Final Year Project Report

**Full Unit – Final Report**

Value at Risk

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A report submitted in part fulfilment of the degree of

**BSc (Hons) in Computer Science**

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Department of Computer Science

Royal Holloway, University of London

March 29, 2023

**Declaration**

This report has been prepared on the basis of my own work. Where other published and unpublished source materials have been used, these have been acknowledged.

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Abstract

The use of computers has become increasingly crucial in the modern finance environment. From sending financial reports to conducting meetings, technology plays a significant role in this field. This project focuses specifically on finance strategies, which are essential for the planned development of the Finance function. By building on insights from a business context, stakeholder expectations, and own performance and capabilities, a finance strategy aims to focus on opportunities that create value.

One critical aspect of investing is controlling risk, as noted by Warren Buffett. This project explores the use of Value at Risk (VaR) as a strategy for quantifying financial risk within a firm or portfolio over a specified time frame. VaR provides an estimate of the maximum loss from a given position or portfolio over a period of time, and can be calculated across various confidence levels. The project involves developing a program for computing VaR and testing its performance through backtesting.

The project's main objective is to explore the effectiveness of VaR as a risk management strategy and to develop a program that can accurately compute VaR across various confidence levels. This will be achieved by conducting backtesting on the program and comparing its results to actual historical data to ensure its accuracy. The program will also be evaluated based on its ability to provide insights into potential investment opportunities and the level of risk associated with each.

To sum up t the goal of this project is to contribute to the development of effective risk management methods in finance and to give insights into the possible benefits of employing VaR as a tool for financial risk management. This project will give significant insights into the effectiveness of VaR as a risk management approach and its possible uses in the financial industry by building and testing a programme that accurately computes VaR.

Project Specification

Your project specification goes here.

Objectives:

* Develop a proof-of-concept program for computing Value at Risk (VaR) for a portfolio consisting of 1 or 2 stocks using model-building and historical simulation methods.
* Analyse different ways of computing VaR and back test them to evaluate their statistical significance.
* Extend the program to allow derivatives (such as options) in the portfolio and use Monte Carlo simulation.
* Allow an arbitrary number of stocks in the portfolio using eigen- or Cholesky decomposition.
* Design and implement the final program with full object-oriented design and modern software engineering principles, including a graphical user interface.
* Conduct computational experiments with different data sets, methods, and parameters.

Background:

Estimating the riskiness of a portfolio is a complex and important problem in finance. Value at Risk (VaR) is a widely used tool for measuring financial risk. This project aims to develop a program for computing VaR for portfolios using model-building and historical simulation methods, and to extend the program to allow derivatives and Monte Carlo simulation. The final program will have a full object-oriented design and modern software engineering principles.

Deliverables:

* Proof-of-concept program for computing VaR for a portfolio consisting of 1 or 2 stocks using model-building and historical simulation methods.
* Analysis of different ways of computing VaR and their statistical significance.
* Extended program that allows derivatives and Monte Carlo simulation, and allows an arbitrary number of stocks in the portfolio using eigen- or Cholesky decomposition.
* Final program with full object-oriented design and modern software engineering principles, including a graphical user interface.
* Report detailing the theory behind the algorithms, implementation issues, software engineering process, and computational experiments with different data sets, methods, and parameters.

# Introduction

## The Problem

The capacity to create higher returns while limiting risk is essential for a successful investment. Risk is a significant component that investors and traders evaluate when making investment decisions, and it is frequently the key determinant in accepting or rejecting an asset or security. However, while deciding whether to buy or sell an investment, the first worry for any investor is the greatest amount they may lose or the entire value at risk.

During the project, I will try to make an app that can simplify the mathematical formula to some simple button to help user to value their own investment portfolio risk easily.

## Aims and Goals of the Project

The aim of this project is to develop a program that simplifies the process of calculating Value at Risk (VaR) for investment portfolios. The program will allow investors and traders to easily evaluate the risk of their investment decisions, which is crucial for successful investment strategies.

The following goals was achieved in the first term of the project:

* Implement the historical simulation method for calculating VaR in single stocks using a proof-of-concept program.
* Implement the historical simulation method for calculating Conditional VaR (CVaR) in single stocks using the same program.
* Implement the historical simulation method for calculating VaR in portfolios using the same program.
* Implement the historical simulation method for calculating CVaR in portfolios using the same program.
* Implement the model building method for calculating VaR in single stocks using the same program.
* Back test the different methods for computing VaR and analyse the statistical significance of the results.

The following goals was achieved in the final term of the project:

* Extend the program to allow for derivatives such as options in the portfolio using Monte Carlo simulation and historical data.
* Allow an arbitrary number of stocks in the portfolio by using Cholesky decomposition.
* Implement a full object-oriented design with a complete implementation life cycle using modern software engineering principles.
* The program have a graphical user interface to provide an intuitive user experience.

## Survey of Related Literature

This section provides an extensive overview of the key literature sources that have informed the development and understanding of the financial risk assessment tool. These sources have been instrumental in shaping the tool's theoretical foundation and practical implementation.

**Hull, J. C. (2022). Options, Futures, and Other Derivatives (11th ed.). Pearson Educational Limited.**

In this comprehensive book presents a detailed overview of the different financial instruments, such as options, futures, and other derivatives, as well as their pricing and risk management. The book covers essential concepts, including the estimation of Value at Risk (VaR) and other risk measures, which are directly relevant to the development of the financial risk assessment tool. This book makes a foundation for me to understand the underlying financial theories and quantitative methods used in the tool. The book also delves into various risk management strategies, hedging techniques, and the role of regulation in the financial industry. This book is an indispensable resource for building a solid theoretical understanding of the financial risk assessment tool's underlying principles.

**Jorion, P. (2007). Value at risk: The new benchmark for managing financial risk. McGraw-Hill.**

In this influential book, it provided an in-depth analysis of the Value at Risk (VaR) concept and its application in managing financial risk. This book presents various methodologies for estimating VaR, such as the historical simulation approach, the parametric method, and the Monte Carlo simulation. The book also discusses back testing and model validation, which are crucial for ensuring the reliability of the financial risk assessment tool. This book help me to understand the practical implementation of VaR methodologies and their application in the risk assessment tool. Furthermore, the book explores the limitations and potential pitfalls of VaR, offering valuable insights into the challenges that practitioners may face when employing this risk measure in real-world scenarios.

**Dowd, K., & Hutchinson, M. (2010). Measuring Market Risk (2nd ed.). Wiley.**

Kevin Dowd and Martin Hutchinson's book focuses on the measurement and management of market risk. The authors provide a thorough examination of different risk measures, including Value at Risk (VaR), Conditional Value at Risk (CVaR), and stress testing. They also discuss various estimation methods, model validation techniques, and regulatory frameworks for market risk. This book offers valuable insights into the practical aspects of measuring and managing market risk, which can be applied in the development of the financial risk assessment tool. Additionally, the authors emphasize the importance of tail risk and the potential consequences of extreme market events, highlighting the need for robust risk management practices that account for such occurrences.

These three books serve as essential resources for understanding the theoretical and practical aspects of financial risk management, as well as the methodologies and best practices for developing a robust financial risk assessment tool. By examining these sources, we ensure that our tool is grounded in well-established concepts and methods in the field of finance and risk management. This comprehensive literature review helps to guarantee that the financial risk assessment tool adheres to industry standards and remains adaptable to the evolving needs of its users.

## Milestones Summary (timeline)

### Term 1

**Week 1:**

During this week, I began studying Value at Risk (VaR) and its underlying calculations. I focused on understanding the fundamental concepts and applications of VaR in financial risk management. I also identified and reviewed relevant literature and resources that would help me deepen my understanding of the topic and provide guidance for the project. I explored various risk assessment methods, their advantages and disadvantages, and how they have evolved over time.

**Week 2:**

In this week, I started planning the first term of the project and began learning how to use Python packages (yfinance, NumPy, pandas, and matplotlib) essential for data analysis in the financial domain. I researched the functionality and capabilities of these packages, studied their documentation, and explored sample use cases to gain hands-on experience. This week's focus was to develop a solid foundation for the data analysis and visualization components of the project.

**Week 3:**

This week, I started implementing simple calculations using Jupyter notebook and the Python packages learned in Week 2. I successfully initialized market data using the yfinance package and began experimenting with data manipulation and visualization using pandas and matplotlib. The goal was to become proficient in working with financial data, which would be crucial for the subsequent development of the financial risk assessment tool.

**Week 4:**

During this week, I successfully implemented a proof-of-concept program for computing Value at Risk (VaR) using the historical simulation method for both single stock and portfolio. I focused on understanding the underlying mechanics of the historical simulation method and its suitability for different types of financial assets. The proof-of-concept program allowed me to test my understanding of the method and served as a starting point for further development.

**Week 5:**

In this week, I implemented a proof-of-concept program for computing Conditional Value at Risk (CVaR) using the historical simulation method for both single stock and portfolio. I explored the differences between VaR and CVaR and learned about the importance of considering tail risk in financial risk management.

**Week 6:**

During this week, I enhanced the functions for calculating VaR and CVaR to accept different variables, allowing for more flexibility in the risk assessment process. I refined the calculation logic and ensured the functions' reliability and accuracy, which is crucial for the tool's effectiveness in risk management applications.

**Week 7:**

This week, I successfully implemented a proof-of-concept program for computing VaR using the model-building method for single stock. I compared the results with those obtained from the historical simulation method and evaluated the strengths and weaknesses of the model-building approach. This week's focus was to expand the project's scope by exploring alternative methodologies for risk assessment.

**Week 8:**

During this week, I refactored the code for computing VaR using the historical simulation method and the data initialization process. I aimed to improve the code's readability, maintainability, and efficiency to ensure the project's long-term sustainability and ease of use for future developers and users.

**Week 9:**

This week, I worked on implementing a proof-of-concept program for computing VaR using the model-building method for portfolio. I extended the single stock model-building approach to handle portfolios and assessed the accuracy and efficiency of this method for multi-asset risk management.

**Week 10:**

During this week, I continued working on the model-building method for portfolio risk assessment. Simultaneously, I implemented backtesting functionality for the historical simulation method for single stock, which allowed me to validate the performance and reliability of the risk assessment tool.

**Week 11:**

In this week, I prepared for the midterm submission and presentation. I consolidated my progress, documented the work completed thus far, and prepared a comprehensive report and presentation for the midterm evaluation. I focused on showcasing the project's objectives, methodology, and results, highlighting the challenges and lessons learned during the development process. I also prepared to address any questions or concerns that might arise during the presentation.

**Week 12:**

In the final week of Term 1, I reviewed and reflected on my progress, evaluated the project's current state, and identified areas for improvement and further development. I also gathered and incorporated feedback from the midterm presentation to refine the project's direction and goals. I created a plan for the upcoming term, outlining the tasks and milestones to be achieved, including the implementation of additional risk assessment methods, improving the user interface, and enhancing the overall user experience.

### Term 2

**Week 1:**

During this week, I upgraded the programs to API and began my research on Monte Carlo Simulation. I delved into Brownian motion, drift, and Cholesky decomposition to better understand the principles and methodology behind the simulation.

**Week 2:**

I implemented several functions related to Monte Carlo Simulation, including logarithmic\_returns, compute\_drift, and predict\_daily\_price. I also developed a function to combine the predicted prices into a dataframe and calculate the VaR using the historical simulation method.

**Week 3:**

I continued my work on Monte Carlo Simulation by implementing a variation using Cholesky decomposition. Additionally, I created test cases for the new functions and started looking into derivatives as another aspect of the project.

**Week 4:**

After meeting with my professor and receiving valuable feedback, I updated the project report and revised the formulas and styles within. I then added back tests for historical simulation and parametric methods for single stocks and portfolios.

**Week 5:**

I continued working on back tests for the parametric methods and resolved some importing bugs with Django. I also restructured the code to improve its organization and added driver code for Monte Carlo simulation methods for single stocks.

**Week 6:**

During this week, I implemented functions to check user input for stock lists and weights, and updated the app.py functions to accept user input. I upgraded the software to an API and refactored the code to remove dead code.

**Week 7:**

I began working on the frontend of the project using React, creating several pages and components such as navBar, SideBar, and a form component for user input. I also implemented a function to fetch the API with given parameters.

**Week 8:**

I focused on developing frontend components, including a graph component to display closing prices and updating the sideBar. I then created a new page in the project to display the calculated VaR in different methods and with option prices.

**Week 9:**

This week, I implemented various graphs to showcase closing prices and returns. I added a selection box for users to choose different methods for calculating VaR and started working on the VaR for option prices.

**Week 10:**

I continued working on the VaR for option prices, creating a class called cal\_option\_price for calculating option prices. I implemented the Black-Scholes formula and developed functions for cal\_sigma, cal\_d1\_d2, and black\_scholes.

**Week 11:**

I implemented the Option VaR class and tried to integrate historical simulation and Monte Carlo Simulation with the Option VaR. I then converted the functions to an API and started designing the interface for the OptionVaR.

**Week 12:**

In the final week of Term 2, I integrated the OptionVaR API with the frontend, developed the OptionSideBar component, and refactored the code to improve its overall structure and organization. This concluded the second term of the project with significant progress in both backend calculations and frontend user interface development.

# Background Research

## Value at Risk

Value at risk is a simple way to describe the magnitude of the likely losses on the portfolio. Based on simplified assumptions used in the calculation, VaR aggregates all risks in a portfolio into a single number that applies to the board, is reported to regulators, or is disclosed in annual reports. By the definition, it is an attempt to provide a single number summarizing the total risk in a portfolio of financial assets. But in simple way to explain it is a single, summary, statistical measure of possible portfolio losses from the market that have a “normal” market movement.

When using the Value at Risk measure, people will make the statement as follow

‘I am **X** percent certain there will not be a loss of more than **V** dollars in the next **N** days.’

we are interested in 3 variables which are

1. **V** it is the VaR of the portfolio
2. **N** is the time horizon (N days), normally will be 1 – 5 days
3. **X** is the confidence level (X %), we normally will put 99, 95 ,90

For example, we will say I am **5** percent certain there will not be a loss of more than **1000** dollars in the next **2** days.

VaR is the loss corresponding to the (100 - x) percentile of the distribution of the gain in the value of the portfolio over the upcoming N days when N days is the time horizon and X% is the confidence level. (Remark: When we look at the probability distribution of losses, the gains are negative losses and VaR is related to the right tail of the distribution. When we look at the probability distribution of returns, losses are negative returns and VaR is related to the left tail of the distribution.) For example, When N = 2 and X = 99 VaR is the first percentile of the distribution of gain in the value of the portfolio over 2 days.

A picture containing text, lamp

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Figure 1 Calculation of VaR from the probability distribution of the change in the portfolio value; confidence level is X%. Gains in portfolio value are positive; losses are negative [[1]](#footnote-2)

### Mathematical definition[[2]](#footnote-3)

Mathematically we can define as follow:

Let X be the distribution of profit and loss. (Profit is positive, and loss is negative). The VaR at level is the smallest number such that the probability that does not exceed is at least .Mathematically, is the quantile of

This is the most general definition of VaR, and the two identities are equivalent (in fact, for any real random variable X, its cumulative distribution function is well-defined). However, this formula cannot be used directly for calculations unless we assume that X has some parametric distribution.

## Conditional Value at Risk (CVaR)

Conditional Value at Risk (CVaR), commonly referred to as the expected shortfall or Mean Excess Loss, it estimates the amount of tail risk present in an investment portfolio. A weighted average of the "extreme" losses in the tail of the distribution of potential returns, above the value at risk (VaR) cut-off point, is used to calculate CVaR. Conditional value at risk is used in portfolio optimization for effective risk management.

Generally speaking, the VaR may be enough for risk management in a portfolio that contains an investment if it shows stability over time. However, because VaR is unconcerned with anything that goes above its own threshold, it is more likely that VaR will not accurately reflect risk for investments that are more volatile.

The Conditional Value at Risk (CVaR) model seeks to address the shortcomings of the VaR model, a statistical technique used to assess the level of financial risk in a company or portfolio over a specified time horizon. CVaR is the expected loss when the worst-case threshold is exceeded, whereas VaR represents the worst-case loss in terms of probability and time horizon. CVaR, in other words, quantifies the expected loss above the VaR breakpoint.

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Figure 2 Alternative situation to Figure 1. VaR is the same, but the potential loss is larger.

### Mathematical definition[[3]](#footnote-4)

Since the CVaR value is derived from the calculation of the VaR itself, the assumptions on which the VaR is based, such as the shape of the return distribution, the cut-off levels used, the periodicity of the data, and assumptions about stochastic volatility, can affect the value of the CVaR. Once VaR is calculated, calculating CVaR is straightforward. It is the average of values beyond VaR:

= the probability density of getting a return with value “”

= the cut-off points on the distribution where the analyst sets the VaR breakpoint

= the agreed-upon VaR level

## Time Horizon[[4]](#footnote-5)

For calculating the VaR we need two parameters: Time horizon N (days) and the confidence level X. In practise, when estimating the VaR for market risk, analysts almost always start with N = 1. This is due to the fact that there is frequently insufficient data to directly estimate the behaviour of market variables over time periods longer than one day. The assumption is:

N-day VaR = 1 - day VaR

When the changes in portfolio value over consecutive days have independent identical normal distributions with a mean of 0, the formula is completely correct. In other cases, it is a rough estimate.

## Historical Returns

To explain it mathematically, suppose today is Day n, the closing price is C, and the returns of a stock variable on Day i will be defined as r. In the historical simulation approach, the i th scenario of the market returns will be.

Returns under th scenario

## Historical Simulation

Historical simulation is one of the easy and popular way of calculating VaR It entails using past data to predict what will happen in the future. Let said we want to calculate the VaR for a portfolio using a one-day time horizon with 99% confidence level and 501 days of data. (We normally will put 99, 95 ,90 to the confidence level and 501 is a popular choice for the number of days of data used because this provides 500 alternative scenarios for what can happen between today and tomorrow.)

Data will be collected by the movements in the market variables over the most recent 501 days. Day 0 represents the first day for which we have data, Day 1 represents the second day, and so on. Scenario 1 is the same as Day 0 and Day 1, Scenario 2 is the same as Day 1 and Day 2, and so on. The dollar changes in the portfolio's value between today and tomorrow is calculated for each scenario. This defines a probability distribution for the value of our portfolio's daily loss (gains are negative losses). The distribution's 99th percentile can be estimated as the fifth-highest loss. The loss when we reach the 99th percentile is the estimate of VaR If the changes in market variables over the last 501 days are representative of what will happen between today and tomorrow, we are 99% certain that we will not take a loss greater than the VaR estimate.

### Historical Simulation – Single Asset

Let said we have 10K investing in Apple. We are interested in the loss level over 5 days that we are 99% certain will not be exceeded in a 1-day time horizon. Therefore N = 5 and X = 99. First, we need to have a table listing all the historical data.

Text

Description automatically generated with medium confidence

Table 1: 501 day’s closing prices for Apple.

Then we calculated their return and use the above table to create a scenario table.

Text

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Table 2: 500 scenarios for Apple

Then we sorted the table 2, from largest loss to profit.

Table

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Table 3

Since we are interested in 99%VaR it means we need to that the take 1% of the total day, it means days. we will take the fifth scenario, in this case will be 460, So the VaR will be.

So for N day VaR it will calculate by times the 1-day VaR, so the 5-days VaR for apple is:

### Historical Simulation – Portfolio

Let said we have 10K investing in the Portfolio which contains 5 stocks which is TSM, TSLA, GOOGL, MSFT and AAPL with weights of 20%,15%,15% 30% and 20 %. We are interested in the loss level over 5 days that we are 99% certain will not be exceeded in 1 day time horizon. So, N = 5 and X = 99.

For Portfolio we basically do the same things, but this time we need to have the portfolio weight (Portfolio) columns, so here we need to do is get the closing price.

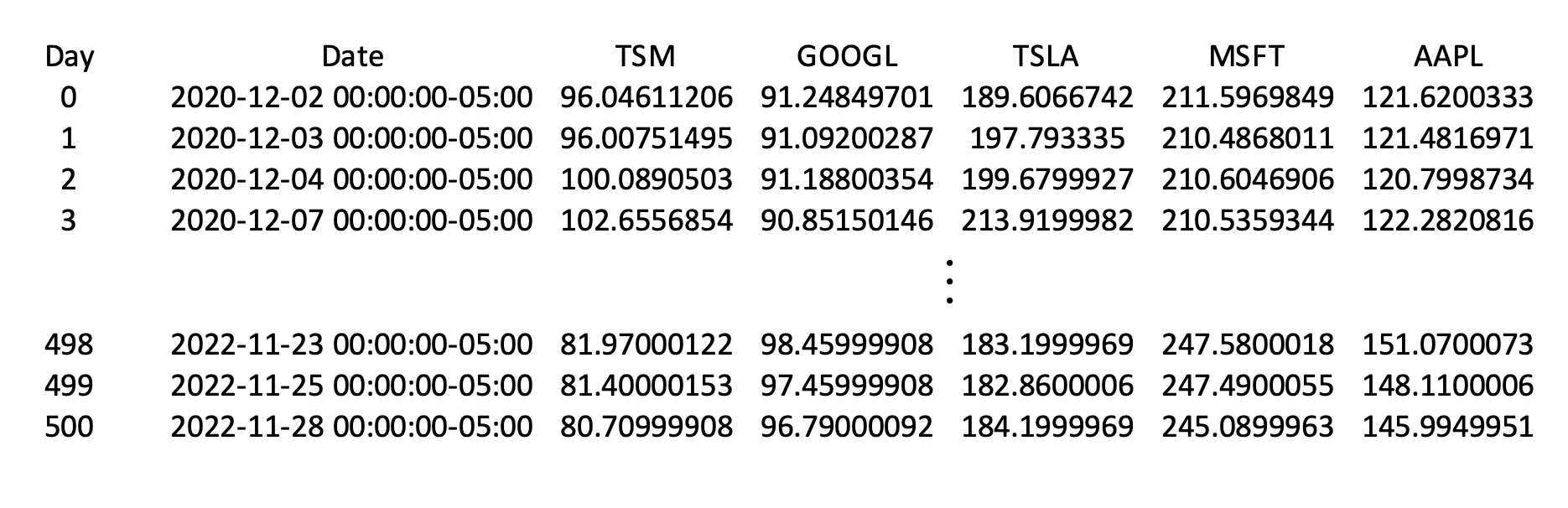


Table 4

Then replace the closing price with returns and use dot product to create a new columns Portfolio with the given weight 20%,15%,15% 30% and 20% (which is the combined returns with all stock provide).

Table

Description automatically generated

Table 5

Then we sort Table 5, from the largest loss to profit.

Table

Description automatically generated

Table 6

Since we are interested in 99%VaR it means we need to that 1% of the total day, it means days. we will take the fifth scenario, in this case, it will be 367, So the VaR will be:

So for N day VaR it will calculate by times the 1-day VaR, so the 5-days VaR for apple is:

## Model Building method

The model-building method is the primary alternative to historical simulation. Before delving into the method, we need to define clearly the volatility unit first.

### Daily Volatilities

In option pricing, time is normally defined in years, and an asset's volatility is usually expressed as a "volatility per year." When utilising the model-building approach to calculate VaR for market risk, time is typically measured in days, and an asset's volatility is typically expressed as a "volatility per day."

Let's define the volatility per year of a certain asset be and the equivalent volatility per day of the asset as . Assume a year has 252 trading days, the daily volatility will be :

So the daily volatility will be around 6% of annual volatility. In calculating VaR, we assume that the daily volatility of a stock is equal to the standard deviation of the percentage change within a day.

### Model Building method – Single Asset [[5]](#footnote-6)

Let said we have 10K in a share of Apple. We are interested in the loss level over 5 days that we are 99% certain will not be exceeded in 1 day time horizon. So N = 5 and X = 99, Assuming the daily volatility of Apple is 2% (32 % in a year) the standard deviation of daily change will be 2 % of 10K which is $ 200.

In the model-building methods, it is common to assume that the predicted change in a market variable over the time period under consideration is zero. Although this is not precisely correct, it is a valid assumption. When compared to the standard deviation of the change, the expected change in the price of a market variable over a short time period is often tiny. For example, Apple is predicted to yield 20% every year. The expected return during a one-day period is 0.20/252, or around 0.08%, with a standard deviation of 2%. The predicted return over a 10-day period is 0.08 x 10, or about 0.8%, while the standard deviation of the return is 2 , or about 4.5%.

From the standard normal cumulative distribution function, we know that . This means that there is only 1% chance that the value of a normally distributed variable will change by more than 2.326 standard deviations. It also means that we are 99% certain that the value of a normally distributed variable will not decrease by more than 2.326 standard deviations. So, let’s put the number together.

So for N day VaR it will calculate by times the 1-day VaR, so the 5-days VaR for apple is :

### Model Building method – Portfolio

Let said we have 10K investing in the Portfolio which contains 5 stocks which is TSM, TSLA, GOOGL, MSFT and AAPL with weights 20%,15%,15% 30% and 20 % . We are interested in the loss level over 5 days that we are 99% certain will not be exceeded in 1 day time horizon. So, N = 5 and X = 99.

By the model-building methods, we also need to gather all the data (see Table 4), then we calculate their returns.

A picture containing table

Description automatically generated

Table 6

Then we need to calculate the covariance for each stock, by using the formula below:

In the formula R1 and R2 is representing all the returns for Stock 1 and Stock 2 , n is how many days we have in the data , and will be the daily return . In this example, we have 5 stocks, so we will have 25 covariances

Table

Description automatically generated with medium confidence

Table 7

Then we need to calculate the standard deviation for the portfolio. With n stock the formula will be :

In this formula is the amount of money to put into this stock

In our example, we have initial investment 10K, we need to extract the amount with the weight So , …

Then to calculate the we need to

Then VaR can be calculated by Percentile point function, so we give the function our confidence level which is and standard deviation 183.43. As a result, the VaR will be $ 301.79.

## Monte Carlo simulation

Monte Carlo simulation is a method of statistical modelling that uses random sampling to simulate possible outcomes of a system. It is commonly used in finance to estimate the potential losses in a portfolio of financial assets. Before I show case how to use it , let us discuss the theory behind.

### Random Walk

In finance and economics, a random walk is a simple framework for modelling the evolution of asset prices and other economic variables over time. The path travelled by a variable that changes over time and the future value is unpredictable, such as the stock price, is referred to as its path. This means that future values of the variable cannot be predicted with certainty, as they move in a sequence of steps over time that are random and independent of the previous ones.

one example of a random walk is a coin toss. Assume we start with balance of zero, every time we toss a coin if it is head then add one, otherwise subtract one .Since the value of the balance will follow a random sequence of coin tosses, each toss being independent of the previous toss, the result can be considered a random walk.[[6]](#footnote-7)

The concept is that the price of a stock can randomly rises or fall over time, with both possibilities being equally probable. Therefore, the stock price at any point can be seen as a random variable, the stock price's movement over time can be represented by a sequence of random steps or increments. So, it can be treated as random walk.

where:

is the stock price at time t

is the stock price at the previous time step

is a random variable representing the change in stock price from t-1 to t

### Wiener Process[[7]](#footnote-8)

The Wiener process, also known as Brownian motion, is a continuous-time stochastic process that is widely used in finance and economics to model random variables that evolve continuously over time. It is characterized by two properties: independence of increments and Gaussian distribution. The Wiener process is named after the mathematician Norbert Wiener, who first introduced it in 1923.

In mathematical terms, the Wiener process is defined as a continuous-time stochastic process with the following properties:

1. The increments are independent for any time t1 < t2
2. The increments are normally distributed with mean 0 and variance (t2 - t1)

In other words, the Wiener process is a random walk with infinitely small steps that are normally distributed. The variance of the increments increases with the length of the time interval, which means that the process becomes more volatile over time.

The following equation represents the Wiener process:

where is the increment of the process over an infinitely small time interval dt, and is a normally distributed random variable with mean 0 and variance dt.

### Cholesky decomposition

In mathematical optimization and statistics, Cholesky decomposition is a matrix factorization of a Hermitian, positive-definite matrix into the product of a lower triangular matrix and its conjugate transpose, which is useful for efficient numerical solutions, such as Monte Carlo simulations, and for generating correlated random variables.

The Cholesky decomposition of a positive-definite matrix A can be written as:

Where L is a lower triangular matrix with real and positive diagonal entries, and L\* is its conjugate transpose. The decomposition is unique for positive-definite matrices, which are symmetric and have all positive eigenvalues.

One important application of Cholesky decomposition is in Monte Carlo simulations, which are widely used for financial risk management and option pricing. In Monte Carlo simulations, we generate a large number of random samples from a multivariate distribution with a specified covariance matrix, which is often positive-definite. The Cholesky decomposition allows us to efficiently transform independent, normally distributed random variables into correlated random variables with the specified covariance matrix.

### Monte Carlo simulation

Monte Carlo simulation is a technique used to generate numerous potential outcomes for a given system or process by using random sampling. It is often used in finance to simulate the behaviour of financial assets such as stocks, options, or portfolios. Monte Carlo simulation is a statistical method that can help estimate the range of possible outcomes and their associated probabilities. It can be used to calculate various financial metrics such as value at risk (VaR), expected return, and portfolio risk.

The Monte Carlo simulation is based on the principle of generating many random sample paths for a given financial asset's price. Each sample path is constructed by generating random variables for each of the inputs that drive the process. For example, for a stock price simulation, we would generate random variables for the expected return and volatility of the stock. Once the inputs have been determined, we simulate the stock price movement using the Wiener process, which is a continuous-time stochastic process that is also a type of Brownian motion.

Using Monte Carlo simulation, we can generate many possible stock price paths. Based on these paths, we can calculate the statistical properties of the resulting distribution of prices, such as the mean, standard deviation, and VaR. Monte Carlo simulation provides a powerful tool to estimate the range of possible outcomes for a given financial asset or portfolio.

In the following section, we will illustrate how Monte Carlo simulation can be applied to predict stock prices for a single stock. For the purpose of this example, we will use the stock of Apple Inc., which is commonly referred to by its ticker symbol 'AAPL'.

Step 1: Collect historical stock price data and calculate logarithmic returns for each stock.

Graphical user interface, text, application

Description automatically generated

Table 8

Step 2: Compute the drift (expected return) and standard deviation for each stock using the historical data.

Where:

is the mean return of the stock (typically calculated using historical data)

is the variance of the stock's returns

Step 3: Generate random variables for each stock using cumulative distribution function. This step assumes that the stocks are independent.

Where:

U is a uniformly distributed random number between 0 and 1

Step 4: Calculate the predicted daily returns using the drift and standard deviation for each stock.

Where:

is the drift

is the standard deviation ()

Z is the random variable generated in step 3.

Step 5: Simulate the stock prices using the predicted daily returns and the most recent stock price.

Graphical user interface, table

Description automatically generated

Table 9

If we want to predict stock prices for multiple stocks, i.e., a portfolio, there are two methods to do it.

Method 1: Monte Carlo Simulation with Independent Stocks

We assume that each stock in the portfolio has a separate random walk and generate simulations for each stock individually. We can then combine the results to get simulations for the overall portfolio. The following steps can be taken:

Step 1: Collect historical stock price data and calculate logarithmic returns for each stock.

Step 2: Compute the drift (expected return) and standard deviation for each stock using the historical data.

Step 3: Generate random variables for each stock using cumulative distribution function. This step assumes that the stocks are independent.

Step 4: Calculate the predicted daily returns using the drift and standard deviation for each stock.

Step 5: Simulate the stock prices using the predicted daily returns and the most recent stock price.

(The first 5 step is same with the single stock)

Step 6: Repeat Steps 1-5 for each stock in the portfolio separately, generating simulations for each stock individually.

Step 7: Concatenate the simulation results for each stock from Step 6 to obtain the simulation result for the portfolio. This can be done by adding the simulated stock prices for each stock on the corresponding date. At the end of this step, we will have 1000 tables (if we do 1000 iterations) with simulated prices for the entire portfolio.

Table

Description automatically generated

Table 10

Method 2: Monte Carlo Simulation with Cholesky Decomposition

We take into account the correlations between the stocks in the portfolio. We can do this by using the Cholesky decomposition of the covariance matrix to generate correlated random variables and then simulating the prices of each stock using these variables. The following steps can be taken:

The first 2 step is same, so let start at Step 3

Step 3: Calculate the covariance matrix for the logarithmic returns.

Text

Description automatically generated

Table 11

Step 4: Perform Cholesky decomposition on the covariance matrix to obtain a lower triangular matrix.

Table

Description automatically generated with medium confidence

Table 12

Step 5: Generate uncorrelated random variables and use the Cholesky decomposition matrix to transform them into correlated random variables.

A picture containing table

Description automatically generated

Table 13

Step 6: Calculate the predicted daily returns using the drift and correlated random variables.

Text, table

Description automatically generated

Table 14

Step 7: Simulate the stock prices using the predicted daily returns and the most recent stock price.

Step 8: Generating simulations for each stock by using the correlated random variables in Step 6. Like(Table 9)

Step 9: Concatenate the simulation results for each stock from Step 8 to obtain the simulation result for the portfolio. This can be done by adding the simulated stock prices for each stock on the corresponding date. At the end of this step, we will have 1000 tables (if we do 1000 iterations) with simulated prices for the entire portfolio.(Like Table 10)

Overall, Cholesky Decomposition may provide more accurate simulations for the portfolio since it considers the interdependence of the stocks.

## Monte Carlo simulation for VaR

Monte Carlo simulation for VaR involves using the simulated stock prices to calculate the potential losses in a portfolio at a given confidence level. This can be done using the same Historical Simulation approach discussed earlier.

Suppose we want to compute the 1-day 99% VaR for a portfolio having 5 stocks (AAPL, GOOGL, MSFT, TSLA, and TSM) with the following weights: 20%, 15%, 30%, 15%, and 20%. We can perform a Monte Carlo simulation to generate the stock price paths for each stock in the portfolio, as described in the previous section.

Next, we can use Historical Simulation to calculate the potential losses for the portfolio at the 99th percentile level. This involves calculating the portfolio value for each simulated stock price path and sorting the resulting portfolio returns from lowest to highest. The 99th percentile portfolio return represents the 1-day 99% VaR for the portfolio.

Finally, we can use the same method to determine the portfolio's 5-day 99% VaR by multiplying the 1-day VaR by the square root of 5. This provides an estimate of the potential losses that the portfolio could experience over a 5-day period at the 99% confidence level, based on the simulated stock price paths generated by the Monte Carlo simulation.

## Option

An option is a financial contract between two parties, giving the buyer (holder) the right, but not the obligation, to buy or sell an underlying asset at a predetermined price (strike price) within a specific time frame. The seller (writer) of the option is obligated to buy or sell the underlying asset at the strike price if the buyer chooses to exercise the option. Also the date specified in the contract is called the expiration date or the maturity date, and the price specified in the contract is called the exercise price or the strike price.

Since the option is a financial instruments, it can be traded on different kind of underlying assets, including stocks, bonds, currencies, cryptocurrencies or even commodities. Option letting investor to achieve various objectives, such as hedging risk, speculating on price movements, and generating income.  
  
There are two type of option, American or European, and this distinction has nothing to do with their geographic location. American options can be exercised at any time up to the expiration date, while European options can only be exercised on the expiration date itself. Most options traded on exchanges are American, but European options are generally easier to analyse than American options.

### Option Type

There are two main types of options: call options and put options. A call option gives the holder the right to buy the underlying asset at the strike price, while a put option gives the holder the right to sell the underlying asset at the strike price. Both call and put options have an expiration date, after which the option is no longer valid. I will explain in more details in call and put option. For make it simple we will talk about the European option only

**Call Option**

Call options give the holder the right to buy an underlying asset at a predetermined price (strike price) on the expiration date. Consider an investor who buys a European call option with a strike price of $100 to purchase 100 shares of a certain stock. If the stock price is above $100 on the expiration date, investor will exercise the option. For example, the stock price(market price) is $115. By exercising the option, the investor is able to buy 100 shares for $100 per share. If the shares are sold immediately, the investor makes a gain of $15 per share, or $1,500, ignoring transaction costs. When the initial cost of the option is taken into account, the net profit to the investor is $1,000. However, if the stock price on the expiration date is less than $100, the investor will choose not to exercise and will lose the initial investment.

Chart, line chart

Description automatically generated

Figure 3: Profit from buying a European call option on one share of a stock. Where option price = $5, strike price = $100

**Put Option**

Put options allow the holder to sell an underlying asset at a predetermined price (strike price) on the expiration date. Consider an investor who buys a European put option with a strike price of $70 to sell 100 shares of a certain stock. If the stock price falls below $70 by the expiration date, the investor can exercise the option and sell the 100 shares for $70 each, realizing a gain of $15 per share, or $1,500. When the initial cost of the option is taken into account, the investor's net profit is $800. However, if the final stock price is above $70, the put option will expire worthless, and the investor will lose the initial investment of $700.

Chart

Description automatically generated

Figure 4: Profit from buying a European put option on one share of a stock. Option price is $7 , Strike Price is $70

**Early Exercise**

European options can only be exercised at the expiration date. However American options, which can be exercised at any time before the expiration date. In the case of European options, the holder must wait until the expiration date to exercise the option.

### Calculate Option Price

There are two main ways to calculate the price of an option: using Binomial Tree and using the Black-Scholes formula.

**Binomial trees**

Binomial trees

One method for pricing options is to use a binomial tree model. The binomial tree is a mathematical tool used to calculate the probabilities of future stock prices and to price options based on these probabilities. The tree consists of a series of nodes, where each node represents a possible stock price at a future time. Starting from the current stock price, the tree branches out to two possible future prices: one up and one down. The branching continues until the final nodes are reached, which represent the possible stock prices at the expiration date of the option.

To compute the option price using a binomial tree, we must first compute the probability of the stock price moving up or down at each node. The probability are determined by the volatility of the stock price and the period before the option expires. Therefore, using probabilities, we can compute the predicted value of the choice at each node.

To calculate the option price using a binomial tree model, the expected value at each node is computed as the discounted value of the future payoffs of the option. For a call option, the payoff at each node is the maximum difference between the stock price and the strike price, or zero. Mathematically, the call option payoff at a node is:

where is the stock price at a given node and is the strike price of the option. For a put option, the payoff at each node is the maximum of the difference between the strike price and the stock price, or zero. Mathematically, the put option payoff at a node is:

The expected value is then calculated as the weighted average of the payoffs, using the probabilities of the stock price moving up or down at each node.

To determine the option price at the current time using the binomial tree model, we work backwards through the tree after calculating the expected values at each node. The expected value at each node is then discounted using the risk-free interest rate and the time to expiration of the option. This allows us to determine the option price at the current time based on the expected values at the expiration of the option.

The final result is the option price at the current time, which represents the fair value of the option based on the assumptions used to construct the binomial tree. Deviations from these assumptions can affect the accuracy of the calculated option price.

The mathematical equation for pricing a European call option using a binomial tree is as follows:[[8]](#footnote-9)[[9]](#footnote-10)

where:

is the current price of the call option

is the current price of the put option

is the current stock price

is the strike price

is the risk-free interest rate

is the number of periods in the binomial tree

is the probability of the stock price moving up at each node

is the factor by which the stock price moves up at each node

is the factor by which the stock price moves down at each node

is the binomial coefficient, which represents the number of ways to choose up movements out of total movements.

**Black-Scholes Formula**

The Black-Scholes model is a widely used mathematical model for pricing options contracts. The model takes several factors to calculate the option price, such as the current stock price (), the strike price(K), the time to maturity(T), the risk-free interest rate(r), and the volatility of the underlying asset ().

The model considers several factors that affect the value of an option, including the current stock price, the strike price, the time to expiration, the risk-free interest rate, and the volatility of the underlying asset.

The Black-Scholes model assumes that the price of the underlying asset follows a lognormal distribution, which means that it has a long-term average growth rate and a certain degree of randomness. The model also assumes that there are no dividends paid out during the life of the option.

The formula for the Black-Scholes model is given as:[[10]](#footnote-11)

Where

is the price of a call option at time

is the price of a call option at time

is the current stock price

is the strike price

is the risk-free interest rate

is the time to expiration

is the cumulative standard normal distribution.

The value of can be found in standard statistical tables or calculated using a computer program.

The values of and are calculated as follows:

where is the volatility of the underlying asset.

here's an example using the Black-Scholes formula to price a call option:

Suppose we want to price a European call option on a stock with a current price of $100. The option has a strike price of $120, an expiration date in 6 months, and a volatility of 20%. The risk-free interest rate is 5%.

First, we calculate the value of d1 and d2 using the Black-Scholes formula:

Next, we calculate the value of N(d1) and N(d2) using a standard normal distribution table or calculator. For our example, we have:

Finally, we use the Black-Scholes formula to calculate the price of the call option:

So the price of the call option is approximately $1.02.

If we use the Black-Scholes formula to calculate the price of the put option:

So the price of the call option is approximately $18.06.

## Option VaR

There are several methods to calculate option VaR, including historical simulation and Monte Carlo simulation. Both methods involve simulating the future prices of the underlying asset, based on historical data, or assumed probability distributions, and using these simulations to calculate the potential losses of the option at a specified confidence level.

In both historical and Monte Carlo simulations, the Black-Scholes formula can be used to calculate the option price at each simulated price of the underlying asset, based on the specified option parameters such as the strike price, time to expiration, and volatility.

### Historical Simulation to Calculate Option VaR

Historical simulation is a widely-used method for calculating the VaR of financial instruments, including options. The method involves using historical data to simulate the potential future price movements of the underlying asset, and then using these simulations to estimate the potential losses of the option at a specified confidence level.

To apply historical simulation to options, we first need to determine the historical daily returns of the underlying asset over a specified time horizon, such as a month or a year. These returns can be calculated using the formula at section 2.4 Historical Returns.

Once the historical returns are calculated, we randomly select a set of returns from the historical data, with replacement, and use these returns to calculate the future prices of the underlying asset. This process is repeated multiple times, generating a distribution of potential future prices of the asset.

To calculate the VaR of the option at a specified confidence level, we then calculate the potential losses of the option at each simulated price, using the option's payoff function. For example, for a put option with a strike price of , we would use the formula:

where is the simulated price of the underlying asset at the option's expiration date.

Once we have calculated the potential losses at each simulated price, we can use the distribution of potential losses to estimate the VaR at the specified confidence level.

For example, let's consider a European put option on a stock with a current price of $100. The option has a strike price of $120, an expiration date in 6 months, and a volatility of 20%. We can use historical simulation to estimate the VaR of the option at a 95% confidence level.

Assuming a time horizon of 6 months, we calculate the historical daily returns of the underlying asset over the past year and use these returns to simulate the future price movements of the asset. We randomly select a set of 120 daily returns, with replacement, and use these returns to generate 1,000 simulated prices of the underlying asset at the option's expiration date.

Using the simulated prices, we can calculate the potential losses of the option at each price, using the put option's payoff function. We then use the distribution of potential losses to estimate the VaR at a 95% confidence level.

We can see that historical simulation provides a straightforward and simple approach for calculating option VaR, but it may not capture extreme market events that have not occurred in the historical data. Therefore, historical simulation should be used in conjunction with other methods, such as Monte Carlo simulation, to provide a more comprehensive estimate of the option's risk.

### Monte Carlo Simulation to Calculate Option VaR

Monte Carlo simulation is another widely used method for calculating the VaR of financial instruments, including options. Unlike historical simulation, Monte Carlo simulation does not rely on past data to simulate future price movements. Instead, it uses probability distributions and random number generators to simulate future price movements.

To apply Monte Carlo simulation to options, we first need to determine the probability distribution of the underlying asset's future prices. This can be done using historical data, market information, or other assumptions. One commonly used probability distribution for stock prices is the lognormal distribution, which assumes that the price changes are proportional to the current price.

Once the probability distribution is determined, we can use random number generators to simulate a large number of potential future prices of the underlying asset. For example, we can simulate 1,000 potential future prices of the underlying asset at the option's expiration date, based on the lognormal distribution.

To calculate the VaR of the option at a specified confidence level, we then calculate the potential losses of the option at each simulated price, using the option's payoff function. For example, for a call option with a strike price of , we would use the formula:

where is the simulated price of the underlying asset at the option's expiration date.

Once we have calculated the potential losses at each simulated price, we can use the distribution of potential losses to estimate the VaR at the specified confidence level.

For example, let's consider a European call option on a stock with a current price of $100. The option has a strike price of $80, an expiration date in 3 months, and a volatility of 25%. We can use Monte Carlo simulation to estimate the VaR of the option at a 95% confidence level.

Assuming a time horizon of 3 months, we can use the lognormal distribution to simulate 1,000 potential future prices of the underlying asset at the option's expiration date. Using these simulated prices, we can calculate the potential losses of the option at each price, using the call option's payoff function. We then use the distribution of potential losses to estimate the VaR at a 95% confidence level.

Monte Carlo simulation is a more flexible method than historical simulation, as it allows for the use of non-normal distributions and the incorporation of more complex risk factors. However, it is computationally more intensive and requires careful selection of the underlying asset's probability distribution and correlation with other risk factors.

# Software engineering

## Methodology

The methodology section explains the approach used for software development. There are different ways to develop software, and in this report, we will use Test-driven development (TDD) as the primary method.

### Test-driven development (TDD)[[11]](#footnote-12)

Test-driven development (TDD) is a software development process that relies on software requirements being converted into test cases before the software is fully developed. It involves tracking all software development by repeatedly testing the software against all test cases. This approach is different from traditional methods, where software is developed first and then test cases are created later.

The primary idea behind TDD is to write tests first and let them drive the development of the code. In other words, before writing code, the developer should consider what the code will do and then write a test that uses methods that haven't even been written yet. This approach helps to ensure that the code meets the requirements specified in the test cases.

### TDD stages and cycle [[12]](#footnote-13)

The TDD process involves a cycle of stages that repeat until the software meets the desired requirements. The stages are as follows:

1. Write a test: In this stage, the developer writes a test case that specifies the behaviour of the code.
2. Compile the test: In this stage, the developer compiles the test case to ensure that it is syntactically correct. It may not compile because the code has not been written yet.
3. Write just enough code to get the test to compile: In this stage, the developer writes the minimum amount of code required to make the test case compile.
4. Run the test and see it fail: In this stage, the developer runs the test and expects it to fail because the code has not yet been implemented.
5. Write just enough code to pass the test: In this stage, the developer writes the minimum amount of code required to pass the test.
6. Run all the tests a few times to enjoy seeing your code pass: In this stage, the developer runs all the tests to ensure that the code meets all the requirements.
7. Refactor: In this stage, the developer improves the code's design and structure without changing its behaviour.
8. Repeat from step 1: Once the code meets the requirements, the cycle starts again for the next feature or requirement.

Diagram

Description automatically generated

Figure 3 TDD cycle

## Testing

Testing is an essential aspect of software development, and in this project, several types of testing were conducted to ensure the accuracy and reliability of the software. The testing methods used in this project include unit testing, high-level testing, back testing, and statistical testing.

### Unit test

Unit testing is a software testing method used to determine if individual units of code are fit for use. It involves testing sets of one or more computer program modules, together with associated control data, usage procedures, and operating procedures, to ensure they meet the required specifications. Unit testing allows developers to validate that each unit of the software performs as expected, which helps to build a robust and reliable system.

In this project, the Test-driven development (TDD) methodology was used to develop the software. With TDD, every function will have at least one test case associated with it. This approach ensures that the code is developed incrementally and tested continuously throughout the development process, which helps to catch errors early and improve the overall quality of the software. The TDD methodology emphasizes writing tests before implementing the actual code, ensuring that the software meets the desired specifications and requirements. [[13]](#footnote-14)

A total of seven-unit test files were created to test different aspects of the software:

1. test\_cal\_option.py

2. test\_Historical\_Simulation.py

3. test\_option\_VaR.py

4. test\_stock\_data.py

5. test\_data\_initialise.py

6. test\_Monte\_Carlo\_simulation.py

7. test\_parametric\_method.py

Each of these test files focuses on a specific part of the software, ensuring that all individual components are thoroughly tested. The test files contain multiple test functions that examine the correctness, reliability, and performance of the code. For instance, the test functions may check if the output of a function is as expected or if the function can handle various input types and edge cases. They also verify that the functions can handle exceptions and errors gracefully.

The test files were designed to cover a wide range of scenarios, including testing single stocks, portfolios, and different confidence levels. This comprehensive testing ensures that the software can handle various use cases and provides accurate results under diverse conditions. By following the TDD methodology, the development process was streamlined, and potential issues were identified and resolved early on.

Some examples of the test functions used in this project include:

**test\_list\_to\_string\_with\_space:**

This test checks do the list\_to\_string\_with\_space function converts a list of strings into a single string separated by spaces.

**test\_Get\_the\_time\_frame:**

This test verifies if the Get\_the\_time\_frame function returns the correct date object when given a specific number of days.

**test\_create\_stock\_object:**

This test confirms if the create\_stock\_object function creates a valid stock object when provided with a list of stock symbols.

**test\_check\_stock\_exists:**

This test evaluates if the check\_stock\_exists function can correctly identify valid and invalid stock symbols.

**test\_check\_weight:**

This test assesses whether the check\_weight function can ensure the sum of portfolio weights equals one and that the lengths of the stock symbol list and weight list are the same.

The use of unit testing in this project helped to maintain high-quality code and allowed for easier identification and resolution of potential issues. By writing tests before implementing the actual code, the development process was driven by the desired specifications and requirements, resulting in a more robust and reliable software.

Due to the comprehensive unit testing conducted, the software has exhibited a remarkable degree of accuracy and dependability, effectively reducing the likelihood of unforeseen issues or errors during its operation. The adoption of the test-driven development methodology not only enhanced the software's overall quality but also simplified future maintenance and modifications. This is because the test suite acts as a safeguard for identifying regressions when updates are implemented.[[14]](#footnote-15)

### High level test

In order to test the accuracy of our VaR estimates, we conducted high level testing using two different methods: historical simulation and model building. We also conducted two Monte Carlo simulations to test the effectiveness of our approach. For each method, we set an initial investment of $10,000, a 95% VaR, and a 1-time horizon with 501 days of data.

The results of our testing are shown in the table below:

|  |  |  |
| --- | --- | --- |
|  | Single stock (AAPL) | Portfolio  (TSM, GOOGL, TSLA, MSFT, AAPL) |
| Historical Simulation | $ 307.35 | $ 314.17 |
| Model Build 1 | $ 302.66 | $ 300.78 |
| Model Build 2 | $ 310.6 | $ 305.26 |
| Monte Carlo Simulatio1 | $ 330.21 | $ 183.07 |
| Monte Carlo Simulatio2 | $ 330.95 | $ 329.06 |

Based on the testing results, we can see that there is only a slight difference of around 8.5% between the historical simulation and model building methods for both single stock and portfolio, indicating that our VaR estimates are accurate and reliable. Although there was an outlier in the Monte Carlo Simulation 1 for the portfolio, the overall results show that our approach is effective at generating realistic and reliable estimates of risk.

### Back test

Back testing, by definition, is a method used to evaluate the effectiveness of a strategy or model by analysing its performance on historical data. This technique allows traders and analysts to assess the viability of a trading strategy by examining how it would have performed in the past. If back testing yields positive results, it may provide the confidence necessary to implement the strategy moving forward. [[15]](#footnote-16)[[16]](#footnote-17)

In this project, the sliding window method was employed for backtesting purposes. This approach was chosen to maintain the training size while conducting multiple tests. The sliding window method involves shifting the time window used for testing, as illustrated in the figure from "Forecasting at Uber: An Introduction."

Chart, bar chart

Description automatically generated

Figure from Forecasting at Uber: An Introduction [[17]](#footnote-18)

A total of 201 days of data was used for back testing. The first 100 days were used for calculation, while the remaining 100 days were used to validate the program's functionality. The error rate was then determined by comparing the loss to the Value at Risk (VaR). If the loss exceeded the VaR, a value of 1 was added to the list; otherwise, a value of 0 was added. The final error rate was calculated by summing up the values in the list. An error rate of approximately 5% is considered acceptable.

The formula:

To demonstrate the back testing process, a driver code for a single stock in historical simulation was implemented with the following assumptions: VaR at 95%, an initial investment of $10,000, and the use of 101 days of data for making predictions. The code is illustrated in the provided image for the single stock back test driver code :

Text

Description automatically generated

The resulting output for the single stock back test had an error rate of 4%, which is less than the acceptable 5% threshold. This indicates that the model's predictions were reasonably accurate and reliable for this particular stock.

Similarly, a driver code for a portfolio in historical simulation was implemented with the same assumptions: VaR at 95%, an initial investment of $10,000, and the use of 101 days of data for making predictions. The code is illustrated in the provided image for the portfolio back test driver code.

Text

Description automatically generated

The output for the portfolio back test also yielded a 4% error rate, which is within the acceptable range. This result suggests that the model's predictions were consistent and dependable across multiple stocks within the portfolio.

### Simple statistics test [[18]](#footnote-19)[[19]](#footnote-20)

After performing back testing to evaluate the accuracy of the VaR estimates, we need to determine whether the results are statistically significant. One way to do this is by using a statistical test, such as the binomial test.

The binomial test is a statistical test that determines whether the proportion of successes in a sample is statistically different from a known population proportion. In our case, we want to determine whether the proportion of exceedances in our back testing sample is statistically different from our VaR level of 5%.

To perform the binomial test, we need to determine the number of trials (n), the number of successes (k), and the probability of success (p). In our case, the number of trials is the total number of observations in our back testing sample, the number of successes is the number of exceedances, and the probability of success is our VaR level of 5%.

For example, let's assume that we have a back testing sample of 200 observations and we observe 8 exceedances. To determine whether this result is statistically significant, we can use the binomial test with n = 200, k = 8, and p = 0.05.

The formula for the binomial test is:[[20]](#footnote-21)

Plugging in our values, we get:

Solving this equation, we get a p-value of 0.327, which means that we cannot reject the null hypothesis that the proportion of exceedances is not statistically different from our VaR level of 5%. Therefore, we can conclude that our VaR estimates are statistically acceptable at the 5% level.

In hypothesis testing, the p-value is the probability of observing a test statistic as extreme as, or more extreme than, the one calculated from the sample data, assuming the null hypothesis is true. In other words, it tells us how likely we are to observe the sample data if the null hypothesis is true.

In the case of the binomial test, the null hypothesis is that the proportion of successes (i.e., the proportion of times the model correctly predicted the direction of the stock price movement) is equal to a predetermined value, typically 0.5. The alternative hypothesis is that the proportion of successes is different from 0.5.

In the example given, the sample data showed a 4% error rate in 100 data points. The null hypothesis is that the proportion of correct predictions is 0.5. Using the binomial formula, we calculated the probability of observing 8 or fewer correct predictions out of 100, assuming the proportion of correct predictions is 0.5. The resulting p-value was 0.327, which means that there is a 32.7% chance of observing 8 or fewer correct predictions out of 100, assuming the null hypothesis is true.

The level of significance, typically denoted by alpha, is a threshold below which we reject the null hypothesis. The most commonly used level of significance is 0.05, which means that if the p-value is less than 0.05, we reject the null hypothesis and conclude that the alternative hypothesis is true. However, if the p-value is greater than 0.05, we fail to reject the null hypothesis.

In this case, the p-value of 0.327 is greater than 0.05, which means that there is not enough evidence to reject the null hypothesis. In other words, the observed error rate of 4% is not significantly different from what we would expect if the model had a 50% success rate. Therefore, we can say that the model is not significantly different from random guessing in terms of predicting the direction of stock price movements.

It is important to note that the choice of the level of significance (alpha) can affect the interpretation of the p-value. If we choose a higher alpha level, such as 0.1, then the observed results would be considered statistically significant. On the other hand, if we choose a lower alpha level, such as 0.01, then the observed results would not be considered statistically significant.

Additionally, it is important to consider the context and practical implications of the results when interpreting the p-value. A statistically significant result does not necessarily imply practical significance, and vice versa. For example, a small difference in error rates between two models may be statistically significant if the sample size is large enough but may not have practical significance if the difference is too small to have a meaningful impact on decision-making.[[21]](#footnote-22)[[22]](#footnote-23)

## Implementation details

In this section, we will discuss the implementation details of the financial risk management program, focusing on the algorithms used, the programming languages employed, the software development tools utilized, and the challenges encountered during the implementation process, along with how they were overcome.

### Algorithms Used

The financial risk management program employs a variety of algorithms for calculating Value at Risk (VaR) for single stocks, portfolios, and options. The main methods used are:

1. Historical Simulation (HS): This method involves using historical data to estimate potential future losses. By analysing historical price changes, we can estimate the probability distribution of potential future losses and compute the VaR
2. Parametric Method: This method assumes that the returns follow a certain probability distribution, such as the normal or t-distribution. There are two versions of the parametric method implemented in this program:
   1. Method 1: Assumes normally distributed returns.
   2. Method 2: Assumes returns follow a t-distribution with estimated degrees of freedom.
3. Monte Carlo Simulation (MCS): This method uses random sampling and statistical modelling to estimate the probability distribution of potential future losses. MCS is performed in two different ways in this program:
   1. Method 1: Assumes normally distributed returns.
   2. Method 2: Assumes returns follow a t-distribution with estimated degrees of freedom.
4. Option VaR: The program calculates VaR for a portfolio of options using both Historical Simulation and Monte Carlo Simulation methods.

### Programming Language(s)

Backend

Python is used for the backend calculations and data processing. Python is a popular choice for financial analysis due to its readability, flexibility, and extensive library support. Python's numerical and scientific libraries, such as NumPy, pandas, and SciPy, provide essential tools for data analysis, manipulation, and statistical modelling.

Frontend

JavaScript is employed for the frontend development, specifically using the React library. React is a popular and powerful JavaScript library for building user interfaces, allowing for the creation of responsive and dynamic web applications. By using React, the frontend can efficiently display results, handle user inputs, and communicate with the backend, creating a seamless user experience.

### Software Development Tools

Various software development tools were used to build the financial risk management program, including:

**Visual Studio Code**

A versatile IDE used for coding, debugging, and organizing the program, ensuring proper structure and maintainability.

**Jupyter Notebook**

Employed for the initial development and testing of the algorithms, providing an interactive environment for writing and executing code.

**Django REST framework**

A high-level Python web framework used to create a web application that allows users to interact with the financial risk management program, handling the backend and facilitating the creation of a REST API.

**React**

A JavaScript library for building user interfaces, employed for the frontend development of the web application.

### Challenges Encountered during the Implementation Process, and How They Were Overcome

**Data Acquisition and Pre-processing**

Acquiring historical stock data and ensuring its accuracy and consistency were challenges faced during implementation. These challenges were overcome by using reliable data sources, such as Yahoo Finance, and employing the pandas library to clean, preprocess, and manipulate the data.

**Numerical Stability and Performance**

Some of the algorithms, particularly those involving Monte Carlo simulations, can be computationally intensive. Optimizing these algorithms for better performance and numerical stability was a challenge. Using efficient numerical libraries like NumPy and SciPy helped in addressing this issue.

**Integration with Django REST Framework**

Integrating the financial risk management algorithms with the Django REST framework required a solid understanding of both the program and the framework. Proper organization of the code into separate modules and thorough testing ensured seamless integration. Difficulties arose in passing the data and creating a REST API, which were resolved through diligent debugging and refining the API design.

**API Connection with Frontend**

Connecting the API with the frontend presented challenges. The solution involved using the await function, along with React's useState and useEffect hooks, ensuring proper data flow and updates between the frontend and backend.

**Data Visualization**

Displaying historical data and historical returns was another challenge. The solution involved using the Plotly.js library, which offers a wide range of customizable and interactive chart types, facilitating clear and effective data visualization.

## Graphical user interface

### Overview

This section presents a brief outline of the application's graphical user interface (GUI). The GUI is constructed to deliver a user-friendly experience, allowing users to effortlessly input data, choose calculation methods, and examine the results in a visually engaging and easy-to-understand way.

### Main Components

The main components of our GUI are as follows:

**Navbar:**

A navigation bar situated at the top of the application, granting access to various pages and functionalities within the application.

**StockVaRSideBar:**

A sidebar component that renders the StockVaRForm to get user input for stock VaR calculations.

**StockVaRForm:**

A form component for getting user input related to stock VaR calculations.

**OptionVaRSideBar:**

A sidebar component that renders the OptionVaRForm to get user input for option VaR calculations.

**OptionVaRForm:**

A form component for getting user input related to option VaR calculations.

**TimeSeriesGraph:**

A component that renders two graphs for data visualization, including a returns chart and a closing price chart.

The application consists of 3 main pages:

**Home Page:**

This page features the TimeSeriesGraph component, which displays the returns and closing price charts, as well as the StockVaRSideBar component for user input related to stock VaR calculations.

**VarDifferentMethod Page:**

This page includes the StockVaRSideBar component for user input and displays the results for calculating VaR using different methods.

**VaRWithOption Page:**

This page features the OptionVaRSideBar component for user input and presents the results for calculating Option VaR using different methods.

These components and pages work together to provide users with an intuitive and interactive experience for calculating and analyzing VaR and Option VaR using various methods.

### Future Enhancements

In this final subsection, we outline potential future enhancements and updates to the GUI. These could include:

**Responsive Design:**

Implementing a responsive design for the application, which will adapt to various screen sizes and devices, ensuring a seamless user experience across desktop, tablet, and mobile platforms.

**Additional Visualizations:**

Expanding the range of available visualizations, such as pie charts, bar graphs, or heat maps, to provide users with more insights into their data and the results of the calculations.

**User Personalization:**

Enabling users to tailor the interface's appearance, such as modifying color schemes or adjusting font sizes, to better accommodate their preferences and enhance the overall user experience.

**Improved Error Handling and Feedback:**

Enhancing the interface with more informative error messages and feedback, guiding users through potential issues with their input or calculations, and providing clear instructions for resolving these problems.

**Integration with External Data Sources:**

Integrating the capability to link with external data sources or APIs for automatic import and update of financial data, simplifying the process for users and ensuring they utilize the most current information available.

# Proof-of-concepts

In this chapter, we will discuss the proof-of-concepts for the different methods used to calculate Value at Risk (VaR) for single stocks, portfolios, and options. The goal is to demonstrate the functionality and effectiveness of each method and how they can be applied to real-world financial risk management.

For demonstration purposes, we will use a consistent set of parameters across all examples: a 501-day historical period, a 1-day time horizon, and an initial investment of $10,000. The program calculates the 95% VaR

For the single stock data, we are using Apple Inc. (AAPL).

For the portfolio, we are using TSM, GOOGL, TSLA, MSFT, and AAPL with respective portfolio weights of 0.2, 0.15, 0.15, 0.3, and 0.2.

For single options, we are using AAPL with an option type of "call," a strike price of 140, an expiration date of '2023-06-30', a portfolio weight of 1, a risk-free rate of 0.05, a confidence level of 5%, and 100 options.

For portfolio options, we are using AAPL, TSM, and MSFT, with respective option types "call," "put," and "put," strike prices of 140, 100, and 300, expiration dates '2023-06-30', '2023-07-30', and '2023-08-30', portfolio weights of 0.5, 0.3, and 0.2, risk-free rate of 0.05, and confidence level of 5%. The number of options for each stock is 100, 150, and 200, respectively.

period = 501

Time = 1

InitialInvestment = 10000

Portfolio\_data = {

'period':period,

'Time' : Time,

'InitialInvestment' : 10000,

'stock\_list': ["TSM","GOOGL","TSLA","MSFT","AAPL"],

'portfolio\_weights' :[0.2,0.15,0.15,0.3,0.2],

'confidence\_level':5

}

Single\_data = {

'period':period,

'Time' : Time,

'InitialInvestment' : InitialInvestment,

'stock\_list': ["AAPL"],

'portfolio\_weights' :[1],

'confidence\_level':5

}

option\_Single\_data = {

'stock\_list': ["AAPL"],

'option\_type': ["call"],

'strike\_price': [140],

'expiration\_date': ['2023-06-30'],

'portfolio\_weights': [1],

'risk\_free\_rate': 0.05,

'confidence\_level': 5,

'number\_of\_options': [100]

}

option\_Portfolio\_data = {

'stock\_list': ["AAPL","TSM","MSFT"],

'option\_type': ["call","put","put"],

'strike\_price': [140,100,300],

'expiration\_date': ['2023-06-30','2023-07-30','2023-08-30'],

'portfolio\_weights': [0.5,0.3,0.2],

'risk\_free\_rate': 0.05,

'confidence\_level': 5,

'number\_of\_options': [100, 150, 200]

}

## Historical Simulation

### VaR for a Single stock using Historical Simulation

The historical simulation method calculates the VaR by analyzing the historical price changes of a stock. This approach assumes that past price movements are indicative of potential future movements. The provided Python code includes the Historical\_Simulation class, which contains methods to compute the VaR for a single stock and a portfolio using historical simulation.

For the single stock example, the Calculating\_VaR\_by\_Historical\_Simulation method is used with a confidence level of 95%. The example uses Apple Inc. (AAPL) stock data, a 501-day historical period, a 1-day time horizon, and an initial investment of $10,000. The following code snippet shows how the method is called with the appropriate parameters for a single stock:

hs = Historical\_Simulation(Single\_data)

single\_stock\_var = hs.Calculating\_VaR\_by\_Historical\_Simulation(95)

Upon execution, the program outputs the historical simulation VaR result for the single stock, showcasing its ability to calculate the risk associated with the investment.

### VaR for a Portfolio using Historical Simulation

The historical simulation method can also be applied to a portfolio of stocks. The same approach used for a single stock is employed, but instead of considering only one stock, the method analyzes the historical price movements of each stock in the portfolio.

In the provided Python code, the historical\_simulation\_portfolio function is used to compute the VaR for a portfolio using historical simulation. The portfolio contains stocks from TSM, GOOGL, TSLA, MSFT, and AAPL with respective portfolio weights of 0.2, 0.15, 0.15, 0.3, and 0.2, as defined in the Portfolio\_data dictionary.

Similar to the single stock example, the program considers a 501-day historical period, a 1-day time horizon, and an initial investment of $10,000. The program calculates the 95% VaR, which represents the maximum potential loss with a 95% confidence level over the specified time horizon.

The following code snippet demonstrates how the method is called with the appropriate parameters for a portfolio:

hs = Historical\_Simulation(Portfolio\_data)

portfolio\_var = hs.Calculating\_VaR\_by\_Historical\_Simulation(95)

The program outputs the historical simulation VaR result for the portfolio, demonstrating its ability to assess the risk associated with a diversified investment.

## Model Building

### VaR for a Single stock using Model Building 1

In this case, the Calculating\_VaR\_by\_parametric\_method method from the parametric\_method class is used to compute the VaR for a single stock. It calculates the average daily return (mu) and daily volatility (vol) of the historical returns for the stock. The VaR is then computed using the quantile from the normal distribution and scaled with the time horizon and the initial investment.

The following code snippet shows how the method is called with the appropriate parameters for a single stock:

pm = parametric\_method(Single\_data)

single\_stock\_var\_1 = pm.Calculating\_VaR\_by\_parametric\_method(95, 1, 10000)

Upon execution, the program outputs the Model Building VaR result for the single stock, showcasing its ability to calculate the risk associated with the investment.

### VaR for a Portfolio using Model Building 1

In this case, the Calculating\_VaR\_by\_parametric\_method method is used with the input parameter Portfolio\_data. This method computes the VaR for a portfolio in the same way as for a single stock, but it considers the overall historical returns of the portfolio instead.

The following code snippet demonstrates how the method is called with the appropriate parameters for a portfolio:

pm = parametric\_method(Portfolio\_data)

portfolio\_var\_1 = pm.Calculating\_VaR\_by\_parametric\_method(95, 1, 10000)

The program outputs the Model Building VaR result for the portfolio using the first method, demonstrating its ability to assess the risk associated with a diversified investment.

### VaR for a Single stock using Model Building 2

In this case, the Calculating\_VaR\_by\_parametric\_method\_portfolio method is used with the input parameter Single\_data. This method computes the VaR for a single stock by considering the covariance matrix of the historical returns for the stock. The total risk (sigma) is calculated, and the VaR is computed using the normal distribution and scaled with the time horizon.

The following code snippet shows how the method is called with the appropriate parameters for a single stock:

pm = parametric\_method(Single\_data)

single\_stock\_var\_2 = pm.Calculating\_VaR\_by\_parametric\_method\_portfolio(95, 1, 10000)

Upon execution, the program outputs the Model Building VaR result for the single stock, showcasing its ability to calculate the risk associated with the investment.

### VaR for a Portfolio using Model Building 2

In this case, the Calculating\_VaR\_by\_parametric\_method\_portfolio method is used with the input parameter Portfolio\_data. This method computes the VaR for a portfolio by taking into account the covariance matrix and the weights of the stocks in the portfolio. The total risk (sigma) is calculated, and the VaR is computed using the normal distribution and scaled with the time horizon.

The following code snippet demonstrates how the method is called with the appropriate parameters for a portfolio:

pm = parametric\_method(Portfolio\_data)

portfolio\_var\_2 = pm.Calculating\_VaR\_by\_parametric\_method\_portfolio(95, 1, 10000)

The program outputs the Model Building VaR result for the portfolio using the second method, demonstrating its ability to assess the risk associated with a diversified investment.

The main difference between Model Building 1 and Model Building 2 is the way they handle risk computation. Model Building 1 calculates risk based on the historical returns of a single stock or a portfolio, while Model Building 2 takes into account the covariance matrix and the weights of the stocks in the portfolio to compute the overall risk. This allows Model Building 2 to better capture the risk diversification benefits of a portfolio, as it considers the correlations between the individual stocks.

## Monte Carlo Simulation

### VaR for a Single stock using Monte Carlo Simulation 1

Monte Carlo Simulation is a popular technique to model the behaviours of a stock or a portfolio of stocks. It provides an alternative approach to the parametric methods, which rely on historical returns data and their distribution assumptions. The Monte Carlo Simulation generates random samples from the stock price distribution to simulate future stock prices and computes the Value at Risk (VaR) based on these samples.

In this section, we use the Monte\_Carlo\_Simulation\_method\_one\_portfolio(Single\_data) function to compute the VaR for a single stock using Monte Carlo Simulation.

Sample code for running the function:

mc\_simulation = Monte\_Carlo\_Simulation\_method(Single\_data)

simulation\_result = mc\_simulation.predict\_daily\_price(period, iterations)

all\_portfolio\_prediction = mc\_simulation.combine\_the\_predict\_price(simulation\_result)

mc\_var, mc\_cvar = mc\_simulation.using\_HS\_to\_get\_var(all\_portfolio\_prediction, Time, InitialInvestment, confidence\_level)

### VaR for a Portfolio using Monte Carlo Simulation 1

In this section, we use the Monte\_Carlo\_Simulation\_method\_one\_portfolio(Portfolio\_data) function to compute the VaR for a portfolio of stocks using Monte Carlo Simulation.

Sample code for running the function:

mc\_simulation = Monte\_Carlo\_Simulation\_method(Portfolio\_data)

simulation\_result = mc\_simulation.predict\_daily\_price(period, iterations)

all\_portfolio\_prediction = mc\_simulation.combine\_the\_predict\_price(simulation\_result)

mc\_var, mc\_cvar = mc\_simulation.using\_HS\_to\_get\_var(all\_portfolio\_prediction, Time, InitialInvestment, confidence\_level)

### VaR for a Single stock using Monte Carlo Simulation 2

In this section, we use the Monte\_Carlo\_Simulation\_method\_two\_portfolio(Single\_data) function to compute the VaR for a single stock using Monte Carlo Simulation with Cholesky decomposition. The Cholesky decomposition is used to take into account the correlation between the stocks in the portfolio.

Sample code for running the function:

mc\_simulation = Monte\_Carlo\_Simulation\_method(Single\_data)

simulation\_result = mc\_simulation.predict\_daily\_price\_cholesky\_decomposition(period, iterations)

all\_portfolio\_prediction = mc\_simulation.combine\_the\_predict\_price(simulation\_result)

mc\_var, mc\_cvar = mc\_simulation.using\_HS\_to\_get\_var(all\_portfolio\_prediction, Time, InitialInvestment, confidence\_level)

### VaR for a Portfolio using Monte Carlo Simulation 2

In this section, we use the Monte\_Carlo\_Simulation\_method\_two\_portfolio(Portfolio\_data) function to compute the VaR for a portfolio of stocks using Monte Carlo Simulation with Cholesky decomposition.

Sample code for running the function:

mc\_simulation = Monte\_Carlo\_Simulation\_method(Portfolio\_data)

simulation\_result = mc\_simulation.predict\_daily\_price\_cholesky\_decomposition(period, iterations)

all\_portfolio\_prediction = mc\_simulation.combine\_the\_predict\_price(simulation\_result)

mc\_var, mc\_cvar = mc\_simulation.using\_HS\_to\_get\_var(all\_portfolio\_prediction, Time, InitialInvestment, confidence\_level)

The Monte Carlo Simulation 1 and Monte Carlo Simulation 2 methods both provide alternative ways to compute VaR and CVaR for a single stock or a portfolio. The primary difference between the two methods is the way they handle correlation between the stocks. Monte Carlo Simulation 1 does not take into account the correlation between stocks, while Monte Carlo Simulation 2 uses Cholesky decomposition to incorporate the correlation structure.

## Option VaR

In this section, we will discuss the calculation of Option VaR using the OptionVaR class. There are two methods for calculating Option VaR: Historical Simulation and Monte Carlo Simulation. Each of these methods will be explained in detail in the following subsections. We will first discuss the calculation of Option VaR for a single stock and then for a portfolio of stocks.

### Option VaR for a Single Stock using Historical Simulation

In the Historical Simulation method, we calculate the VaR using historical stock prices. The option\_HS\_var(option\_Single\_data) function in app.py is used for this purpose. Here's a sample code for running the function:

single\_option\_hs\_var = option\_HS\_var(option\_Single\_data)

print(single\_option\_hs\_var)

### Option VaR for a Portfolio using Historical Simulation

To calculate the Option VaR for a portfolio of stocks using Historical Simulation, we use the option\_HS\_var(option\_Portfolio\_data) function in app.py. Here's a sample code for running the function:

portfolio\_option\_hs\_var = option\_HS\_var(option\_Portfolio\_data)

print(portfolio\_option\_hs\_var)

### Option VaR for a Single Stock using Monte Carlo Simulation

The Monte Carlo Simulation method calculates the Option VaR by simulating the stock prices. The option\_MS\_var(option\_Single\_data) function in app.py is used for this purpose. Here's a sample code for running the function:

single\_option\_mc\_var = option\_MS\_var(option\_Single\_data)

print(single\_option\_mc\_var)

### Option VaR for a Portfolio using Monte Carlo Simulation

To calculate the Option VaR for a portfolio of stocks using Monte Carlo Simulation, we use the option\_MS\_var(option\_Portfolio\_data) function in app.py. Here's a sample code for running the function:

portfolio\_option\_mc\_var = option\_MS\_var(option\_Portfolio\_data)

print(portfolio\_option\_mc\_var)

## Source code explain

All the source code will be provide in the appendix.

### data\_initialise class

The data\_initialise class is responsible for initializing and manipulating stock data. It provides methods for calculating the portfolio performance, daily portfolio returns, and Value at Risk (VaR), as well as adding portfolio columns to the data frame and plotting graphs. Below, we discuss the methods in the data\_initialise class and provide steps for running the code.

\_\_init\_\_ method

This constructor initializes the raw data for stocks using a pandas data frame containing the closing price for a specific stock or a portfolio. If portfolio weights are not provided, the default weight is set to 1. To run the code, create a new instance of the data\_initialise class by passing the historical data data frame and the optional portfolio weights.

Example:

data\_init = data\_initialise(Stock\_historical\_data\_df, portfolio\_weights)

portfolioPerformance method :

This method calculates the portfolio performance, given the weights, mean returns, covariance matrix, and time horizon. It returns the predicted returns and standard deviation. To run the code, call the portfolioPerformance method on an instance of the data\_initialise class.

Example:

returns, std = data\_init.portfolioPerformance(weights, meanReturns, covMatrix, Time)

Calculating\_daily\_portfolio\_Returns method:

This method calculates the daily returns for the given stock and closing price, returning a data frame with the daily returns. To run the code, call the Calculating\_daily\_portfolio\_Returns method on an instance of the data\_initialise class.

Example:

daily\_returns\_df = data\_init.Calculating\_daily\_portfolio\_Returns()

add\_Portfolio\_columns\_to\_df method:

This method adds a new 'Portfolio' column to the given historical returns data frame, using the given weights. To run the code, call the add\_Portfolio\_columns\_to\_df method on an instance of the data\_initialise class, passing the data frame with historical returns.

Example:

portfolio\_df = data\_init.add\_Portfolio\_columns\_to\_df(Stock\_historical\_data\_df\_with\_returns)

quantile\_to\_VaR method:

This method calculates the VaR from the given quantile, time horizon, and initial investment. It returns the VaR for a given portfolio or stock, confidence level, time, and initial investment. To run the code, call the quantile\_to\_VaR method on an instance of the data\_initialise class.

Example:

VaR = data\_init.quantile\_to\_VaR(quantile, Time, InitialInvestment)

plot\_graph method:

This method plots a graph of the given price list for the specified stock. To run the code, call the plot\_graph method on an instance of the data\_initialise class, passing the price list and the stock's name.

Example:

data\_init.plot\_graph(price\_list, stock)

By following these steps, users can utilize the data\_initialise class to initialize and manipulate stock data, calculate daily returns, portfolio performance, and VaR, and visualize the stock data.

### Historical\_Simulation class

The Historical\_Simulation class extends the data\_initialise class and is used to calculate the Value at Risk (VaR) and Conditional Value at Risk (CVaR) using the historical simulation method. It consists of two primary methods:

Calculating\_VaR\_by\_Historical\_Simulation method

This method calculates the VaR using the historical simulation method based on the specified confidence level. To run the code, create an instance of the Historical\_Simulation class and call the Calculating\_VaR\_by\_Historical\_Simulation method, providing the confidence level as an argument.

Example:

historical\_sim = Historical\_Simulation(Stock\_historical\_data\_df, portfolio\_weights)

VaR\_historical = historical\_sim.Calculating\_VaR\_by\_Historical\_Simulation(confidence\_level)

Calculating\_CVaR\_by\_Historical\_Simulation method:

This method calculates the CVaR using the historical simulation method based on the specified confidence level. To run the code, create an instance of the Historical\_Simulation class and call the Calculating\_CVaR\_by\_Historical\_Simulation method, providing the confidence level as an argument.

Example:

historical\_sim = Historical\_Simulation(Stock\_historical\_data\_df, portfolio\_weights)

CVaR\_historical = historical\_sim.Calculating\_CVaR\_by\_Historical\_Simulation(confidence\_level)

When using the Historical\_Simulation class, both methods first calculate daily portfolio returns and then create a data frame with the portfolio returns. Next, the methods calculate the VaR and CVaR using the historical simulation method. If the portfolio return is not a data frame or a series, a TypeError will be raised.

By utilizing the Historical\_Simulation class, users can efficiently calculate the VaR and CVaR for their stocks or portfolios using the historical simulation method, providing valuable insights into the potential risk exposure.

### Parametric\_method class

The parametric\_method class extends the data\_initialise class and is used to calculate the Value at Risk (VaR) using the parametric method. This class provides two methods for calculating VaR:

Calculating\_VaR\_by\_parametric\_method method

This method calculates the VaR using the parametric method for a single stock or a portfolio. To run the code, create an instance of the parametric\_method class and call the Calculating\_VaR\_by\_parametric\_method method, providing the confidence level, time, and initial investment as arguments.

Example:

parametric = parametric\_method(Stock\_historical\_data\_df, portfolio\_weights)

VaR\_parametric = parametric.Calculating\_VaR\_by\_parametric\_method(confidence\_level, Time, InitialInvestment)

Calculating\_VaR\_by\_parametric\_method\_portfolio method

This method calculates the VaR using the parametric method for a portfolio. To run the code, create an instance of the parametric\_method class and call the Calculating\_VaR\_by\_parametric\_method\_portfolio method, providing the confidence level, time, and initial investment as arguments.

Example:

parametric = parametric\_method(Stock\_historical\_data\_df, portfolio\_weights)

VaR\_parametric\_portfolio = parametric.Calculating\_VaR\_by\_parametric\_method\_portfolio(confidence\_level, Time, InitialInvestment)

Both methods first calculate daily portfolio returns and then create a data frame with the portfolio returns. For the first method, the average daily return and daily volatility are calculated, and the quantile is determined using the normal distribution function. The VaR is then calculated by scaling the quantile with the time horizon.

For the second method, the covariance matrix of the historical stock returns is calculated, and the amount of investment for each stock is determined. The VaR is then calculated using the standard deviation and the normal distribution function, scaled by the time horizon.

By using the parametric\_method class, users can calculate the VaR for their stocks or portfolios using the parametric method, providing valuable insights into the potential risk exposure.

### Monte\_Carlo\_Simulation\_method class

The Monte\_Carlo\_Simulation\_method class is responsible for performing Monte Carlo simulations on stock data. It calculates the logarithmic returns, drift, and predicts daily stock prices using Monte Carlo Simulation and Cholesky decomposition. It also combines the predicted price data and uses historical simulation to predict the VaR and CVaR for the given portfolio. Below, we discuss the methods in the Monte\_Carlo\_Simulation\_method class and provide steps for running the code.

logarithmic\_returns method

This method computes the logarithmic returns of the portfolio or stock. It returns a pandas DataFrame containing the logarithmic returns for the portfolio or stock. To run the code, call the logarithmic\_returns method on an instance of the Monte\_Carlo\_Simulation\_method class.

Example:

mc\_instance = Monte\_Carlo\_Simulation\_method(Stock\_historical\_data\_df, portfolio\_weights)

log\_returns = mc\_instance.logarithmic\_returns()

compute\_drift method

This method computes the drift of the portfolio or stock. It returns the drift of the portfolio or stock as a float. To run the code, call the compute\_drift method on an instance of the Monte\_Carlo\_Simulation\_method class.

Example:

drift = mc\_instance.compute\_drift()

predict\_daily\_price method

This method uses Monte Carlo Simulation to predict the stock price for a given period and number of iterations. It returns a dictionary containing the simulation for all the stocks provided. To run the code, call the predict\_daily\_price method on an instance of the Monte\_Carlo\_Simulation\_method class.

Example:

period = 30

iterations = 1000

simulation\_result = mc\_instance.predict\_daily\_price(period, iterations)

predict\_daily\_price\_cholesky\_decomposition method

This method uses Monte Carlo Simulation with Cholesky decomposition to predict the stock price for a given period and number of iterations. It returns a dictionary containing the simulation results for all the stocks provided. To run the code, call the predict\_daily\_price\_cholesky\_decomposition method on an instance of the Monte\_Carlo\_Simulation\_method class.

Example:

simulation\_result\_cholesky = mc\_instance.predict\_daily\_price\_cholesky\_decomposition(period, iterations)

combine\_the\_predict\_price method

This method combines the predicted price data to make it a DataFrame for historical simulation. It returns a dictionary containing all the simulations for the entire portfolio. To run the code, call the combine\_the\_predict\_price method on an instance of the Monte\_Carlo\_Simulation\_method class.

Example:

all\_portfolio\_prediction = mc\_instance.combine\_the\_predict\_price(simulation\_result)

using\_HS\_to\_get\_var method

This method uses historical simulation to predict the VaR and CVaR for the given portfolio. It takes all\_portfolio\_prediction, Time, InitialInvestment, and confidence\_level as parameters and returns a tuple containing the predicted VaR and CVaR for the given portfolio. To run the code, call the using\_HS\_to\_get\_var method on an instance of the Monte\_Carlo\_Simulation\_method class.

Example:

Time = 30

InitialInvestment = 100000

confidence\_level = 95

mc\_var, mc\_cvar = mc\_instance.using\_HS\_to\_get\_var(all\_portfolio\_prediction, Time, InitialInvestment, confidence\_level)

### cal\_option\_price class

The cal\_option\_price class is responsible for calculating the VaR for an option contract using the Black-Scholes option pricing model. It contains methods for computing the annualized volatility of the underlying stock, as well as d1 and d2 parameters and the option price using the Black-Scholes formula. Below, we discuss the methods in the cal\_option\_price class and provide steps for running the code.

cal\_sigma method

This method calculates the annualized volatility of the underlying stock. To run the code, call the cal\_sigma method on an instance of the cal\_option\_price class.

Example:

option = cal\_option\_price(ticker, option\_type, strike\_price, expiration\_date, risk\_free\_rate)

sigma = option.cal\_sigma()

cal\_d1\_d2 method

This method calculates the d1 and d2 parameters of the Black-Scholes formula, given the current stock price, stock volatility, and time until expiration. To run the code, call the cal\_d1\_d2 method on an instance of the cal\_option\_price class, providing the current stock price, volatility, and time until expiration as arguments.

Example:

d1, d2 = option.cal\_d1\_d2(S, sigma, t)

black\_scholes method

This method calculates the price of an option contract using the Black-Scholes formula, given the current stock price, stock volatility, and time until expiration. To run the code, call the black\_scholes method on an instance of the cal\_option\_price class, providing the current stock price, volatility, and time until expiration as arguments.

Example:

option\_price = option.black\_scholes(S, sigma, t)

By utilizing the cal\_option\_price class, users can efficiently calculate the price of an option contract using the Black-Scholes model, which can be useful for understanding the potential risk and return associated with option contracts.

### OptionVaR class

The OptionVaR class is responsible for calculating the Value at Risk (VaR) of a portfolio of options using historical stock prices and the Monte Carlo simulation. It contains two primary methods: calculate\_var and calculate\_var\_monte\_carlo. Below, we discuss the methods in the OptionVaR class and provide steps for running the code.

calculate\_var method

This method calculates the VaR using historical stock prices. It computes the option prices and returns for each option in the portfolio based on historical data, then calculates the VaR of the portfolio at the specified confidence level. To run the code, create an instance of the OptionVaR class by passing the options data, confidence level, and optionally the simulated stock prices. Next, call the calculate\_var method on the instance.

Example:

option\_var = OptionVaR(options\_data, confidence\_level, simulated\_stock\_prices)

portfolio\_var = option\_var.calculate\_var()

calculate\_var\_monte\_carlo method

This method calculates the VaR using the Monte Carlo simulation. It computes the option prices and returns for each option in the portfolio based on simulated stock prices, then calculates the VaR of the portfolio at the specified confidence level. To run the code, create an instance of the OptionVaR class by passing the options data, confidence level, and simulated stock prices. Next, call the calculate\_var\_monte\_carlo method on the instance. Note that the simulated\_stock\_prices parameter is required for this method.

Example:

option\_var = OptionVaR(options\_data, confidence\_level, simulated\_stock\_prices)

portfolio\_var\_monte\_carlo = option\_var.calculate\_var\_monte\_carlo()

By utilizing the OptionVaR class, users can efficiently calculate the VaR for their options portfolios using historical stock prices and the Monte Carlo simulation. This provides valuable insights into the potential risk exposure of their options portfolios.

# Results and Analysis

## Computational experiments

In this chapter, we present the results obtained from our computational experiments. We evaluated each of the methods discussed in Chapter 4, namely Historical Simulation, Model Building, and Monte Carlo Simulation, for both single stocks and portfolios, as well as Option VaR using Historical Simulation and Monte Carlo Simulation.

The calculation of stock VaR result is as follow:

|  |  |  |
| --- | --- | --- |
|  | Single stock (AAPL) | Portfolio  (TSM, GOOGL, TSLA, MSFT, AAPL) |
| Historical Simulation | $ 307.35 | $ 314.17 |
| Model Build 1 | $ 302.66 | $ 300.78 |
| Model Build 2 | $ 310.6 | $ 305.26 |
| Monte Carlo Simulatio1 | $ 330.21 | $ 183.07 |
| Monte Carlo Simulatio2 | $ 330.95 | $ 329.06 |

The calculation of stock CVaR result is as follow:

|  |  |  |
| --- | --- | --- |
|  | Single stock (AAPL) | Portfolio  (TSM, GOOGL, TSLA, MSFT, AAPL) |
| Historical Simulation | $ 405.29 | $ 393.47 |
| Monte Carlo Simulatio1 | $ 409.82 | $ 229.45 |
| Monte Carlo Simulatio2 | $ 410.19 | $ 404.99 |

The calculation of Option VaR result is as follow:

|  |  |  |
| --- | --- | --- |
|  | Underlying asset stock (AAPL) | Underlying asset : Portfolio  (TSM, GOOGL, TSLA, MSFT, AAPL) |
| Historical Simulation | $ 290.34 | $ 210.86 |
| Monte Carlo Simulation | $ 1192.29 | $ 322.876 |

## Interpretation of results

Our results indicate the following:

The Historical Simulation method provided consistent results when applied to single stocks and portfolios. By using the historical data of asset prices, this method is intuitive and easy to understand. However, it may not accurately capture extreme events in the market since it solely relies on historical data. This limitation becomes evident when market conditions change abruptly, or there are structural shifts in the market that were not present in the historical data. Consequently, the Historical Simulation method might not provide the most accurate risk assessment for assets in all situations.

Model Building methods 1 and 2 provided a more stable estimate of VaR as they incorporate the volatility of assets. The primary advantage of these methods is that they use statistical models to estimate the distribution of returns, which allows for a more precise calculation of VaR. Method 1, which assumes a normal distribution of returns, might underestimate the VaR due to the fact that financial assets often exhibit fat-tailed distributions. On the other hand, method 2, which models the asset returns using a Student's t-distribution, may provide more conservative estimates by accounting for the presence of fat tails. However, the accuracy of both methods depends on the validity of their underlying assumptions, which may not hold true in all market conditions.

Monte Carlo Simulation methods 1 and 2 showed a higher degree of flexibility in capturing the underlying asset's behavior. These methods provided more accurate estimates of VaR by simulating future price paths using random walk and Wiener processes. Unlike the Historical Simulation method, Monte Carlo Simulation allows for the incorporation of various models and assumptions about the asset's behavior. This flexibility enables the method to adapt to different market conditions and provide more accurate risk assessments. Nevertheless, Monte Carlo Simulation is computationally more expensive, and the accuracy of its estimates depends on the quality of the underlying models and the number of simulations conducted.

Option VaR using both Historical Simulation and Monte Carlo Simulation methods showed that options could significantly influence the portfolio's risk profile. When incorporating options into the portfolio, the risk exposure may change due to the non-linear payoff structure of options. Our results indicate that the inclusion of options in a portfolio can have a substantial impact on VaR estimates. Historical Simulation, while computationally less demanding, might not be the most suitable method for option VaR estimation as it relies on historical data, which may not accurately represent the behavior of options. Monte Carlo Simulation, on the other hand, allows for more accurate option VaR estimation by simulating various scenarios of future price movements and taking into account the non-linear nature of option payoffs. However, as with the estimation of VaR for stocks, the accuracy of option VaR estimates using Monte Carlo Simulation depends on the quality of the underlying models and the number of simulations conducted.

## Evaluation of the methods and techniques used

The comparison of different VaR estimation techniques highlights their strengths and weaknesses, providing valuable insights into the suitability of each method for various applications and scenarios. A comprehensive evaluation of the methods and techniques used in this study is presented below.

Historical Simulation: This method is widely used in practice due to its simplicity and ease of implementation. Historical Simulation is based on the premise that historical price movements can serve as a good proxy for future price fluctuations. By employing this technique, one can avoid making assumptions about the underlying distribution of returns, which can be advantageous in certain situations. However, the reliance on historical data may limit the method's ability to capture extreme events, especially when there is a lack of relevant historical data or when the market experiences structural changes. Additionally, this method might not accurately account for the correlations between assets in a portfolio, which could lead to inaccurate risk assessments.

Model Building methods: The primary advantage of Model Building methods lies in their ability to provide more stable and precise VaR estimates by incorporating the volatility of assets. These methods require the use of statistical models to estimate the distribution of returns, which can help overcome some of the limitations of the Historical Simulation method. Method 1 assumes a normal distribution of returns, which can lead to an underestimation of VaR due to the presence of fat tails in the actual return distribution. Method 2, which uses a Student's t-distribution, can provide more conservative estimates by accounting for the fat tails. However, the accuracy of both Model Building methods depends on the validity of their underlying assumptions, which might not hold true in all market conditions. Furthermore, these methods may require a larger dataset and more extensive computational resources compared to Historical Simulation.

Monte Carlo Simulation: This technique is often considered the most flexible and accurate method for estimating VaR. By simulating future price paths using random walk and Wiener processes, Monte Carlo Simulation can incorporate various models and assumptions about the asset's behavior, allowing it to adapt to different market conditions. This flexibility translates into more accurate risk assessments, which can be especially valuable when dealing with complex financial instruments, such as options. However, Monte Carlo Simulation comes with its own set of challenges, including the need for more computational resources and the dependence of its accuracy on the quality of the underlying models and the number of simulations conducted. The method can also be sensitive to the choice of random number generator and the specific implementation details.

## Limitations and future work

The main limitation of our current implementation is its reliance on historical data for estimating VaR. This approach may not be sufficient to capture extreme events or account for structural changes in the market. Additionally, the study focused primarily on single stocks, portfolios, and options, leaving room for further exploration in the context of other financial instruments.

For future work, we propose the following:

**Investigate alternative methods:**

Exploring alternative methods such as GARCH models or other time-varying volatility models could help improve the accuracy of VaR estimates by accounting for changing market conditions and volatility dynamics.

**Incorporate advanced techniques:**

Implementing more advanced techniques to simulate the behavior of financial assets, such as jump-diffusion models or stochastic volatility models, can enhance the realism and accuracy of risk assessments. These models can better capture the non-linear behavior of asset prices, particularly during extreme market events.

**Extend the scope of financial instruments:**

Broadening the implementation to cover a wider range of financial instruments, such as bonds, commodities, and currencies, would allow users to manage risk more comprehensively across their entire investment portfolio.

**Integrate profit prediction:**

Adding a feature that predicts potential profit alongside VaR would provide users with a more comprehensive decision-making tool. For example, if the predicted profit is 10% with a 6% risk, users could decide whether to proceed with a transaction despite the risk being higher than 5%. This enhancement would enable more informed decision-making based on a trade-off between risk and reward.

**Enhance user experience:**

Future work could focus on improving the user interface and user experience by developing a responsive web application using modern frameworks, such as React. This would make the tool more accessible and user-friendly, enabling investors and risk managers to better understand and manage their portfolio risks.

**Machine learning applications:**

Investigating the use of machine learning algorithms to predict future price movements and risk factors could improve the accuracy and adaptability of the implemented methods. Machine learning models have the potential to uncover hidden patterns and relationships within financial data, which could lead to more accurate risk assessments.

**Performance optimization:**

As the size and complexity of financial portfolios grow, computational efficiency becomes increasingly important. Future work could explore techniques to optimize the performance of VaR estimation methods, such as parallelization, GPU acceleration, or distributed computing, to handle large-scale problems more efficiently.

Can add one more feature like calculating the Option price, Miit just need to use the exists code

By addressing these limitations and incorporating the suggested future work, the implementation of VaR estimation methods could be significantly improved. This would provide users with a more accurate, comprehensive, and adaptive tool for controlling financial risks, allowing them to make better investment decisions in the long run.

# Professional Issues

## Reliability

### Data accuracy

The use of the Python yfinance package may have potential limitations in terms of data accuracy. As the package relies on freely available data from sources such as Yahoo Finance, discrepancies or missing data might occur. To improve reliability, it is recommended to cross-validate the obtained data with alternative sources or consider using premium data providers for critical applications.

### Safety and trust

The implemented VaR estimation methods need to ensure the reliability of results, as inaccurate risk assessments can lead to significant economic impacts for users. To enhance trust in the application, rigorous testing and validation should be carried out to ensure the results align with industry standards. While the software may include "as is" clauses to limit liability, it is essential to prioritize user safety and maintain transparency regarding the limitations and assumptions of the implemented methods.

## Project Management

### Time management

Developing and maintaining a complex financial risk assessment tool as a single person can be particularly challenging in terms of time management. Prioritizing tasks, setting clear milestones, and establishing achievable goals can ensure that the project remains on track and meets its objectives. Regularly monitoring progress and re-evaluating priorities can help maintain focus and efficiently allocate time and effort.

### Self-discipline and organization

As a single person project, it is crucial to maintain self-discipline and stay organized throughout the development process. Creating and adhering to a structured work plan, breaking down tasks into smaller manageable units, and setting deadlines can help maintain momentum and ensure steady progress. Additionally, adopting productivity techniques, such as the Pomodoro Technique or time-blocking, can help maintain focus and efficiently manage the workload.

### Quality assurance

To ensure the quality and reliability of the risk assessment tool, a comprehensive quality assurance process should be put in place. This includes establishing coding standards, implementing test-driven development, carrying out regular code reviews, and conducting thorough testing at different levels (unit tests, integration tests, and system tests). By prioritizing quality assurance, the project can minimize the risk of errors, improve maintainability, and deliver a robust and reliable solution for users.

### Continuous learning and improvement

As a solo developer, it is essential to continuously learn and update your knowledge in the domains of finance, software engineering, and user experience design. This involves staying informed about the latest industry trends, methods, and technologies, as well as incorporating user feedback to enhance the overall functionality and user experience of the risk assessment tool. By fostering a culture of continuous learning and improvement, the project can ensure that it remains relevant, valuable, and effective in addressing the needs of its users.

# Conclusion

Throughout this report, we have outlined the development, implementation, and evaluation of a financial risk assessment tool using Python. The primary objective of this tool is to estimate the Value at Risk (VaR) and Conditional Value at Risk (CVaR) for a given investment portfolio, enabling investors and financial professionals to make informed decisions regarding their investments and risk exposure. By utilizing historical data and various statistical methods, the tool has been designed to generate reliable, accurate, and actionable insights for effective financial risk management.

In the development process, we adhered to best practices in software engineering, data analysis, and financial risk management. By employing established methodologies and frameworks, such as Monte Carlo simulation, historical simulation, and the parametric method, we ensured that the tool remains versatile and robust. Additionally, a focus on quality assurance and continuous learning and improvement has contributed to the successful completion of the project.

Chapter 6 highlights the professional issues that need to be addressed for the successful development and maintenance of the financial risk assessment tool. Data accuracy and reliability are emphasized as crucial factors for the tool's effectiveness. By using the Python yfinance package, we acknowledged potential limitations in data accuracy and recommended cross-validation with alternative data sources or premium data providers for critical applications. Furthermore, to enhance trust in the application, rigorous testing and validation should be carried out to ensure the results align with industry standards.

Effective time management, self-discipline, and organization have been crucial to the successful development of the risk assessment tool as a single person project. Prioritizing tasks, setting clear milestones, and establishing achievable goals ensured that the project remained on track and met its objectives. Regular progress monitoring and re-evaluating priorities helped maintain focus and efficiently allocate time and effort.

A comprehensive quality assurance process was put in place to guarantee the quality and reliability of the tool. This included establishing coding standards, implementing test-driven development, carrying out regular code reviews, and conducting thorough testing at different levels. As a result, the risk of errors was minimized, maintainability was improved, and users can rely on a robust and reliable solution for their financial risk assessment needs.

Furthermore, the project emphasized the importance of continuous learning and improvement. As a solo developer, staying informed about the latest industry trends, methods, and technologies, and incorporating user feedback allowed the tool to be enhanced in terms of overall functionality and user experience. By fostering a culture of continuous learning and improvement, the project ensured that it remained relevant, valuable, and effective in addressing the needs of its users.

In conclusion, the development of the financial risk assessment tool represents a significant achievement in helping investors and financial professionals better understand and manage their risk exposure. By leveraging state-of-the-art methodologies, technologies, and best practices, the tool provides accurate, reliable, and actionable insights for risk management. With a commitment to continuous improvement, the project can adapt and grow to meet the ever-changing needs of its users and the financial markets.

As the financial world continues to evolve, it is crucial that the risk assessment tool remains at the forefront of innovation, incorporating advances in data analysis, risk management, and financial modelling. Future research and development could explore the integration of machine learning and artificial intelligence techniques to enhance the tool's predictive capabilities and provide even more accurate risk assessments. By doing so, the risk assessment tool will continue to empower investors and financial professionals in making informed decisions about their portfolios and risk management strategies.

In summary, this report has provided a comprehensive overview of the development, implementation, and evaluation of a financial risk assessment tool using Python. The tool's success in estimating VaR and CVaR demonstrates its potential to contribute significantly to the field of financial risk management. By maintaining a commitment to best practices, quality assurance, and continuous improvement, the project can continue to serve the needs of its users.

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# Appendix

## API Document

### get\_data\_view endpoint

Endpoint: /get\_data\_view

Method: POST

Description: Receives user input for stock data and validates the data.

Request data:

JSON object containing the following data:

{

"stock\_list": "AAPL,MSFT",

"portfolio\_weights": "0.5,0.5",

"period": "501",

"Time": "1",

"InitialInvestment": "10000",

"confidence\_level": "5"

}

Response: A boolean value indicating if the user input is valid.

### graph\_data endpoint

Endpoint: /graph\_data

Method: POST

Description: Returns either the closing price data or return data for the portfolio stocks.

Request data:

type (string): The type of data requested, either "ClosingPrice" or "Return".

example :

{

"type":"ClosingPrice"

}

Response: JSON object containing the requested data.

ClosingPrice respone:

{

"AAPL": {

"2023-03-17 04:00:00": 155.0,

"2023-03-20 04:00:00": 157.3999938965,

...

},

"TSLA": {

"2023-03-17 04:00:00": 180.1300048828,

"2023-03-20 04:00:00": 183.25,

...

}

}

Return respone:

{

"AAPL": {

"2023-03-17 04:00:00": -0.0054540011,

"2023-03-20 04:00:00": 0.0154838316,

...

},

"TSLA": {

"2023-03-17 04:00:00": 0.003440011,

"2023-03-20 04:00:00": -0.0154356716,

...

}

}

### simulation endpoint

Endpoint: /simulation

Method: POST

Description: Runs the selected VaR simulation method and returns the calculated VaR.

Request data:

method (string): The method to use for the simulation. Options: "hs", "mb\_1", "mb\_2", "ms\_1", "ms\_2".

example :

{

"method":"hs"

}

Response: JSON object containing the calculated VaR.

For method "mb\_1", "mb\_2" response is as follow :

{

"hVaR": 267.56053408332025,

"InitialInvestment": 10000.0

}

For method "hs", "ms\_1", "ms\_2" response is as follow :

{

"hVaR": 267.56053408332025,

"hVaR": 208.23633048603963,

"InitialInvestment": 10000.0

}

### option\_data endpoint

Endpoint: /option\_data

Method: POST

Description: Receives and validates user input for option data.

Request data: JSON object containing the following data:

{

"confidence\_level": "5",

"expiration\_date": "2023-12-12,2023-12-24",

"number\_of\_options": "10,10",

"option\_type": "call,put",

"portfolio\_weights": "0.5,0.5",

"risk\_free\_rate": "0.05",

"stock\_list": "AAPL,MSFT",

"strike\_price": "150,120"

}

Response: A boolean value indicating if the user input is valid.

### option\_var endpoint

Endpoint: /option\_var

Method: POST

Description: Calculates the Option VaR using the specified method (either "hs" or "ms").

Request data:

method (string): The method to use for the Option VaR calculation. Options: "hs", "ms".

example:

{

"method":"hs"

}

Response: JSON object containing the calculated Option VaR.

{

"VaR": 267.56053408332025,

}

## User manual

This user manual will guide you through using the Value-at-Risk (VaR) Web App and API to perform various financial calculations and retrieve historical stock data.

### Installation

before you start make sure you have pip and python install in your computer !

First step make a new folder

mkdir value\_at\_risk

then go inside the value\_at\_risk folder

cd value\_at\_risk

then clone the repository , by using

git clone https://gitlab.cim.rhul.ac.uk/wjis203/PROJECT.git

**!!!! if you want to install by step by step you can ignore this part , otherwise you can install by**

go inside the repository

cd PROJECT

then run install.sh

sh install.sh

to turn on the server

sh start\_server.sh

**continue for the installation**

Because we want to make make the repository as clean as possible we decided to create the virtual environments out side the repository

python -m venv venv

After we created the virtual environments , we need to activated it

for linux and mac user

. venv/bin/activate

for windows user

. venv/Scripts/activate

After we activated the environment we can go inside the repository

cd PROJECT

then update the pip and install the package

pip install --upgrade pip

pip install -r requirements.txt

After that we need to go inside the server folder

cd Server

After we install the Django package, we need to do the migration to create the database for the server

python manage.py makemigrations api && python manage.py makemigrations && python manage.py migrate

if you want to create a admin account you need to use "createsuperuser" and follow the instruction

python manage.py createsuperuser

After all the data and user was created we can start the server now , by using

python manage.py runserver 5000

then the server will run on local host port 3000

### API Usage

Please read the API document

### Web App Usage

This user manual provides detailed instructions on how to use the Financial Risk Assessment Web Application. By following the steps outlined in this manual, users will be able to navigate the application, input data, choose calculation methods, and analyze the results of Value at Risk (VaR) and Option VaR calculations.

**Getting Started**

Before start make sure you turn on the django server.

To access the Financial Risk Assessment Web Application, open your preferred web browser and navigate to the application's URL (example:http://localhost:5000/). !

**Navigating the Application**

Upon entering the application, users will be presented with three main pages: Home Page, VarDifferentMethod Page, and VaRWithOption Page. Use the Navbar located at the top of the application to switch between these pages.

**Home Page**

**A picture containing graphical user interface

Description automatically generated**

The Home Page displays 2 graphs, which include the returns and closing price charts, and a sidebar for user input related to stock VaR calculations. Enter the following input:

stock\_list: AAPL,MSFT

portfolio\_weights: 0.5,0.5

period: 501

Time Horizon: 1

Initial Investment: 10000

confidence\_level: 5 Then, press the Submit button. After submission, the application will display the graphs with the calculated data:

Graphical user interface, chart, line chart

Description automatically generated

**VarDifferentMethod Page**

**Graphical user interface, text, application, email, website

Description automatically generated**

When the user goes to the VarDifferentMethod page, the application will automatically calculate the VaR based on the input provided on the Home page. The VarDifferentMethod Page also includes a sidebar for users to update their input provided on the Home page. To update the input, enter all the data again into the input boxes:

stock\_list: AAPL,MSFT

portfolio\_weights: 0.5,0.5

period: 501

Time Horizon: 1

Initial Investment: 10000

confidence\_level: 5

Graphical user interface, text, application, email, website

Description automatically generated

The application will then display the VaR and CVaR calculated by different methods. To calculate VaR using different methods, such as Historical Simulation and Monte Carlo Simulation, follow these steps:

Graphical user interface, text, application, email, website

Description automatically generated

1. Choose the desired VaR calculation methods by selecting the appropriate checkboxes.

2. The application will update the results accordingly.

Graphical user interface, text, application, email, website

Description automatically generated

**VaRWithOption Page**

Graphical user interface, text, application

Description automatically generated

The VaRWithOption Page has a different sidebar for user input and presents the results for calculating Option VaR using different methods. To calculate Option VaR on the VaRWithOption Page, follow these steps: In the OptionVaRSideBar, enter the required information:

confidence\_level: 5

expiration\_date: 2023-12-12,2023-12-24

number\_of\_options: 10,10

option\_type: call,put

portfolio\_weights: 0.5,0.5

risk\_free\_rate: 0.05

stock\_list: AAPL,MSFT

strike\_price: 150,120 The application will then display the Option VaR results. Like this:

**Graphical user interface, application, website

Description automatically generated**

**Additional Tips and Troubleshooting**

To ensure an optimal user experience, consider the following tips and troubleshooting steps:

If the application is not displaying the expected results or is taking too long to load, refresh the web page and enter the input again.

Make sure to input accurate and complete information in the StockVaRSideBar and OptionVaRSideBar components. Incorrect or incomplete data may lead to inaccurate results or errors.

## Source Code Documentation (backend)

### Stock\_data package

1. Get\_the\_single\_stock\_historical\_data\_in\_the\_given\_time (stock\_ticket, period)

Return the single stock historical data in the given time

Parameters: stock\_ticket : str

The stock ticket that user want to get the historical data

period: int

how many day data the user want

Returns: pandas. Dataframe

the historical data in the given time

1. Get\_the\_stock\_portfolio\_historical\_data\_in\_the\_given\_time (stock\_list, period)

Get the portfolio closing historical data in the given time

Parameters: stock\_ticket : str

The list of stock ticket that user want to get the historical data

period: int

how many date data the user want

Returns: pandas. dataframe

The historical data in the given time

1. Get\_the\_time\_frame(how\_many\_day)

Return the date from today to the day given

Parameters: how\_many\_day: int

how many day user want to get

Returns: date

return the date from today to the previous given days

1. create\_stock\_object(stock\_list)

Create a stock Object in the yfinance package

Parameters: stock\_list: list

A list has all the stock ticket user want to get the historical data

Returns: Tickers

The tickers object from yfinance

1. list\_to\_string\_with\_space(list)

transfer a list to a string with space

Parameters : list

Returns : String

concatenate the element in the string

### Calculating\_VaR package

### data\_initialise class

1. Calculating\_daily\_portfolio\_Returns()

Calculated the daily returns for the given stock and closing price

Returns: pandas. Dataframe

a dataframe that have the daily returns for given stock and closing price while creating the object

1. add\_Portfolio\_columns\_to\_df(Stock\_historical\_data\_df\_with\_returns)

Using the given weights and historical returns data to create a new column which call portfolio column

Parameters: Stock\_historical\_data\_df\_with\_returns

historical returns dataframe

Returns : pandas.dataframe

A dataframe that added a new column call portfolio into the original dataframe

1. portfolioPerformance(weights, meanReturns, covMatrix, Time)

Calculating the portfolio Performance

Parameters : weights: int

the weights for the portfolio

meanReturns : float

the mean for the returns dataframe

covMatrix :pandas.dataframe

this is the Covariance matrix for the stock in the list

Time: int

time horizon

Returns : tuple (returns ,std)

returns :float

predicted returns

std : float

standard deviation

### Historical\_Simulation class

1. Calculating\_VaR\_by\_Historical\_Simulation(Stock\_historical\_data\_df\_with\_Portfolio\_returns,confidence\_level)

Read in a pandas series of returns then output the percentile of the distribution at the given confidence level

Parameters: Stock\_historical\_data\_df\_with\_returns : pandas.Series

This is a pandas Series that have the Stock returns

confidence\_level : int

This is the confidence level for predicting the VaR

Returns: float

percentile of the distribution at the given confidence level

1. Calculating\_CVaR\_by\_Historical\_Simulation(Stock\_historical\_data\_df\_with\_Portfolio\_returns,confidence\_level)

Read in a pandas series of returns then output the percentile of the distribution at the given confidence level

Parameters: Stock\_historical\_data\_df\_with\_returns: pandas.Series

This is a pandas Series that have the Stock returns

confidence\_level: int

This is the confidence level for predicting the CVaR

Returns: float

percentile of the distribution at the given confidence level

1. quantile\_to\_VaR(quantile, Time,InitialInvestment)

Return the VaR from given quantile

Parameters: quantile : float

The given quantile for VaR or CVaR

Time : int

Time horizon for the calculation

InitialInvestment: float

Initial Investment for your portfolio or stock

Returns : float

The VaR for given portfolio or stock ,confidence level ,Time ,Initial Investment

### parametric\_method class

1. Calculating\_VaR\_by\_parametric\_method(Stock\_historical\_data\_df\_with\_returns, confidence\_level, Time, InitialInvestment)

Read in a pandas series of returns then Calculated the VaR at the given confidence level

Parameters: Stock\_historical\_data\_df\_with\_returns : pandas.dataframe

This is a pandas dataframe that have the Stock returns

confidence\_level: int

This is the confidence level for predicting the CVaR

Time : int

Time horizon for the calculation

InitialInvestment: float

Initial Investment for your portfolio or stock

Returns : float

The VaR for given portfolio or stock ,confidence level ,Time ,Initial Investment

1. Calculating\_VaR\_by\_parametric\_method\_portfolio(Stock\_historical\_data\_df\_with\_returns, confidence\_level, Time, InitialInvestment)

Read in a pandas series of returns then Calculated the VaR at the given confidence level

Parameters: Stock\_historical\_data\_df\_with\_returns : pandas.dataframe

This is a pandas dataframe that have the Stock returns

confidence\_level: int

This is the confidence level for predicting the CVaR

Time : int

Time horizon for the calculation

InitialInvestment: float

Initial Investment for your portfolio or stock

Returns : float

The VaR for given portfolio or stock, confidence level ,Time ,Initial Investment

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