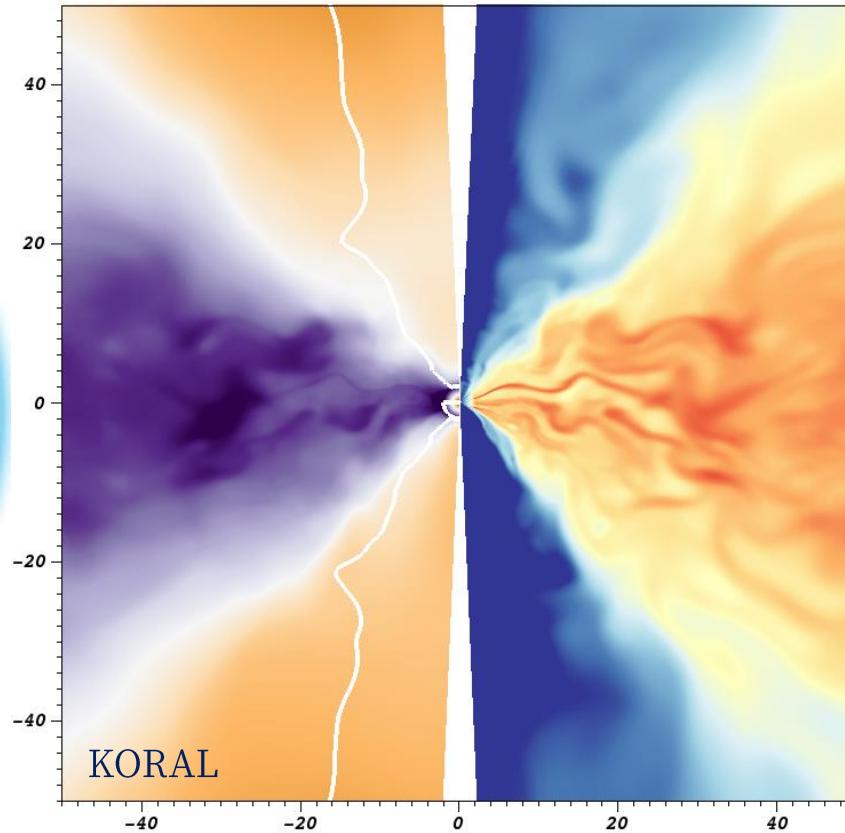


EM waves are our primary tool for understanding the universe  
We need to know how to convert photons into meaningful physical properties.

# Why do we care about radiative processes?



Д.Ильин



Radiation plays important roles in multiple astrophysical systems.

# What does bright actually mean?

## In physical sciences [ edit ]

### Physics [ edit ]

- Intensity (physics), power per unit area ( $\text{W/m}^2$ )
- Field strength of electric, magnetic, or electromagnetic fields ( $\text{V/m}$ ,  $\text{T}$ , etc.)
- Intensity (heat transfer), radiant heat flux per unit area per unit solid angle ( $\text{W}\cdot\text{m}^{-2}\cdot\text{sr}^{-1}$ )
- Electric current, whose value is sometimes called *current intensity* in older books

### Optics [ edit ]

- Radiant intensity, power per unit solid angle ( $\text{W/sr}$ )
- Luminous intensity, luminous flux per unit solid angle ( $\text{lm/sr}$  or  $\text{cd}$ )
- Irradiance, power per unit area ( $\text{W/m}^2$ )

### Astronomy [ edit ]

- Radiance, power per unit solid angle per unit projected source area ( $\text{W}\cdot\text{sr}^{-1}\cdot\text{m}^{-2}$ )

### Seismology [ edit ]

- Mercalli intensity scale, a measure of earthquake impact
- Japan Meteorological Agency seismic intensity scale, a measure of earthquake impact
- Peak ground acceleration, a measure of earthquake acceleration ( $\text{g}$  or  $\text{m/s}^2$ )

### Acoustics [ edit ]

- Sound intensity, sound power per unit area

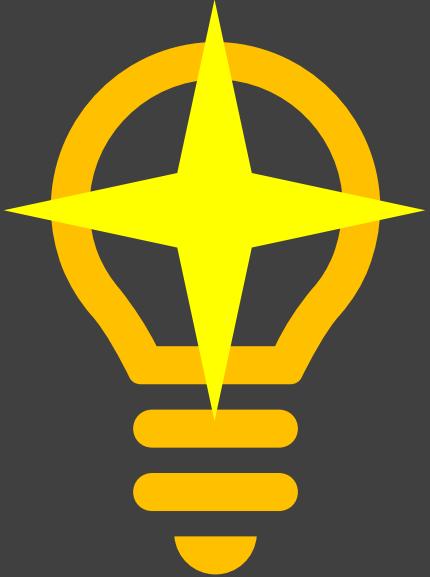
## SI photometry quantities

V · T · E

Quantity		Unit		Dimension [nb 1]	Notes
Name	Symbol [nb 2]	Name	Symbol		
Luminous energy	$Q_v$ <sup>[nb 3]</sup>	lumen second	$\text{lm}\cdot\text{s}$	$\text{T}\cdot\text{J}$	The lumen second is sometimes called the <i>talbot</i> .
Luminous flux, luminous power	$\Phi_v$ <sup>[nb 3]</sup>	lumen (= candela steradian)	$\text{lm}$ (= $\text{cd}\cdot\text{sr}$ )	$\text{J}$	Luminous energy per unit time
Luminous intensity	$I_v$	candela (= lumen per steradian)	$\text{cd}$ (= $\text{lm}/\text{sr}$ )	$\text{J}$	Luminous flux per unit solid angle
Luminance	$L_v$	candela per square metre	$\text{cd}/\text{m}^2$ (= $\text{lm}/(\text{sr}\cdot\text{m}^2)$ )	$\text{L}^{-2}\cdot\text{J}$	Luminous flux per unit solid angle per unit <i>projected</i> source area. The candela per square metre is sometimes called the <i>nit</i> .
Illuminance	$E_v$	lux (= lumen per square metre)	$\text{lx}$ (= $\text{lm}/\text{m}^2$ )	$\text{L}^{-2}\cdot\text{J}$	Luminous flux <i>incident</i> on a surface
Luminous exitance, luminous emittance	$M_v$	lumen per square metre	$\text{lm}/\text{m}^2$	$\text{L}^{-2}\cdot\text{J}$	Luminous flux <i>emitted</i> from a surface
Luminous exposure	$H_v$	lux second	$\text{lx}\cdot\text{s}$	$\text{L}^{-2}\cdot\text{T}\cdot\text{J}$	Time-integrated illuminance
Luminous energy density	$\omega_v$	lumen second per cubic metre	$\text{lm}\cdot\text{s}/\text{m}^3$	$\text{L}^{-3}\cdot\text{T}\cdot\text{J}$	
Luminous efficacy (of radiation)	$K$	lumen per watt	$\text{lm}/\text{W}$	$\text{M}^{-1}\cdot\text{L}^{-2}\cdot\text{T}^3\cdot\text{J}$	Ratio of luminous flux to <i>radiant flux</i>
Luminous efficacy (of a source)	$\eta$ <sup>[nb 3]</sup>	lumen per watt	$\text{lm}/\text{W}$	$\text{M}^{-1}\cdot\text{L}^{-2}\cdot\text{T}^3\cdot\text{J}$	Ratio of luminous flux to power consumption

How do we make sense of all these quantities?

# How should we define **bright**?



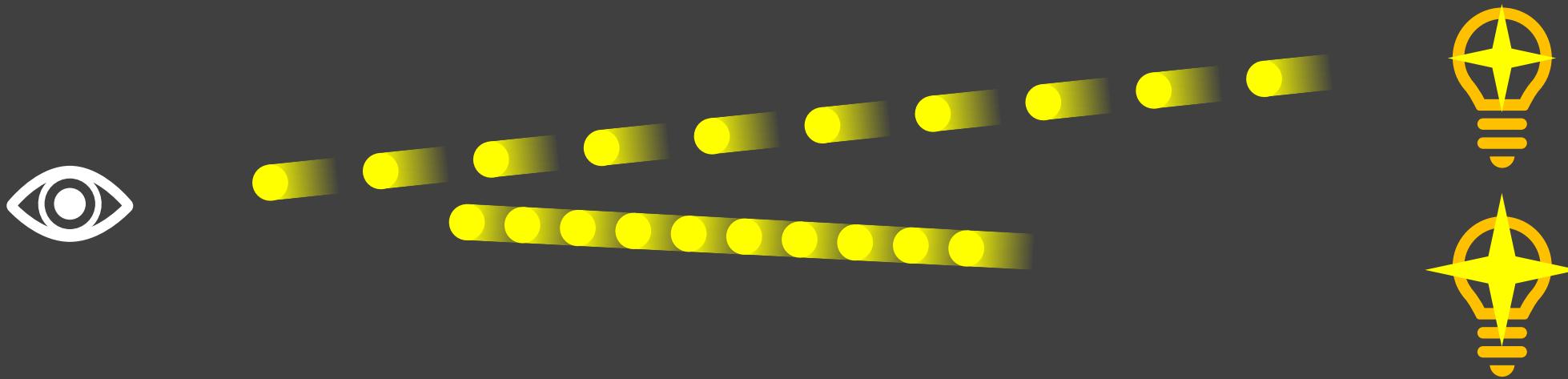
Brightness  $\propto \Delta E$



Maybe **bright** means we receive more energy from the light source?

# How should we define **bright**?

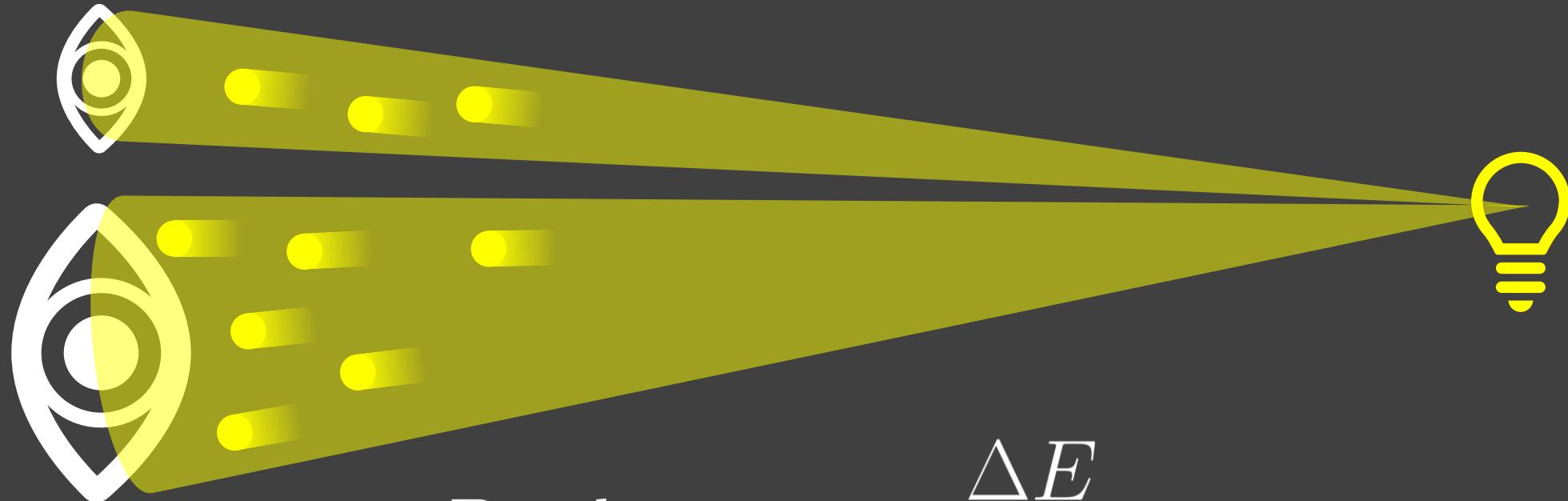
Things are brighter if you receive the same energy in a shorter time.



$$\text{Brightness} \propto \frac{\Delta E}{\Delta t}$$

# How should we define **bright**?

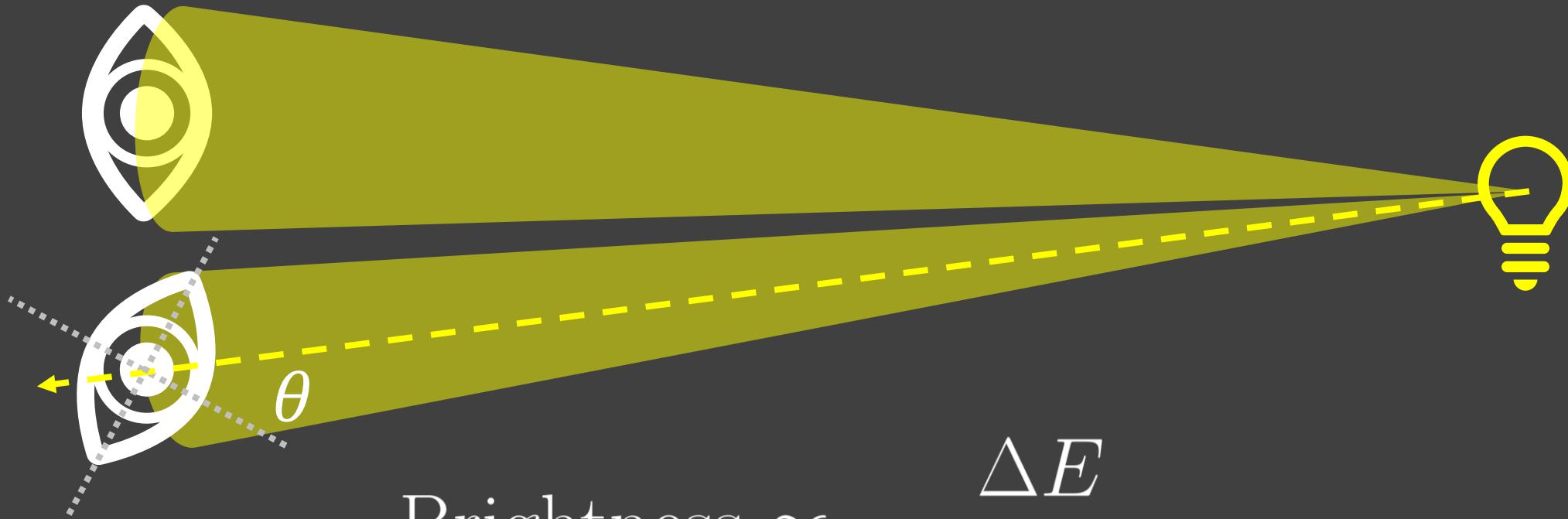
Larger collecting area gets more photons from the same light source.



$$\text{Brightness} \propto \frac{\Delta E}{\Delta A \Delta t}$$

# How should we define **bright**?

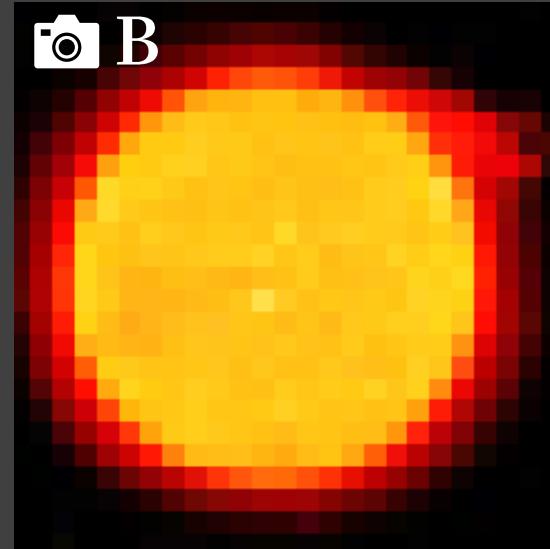
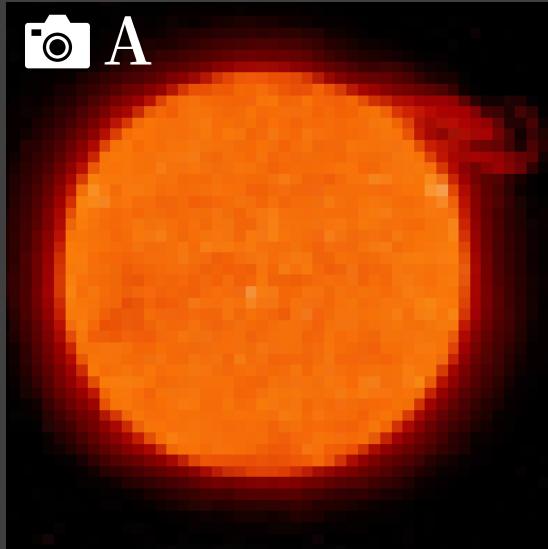
Tilted collecting area is effectively smaller.



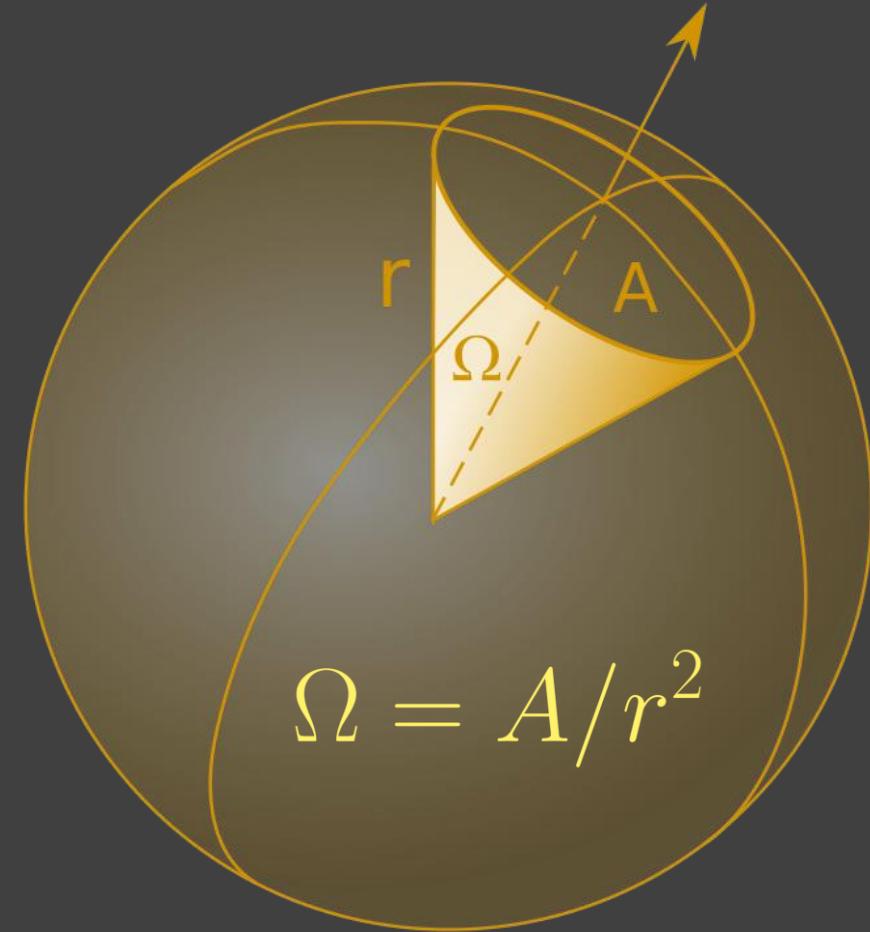
$$\text{Brightness} \propto \frac{\Delta E}{\cos \theta \Delta A \Delta t}$$

# How should we define **bright**?

Consider taking the picture of the sun with 2 different camera.

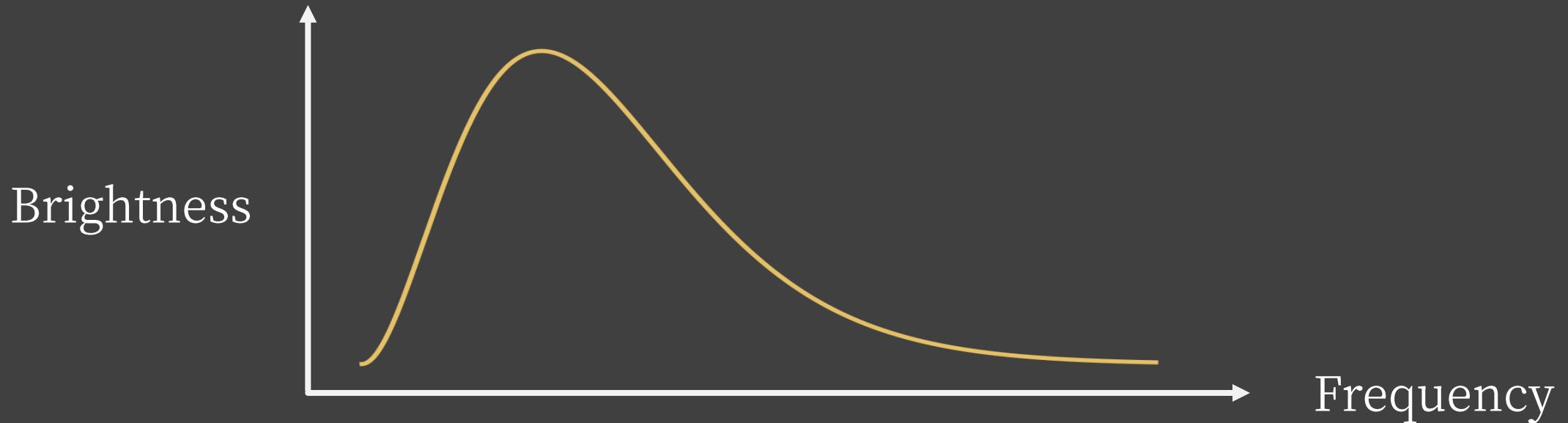


$$\text{Brightness} \propto \frac{\Delta E}{\cos \theta \Delta A \Delta t \Delta \Omega}$$



# How should we define **bright**?

Finally, brightness should be a function of frequency/wavelength.



$$\text{Brightness} \propto \frac{\Delta E}{\cos \theta \Delta A \Delta t \Delta \Omega \Delta \nu}$$

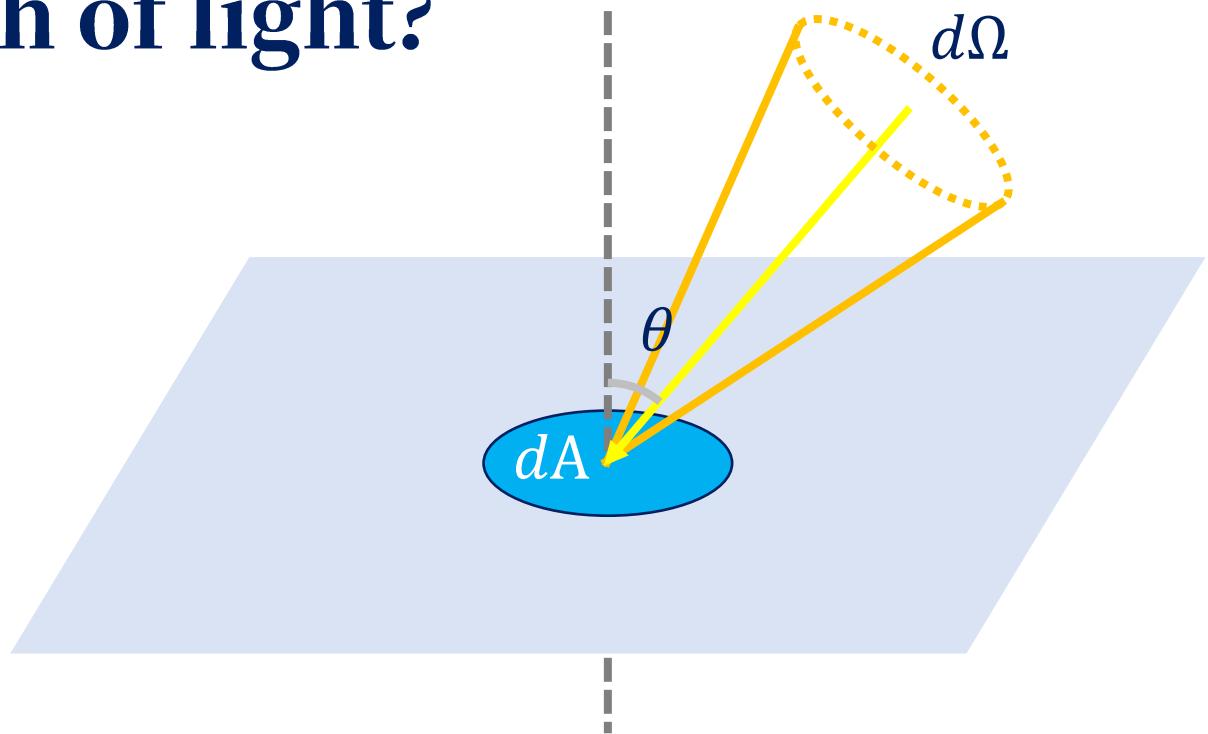
# How to define the strength of light?

The energy we receive is affected by

- Integration time
- Direction
- Collecting area
- Solid angle
- Frequency

From this, we define:

**Specific Intensity ( $I_\nu$ )**



$$I_\nu \equiv \frac{dE}{\cos \theta dA dt d\Omega d\nu}$$

Specific Intensity

# Other quantities

1. Energy Received ( $E$ ). Unit: [ J ].
2. Power ( $P$ ). Unit: [  $\text{J s}^{-1}$  ].
3. Flux ( $F$ ). Unit: [  $\text{J m}^{-2} \text{s}^{-1}$  ].
4. Total Intensity ( $I$ ). Unit: [  $\text{J m}^{-2} \text{sr}^{-1} \text{s}^{-1}$  ]. Also called **Surface Brightness**.
5. Specific Intensity ( $I_\nu$ ). Unit: [  $\text{J m}^{-2} \text{sr}^{-1} \text{s}^{-1} \text{Hz}^{-1}$  ].

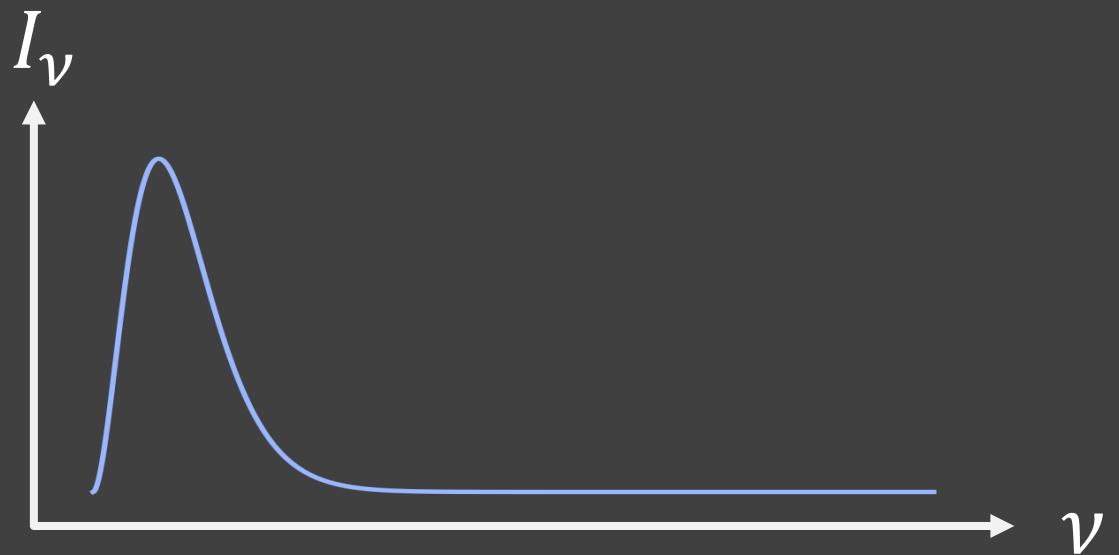
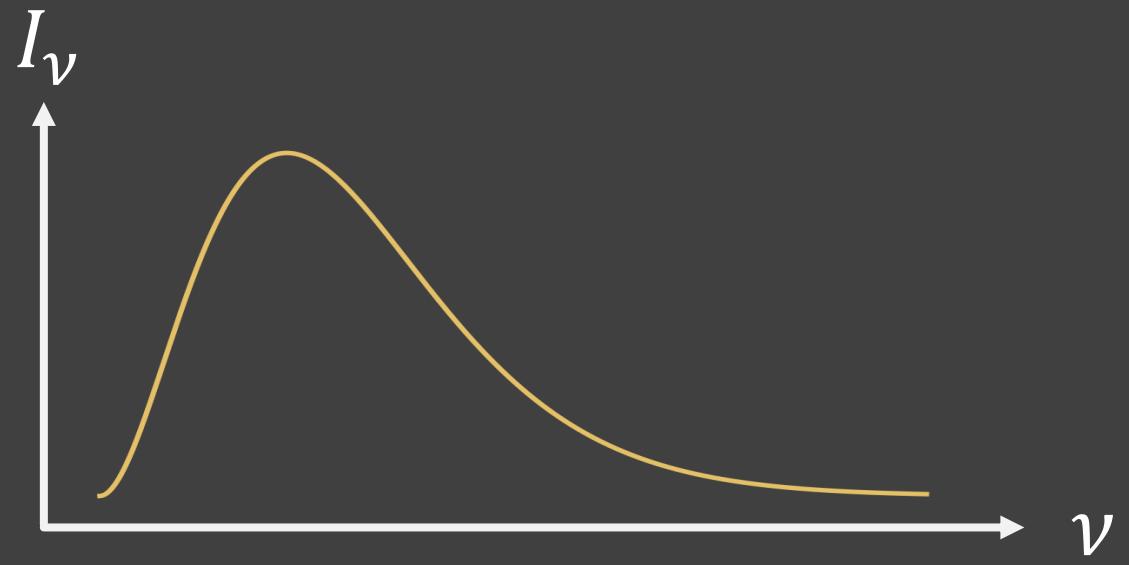
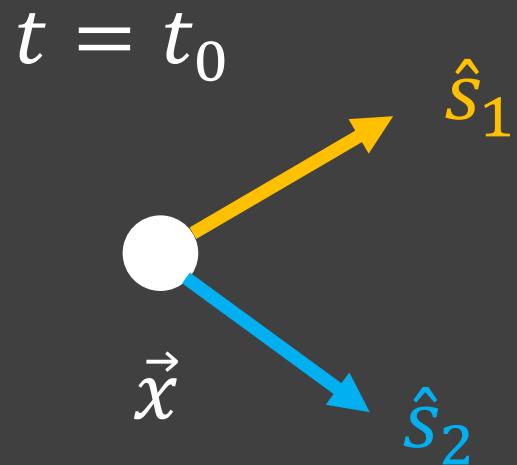
$$\frac{dE}{\cos \theta \, dt dA d\Omega d\nu} = I_\nu$$

The **names** are not important. What you should care about is the **units**.

$I_\nu$  is convenient because it is an **intrinsic** property of the source.

Specific intensity is a function  
of position, direction,  
frequency, and time.

$$I_\nu = I_\nu(\vec{x}, \hat{s}, \nu, t)$$



# Key property: intensity does not decay with distance!!!

With no absorption / emission, specific intensity does not change.

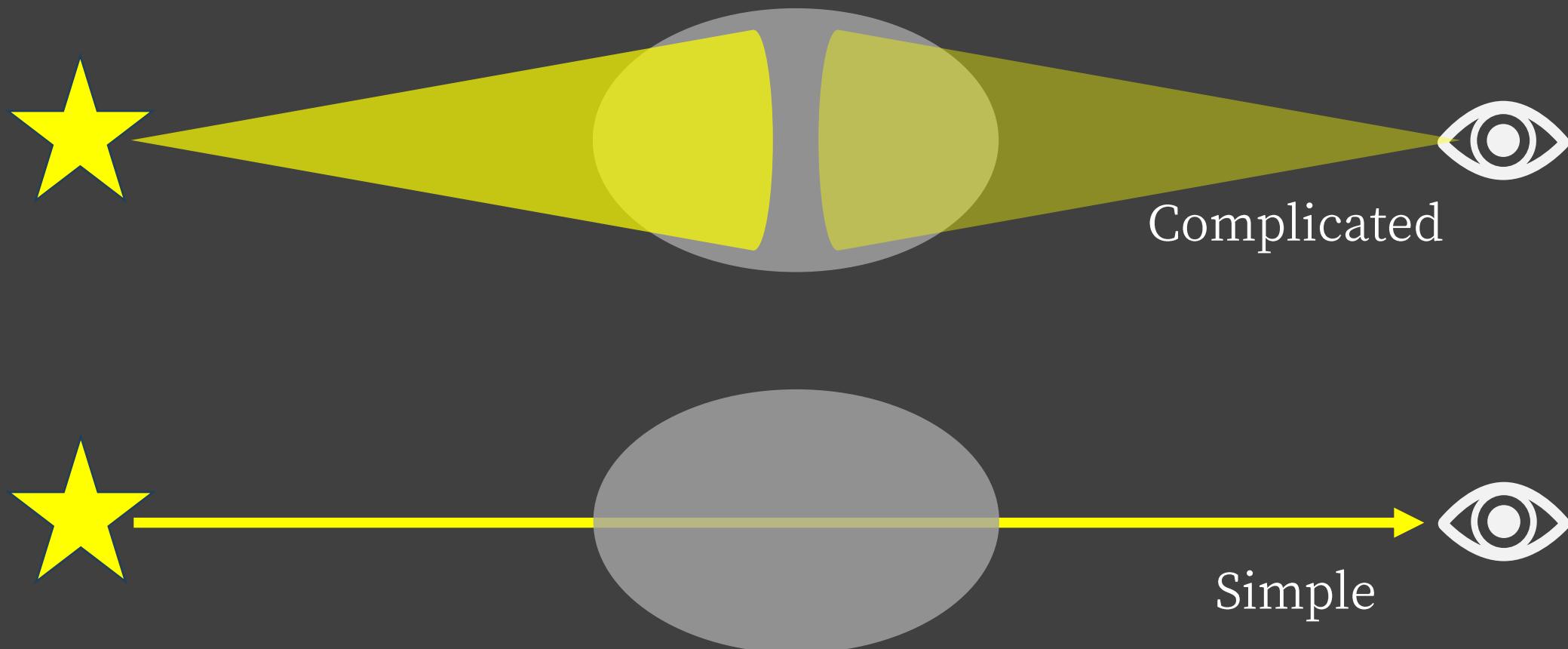


The flux decrease with  $1/r^2$ , but the specific intensity do not, because the solid angle of the Sun also decrease with  $1/r^2$ .

$$I_\nu = \frac{F_\nu}{\Omega} = \frac{F_0(r/r_0)^{-2}}{\Omega_0(r/r_0)^{-2}} = \text{const.}$$

# But how is that useful?

That simplifies the problem into 1D.



## Summary 01

# How do we define brightness?

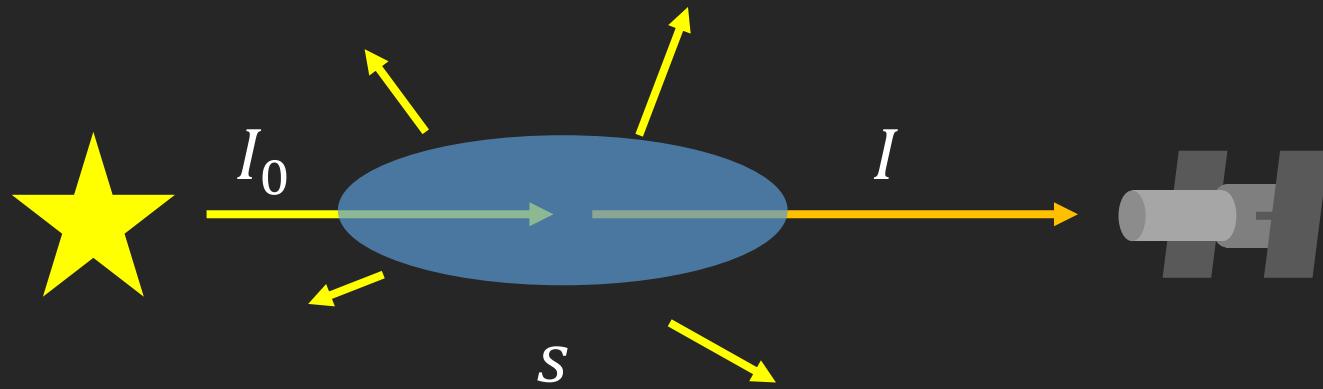
1. Astronomers like to use **specific intensity**.
2. Specific intensity is the **energy** you receive per unit **time, frequency, area, and solid angle**.
3. Specific intensity do **not** decay with distance!
4. Why should you know specific intensity?
  - You better be able to understand what people are saying.
  - You want to find invariant-like quantity in a complicated system, so that the problems are simplified, and you get physical intuition.

$$I_\nu \equiv \frac{dE}{\cos \theta dA dt d\Omega d\nu}$$

# Change of intensity: Radiative transfer

What will change the specific intensity?

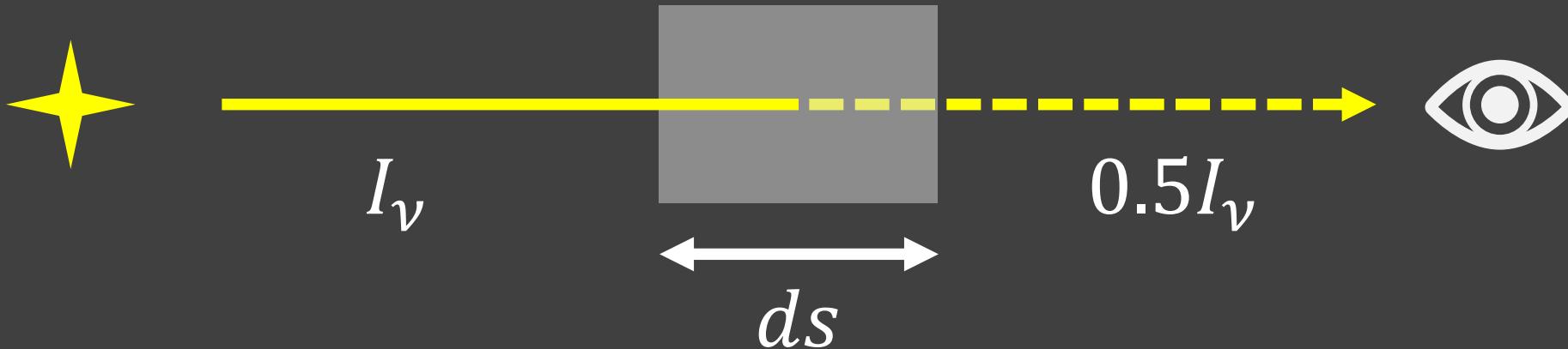
Emission, Absorption and Scattering.



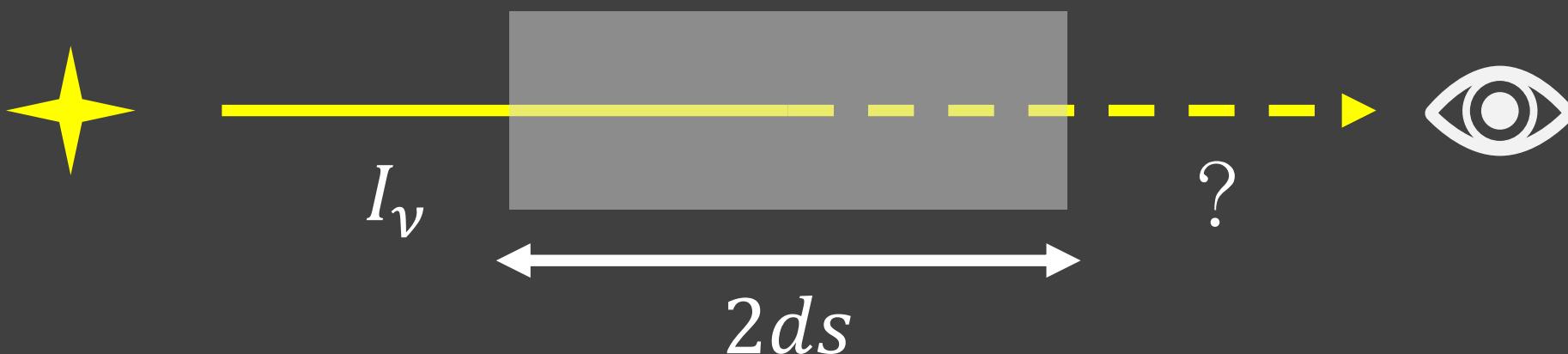
$$\frac{dI_\nu}{ds} = -\alpha_\nu I_\nu + j_\nu$$

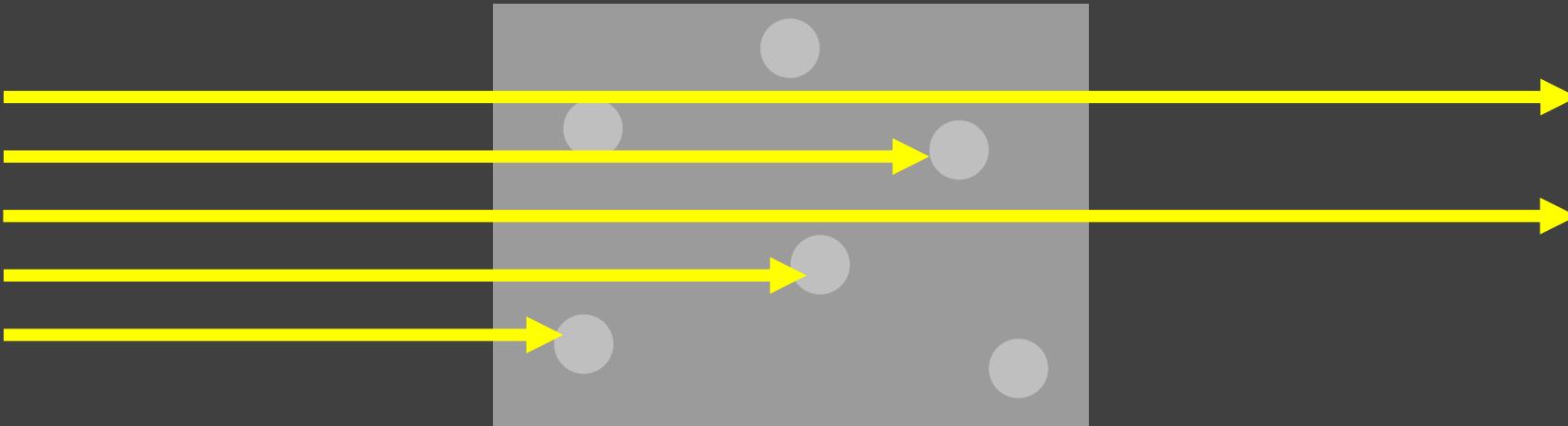
## Case: pure absorption

Consider a gas cloud with length  $ds$  absorbed 50% of the incident light.

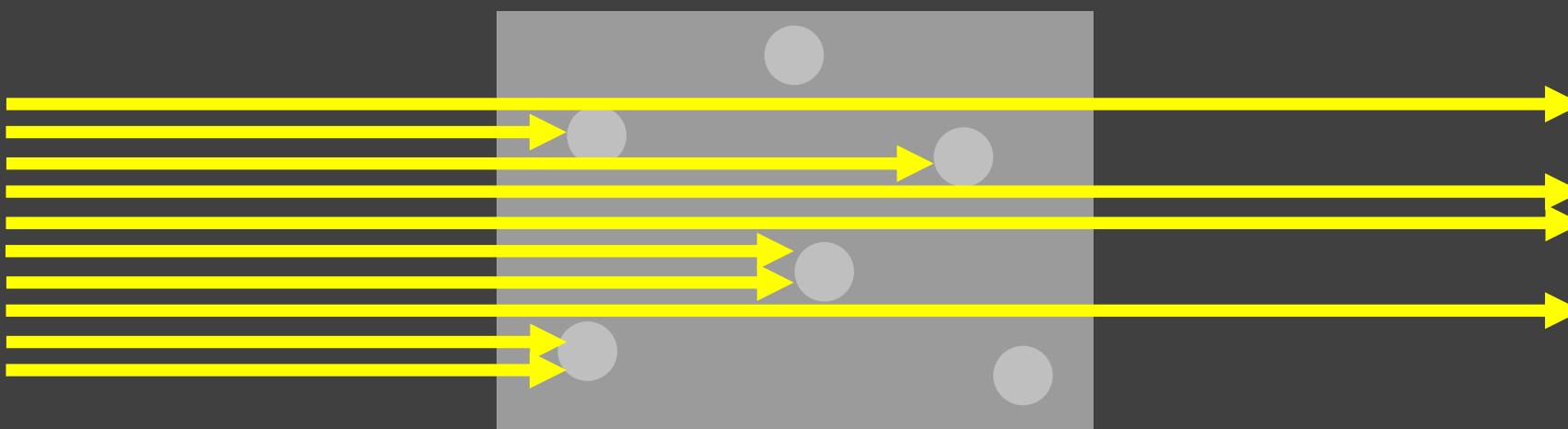


Now if the cloud is 2 times longer, what would the final intensity be?





The fraction of light being absorbed is fixed.



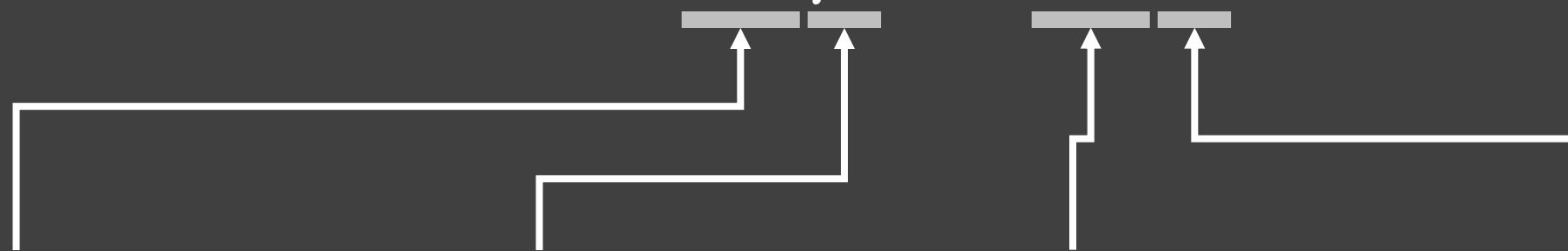
So to put our intuition into the language of physics,  
we can write:

$$dI_\nu = -\alpha_\nu I_\nu ds$$

Where  $\alpha_\nu$  is called the **absorption coefficient**.  
That describe how **opaque** the gas cloud / medium is.

We can further express the absorption coefficient as:

$$\alpha_\nu = \kappa_\nu \rho = \sigma_\nu n$$



Opacity

[ $\text{cm}^2 \text{g}^{-1}$ ]

Density

[ $\text{g cm}^{-3}$ ]

Cross section

[ $\text{cm}^2$ ]

Number density

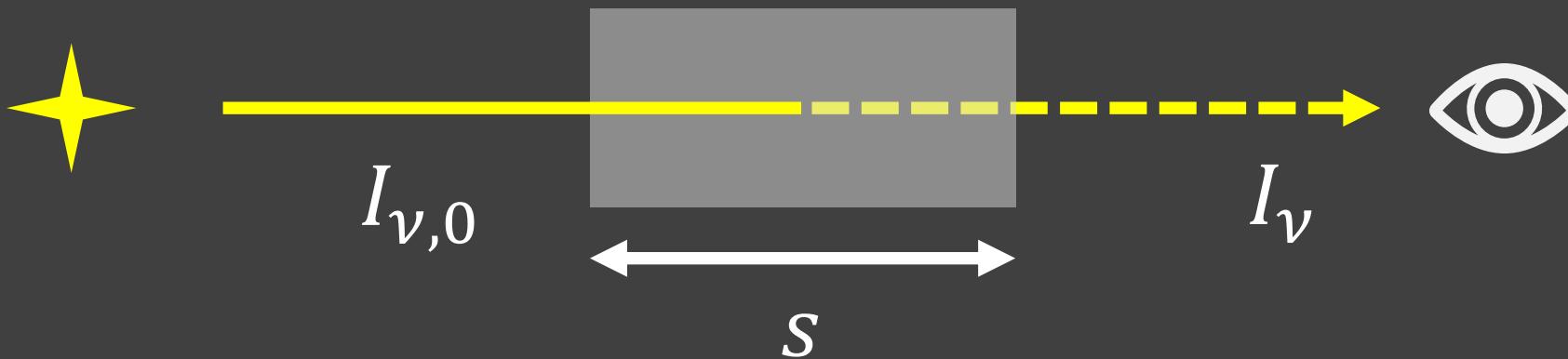
[ $\text{cm}^{-3}$ ]

In astrophysics, people usually use opacity.

So when there is only absorption, we know:

$$\frac{dI_\nu}{ds} = -\rho\kappa_\nu I_\nu$$

In a simple case where the cloud is uniform,  
what is the solution to this ODE?

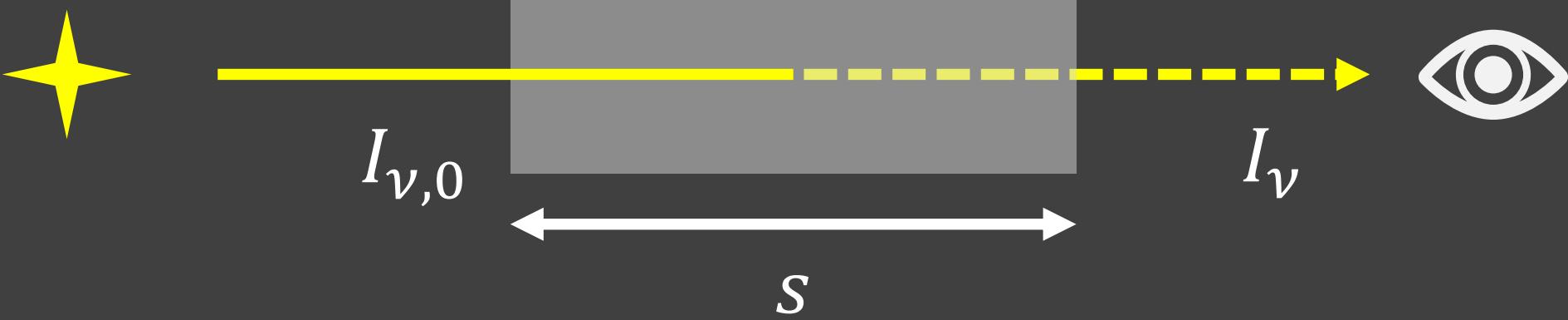
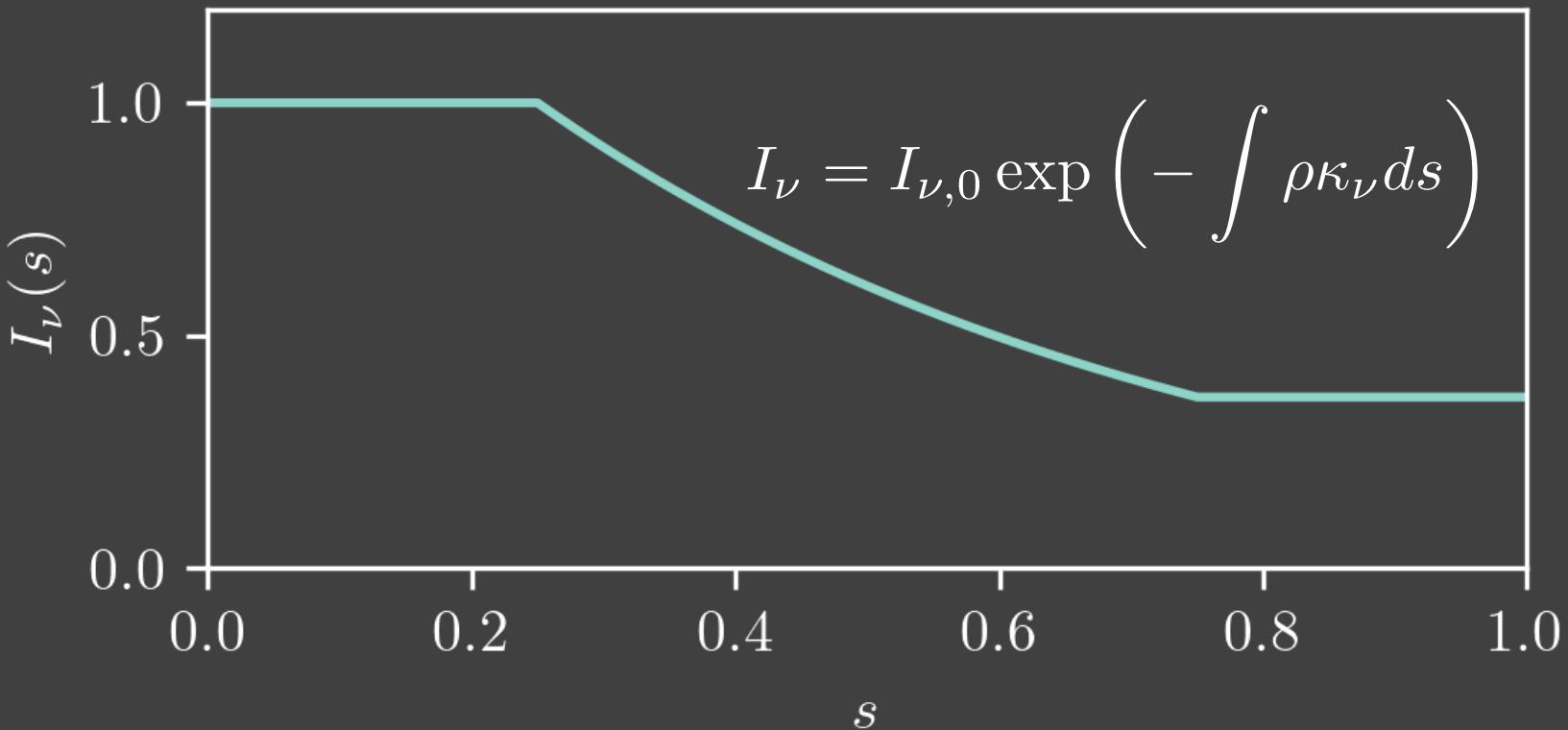


We can do:

$$\frac{dI_\nu}{ds} = -\rho\kappa_\nu I_\nu$$

$$\frac{dI_\nu}{I_\nu} = -\rho\kappa_\nu ds \Rightarrow \int \frac{dI_\nu}{I_\nu} = - \int \rho\kappa_\nu ds$$

$$\ln I_\nu + C = - \int \rho\kappa_\nu ds \Rightarrow I_\nu = I_{\nu,0} \exp \left( - \int \rho\kappa_\nu ds \right)$$



We therefore define the **optical depth**:

$$\tau_\nu = \int \rho \kappa_\nu ds = \ln \left( \frac{I_{\nu,0}}{I_\nu} \right)$$

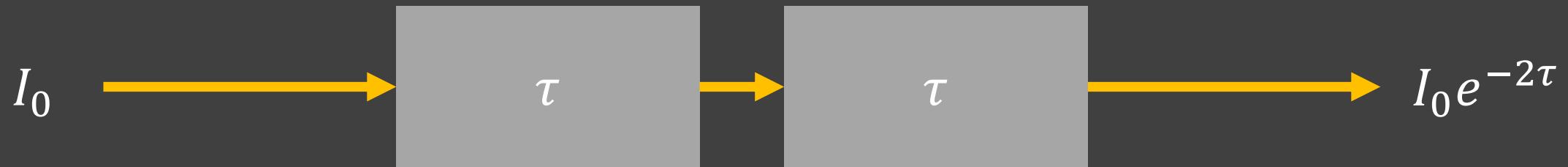
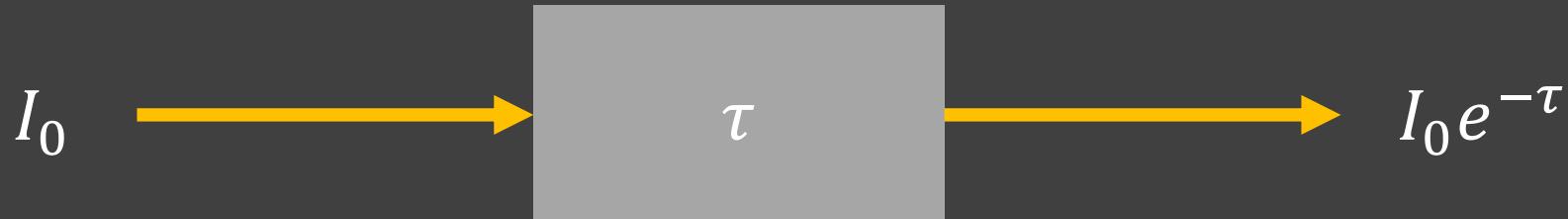
A dimensionless quantity that describes how much light (numbers of e-folding) is absorbed by the medium.

For example, for a gas cloud with:

$$\tau = 1 \Rightarrow I_\nu = I_{\nu,0} e^{-1} = 0.368 I_{\nu,0}$$

$$\tau = 10 \Rightarrow I_\nu = I_{\nu,0} e^{-10} = 4.540 \times 10^{-5} I_{\nu,0}$$

Optical depth is **additive**.



The combined absorption from  
2 clouds each with optical depth  $\tau$  is just  $2\tau$

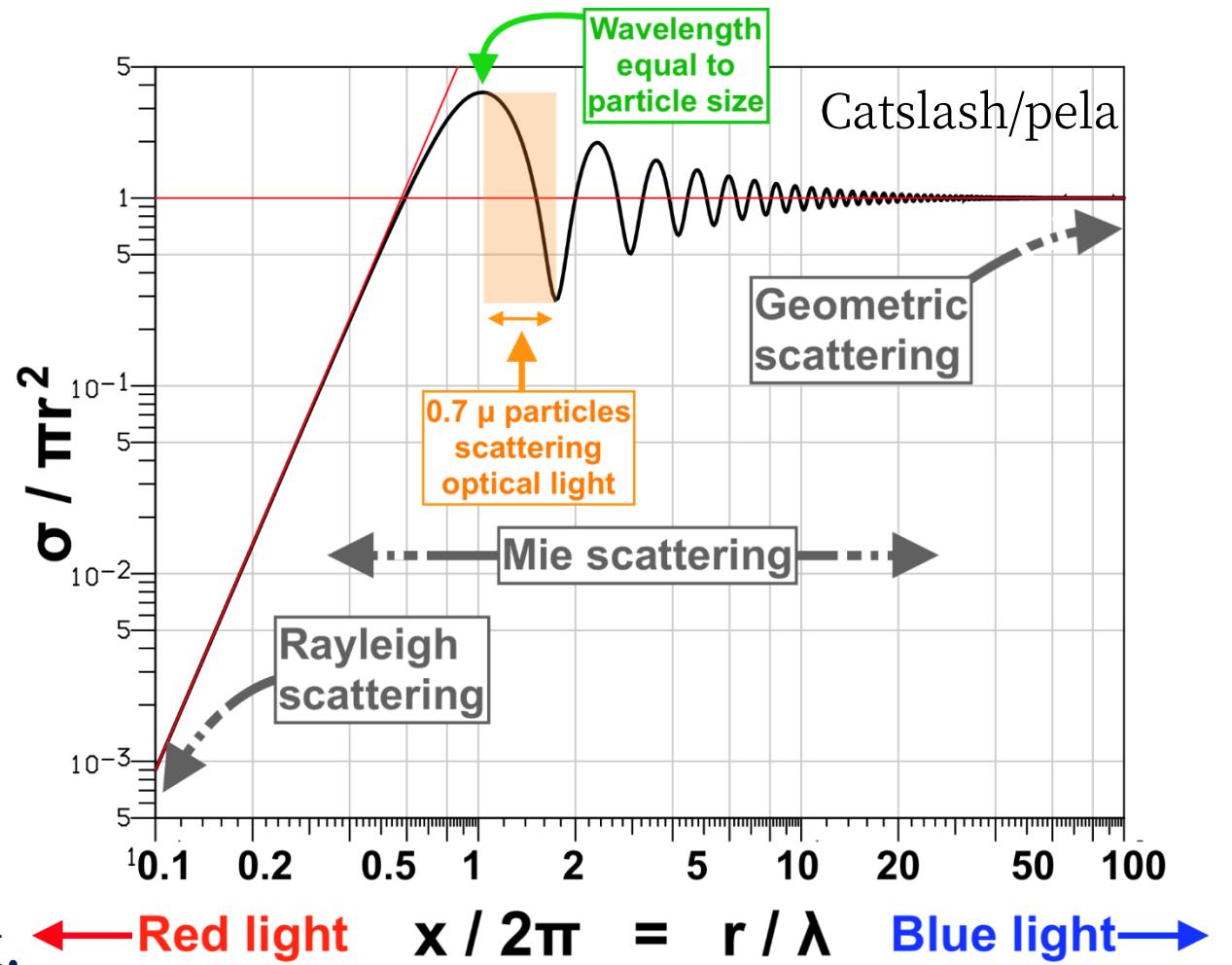
Nightmare

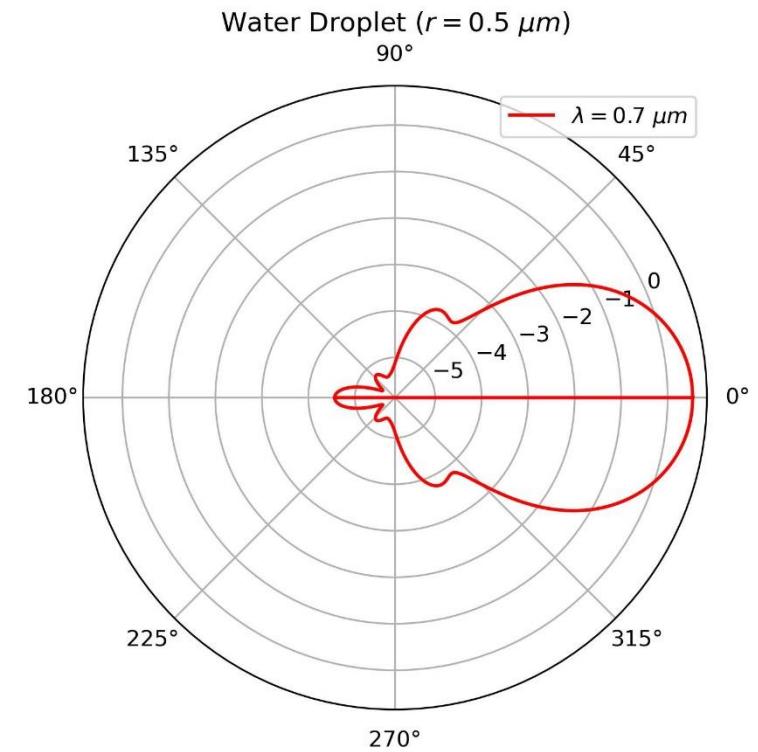
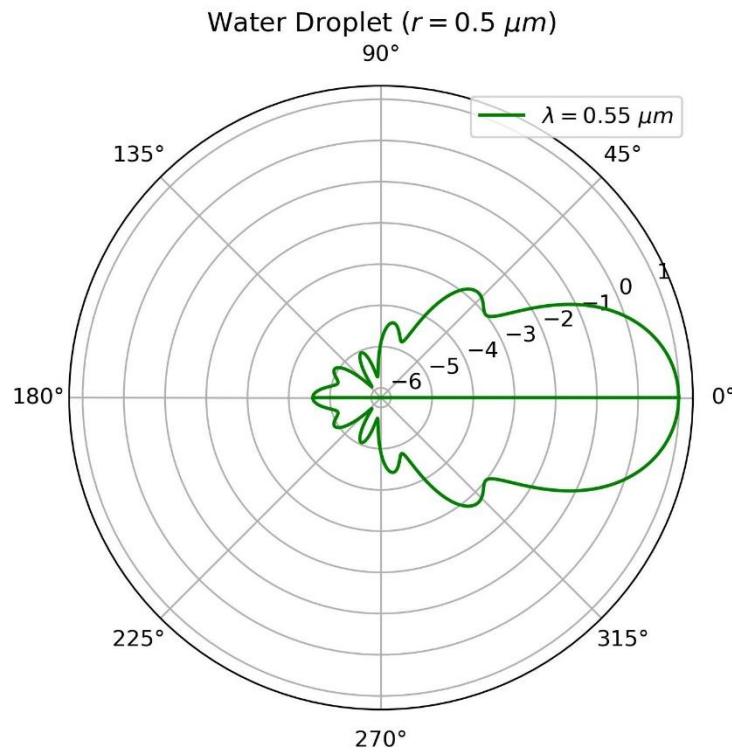
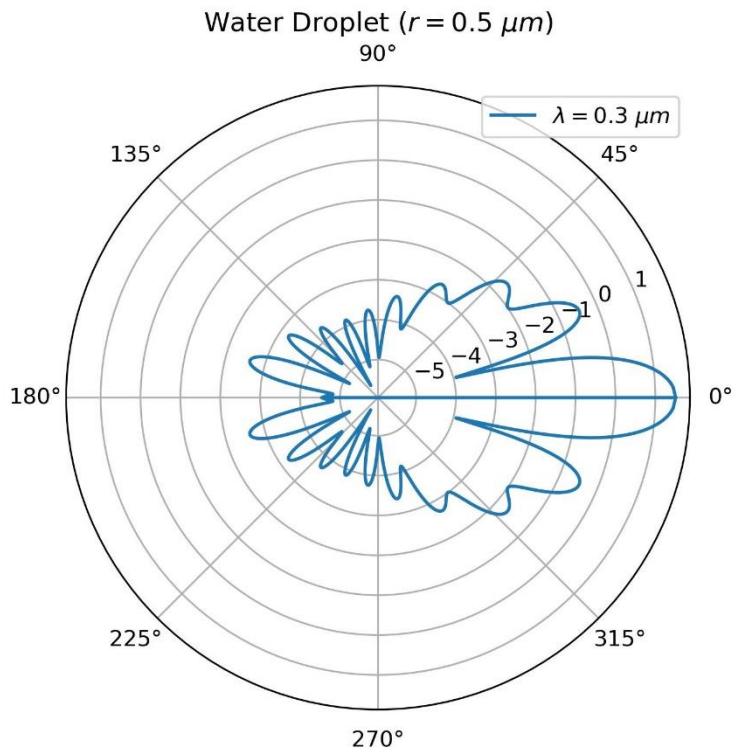
# Scattering

In reality, photons can be scattered back into the line of sight, which screw up everything.

With scattering, our problem is no longer 1 dimensional.

Now, we have to consider the complicated geometry of our target.

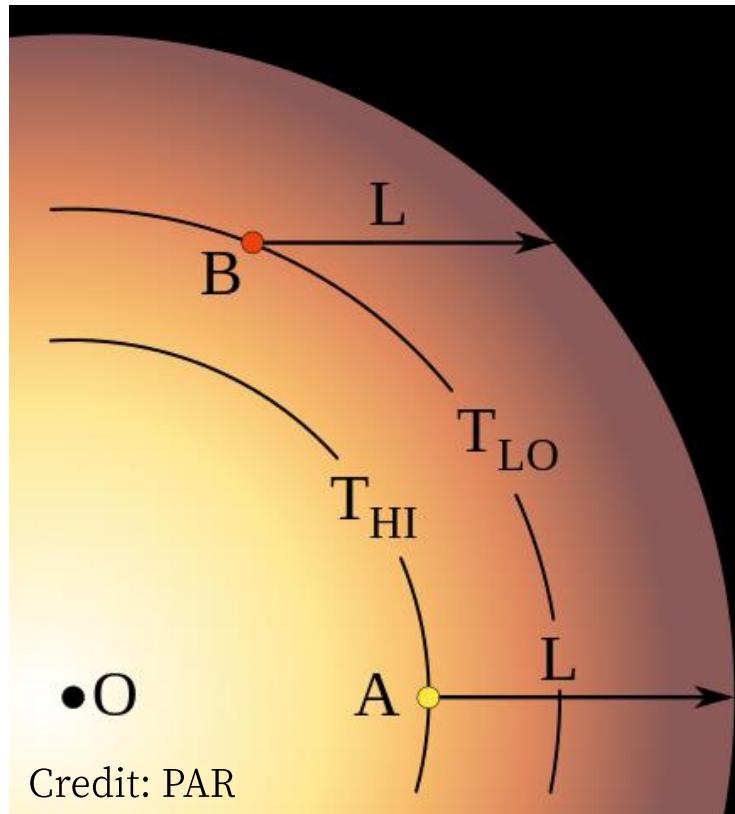




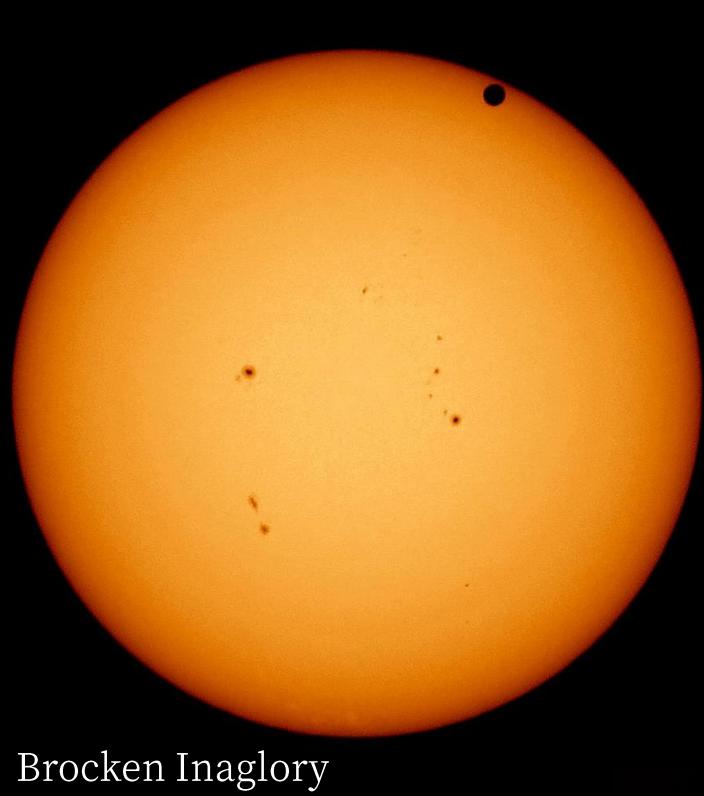
Scattering is not only wavelength dependent, but also anisotropic.  
Different wavelength / grain size, creates different scattering pattern.  
This is very hard to model analytically.

Examples

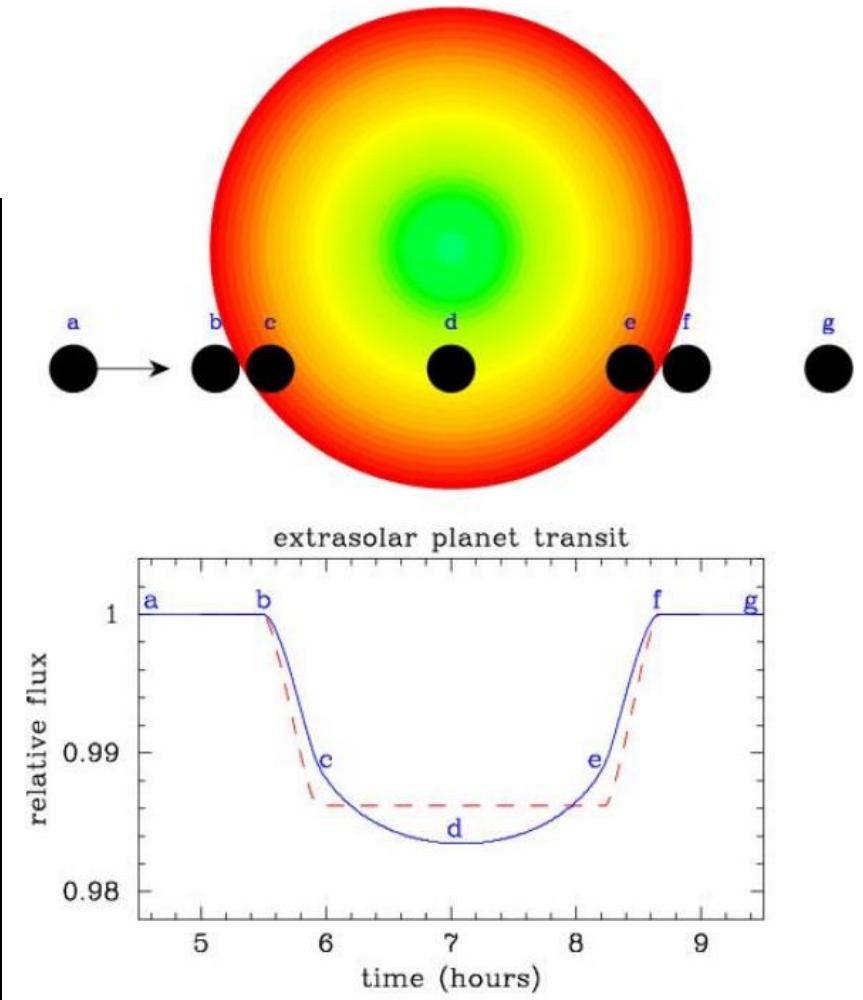
# Limb darkening



Credit: PAR



Brocken Inaglory



Coughlin 2012

Examples

# Dust Extinction

Extinction = absorption + scattering.

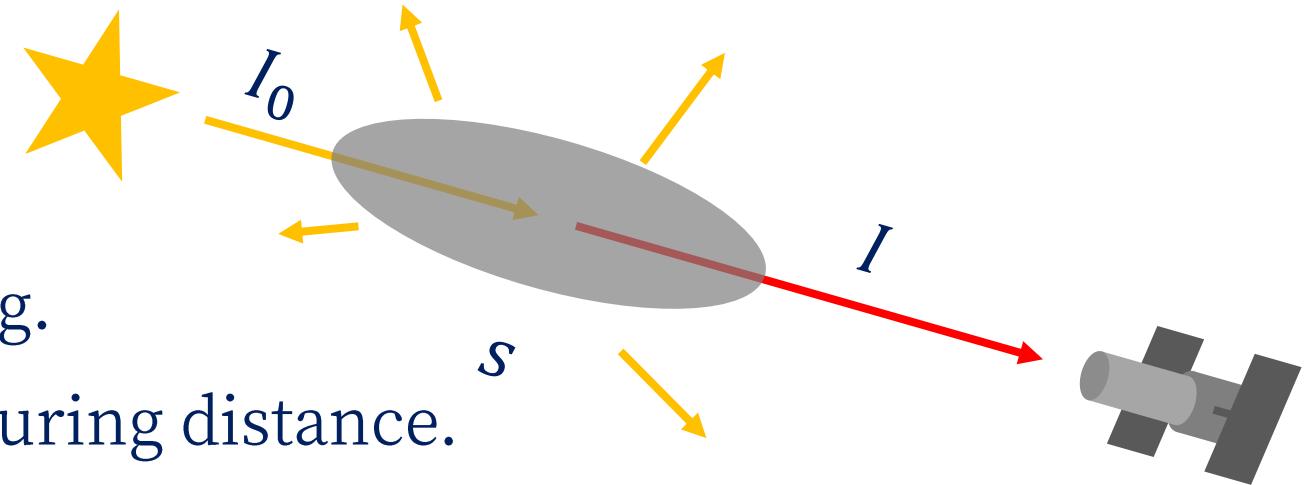
This can be important in e.g. measuring distance.

The original distance modulus is:

$$m_\lambda - M_\lambda = 5 \log D - 5$$

But when there is dust, we should use

$$m_\lambda - M_\lambda = 5 \log D - 5 + A_\lambda$$



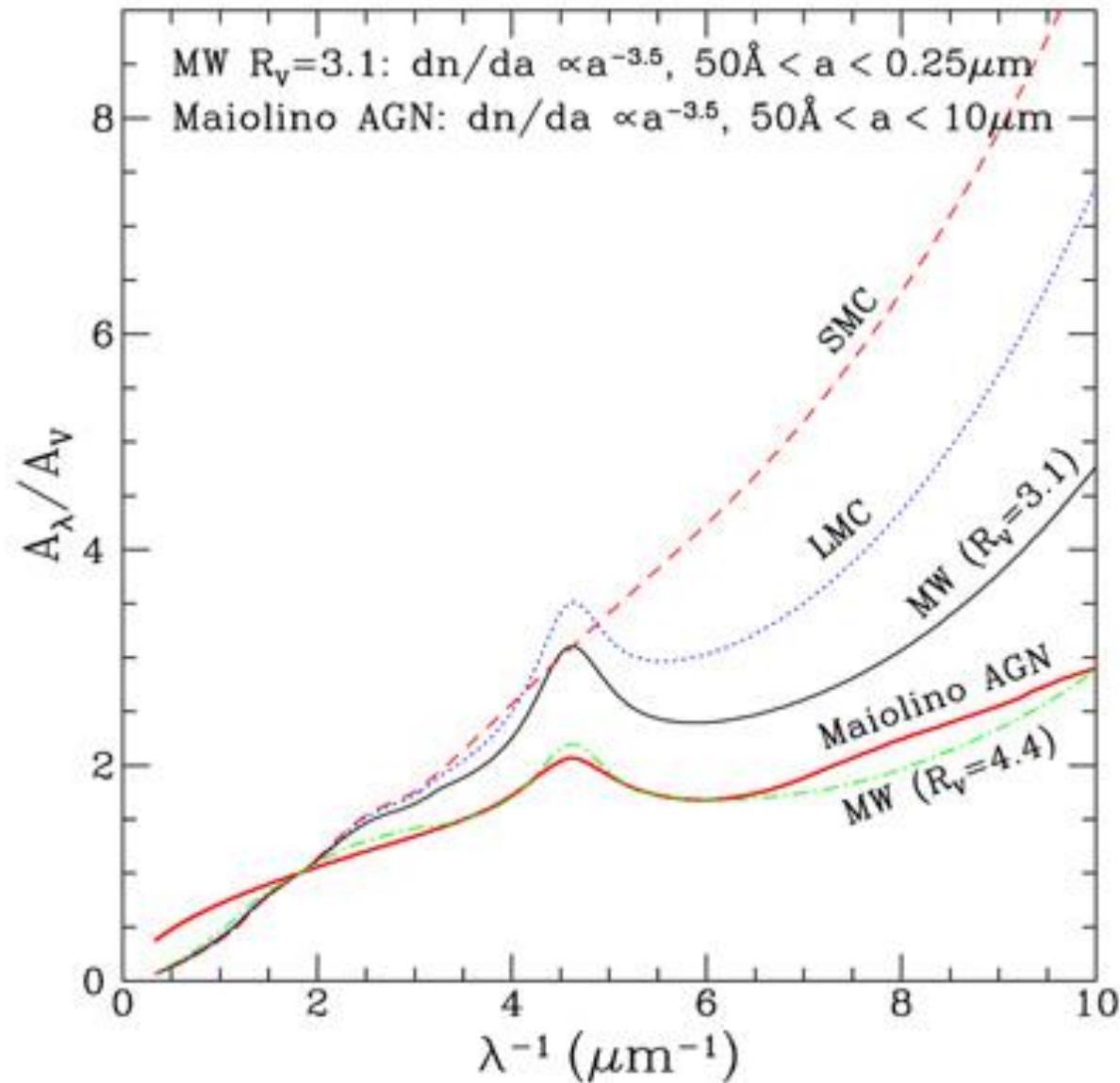
Examples

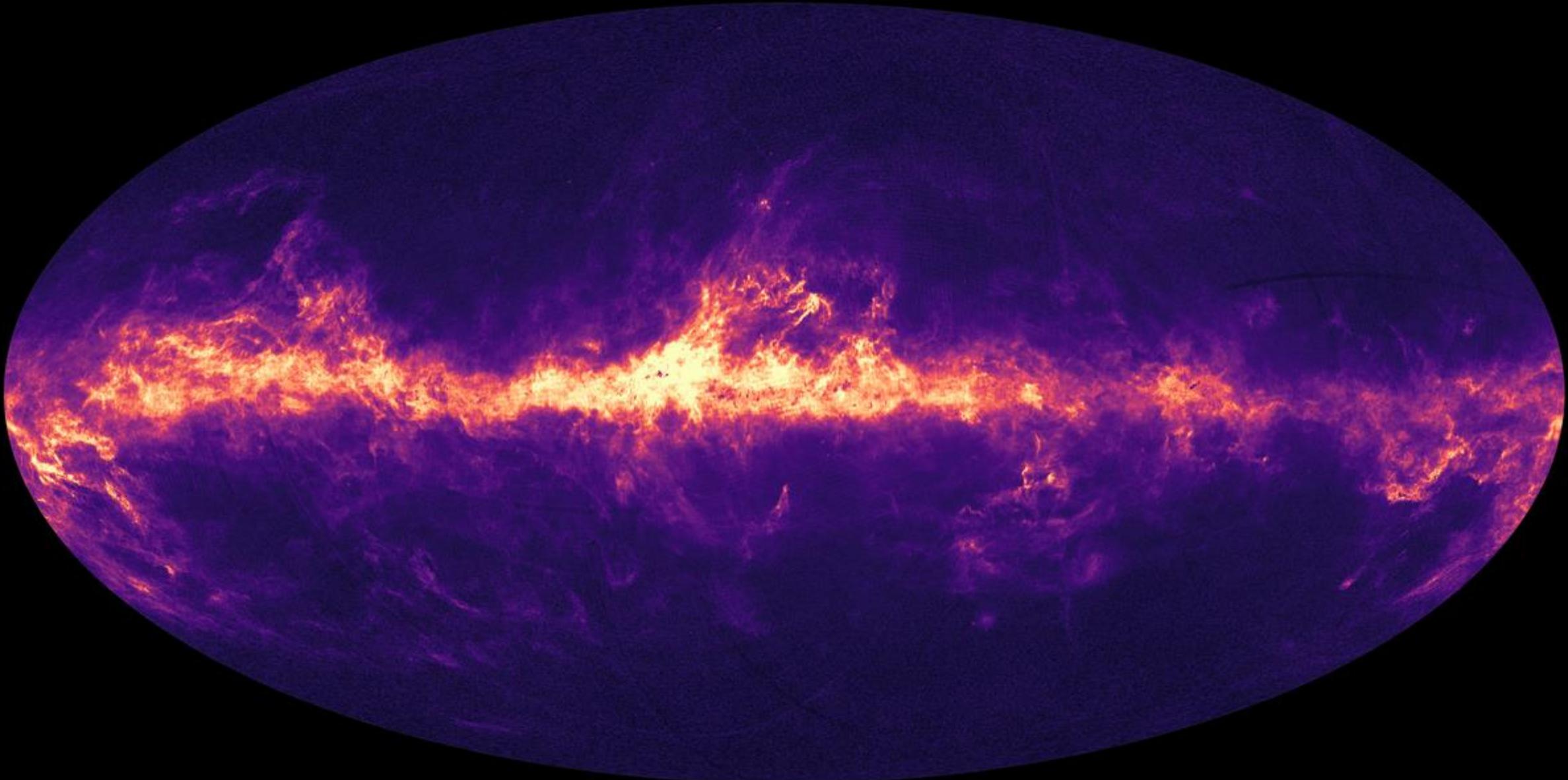
# Dust Extinction

More importantly, extinction strength changes with wavelength.

In optical, the short wavelength light usually suffers stronger extinction, creating the **reddening effect**.

The wavelength dependence of extinction is called **extinction curve**.





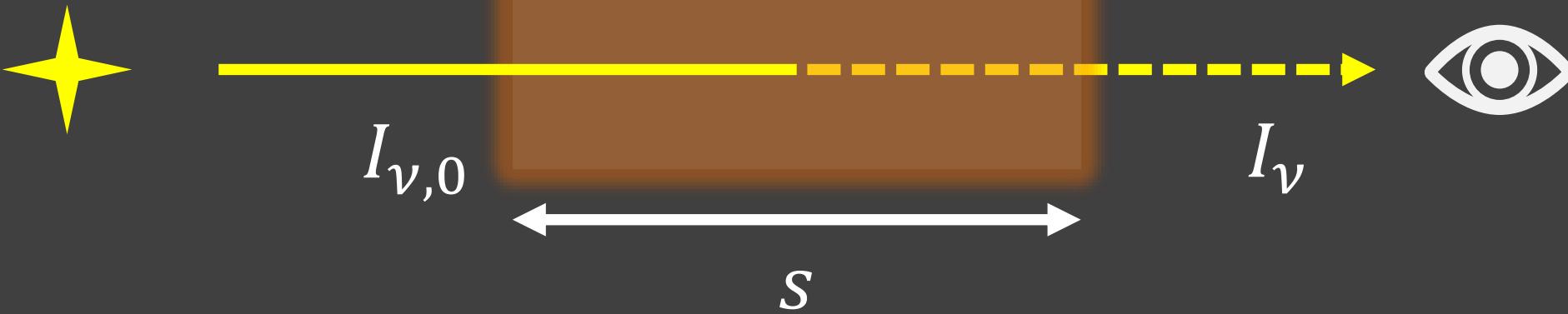
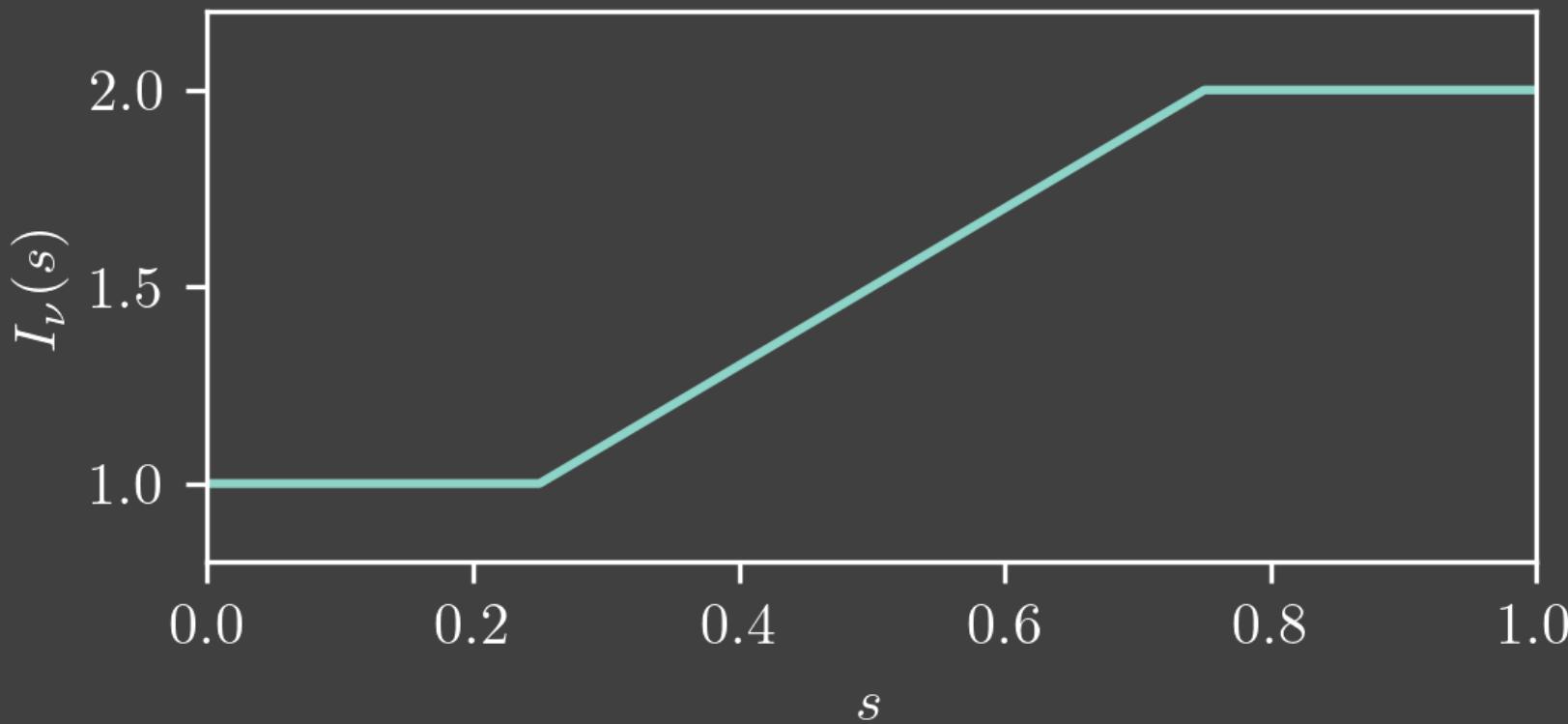
ESA/Gaia/DPAC, CC BY-SA 3.0 IGO

## What about emission?

Since emission does not depends on the incident intensity\*,  
in pure emission case, we simply have

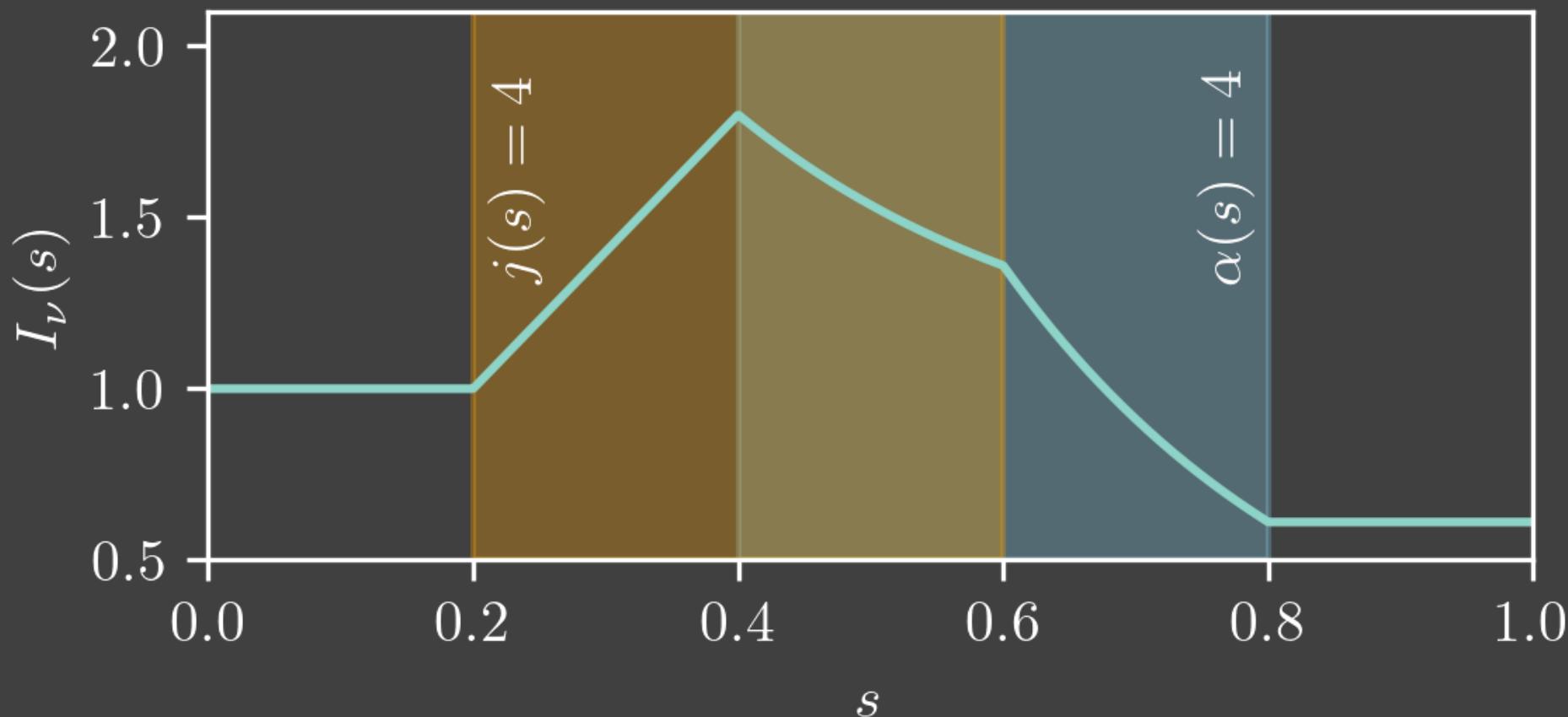
$$dI_\nu = j_\nu ds, \quad I_\nu = \int j_\nu ds$$

Where  $j_\nu$  is called the **emission coefficient**.



# The Radiative Transfer Equation (RTE)

$$\frac{dI_\nu}{ds} = -\kappa_\nu \rho I_\nu + j_\nu$$

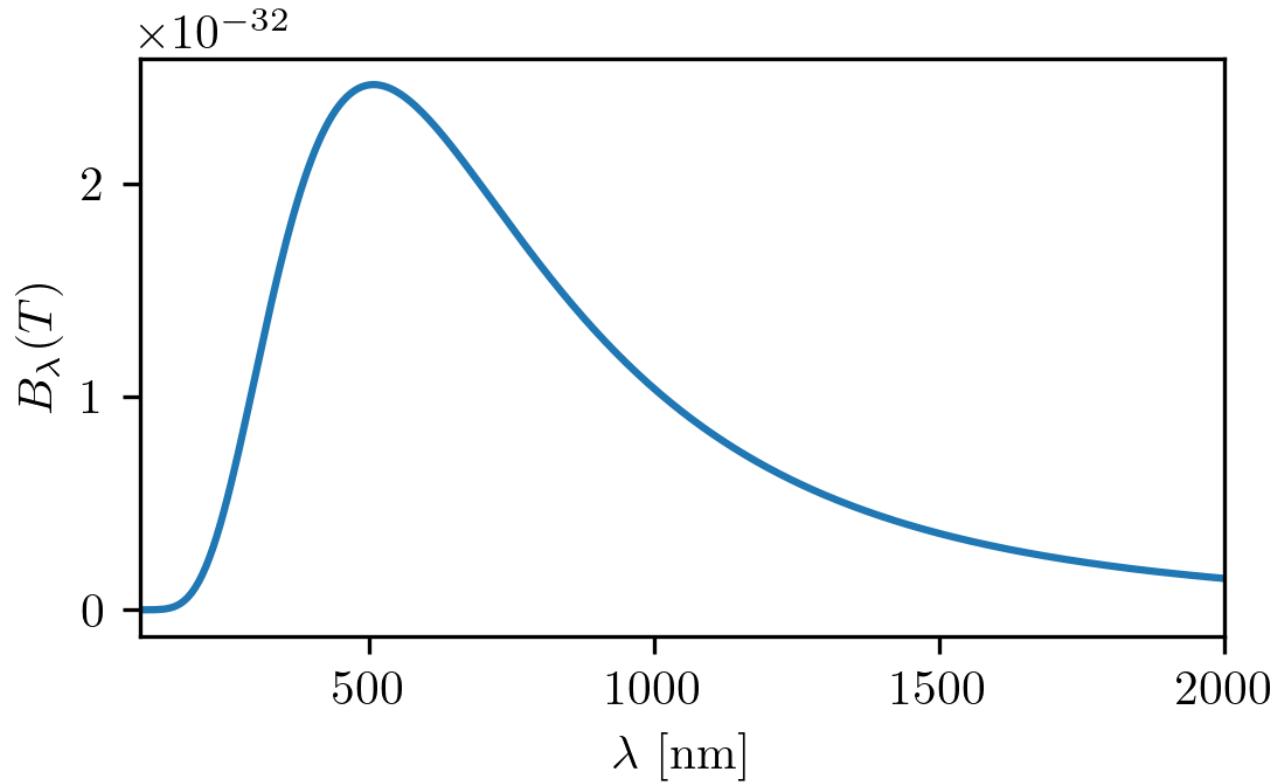


# Emission mechanisms

Emission mechanisms

# Black body radiation (BBR)

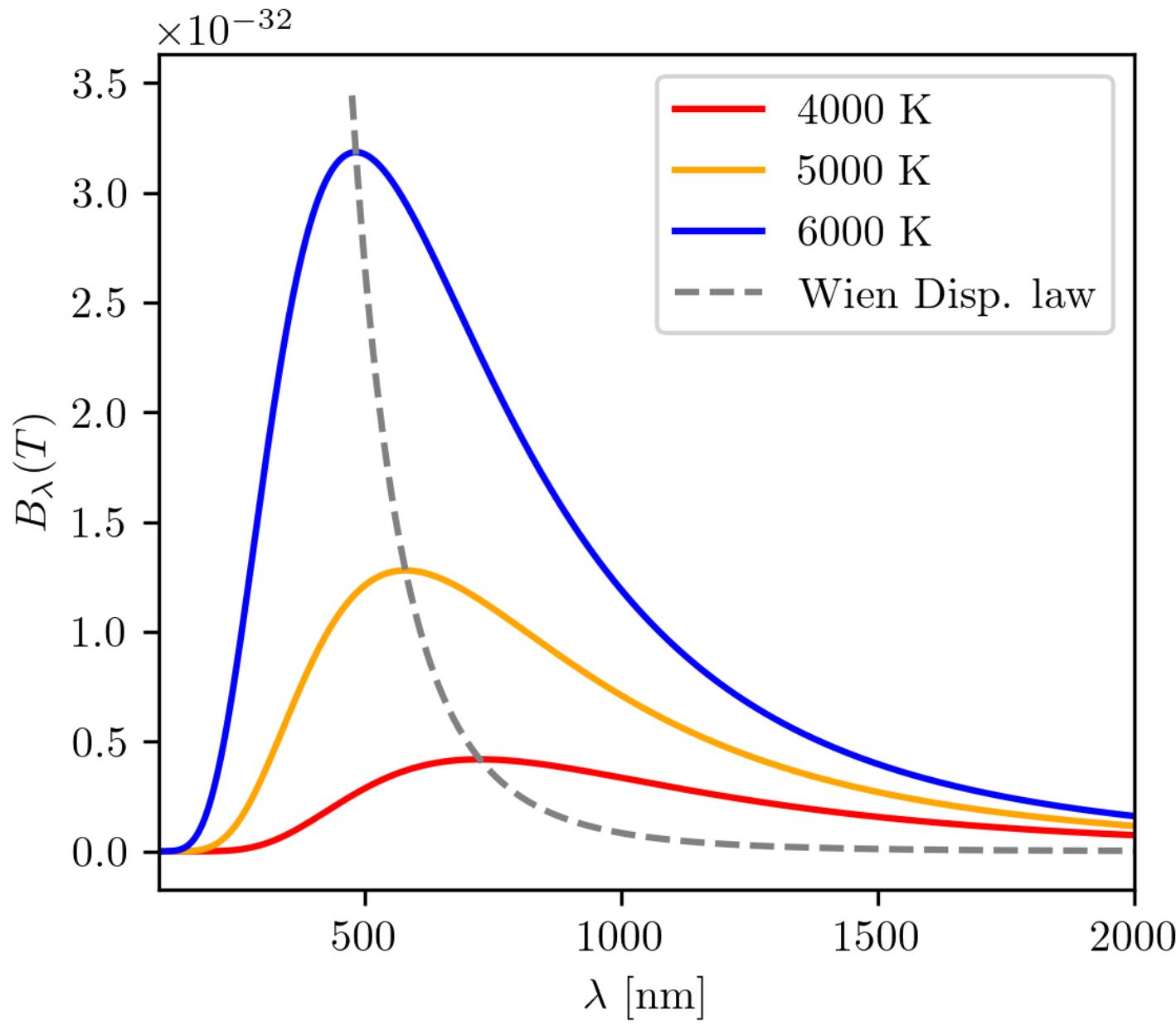
Emission coming from matter (and photons) in thermal equilibrium.



**Planck function**

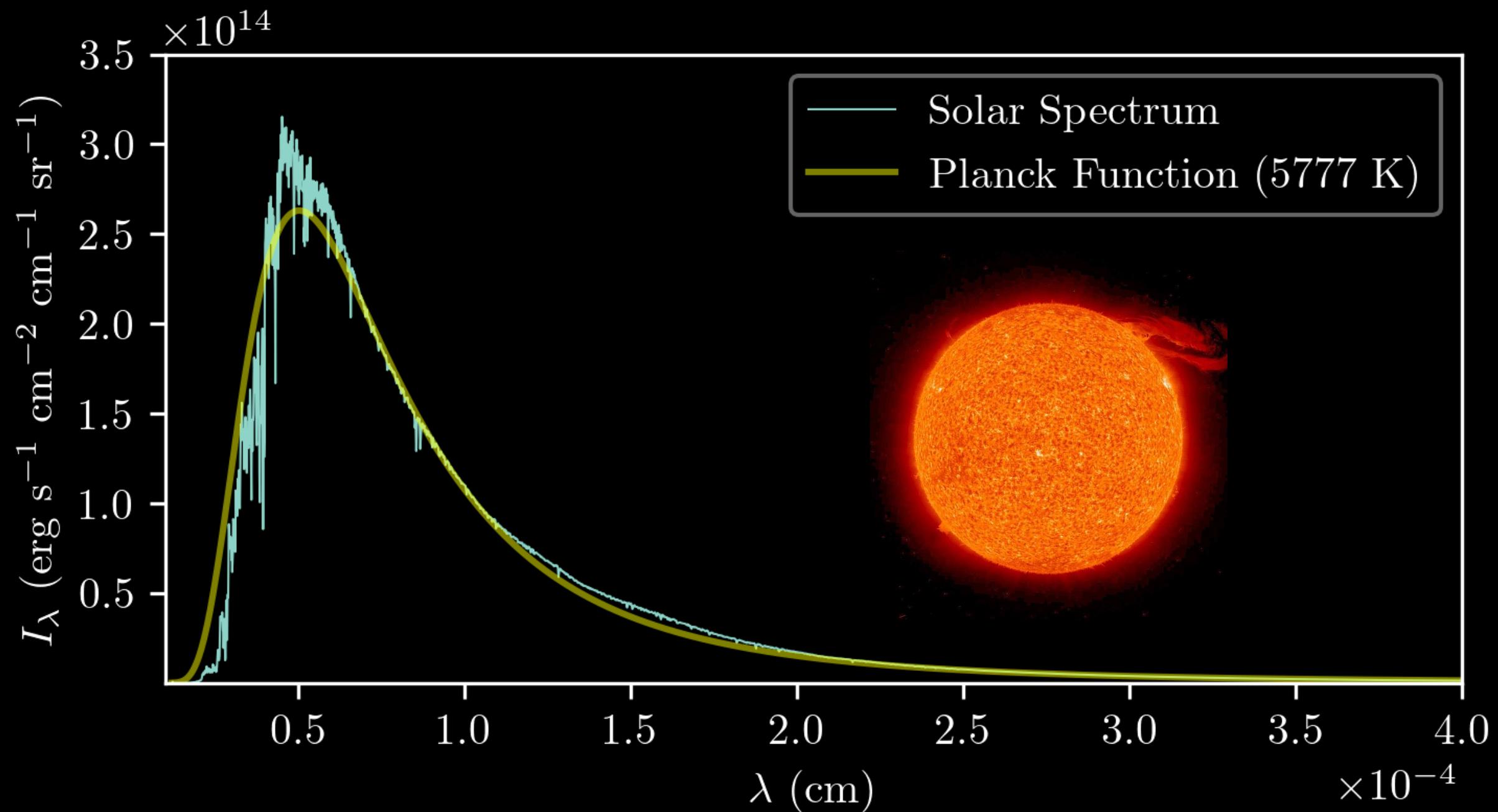
$$B_\lambda(\lambda, T) = \frac{2hc^2}{\lambda^5} \frac{1}{e^{hc/(\lambda k_B T)} - 1}$$

$$B_\nu(\nu, T) = \frac{2h\nu^3}{c^2} \frac{1}{e^{h\nu/(k_B T)} - 1}$$



## Wien Displacement Law

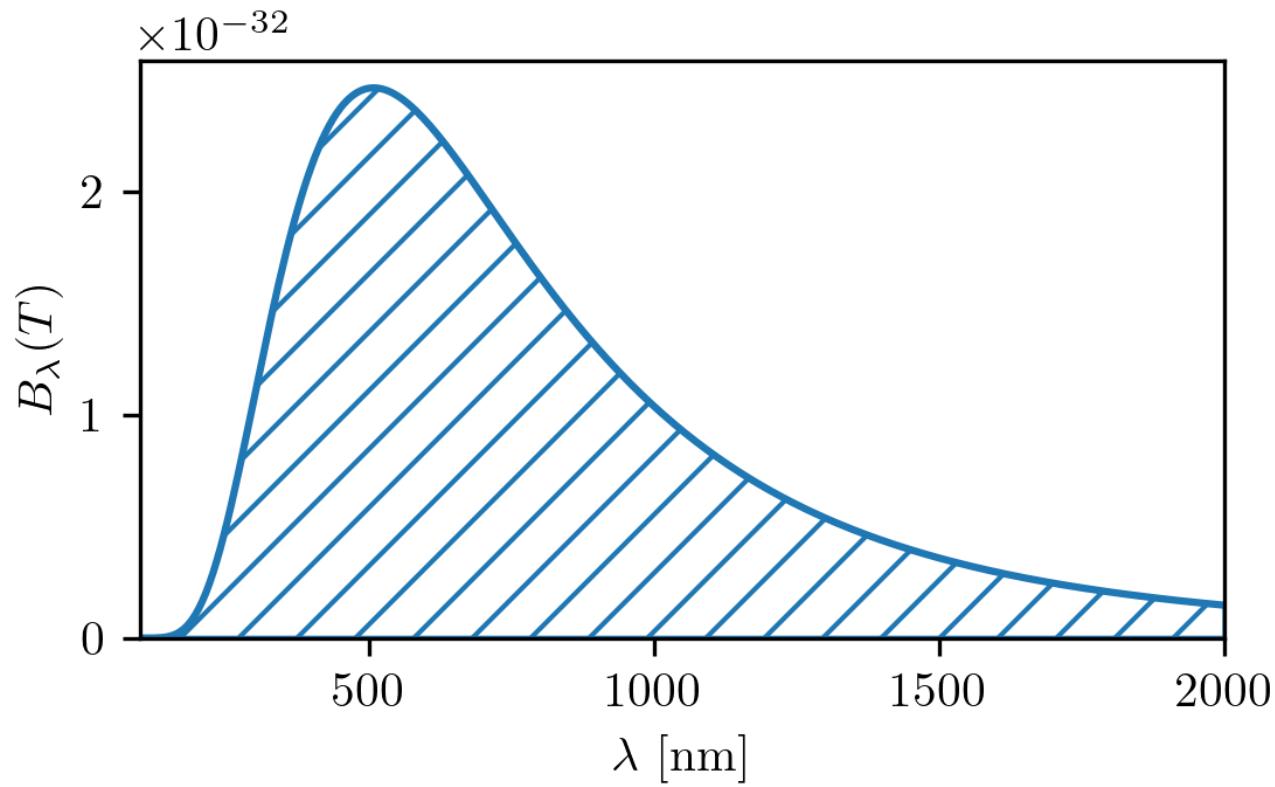
$$\lambda_{\max} = \frac{2.9 \times 10^{-3}}{T \text{ (K)}} \text{ m}$$



Emission mechanisms

# Black body radiation (BBR)

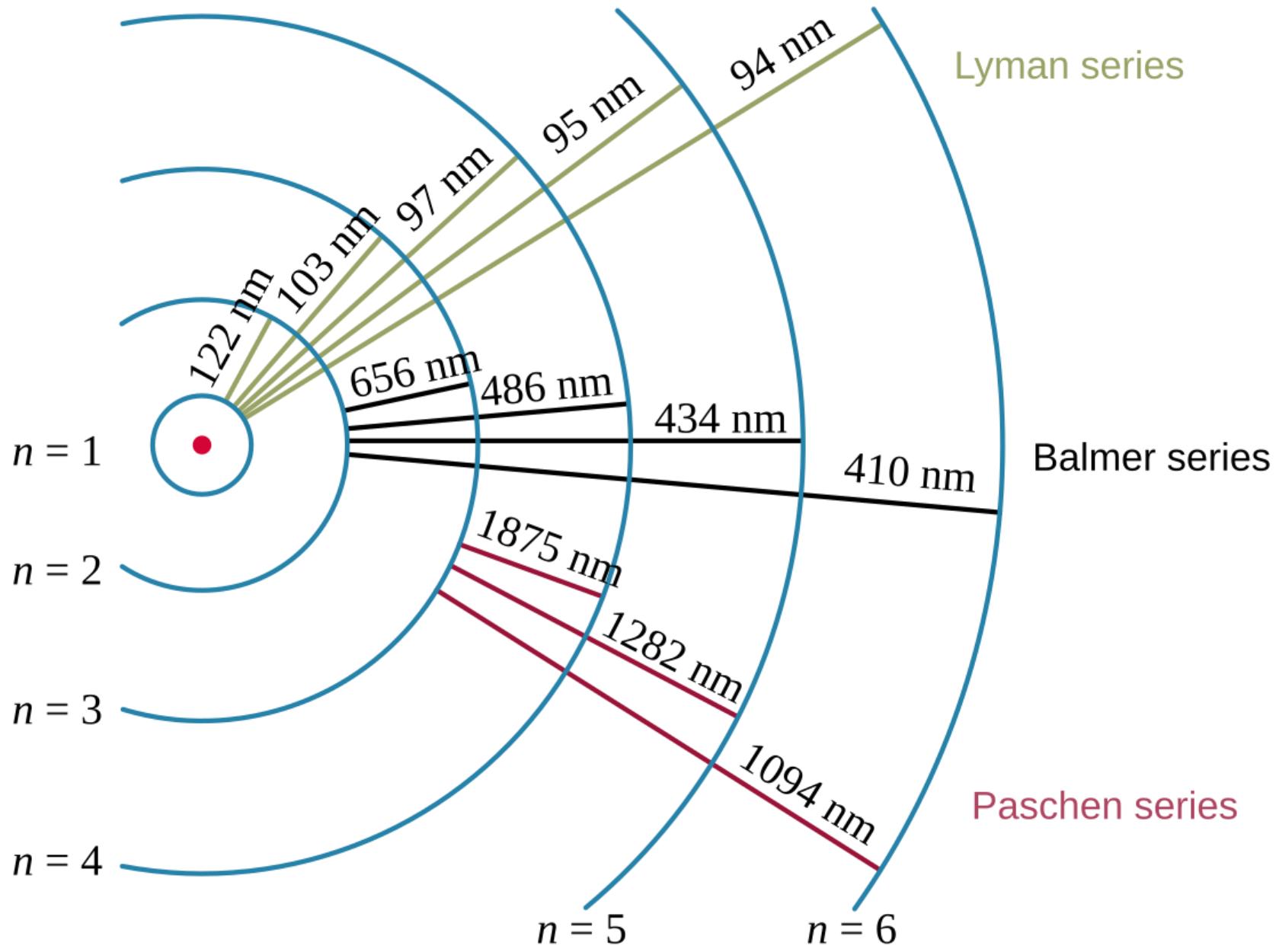
Total (all wavelength/frequency) flux coming from the black body.



**Stefan-Boltzmann Law**

$$F = \int B_\lambda d\lambda = \sigma_{\text{SB}} T^4$$

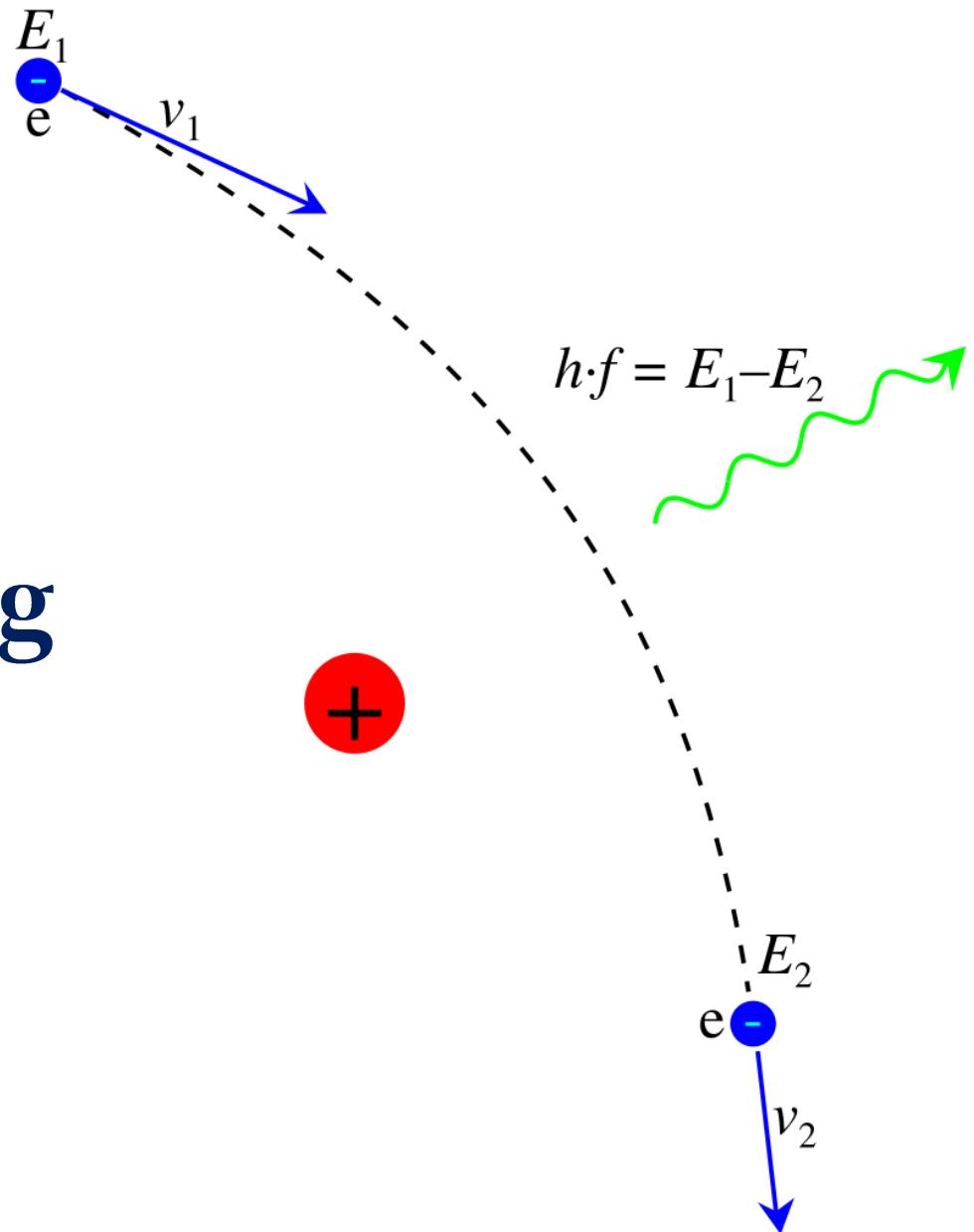
$$L = 4\pi R^2 \sigma_{\text{SB}} T^4$$



Emission mechanisms  
**Electron transitions**

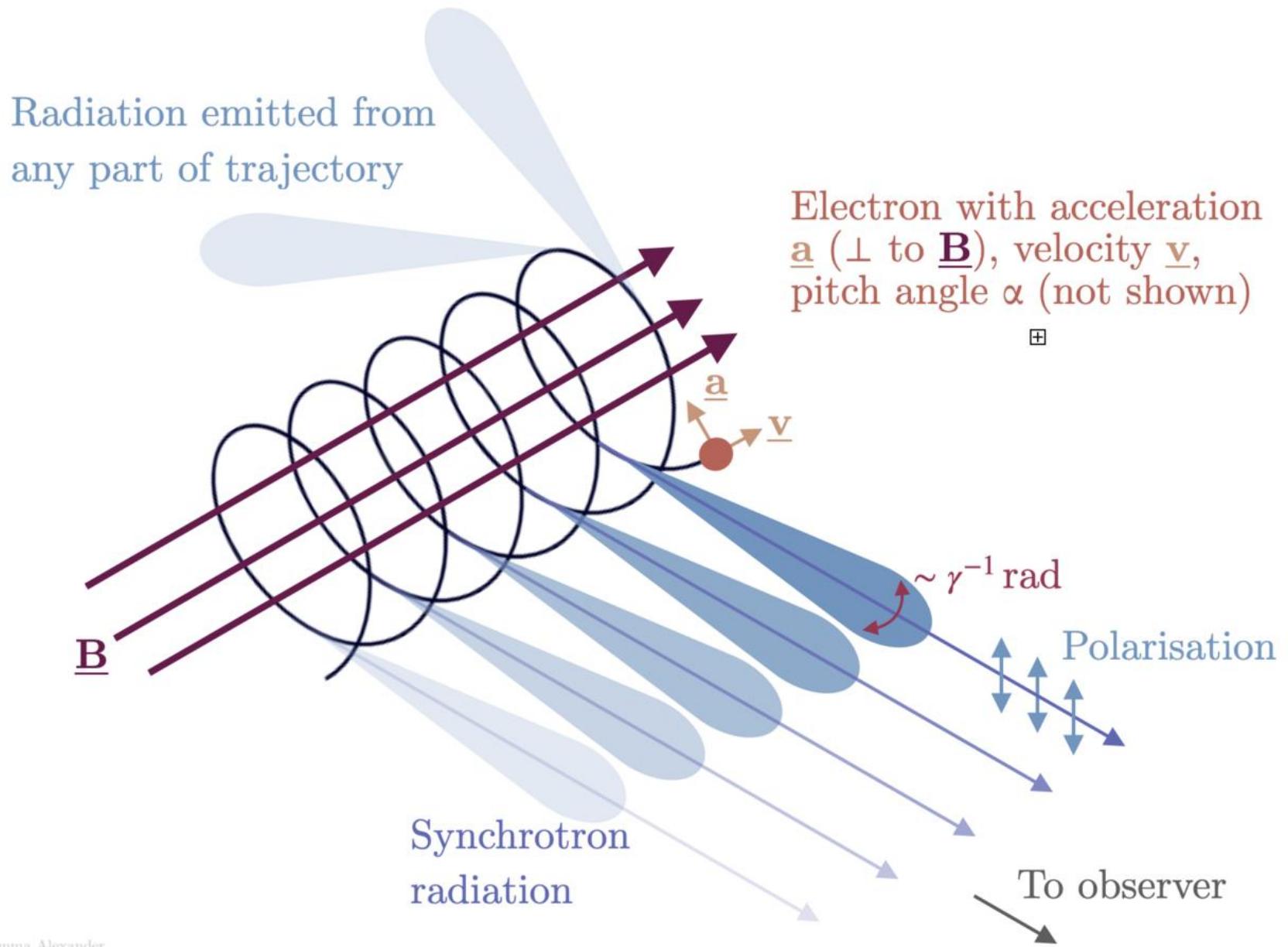
# Free-free / Bremsstrahlung radiation

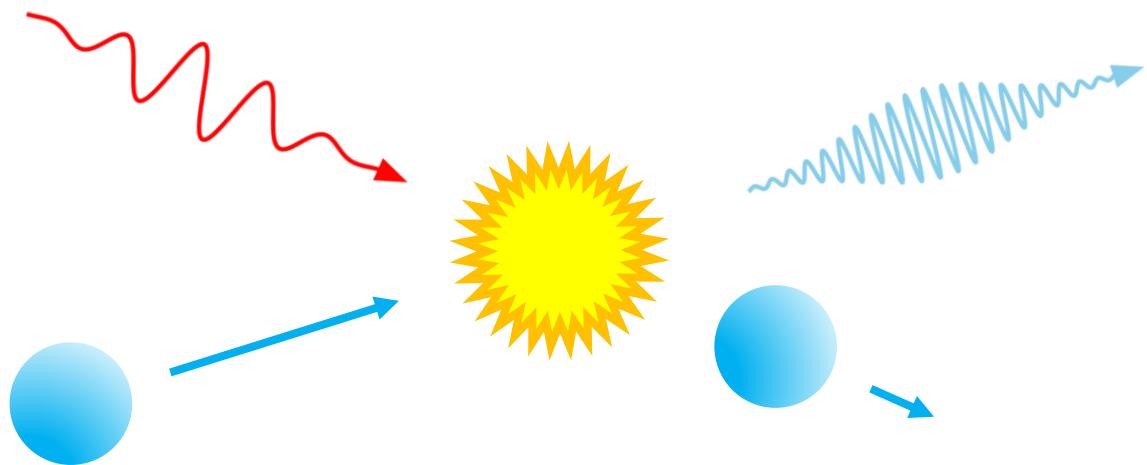
Emission mechanisms



# Synchrotron radiation

Emission mechanisms





Emission mechanisms

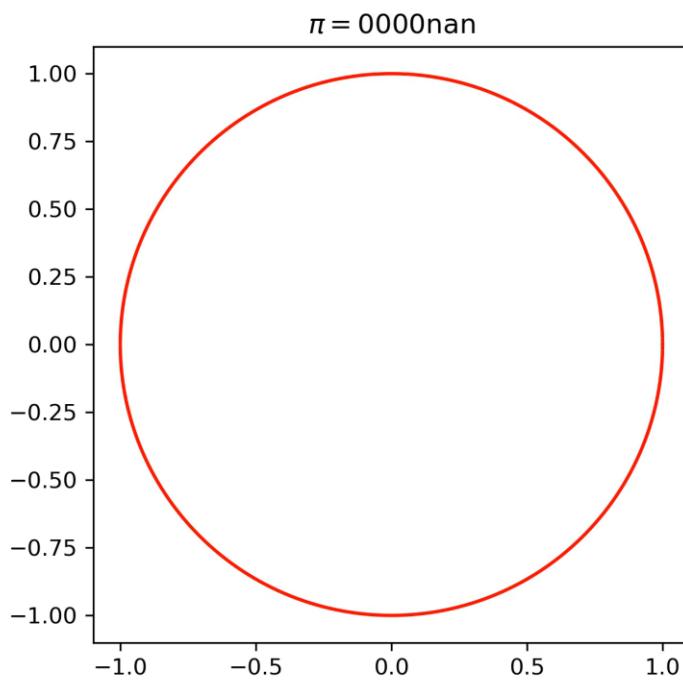
## Inverse Compton scattering

# Complicated situations

Computer go brrrrrrrrrr

# Numerical Radiative transfer

Utilizing Monte-Carlo method and Ray Tracing to solve RTE.

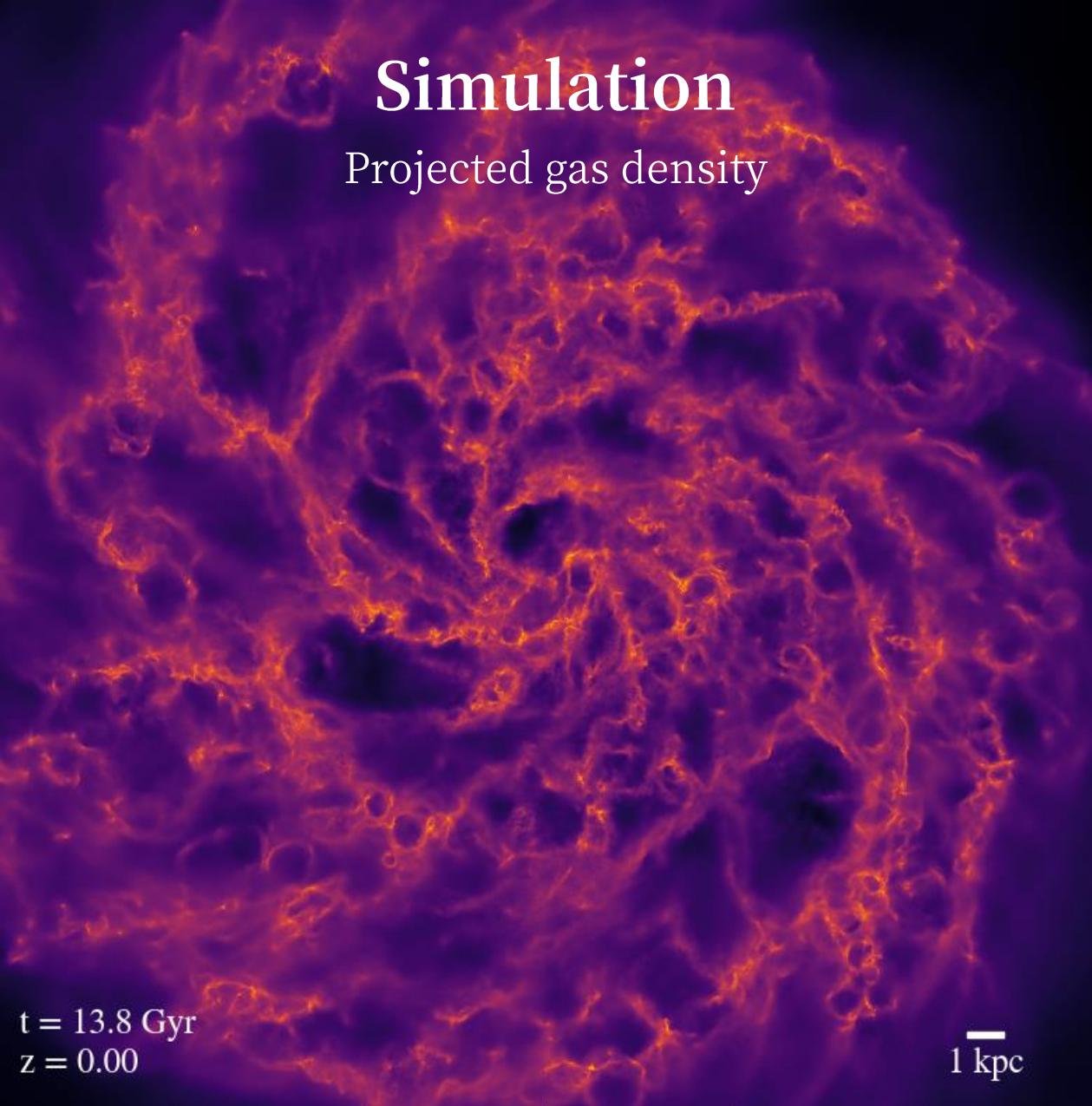




## GR ray tracing

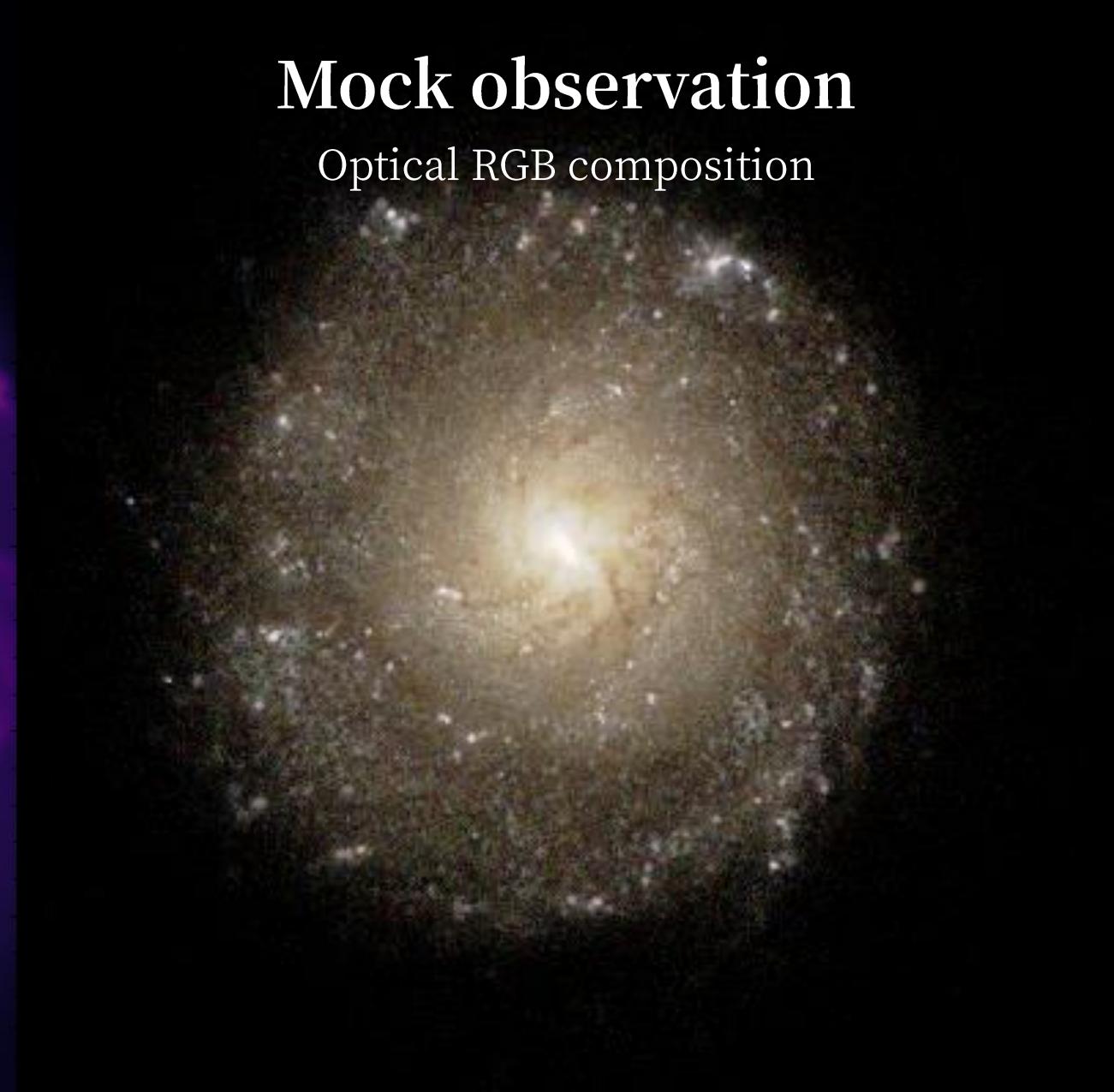
# Simulation

Projected gas density



# Mock observation

Optical RGB composition



Better/direct comparison with observations

Computer go brrrrrrrrrr

# Radiative Hydrodynamics

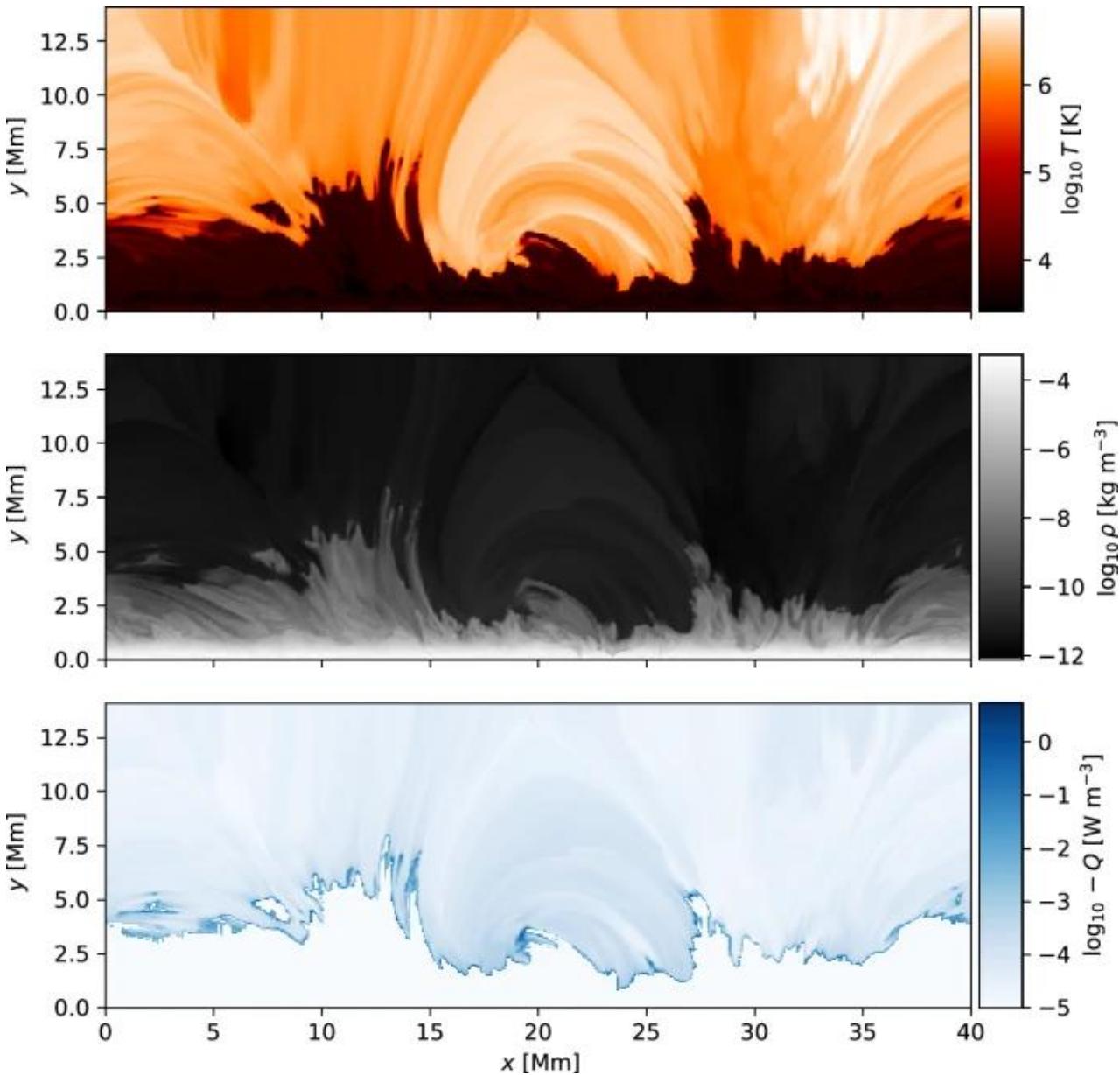
Important in e.g. stellar atmosphere,  
super-Eddington accretion disk.

$$\frac{\partial \rho}{\partial t} = -\nabla \cdot (\rho \mathbf{v})$$

$$\frac{\partial \mathbf{p}}{\partial t} = -\nabla \cdot (\mathbf{v} \otimes \mathbf{p} - \boldsymbol{\tau}) - \nabla P + \mathbf{J} \times \mathbf{B} + \rho \mathbf{g} - \nabla \mathbf{P}_{\text{rad}}$$

$$\frac{\partial e}{\partial t} = -\nabla \cdot (e \mathbf{v}) - P \nabla \cdot \mathbf{v} + Q + Q_{\text{rad}}$$

Jorrit Leenaarts (2021)



# Summary

- In astrophysics, we often use **specific intensity** [  $\text{J m}^{-2} \text{sr}^{-1} \text{s}^{-1} \text{Hz}^{-1}$  ] to describe the strength of light, which does not decay with distance.
- Specific intensity is changed by **absorption, scattering and emission**, described by **radiative transfer equation**.
- Radiative transfer effects are often discussed using **optical depth**.
- There are many mechanisms that generates/absorb radiation.
- Complicated radiative transfer problems are solved numerically.