

## Research Papers

## A novel graph-based framework for state of health prediction of lithium-ion battery

Xing-Yan Yao<sup>a,\*</sup>, Guolin Chen<sup>a</sup>, Michael Pecht<sup>b</sup>, Bin Chen<sup>c</sup><sup>a</sup> Chongqing Engineering Laboratory for Detection Control and Integrated System, Chongqing Technology and Business University, Chongqing 400067, China<sup>b</sup> Center for Advanced Life Cycle Engineering, University of Maryland, College Park, MD 20742, USA<sup>c</sup> China Merchants Testing Vehicle Technology Research Institute Co., Ltd, Chongqing 400067, China

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## ABSTRACT

State of health (SOH) plays a vital role in lithium-ion batteries (LIBs) safety, reliability and lifetime. Health indicators (HIs) are a powerful approach to predict battery SOH. The existing methods for battery SOH prediction according to HIs only consider the temporal features of HIs. The spatial features of interdependence between HIs enrich predicational information especially for the limited data. This paper proposes a novel framework CL-GraphSAGE to predict battery SOH based on graph neural network (GNN), which takes into both temporal and spatial features of HIs. Firstly, the Pearson's correlation coefficients between HIs and SOH are obtained to extract highly correlated HIs to build a graph. Subsequently, the temporal features are extracted by convolutional neural network (CNN) and long short-term memory neural network (LSTM). Finally, the spatial features are obtained by the graph sample aggregate (GraphSAGE) to propagate messages on a pre-defined graph structure, which uncovers the deep information among HIs. The effectiveness of the proposed approach in predicting battery SOH is verified by MIT, NASA datasets and the experimental datasets, and compared with CNN, LSTM and graph convolutional network and graph attention network. The results show that the root mean square error of the proposed approach CL-GraphSAGE can achieve 0.2 %, and the different datasets verify its feasibility.

## 1. Introduction

In response to extreme weather and environmental pollution, electric vehicles are widely used in the world. Lithium-ion batteries (LIBs) are a promising energy source for the electric vehicle due to their high energy, low self-discharge rate, and long storage life [1,2]. Nevertheless, LIBs performance degrades with cycle increases. The battery failure can lead to serious or even safety accidents. Therefore, it is vital to monitor LIBs' state and master the battery health. The state of health (SOH) of the battery is a powerful tool to evaluate the battery current health condition and ensure battery safety and health management [3]. SOH is a percentage of the maximum charge which can be released to the battery rated capacity. However, SOH is difficult to predict since it cannot be tested directly such as via terminal voltage. Moreover, the battery data collected in the real world is a limitation. It is a challenge to obtain

precise SOH due to the lack of data and indirectly measured parameters [4].

The methods for battery SOH prediction can be summarized as model-based and data-driven [5]. Model-based methods include electrochemical models [6,7], equivalent circuit models [8–11], and mathematical models [12–14]. The electrochemical model-based method develops a model to describe the physical and chemical processes of a battery and then evaluate the influence of the aging process on the SOH. This method can be generally used for LIBs to obtain battery aging trajectories. However, the electrochemical model-based method requires lots of parameters, and SOH prediction performance is determined by the given parameters. In addition, the computational complexity is high. The equivalent circuit model is based on battery electrical characteristics combined with amounts of the dataset, and the lithium battery is equivalent to a circuit. Compared with the

**Abbreviations:** LIBs, lithium-ion batteries; SOH, state of health; HIs, health indicators; CL-GraphSAGE, the proposed method in this paper; GNN, graph neural network; GraphSAGE, graph sample aggregate; CNN, convolutional neural network; RNN, recurrent neural network; LSTM, long short-term memory neural network; CC, the current curve of the constant current; CV, the current curve of the constant voltage;  $G = (V, \mathcal{E})$ , graph G,  $\mathcal{E}$  and V are the edge and node set; RMSE, root mean square error; MAPE, the average absolute percentage error;  $R^2$ , coefficient of determination.

\* Corresponding author.

E-mail address: [yaomingyan-jsj@163.com](mailto:yaomingyan-jsj@163.com) (X.-Y. Yao).

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electrochemical model, the computational complexity is less. Furthermore, mathematical models obtain the battery performance by large amounts of experimental data [4]. The SOH prediction is achieved via data analysis, fitting, trial and error, and statistical processing. In this method, the battery physical mechanism is a black box, and the SOH prediction is greatly affected by the experimental environment.

Data-driven methods achieve SOH prediction by utilizing battery signals (current, voltage, temperature, internal resistance, etc.) or health indicators (HIs) extracted from charging and discharging processes. This method does not know the battery complex internal mechanism. With the widespread application of artificial intelligence, machine learning has been widely used in lithium battery SOH prediction [15]. Yang et al. [16] employed Gaussian process regression to predict SOH by four correlated HIs extracted from charging curves and analyzed the correlation between HIs and SOH. Song et al. [17] extracted features to describe the battery aging process and predict battery SOH. Yang et al. [18] extracted HIs from voltage and temperature during discharge, using a multiple kernel relevance vector machine that combined Gaussian with sigmoid function to improve the accuracy of SOH prediction. In addition, other machine learning methods such as random forest [19], Markov chain [20], Monte Carlo [21] and ARIMA [22] are also popular to use.

Although machine learning methods mentioned above achieved great success in processing nonlinear relationships, they are still can be improved to process historical data to predict battery SOH. Many researchers applied recurrent neural network (RNN) [23], gate recurrent unit (GRU) [24] and long-short term memory (LSTM) [25] to predict SOH. In addition, some researchers have used neural ordinary differential equations and recurrent neural networks for the analysis of batteries to predict SOH [26]. Kim et al. [27] used multiple features as the input of LSTM and changed the input sequence length to reflect the historical SOH. Cui et al. [28] proposed a dynamic spatial-temporal attention-based gated recurrent unit (DSTA-GRU) model, which considered both the time domain and space domain of features on SOH. The methods above mentioned typically used the historical data of HIs to establish the mapping between HIs and SOH. However, they ignore the potential interdependence between HIs and the interdependence between HIs on the prediction results either. Furthermore, it is urgent to deep mine hidden information from the limited battery data in the application.

The graph is a special type of data structure that describes the relationship between different entities. For the problem of multi-variate inputs, the graph uses variables as nodes, and the nodes are connected through their hidden dependency. In recent years, graph neural network (GNN) can effectively deal with complex graph structures and has attracted the attention of researchers in various fields [29–31]. GNN relies on the relationships between nodes to capture information in the graph and optimizes the message-passing mechanism between graph nodes to get the dependence between different variables.

GNN has already used to prediction task right now. Yu et al. [32] used spatial-temporal graph convolutional networks to extract spatial-temporal features from the time series of the graph structure to predict traffic flow. Khodayar et al. [33] proposed a novel graph convolutional deep learning structure to predict short-term wind speed combined with LSTM. Vyas et al. [34] proposed a dynamic GNN to predict the soil moisture of multiple locations in a region over time. Wang et al. [35] construct a graph structure on a sensor network with Pearson Correlation Coefficients among sensors. In addition, they combined graph convolutional network and temporal convolutional networks to forecast the remaining useful life of the engine.

The data-driven approach can mine deep information in the limited data without much prior knowledge. The CNN is a powerful deep learning approach to extract local features. The LSTM has the advantage of long-term memory in sequence modeling to overcome the problems of gradient vanishing in the long sequence training. To deal with graph structure data, GNN is a kind of algorithm that uses neural networks to

learn graph structure data, extract and explore features in the graph structure data. GNN is a promising method to deal with time series prediction for data of spatial-temporal characteristics. The spatial characteristic is reflected by deep mining the interdependence between nodes of the features in the GNN, and the temporal characteristic can also be taken into considering the historical data according to the LSTM. As a kind of GNN, GraphSAGE can aggregate the information from nodes of the graph, and the message passing is used to learn features in the graph structure. Therefore, the fusion of CNN, LSTM and GraphSAGE can mine deep information from both the spatial features and temporal features of lithium-ion battery data to achieve SOH prediction. As far as we know, little research on SOH using GNN is demonstrated.

In this paper, a novel framework CL-GraphSAGE for battery SOH prediction is proposed. The HIs extracted from the charging and discharging process are converted into a graph structure. The combination of GNN and CNN-LSTM is employed for the node features and message passing information to obtain the spatial-temporal features of the graph. The CNN-LSTM mines the potential temporal features of historical input of HIs data [36–38], which are used as node features of the graph structure. GraphSAGE is used to carry out message passing in the graph structure composed of HIs. Therefore, all the HIs can obtain complementary information from each other. The main contributions of this paper are as follows:

- A novel framework CL-GraphSAGE is proposed to predict lithium-ion battery SOH, which considers both the temporal and spatial features of HIs.
- The HIs highly correlated with SOH are extracted to form a spatial-temporal graph.
- The relationship between different HIs is deep mined and optimized to enrich the information to predict SOH.
- Graph neural network (GNN) is the first time to use for battery prediction problems.

The rest of the paper is organized as follows: Section 2 describes the lithium-ion battery datasets and feature extraction. Section 3 describes the CL-GraphSAGE SOH prediction method. Section 4 describes the results and discussions, followed by conclusions in Section 5.

## 2. Datasets and feature extraction

This section describes two public lithium-ion battery datasets used to validate the method proposed in this paper. Different HIs are extracted for these two datasets.

### 2.1. Datasets

NASA datasets are used to verify the proposed method [39]. The B0005, B0006, and B0007 batteries are used. All battery charging and discharging processes are carried out at room temperature, with a nominal capacity of 2.0 Ah. During charging, the battery is first charged with a CC at 1.5 A until the voltage reaches 4.2 V; it is then charged with a CV until the current drops below 20 mA. During discharging, the battery is discharged with CC at 2A until cut-off voltage. Repeat the above steps until the battery reaches the end of its life (capacity loss 70 %). Fig. 1(a) shows the capacity curves of cycles.

The MIT lithium-ion battery dataset is currently the largest public dataset used for battery degradation research [40]. The dataset consists of 124 commercial LIBs from A123. The nominal capacity and voltage are 1.1 Ah and 3.3 V, respectively. At 30 °C, all batteries are charged with a multistep fast-charging strategy and then discharged with a CC process. The format of this strategy is “C1(Q1)-C2.” The battery is firstly charged by current C1 until the state of charge reaches S1, and then it is charged with current C2 until the state of charge reaches S2. The battery is charged from 80 % to 100 % SOC at 1C CC-CV. The cutoff voltage is 3.6 V. Subsequently, the battery is discharged at 4C CC, and the battery

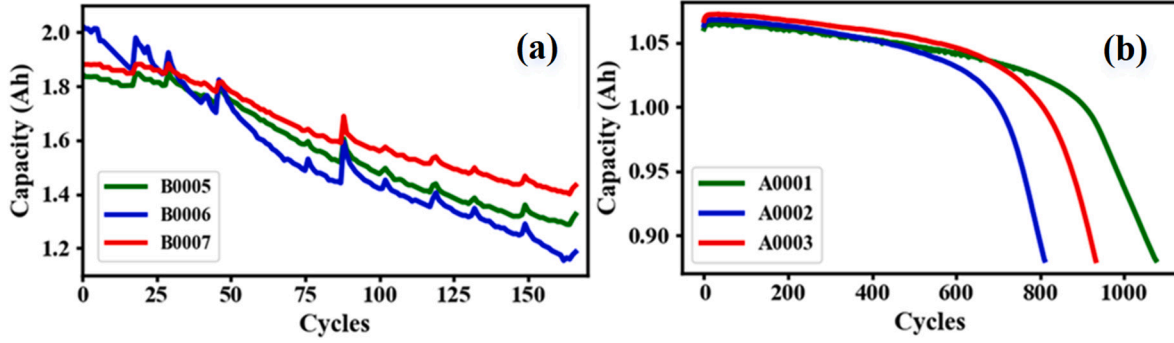


Fig. 1. Capacity degradation curves: (a) NASA datasets; (b) MIT datasets.

life threshold is reduced to 80 % of the nominal capacity. The batteries A0001, A0002, and A0003 are employed in the experiments. Fig. 1(b) shows the capacity degradation of the specific cycle period.

## 2.2. Feature extraction

The HIs used for data-driven approaches depend on the dataset. Different HIs are extracted from NASA and MIT datasets. All the extracted HIs mentioned above are described in Table 1. The HIs involved in this article are divided into four categories, which are voltage-related, current-related, temperature-related, and time-related [41–43].

- **Current-related HIs.** The areas covered under the current curve of the CC process and the discharge process, the area covered under the current curve of the CV process, the CC-CV process, and the discharge process are as HIs. In addition, the maximum slope extracted from the CV process current curve is another HI.

**Table 1**  
Four categories of HIs.

HI type	No.	HIs
Current-related	B1	Area covered under current curves of the CC process
	B2	Area covered under current curves of CV process
	B3	Area covered under current curves of CC-CV process
	B4	Maximum slope of current curves in CV process
	B5	Area covered under current curves of discharge process
Voltage-related	B6	Area covered under voltage curves of CC process
	B7	Area covered under voltage curves of CV process
	B8	Area covered under voltage curves of discharge process
	B9	Maximum slope of voltage curves in CC process
	B10	Maximum temperature of charge and discharge cycles
Temperature-related	B11	Minimum temperature of charge and discharge cycle
	B12	Average temperature of charge and discharge cycle
	B13	Area covered under temperature curves of charge and discharge cycle
	B14	Area covered under temperature curves of the CC process
	B15	Area covered under temperature curves of CV process
Time-related	B16	Area covered under temperature curves of CC-CV process
	B17	Discharge time
	B18	Charging time
	B19	CC stage period
	B20	CV stage period
	B21	CC stage end time
	B22	Time to peak temperature during discharge process
	B23	The time ratio of the CC process and the entire charging process
	B24	The time for voltages increases from 3.7 V to 4.2 V during the CC process
	B25	Time for currents decreases from 1.5 A to 0.3 A during the CV process
	B26	Time for voltages decreases from 3.7 V to 2.7 V during discharging

- **Voltage-related HIs.** The HIs extracted from the voltage curve are similar to the current-related HIs. The areas covered under the voltage curve of the CC process, CV process, and discharge process are HIs. The maximum slope extracted from the CC process voltage curve is also an HI.
- **Temperature-related HIs.** During the charging and discharging process, the temperature changes. The maximum temperature, minimum temperature, and average temperature are taken as HIs. The areas covered under the temperature curve of the CC process, CV process CC-CV process and the entire charge and discharge cycle are HIs.
- **Time-related HIs.** The HIs include CC charging time, CV charging time, charging time, and discharging time. In addition, the time for the temperature to reach the peak during the discharge process is also an HI.

The HIs extracted are multidimensional features. Different HIs have different degrees of correlation with SOH. If all HIs are used as input, it will affect the prediction accuracy and easily lead to overfitting. Therefore, given a threshold, the HIs with a lower correlation are eliminated, and the HIs with a higher correlation as the input of the model are kept. Pearson correlation coefficient [44] is used to evaluate the correlation between HIs and SOH.

The Pearson correlation coefficient calculates the linear correlation between HI and SOH in Eq. (1). Here,  $X_i$  and  $Y_i$  are HI and SOH, respectively.  $\mu_X$  and  $\mu_Y$  are the average values, respectively. The absolute value of Pearson's correlation coefficient is in the range of [0,1]. The larger the absolute value, the stronger the correlation. In this paper, the 6 most relevant HIs with large absolute values are selected as the final subset of HIs by the trials and errors of the experiments.

$$\rho(X, Y) = \frac{\sum_{i=1}^n (X_i - \mu_X)(Y_i - \mu_Y)}{\sqrt{\sum_{i=1}^n (X_i - \mu_X)^2} \sqrt{\sum_{i=1}^n (Y_i - \mu_Y)^2}} \quad (1)$$

## 3. Methodology

This section describes in detail the proposed approach CL-GraphSAGE for the battery SOH prediction in this paper. The components in CL-GraphSAGE are depicted in detail, and all steps of SOH prediction by CL-GraphSAGE are detailed descriptions.

### 3.1. CL-GraphSAGE

Fig. 2 shows the proposed CL-GraphSAGE for battery SOH prediction framework. The CL-GraphSAGE includes CNN, LSTM and GraphSAGE. The extracted HIs in Section 2 are used to build a graph structure. Then the HI's temporal features are extracted by CNN and LSTM, and the spatial features are obtained by GraphSAGE. Finally, the SOH is acquired by multilayer perceptron (MLP).

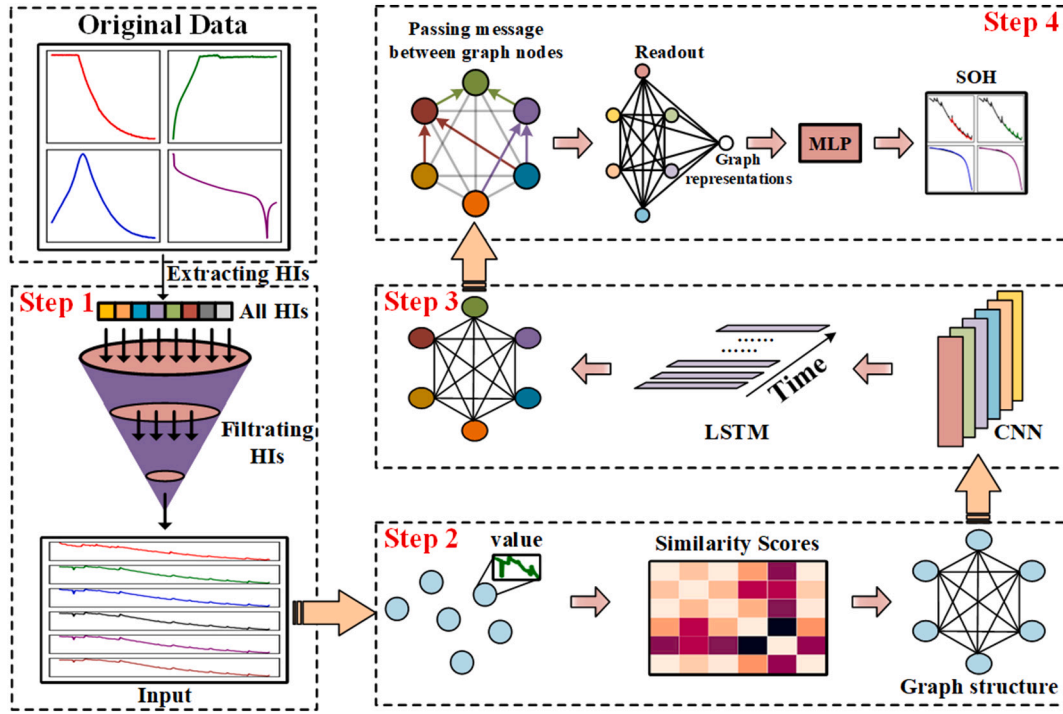


Fig. 2. CL-GraphSAGE framework for battery SOH prediction.

The details of CL-GraphSAGE are as follows:

**Step 1: Extracting and filtrating HIs.** The HIs are extracted from the original datasets. The HI subsets are derived from the Pearson correlation coefficient in Eq. (1).

**Step 2: Building a graph structure.** The input of GraphSAGE is a graph. The HI subset in Step 1 needs to be converted into a graph structure that consists of nodes and edges. Every filtrating HI is taken as one node of the graph. The similarity values between the HIs calculated by Eq. (2) are taken as edges of the graph. Therefore, the graph is represented by nodes set, and the HIs sequence data are the values of the nodes.

**Step 3: Obtaining HIs temporal features.** The HIs sequence data of each node is used as the input of the CNN-LSTM hybrid model. The HIs temporal features are the hidden state vector at the last moment of LSTM output.

**Step 4: Updating node messages.** The GraphSAGE is used to pass messages between graph nodes. The node message is updated by the center node, which receives all the connected node messages. All nodes are aggregated to obtain a global representation of the entire graph. Finally, SOH is predicted by MLP.

The pseudocode of the proposed CL-GraphSAGE is shown in Table 2.

### 3.2. Graph structure of HIs

The determination of nodes and edges is the key to applying graph neural network to battery SOH prediction. In this paper, HIs are regarded as nodes in the graph, and HIs are connected as edges.

Assuming a graph  $G = (V, \mathcal{E})$ , where  $\mathcal{E}$  and  $V = \{v_1, v_2, \dots, v_n\}$  are the edge and node set, respectively. Furthermore, the nodes consist of node sets and the corresponding node values. Here, the HIs subsets are the nodes of the graph, and the node values are obtained by the CNN-LSTM hybrid model.  $|V| = n$  is the numbers of the HIs. For the  $i$ -th node,  $v_i \in V$  with  $T$ -dimension is denoted by  $x_i$ .  $X = \{x_1, x_2, \dots, x_n\} \in \mathbb{R}^{n \times T}$  is the node feature vector.

For all the node vector  $V = \{v_1, v_2, \dots, v_n\}$ , the HIs are connected by

Table 2

Pseudocode of CL-GraphSAGE.

1:	Input: The dataset $\mathcal{O}_{train}, \mathcal{O}_{test}$ .
2:	Calculating similarity scores between HIs and building graph structure.
3:	Training:
4:	for $X$ in $\mathcal{O}_{train}$ do:
5:	$h \leftarrow CNN(X)$ ;
6:	$h \leftarrow LSTM(h)$ ;
7:	$h \leftarrow GraphSAGE(h)$ ;
8:	$h \leftarrow GraphSAGE(h)$ ;
9:	$h \leftarrow ReadOut(h)$ ;
10:	$SOH \leftarrow MLP(h)$ ;
11:	Update model parameter.
12:	end for
13:	Output: The SOH of $\mathcal{O}_{test}$ .

the similarity values from the Eq. (2) [45].  $x_i$  and  $x_j$  are the sample sequence at  $i$ -th and  $j$ -th nodes, respectively.  $\bar{x}_i = x_i/d$  is the average value of  $x_i$ , and  $d$  is the number of elements of  $x_i$ , and the range of  $i$  and  $j$  is  $[1, n]$ .

$$A_{ij} = \frac{(x_i - \bar{x}_i)^T (x_j - \bar{x}_j)}{\sqrt{(x_i - \bar{x}_i)^T (x_i - \bar{x}_i)} \sqrt{(x_j - \bar{x}_j)^T (x_j - \bar{x}_j)}} \quad (2)$$

After defining the nodes and edges to build the graph, the task of SOH prediction is transformed to learn the mapping between HIs and SOH by the given SOH value at the time  $t$ . Specifically, the HIs at different timestamps are used as node data to generate temporal datasets for the graph, and the SOH at the time  $t$  is used for prediction in the graph.

### 3.3. Temporal feature of HIs

LSTM has been widely used in Lithium-ion battery SOH prediction. LSTM overcomes the problem of gradient vanishing and captures the long-term dependence of time series compared with RNN [46]. LSTM



obtains the long-term dependence of time series data by using the storage unit to store useful information and the gating mechanism to discard useless information. LSTM structure includes input gates, forget gates, storage units, and output gates. The input gate saves the information, the forget gate obtains the forgetting information, the output gate represents the output information, and the storage unit keeps the historical information until the current moment.

CNN is a powerful tool to extract local hidden information of data by multi-layer convolution operations [47]. As shown in Fig. 3, CNN is used for extracting deep features from the historical information, which are the input of LSTM to mine temporal features of the sequence data. The feature extraction of every HI time series is separated from each other, and a one-dimensional CNN layer with one kernel of size 1 is used. His temporal features obtained by CNN and LSTM are used as the node features of the graph. The temporal features of every HI constitute the temporal feature matrix  $X$  of the graph.

### 3.4. GraphSAGE

For the SOH prediction, there are two keys to building the GNN model. One is to fuse the local information of nodes in the graph structure, and the other is to embed the updated nodes into vectors. In this paper, GraphSAGE aggregates the information of adjacent nodes to update nodes and obtains the interdependence between HIs. GraphSAGE is used to mine deep information between HIs of the edges in the graph. Therefore, each HI node contains all information of both HI itself and adjacent HIs from the  $k$ -layer GraphSAGE.

The input of GraphSAGE is the graph  $G = (V, \mathcal{E})$ . The node features  $X \in R^{n \times d}$ , that are temporal features, are obtained in Section 3.3, where  $n$  is the number of HIs and  $d$  is the dimension of LSTM output. The similarity between HIs is calculated to obtain the connection between nodes of adjacency matrix  $A \in R^{n \times n}$  in Section 3.2. The adjacency matrix  $A$  and the feature matrix  $X$  are used as the input of GraphSAGE.

Fig. 4 shows the aggregation process of GraphSAGE for the given graph. Fig. 4(b) displays the corresponding topological and node features by the given graph structure in Fig. 4(a). Taking the red node A in Fig. 4(a) as an example, GraphSAGE updates the information of the node A by fusing the neighborhoods' information. To update nodes at  $k$ -layer, the information of the adjacent nodes is first aggregated to  $h_{j \in \mathcal{N}(i)}^k$  by the aggregation function and then integrated and updated with the central node state  $h_i^{k-1}$ , which are shown in Eqs. (3)–(4). Then the aggregated embeddings  $h_{j \in \mathcal{N}(i)}^k$  are obtained by the neighborhood aggregation which is fused with the node information of the previous layer  $h_i^{k-1}$ .

$$h_{j \in \mathcal{N}(i)}^k = \text{Aggregate}\left(\left\{h_j^{k-1}, \forall j \in \mathcal{N}(i)\right\}\right) \quad (3)$$

$$h_i^k = \sigma\left(W^k \text{Concat}\left(h_i^{k-1}, h_{j \in \mathcal{N}(i)}^k\right)\right) \quad (4)$$

Here,  $h_i^k$  is the state of the  $i$ -th node in the  $k$ -th message passing, and  $\mathcal{N}(i)$  is the adjacent nodes set. In Eq. (4), the *Aggregate* function takes the place of the *Mean* aggregation function, and Eqs. (3)–(4) are combined and modified to obtain Eq. (5).

$$h_i^k = \text{ReLU}\left(W \bullet \text{Mean}\left(\left\{h_i^{k-1}\right\} \cup \left\{h_j^{k-1}, \forall j \in \mathcal{N}(i)\right\}\right)\right) \quad (5)$$

After obtaining the final state of all nodes, the readout function is used to aggregate all node representations into a global representation of the graph [48]. The global expression is obtained by one-time aggregation of all inputs. Here, the *Max* function is to aggregate all nodes, and *MLP* outputs the final predicted value  $\hat{y}_t$  as shown in Eq. (6). The number of neurons in the output layer is 1 when the SOH value is at a certain moment. *Huber loss* [36] is used as the regression loss function.  $y_t$  and  $\hat{y}_t$  are the true value and predicted value, respectively.  $\delta$  is the hyper-parameter in Eq. (7).

$$\hat{y}_t = \text{MLP}\left(\text{Readout}\left(\left\{h_i^k | i \in G\right\}\right)\right) \quad (6)$$

$$\mathcal{L} = \begin{cases} \frac{1}{2}(y_t - \hat{y}_t)^2, & |y_t - \hat{y}_t| \leq \delta \\ \delta \cdot \left(|y_t - \hat{y}_t| - \frac{1}{2}\delta\right), & \text{otherwise} \end{cases} \quad (7)$$

### 3.5. Evaluation metrics

The experiments are carried out by PyTorch 3.8, Intel Core i7-10875H 2.30GHz CPU, and NVIDIA GEFORCE RTX 2060 GPU. *Adam* is the optimizer, the learning rate is  $8e-4$ , the  $\delta$  in the *Huber loss* objective function is set to 1, the number of training epochs is 1500, and the batch size is 16. Root mean square error (RMSE), average absolute percentage error (MAPE), and coefficient of determination ( $R^2$ ) are used to evaluate performances, which are as follows:

$$\text{RMSE} = \sqrt{\frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2} \quad (8)$$

$$\text{MAPE} = \frac{1}{n} \sum_{i=1}^n \frac{|y_i - \hat{y}_i|}{y_i} \times 100\% \quad (9)$$

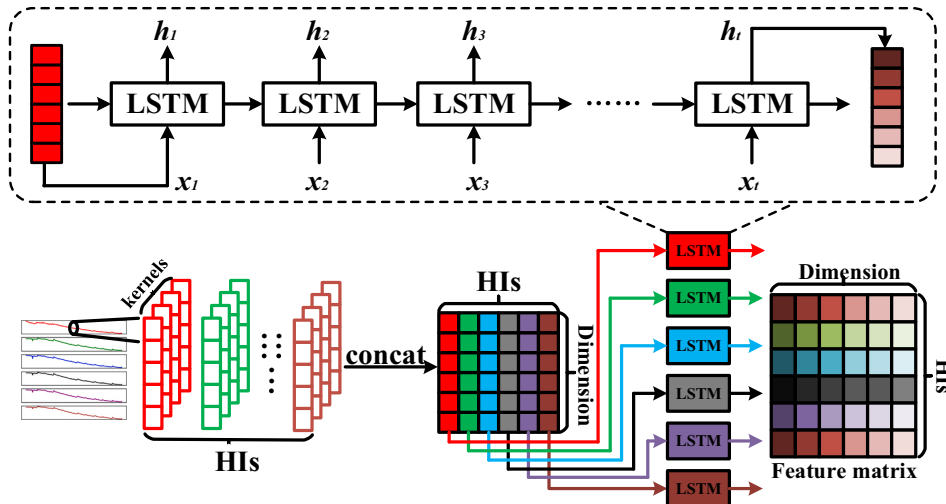


Fig. 3. Temporal feature matrix of HIs.

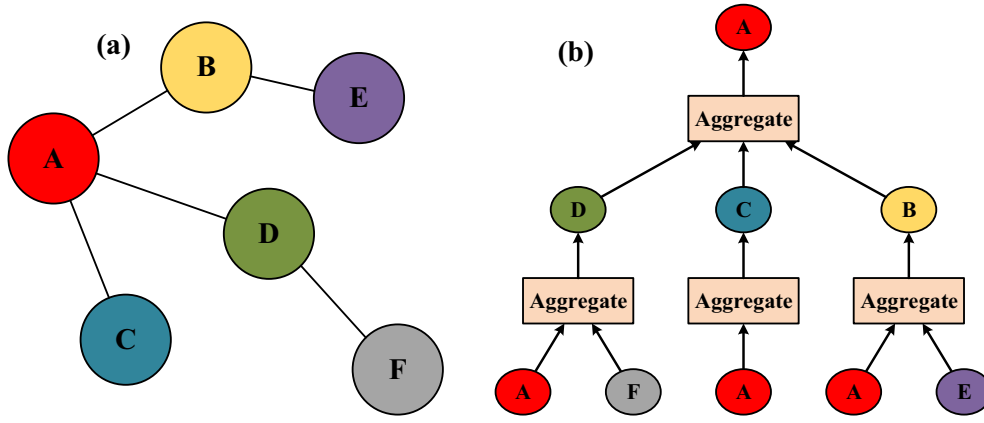


Fig. 4. Aggregation process of GraphSAGE: (a) the given graph; (b) aggregated embedding.

$$R^2 = 1 - \frac{\sum_{i=1}^n (y_i - \hat{y}_i)^2}{\sum_{i=1}^n (y_i - \bar{y})^2} \quad (10)$$

#### 4. Experiments

This section validates the performances of CL-GraphSAGE to predict the SOH for different lithium-ion battery datasets. The three different datasets are employed to discuss the performance by comparing with different models.

##### 4.1. Experiment for NASA dataset

According to HIs in Table 1 described in Section 2.2 and battery characteristics in Fig. 1(a). HIs are extracted from the NASA dataset. The correlation coefficient between HIs and SOH is obtained according to Eq. (2) shown in Table 3.

The first 6 high-correlation HIs (B1, B3, B6, B21, B24, and B26) are adopted as model inputs from Table 3. The similarity of HIs is calculated by Eq. (2). Fig. 5 shows the similarities between nodes. Two nodes with a similarity of 0.95 or more are connected into an edge. Taking B0005 as an example, as shown in Fig. 5(a), the similarities between HIs are all greater than 0.99. The nodes with a similarity of more than 0.95 are connected. Therefore, the six HIs are all connected as edges of the graph, and the graph structure is shown in Fig. 5(d). In Fig. 5(a)–(c), the similarity of HIs is greater than 0.95, and the graph structures are fully connected graphs.

The starting point is of great influence on the prediction results. The data before the starting point are used for training the model, and the remaining data are used for testing. Two kinds of training strategies are

carried out for the comparative experiments. The training data are chosen as the first 80 cycles and the first 100 cycles, respectively, and the corresponding remaining cycles are used as test data.

For the performance comparison, all the models are designed as multi-input and single-output. The 6 HIs selected above as the input of the models, and the battery SOH is the output of the models. The RNN is a classic approach to process sequence data and predicts battery SOH. RNN is a kind of neural network with sequence data as input. The output not only depends on the input at the current time but also is related to the input at the previous time. LSTM is a variant of RNN to improve the performance of RNN by overcoming the gradient vanishing when dealing with long-term memory. To mine the deep temporal features for the HIs sequence data, the CNN is combined with LSTM to predict SOH. In addition, GNN is used in the proposed CL-GraphSAGE to mine relevant information between HIs to obtain the spatial features of HIs. Through comparative verification, GNN has improved the SOH prediction accuracy. The performance of three models RNN, LSTM, and CNN-LSTM are compared with CL-GraphSAGE.

Fig. 6 shows the results starting at 81 of the four models in B0005, B0006, and B0007. Table 4 shows the performance evaluation of the four models from the different starting points. The RMSE of RNN and LSTM are both larger than 0.04, and the MAPE is larger than 4.5. The RMSE of CNN-LSTM and CL-GraphSAGE are both less than 0.035, and the MAPE are both less than 3.5. In some experiments,  $R^2$  of LSTM and RNN is even less than 0, which indicates that LSTM and RNN have poor adaptability and poor predictive ability in these cases. Therefore, the performance of RNN and LSTM in these three batteries is worse than that of CNN-LSTM and CL-GraphSAGE. As cycle numbers increase, the predicted result tends to be a straight line and cannot reflect the nonlinear capacity degradation trend. However, in Fig. 6(c), the predicted result of CNN-LSTM is consistent with that of RNN and LSTM, which is quite different from the true SOH.

Table 3  
Descending order of correlation coefficient of HIs.

Sample	Sort in descending order (from left to right, top to bottom)							
B0005	<b>B26</b>	<b>0.998255</b>	<b>B6</b>	<b>0.996169</b>	<b>B3</b>	<b>0.996047</b>	<b>B21</b>	<b>0.996046</b>
	<b>B1</b>	<b>0.996038</b>	<b>B24</b>	<b>0.996032</b>	B25	0.994137	B14	0.989574
	B2	0.988875	B23	0.988454	B15	0.988875	B9	0.894633
	B4	0.615588	B16	0.311356				
B0006	<b>B26</b>	<b>0.993706</b>	<b>B3</b>	<b>0.991352</b>	<b>B21</b>	<b>0.990314</b>	<b>B6</b>	<b>0.990308</b>
	<b>B24</b>	<b>0.989723</b>	<b>B1</b>	<b>0.988990</b>	B25	0.988074	B14	0.986618
	B23	0.986446	B9	0.961140	B2	0.938323	B15	0.929285
	B4	0.628557	B16	0.201432				
B0007	<b>B26</b>	<b>0.998064</b>	<b>B21</b>	<b>0.992642</b>	<b>B3</b>	<b>0.992558</b>	<b>B1</b>	<b>0.992296</b>
	<b>B6</b>	<b>0.992217</b>	<b>B24</b>	<b>0.988901</b>	B23	0.982533	B14	0.980917
	B2	0.961393	B15	0.883181	B9	0.694442	B4	0.635587
	B25	0.362327	B16	0.288703				

The bold in the table are the selected HIs which is the input of the model in this case study.

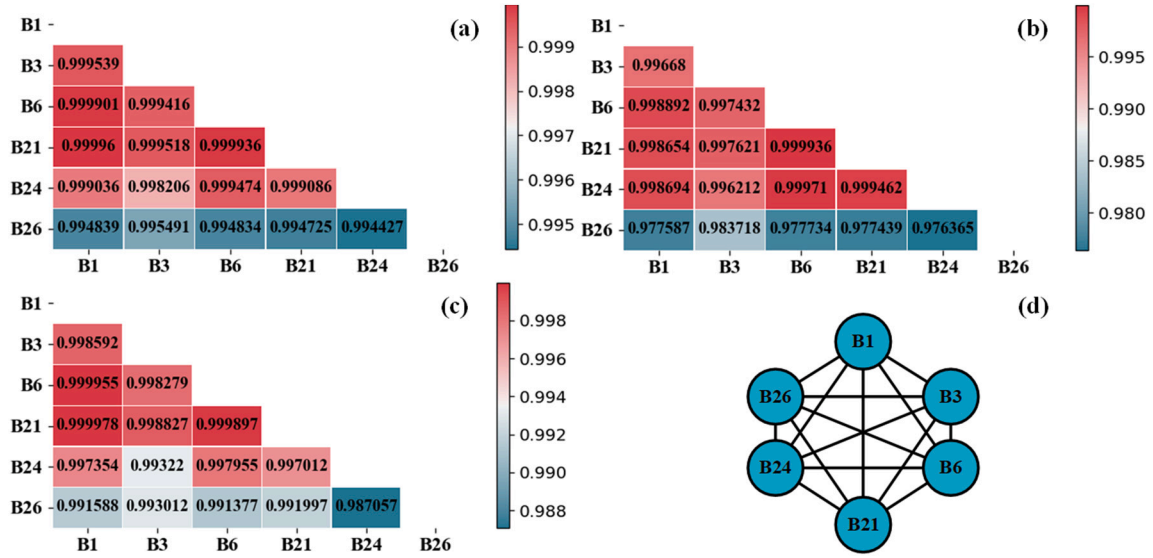


Fig. 5. Node similarity and graph structure: (a) B0005; (b) B0006; (c) B0007; (d) graph of B0005 HIs.

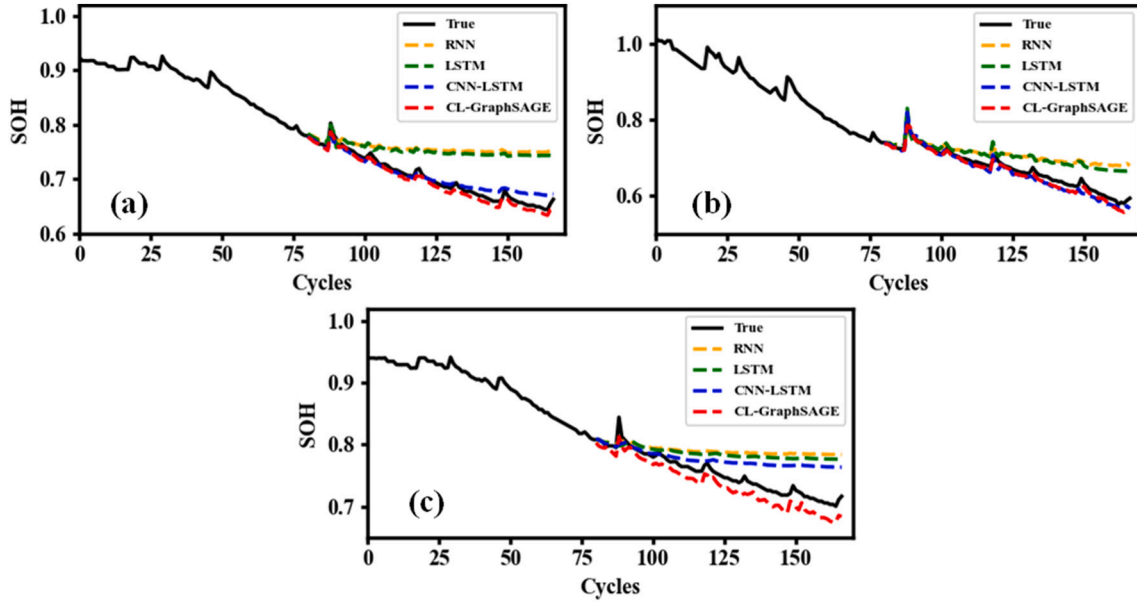


Fig. 6. Prediction results at starting point of 81: (a) B0005; (b) B0006; (c) B0007.

However, the predicted results by CL-GraphSAGE can still capture the tendency of capacity degradation, which indicates the proposed CL-GraphSAGE is **feasibility to the battery SOH prediction. The RMSE and MAPE of CL-GraphSAGE are the lowest among the three experiments.** In battery B0007, the RMSE and MAPE are 0.019028 and 2.383225, respectively, which are much lower than CNN-LSTM. The prediction results of CL-GraphSAGE show good performance. Compared with the other three models in Table 4, CL-GraphSAGE makes full use of the spatio-temporal features of HIs. CL-GraphSAGE can mine the relationship information between HIs and is better for SOH prediction.

Fig. 7 shows results starting at 101 of the four models in B0005, B0006, and B0007. According to Fig. 7, the prediction results of the three models are closer to the actual capacity degradation trend by using more training data. The RMSE and MAPE of RNN and LSTM are larger than those of CNN-LSTM and CL-GraphSAGE.

Table 4 shows the prediction errors of the four models at different starting points for different lithium-ion battery samples. In Table 4, both

RMSE and MAPE of CL-GraphSAGE are the lowest compared with CNN-LSTM, which shows good prediction performance. Moreover, CL-GraphSAGE predicts accurately when the starting point is 101 compared with the starting point at 81. The results show that regardless of whether the prediction starting point is 81 or 101, CL-GraphSAGE is the best choice.

#### 4.2. Experiment of MIT dataset

According to HIs in Table 1 described in Section 2.2 and battery capacity in Fig. 1(b), all HIs extracted from the MIT dataset and the correlation coefficient between HIs and SOH are obtained according to Eq. (2) are shown in Table 5. The first six high-correlation HIs (B1, B5, B6, B8, B17, and B19) are selected as model inputs.

The method to construct the nodes and edges of the graph is the same as in Section 4.1. Fig. 8 shows the similarities between nodes. The similarity values are displayed in Fig. 8(a)–(c). The two nodes are

**Table 4**  
Predicting errors at different starting points by different models.

Sample	Model	Starting points	RMSE	MAPE	R <sup>2</sup>
B0005	RNN	81	0.062645	7.892090	-1.247296
	LSTM		0.058334	7.331871	-0.948624
	CNN-LSTM		0.011572	1.338180	0.923311
	CL-GraphSAGE		<b>0.008281</b>	<b>1.105863</b>	<b>0.960732</b>
	RNN	101	0.040255	5.148115	-1.002669
	LSTM		0.018398	2.179895	0.581690
	CNN-LSTM		0.006289	0.720849	0.951118
	CL-GraphSAGE		<b>0.005808</b>	<b>0.625176</b>	<b>0.958309</b>
	RNN	81	0.046791	5.955632	0.131731
	LSTM		0.041631	5.451267	0.312677
B0006	CNN-LSTM		0.013927	1.802672	0.923077
	CL-GraphSAGE		<b>0.011475</b>	<b>1.470694</b>	<b>0.947783</b>
	RNN	101	0.036882	4.796715	0.130402
	LSTM		0.027935	3.581093	0.501154
	CNN-LSTM		0.013923	1.884062	0.876073
	CL-GraphSAGE		<b>0.010859</b>	<b>1.331990</b>	<b>0.924613</b>
	RNN	81	0.045730	5.199274	-0.879691
	LSTM		0.041061	4.671529	-0.515507
	CNN-LSTM		0.031836	3.398467	0.088939
	CL-GraphSAGE		<b>0.019028</b>	<b>2.383225</b>	<b>0.674550</b>
B0007	RNN	101	0.025090	2.852394	-0.096398
	LSTM		0.015771	1.766805	0.566800
	CNN-LSTM		0.008994	0.956124	0.859108
	CL-GraphSAGE		<b>0.005314</b>	<b>0.606468</b>	<b>0.950810</b>

connected when the similarity value is more than 0.95. All the graph structures are fully connected graphs. Fig. 8(d) shows the graph structures of the battery B0005 HIs.

Compared with the NASA dataset, the MIT dataset has more cycles and a larger amount of data. Different training method is employed in the MIT dataset. A0001 is used for training, and A0002 and A0003 are used for testing.

Fig. 9 shows the prediction results and errors. Table 6 shows the performance evaluation of the four models. Compared with the other three models, CL-GraphSAGE obtains the best prediction performance,

which is the lowest RMSE, MAPE with the highest R<sup>2</sup>.

Experiment results show that the proposed method is better than the comparison model in terms of SOH prediction. Compared with the other three models, CL-GraphSAGE can obtain not only the temporal features of HIs using CNN and LSTM but also the spatial features between HIs. Therefore, CL-GraphSAGE can make full use of the interrelationships between different HIs to deep mine more useful potential features. The fluctuation range of the prediction error of CL-GraphSAGE is smaller for SOH prediction compared with the other three models.

#### 4.3. Experiment of laboratory dataset

In this section, the lithium-ion battery dataset carried out in the laboratory is used to validate the feasibility of CL-GraphSAGE. The experiments are carried out in China Merchants Testing Vehicle Technology Research Institute Co., Ltd. The BAT-NEEFLCT-05500 from NEBULA Co., Ltd. is used to cycle the batteries. The data is collected by Agilent 34901A.

The batteries go through 4 steps in each cycle: 1) Discharging CC at 58A until the voltage drop to 2.5 V. 2) The battery is rest for 1800 s. 3) Charging CC at 38.86 A until the voltage increases to 4.25 V, then CV at 4.25 V until the current drop to 2.9A. 4) Resting 1800 s.

Five strongly correlated HIs (B3, B5, B8, B17, B26) are taken as model input from the charge-discharge curves as CL-GraphSAGE input by using HIs extracted in Section 2.2. The predicted results are shown in Fig. 10. Fig. 10 shows that the CL-GraphSAGE well captures the degradation of LIBs. The RMSE and R<sup>2</sup> are 0.003688 and 0.986188, respectively. Both RMSE and R<sup>2</sup> verify the effectiveness of CL-GraphSAGE.

#### 4.4. Experiment of different graph models

Instead of using GraphSAGE in the NASA dataset, combined with CNN and LSTM, the graph convolutional network (GCN) and graph attention network (GAT) which are CL-GCN and CL-GAT used to compare with the CL-GraphSAGE. The results are shown in Fig. 11 and Table 7. The results are similar to that of CL-GAT and CL-GraphSAGE. However, the running time of CL-GCN, CL-GAT, and CL-GraphSAGE are 169.21 s, 462.63 s, and 110.38 s, respectively. The execution time of CL-GAT is more than four times that of CL-GraphSAGE. In terms of time cost and prediction accuracy, CL-GraphSAGE is the best of the three GCNs proposed in this paper to obtain the spatial features of HIs.

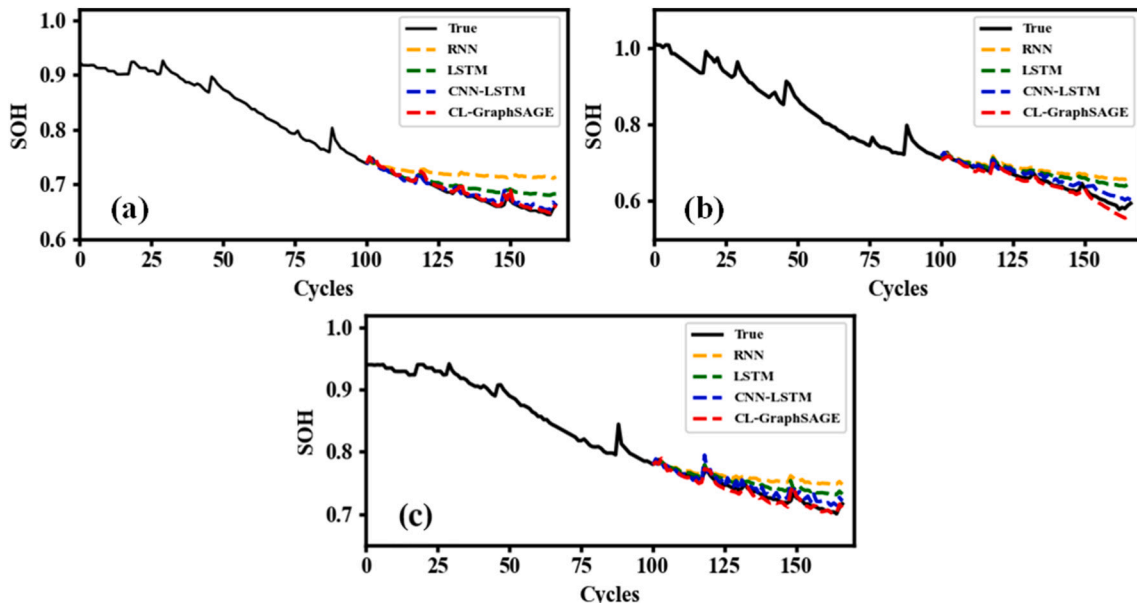


Fig. 7. Prediction results at starting point of 101: (a) B0005; (b) B0006; (c) B0007.

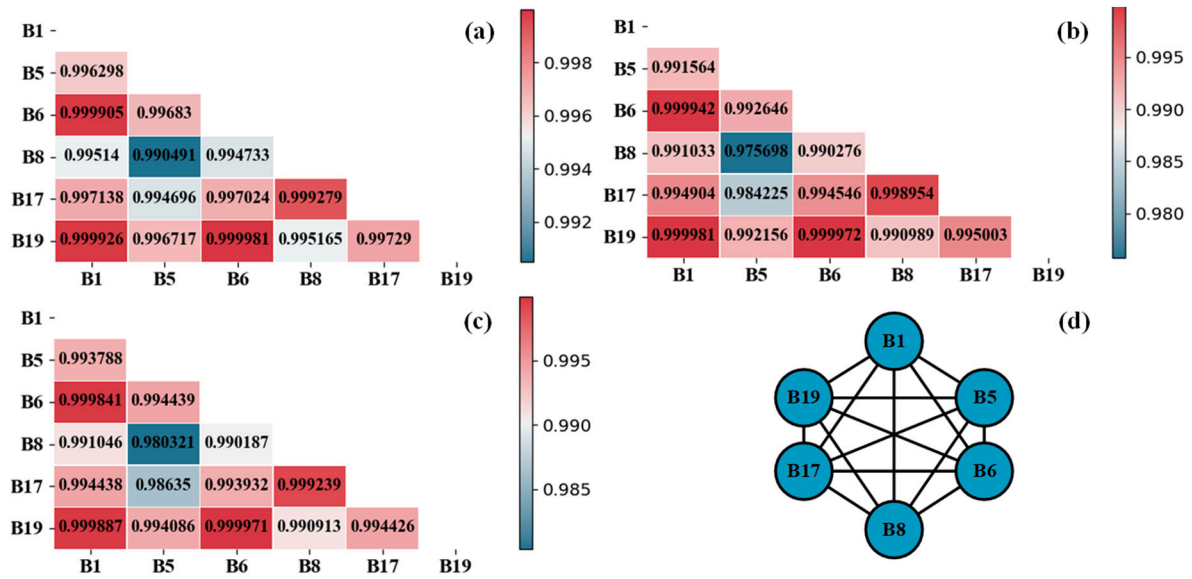
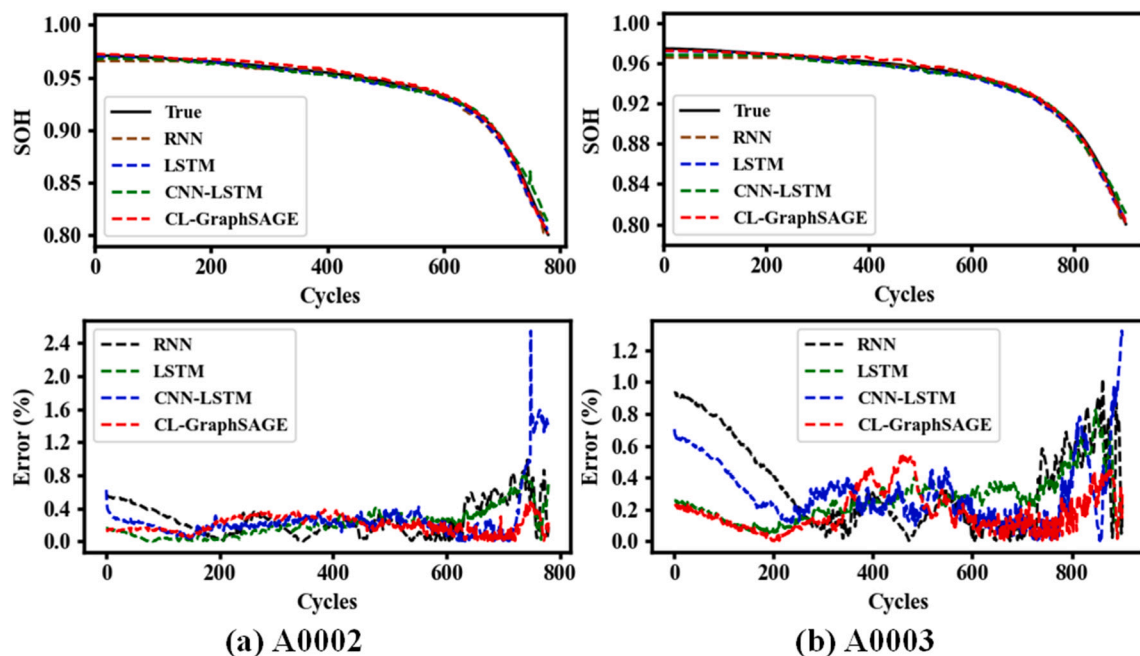


**Table 5**

Descending order of correlation coefficient for HIs.

Sample	Sort in descending order (from left to right, top to bottom)							
A0001	<b>B17</b>	<b>0.999098</b>	<b>B19</b>	<b>0.998555</b>	<b>B6</b>	<b>0.998443</b>	<b>B1</b>	<b>0.998323</b>
	<b>B5</b>	<b>0.997899</b>	<b>B8</b>	<b>0.996969</b>	B13	0.978474	B22	0.975399
	B20	0.749903	B7	0.748421	B18	0.726796	B2	0.508062
	B10	0.398186	B12	0.192002	B11	0.140236		
A0002	<b>B19</b>	<b>0.998027</b>	<b>B6</b>	<b>0.997991</b>	<b>B1</b>	<b>0.997727</b>	<b>B17</b>	<b>0.996563</b>
	<b>B5</b>	<b>0.995133</b>	<b>B8</b>	<b>0.992152</b>	B13	0.970764	B22	0.969931
	B12	0.733495	B20	0.728244	B7	0.727605	B10	0.695812
	B18	0.690713	B11	0.646046	B2	0.250485		
A0003	<b>B19</b>	<b>0.998105</b>	<b>B6</b>	<b>0.998042</b>	<b>B1</b>	<b>0.997935</b>	<b>B17</b>	<b>0.996740</b>
	<b>B5</b>	<b>0.995852</b>	<b>B8</b>	<b>0.993183</b>	B13	0.970857	B22	0.963337
	B18	0.677841	B20	0.611967	B7	0.611051	B10	0.309357
	B12	0.171201	B11	0.038053	B2	0.036999		

The bold in the table are the selected HIs which is the input of the model in this case.

**Fig. 8.** Node similarity and graph structure: (a) A0001; (b) A0002; (c) A0003; (d) graph of A0001 HIs.**Fig. 9.** SOH prediction results: (a) A0002; (b) A0003.

**Table 6**  
Performance evaluation with different models.

Sample	Model	RMSE	MAPE	$R^2$
A0002	RNN	0.003048	0.264716	0.993135
	LSTM	0.002468	0.215389	0.995500
	CNN-LSTM	0.003383	0.266529	0.991545
	CL-GraphSAGE	<b>0.002070</b>	<b>0.197313</b>	<b>0.996834</b>
A0003	RNN	0.004226	0.353931	0.987291
	LSTM	0.002776	0.266655	0.994514
	CNN-LSTM	0.003361	0.304047	0.991960
	CL-GraphSAGE	<b>0.002114</b>	<b>0.184998</b>	<b>0.996818</b>

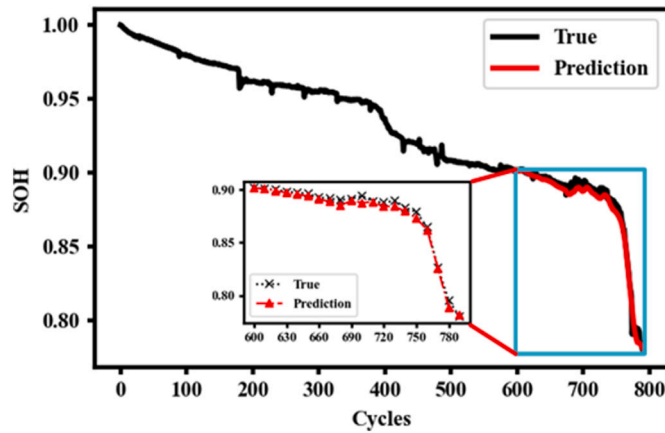


Fig. 10. Prediction results of CL-GraphSAGE.

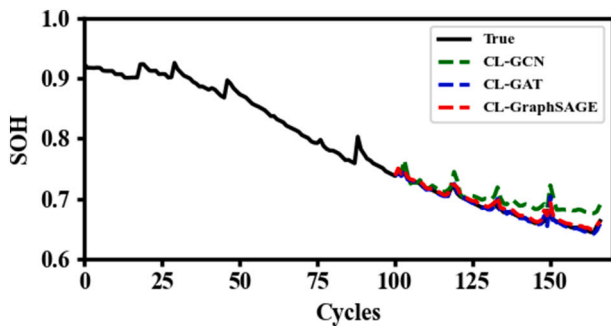


Fig. 11. Results of the three GNN models.

**Table 7**  
Errors of the three GNN models.

Method	RMSE	MAPE	$R^2$
CL-GCN	0.020253	2.504092	0.493080
CL-GAT	0.006454	0.505244	0.948513
CL-GraphSAGE	<b>0.005808</b>	<b>0.625176</b>	<b>0.958309</b>

## 5. Conclusions

The current lithium-ion battery SOH predicted methods by health indicators only take time features into account and ignore the relationship between different features especially for the limited data in the application. In this paper, a novel GNN-based framework is proposed for SOH prediction, which considers both the temporal features and the spatial features of HIs for the limited data. The validation and feasibility of the proposed CL-GraphSAGE are proved by public battery datasets and laboratory experiments. The results show that the CL-GraphSAGE reached minimum error and predicts more accurately and precisely

compared with RNN, LSTM, and CNN-LSTM.

It is understood that there is little research on GNN in LIBs. This work opens a new door for using GNNs to process various structural or unstructured data of batteries. Naturally, there are some limitations to the method. The future work includes: (1) The correlated HIs extracted based on partial charge-discharge curves will be developed in the future. (2) The edges connected are fixed weight by calculating the Pearson correlation coefficient in the proposed approach, which are all fully connected in the graph. Hence, the weight of the edges can be designed to update automatically to determine which edge to connect adaptively. (3) GNN can also be applied to other aspects of batteries, such as remaining life prediction, thermal runaway warning, and fault diagnosis.

## CRedit authorship contribution statement

Xing-Yan Yao: Conception, Methodology, Validation, Formal analysis, Investigation, Writing - Original Draft, Writing - Review & Editing, Visualization, Guolin Chen: Conceptualization, Methodology, Software, Validation, Writing, Bin Chen: providing dataset, Michael Pecht: Review, Supervision.

## Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

## Data availability

Data will be made available on request.

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