



深蓝学院  
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## 第三章作业分享



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# 代码分享

①

$$\begin{bmatrix} 1 & 2 & 0 \\ 1 & 1 & 3 \\ 0 & 2 & 2 \end{bmatrix} \times \begin{bmatrix} 1 & 1 \\ 2 & 2 \end{bmatrix} = \begin{bmatrix} 14 & 20 \\ 15 & 24 \end{bmatrix}$$

②

$$\begin{bmatrix} 1 & 2 & 1 \\ 0 & 1 & 3 \\ 3 & 3 & 2 \end{bmatrix} \times \begin{bmatrix} 1 & 1 \\ 2 & 2 \end{bmatrix} = \begin{bmatrix} 12 & 24 \\ 17 & 26 \end{bmatrix}$$

1. 将图像转化为矩阵, 便于卷积加速

图像  $\begin{cases} W \times \text{宽} \\ H \times \text{高} \\ C \times \text{深} \end{cases}$

卷积核:  $ksize, ksize \Rightarrow$  特征图尺寸:  $feature-w = (W - ksize) // step + 1$  应感受野中元素个数、(卷积核元素个数)。

kernel

$$\begin{bmatrix} 1 & 1 \\ 1 & 0 \\ 2 & 0 \\ 2 & 1 \end{bmatrix}$$

① 共有  $C \times$  个矩阵块。

② 每个矩阵块  $row$  个数为: feature map 中元素个数

③ 每个矩阵块  $col$  个数为: feature map 中单个元素所对感受野中元素个数、(卷积核元素个数)。

# 代码分享

```
for deep in range(cx):
    temp=np.zeros((feature_w * feature_w, ksize * ksize))
    num=0;
    for i in range(feature_w):
        for j in range(feature_w):
            temp[num]=x[i*step:i*step+ksize,j*step:j*step+ksize,deep].reshape(-1)
            num=num+1
        image_col[:,deep*ksize * ksize:(deep+1)*ksize * ksize]=temp
return image_col
```

→ 单个像素点的尺寸

→ 水平移动总次数

→ 垂直移动总次数

→ 感受野中的元素重新排列

张

行排列

# 代码分享

## 训练过程

```
def train(batch=32, lr=0.01, epochs=10):
    # Mnist手写数字集
    dataset_path = "/datasets/mnist"
    train_data = torchvision.datasets.MNIST(root=dataset_path, train=True, download=False)
    train_data.data = train_data.data.numpy() # [60000, 28, 28]
    train_data.targets = train_data.targets.numpy() # [60000]
    train_data.data = train_data.data.reshape(60000, 28, 28, 1) / 255. # 输入向量处理
    train_data.targets = onehot(train_data.targets, 60000) # 标签one-hot处理 (60000, 10)

    # [28, 28] 卷积 6x[5, 5] -> 6x[24, 24]
    conv1 = Conv(kernel_shape=(5, 5, 1, 6))
    relu1 = Relu()
    # 6x[24, 24] -> 6x[12, 12]
    pool1 = Pool()
    # 6x[12, 12] 卷积 16x(6x[12, 12]) -> 16x[8, 8]
    conv2 = Conv(kernel_shape=(5, 5, 6, 16)) # 8x8x16
    relu2 = Relu()
    # 16x[8, 8] -> 16x[4, 4]
    pool2 = Pool()

    # 在这里可以尝试增加网络的深度, 再实例化conv3和pool3, 记得后面的前向传播过程
    # 和反向传播过程也要有对应的过程
    nn = Linear(256, 10)
    softmax = Softmax()
    for epoch in range(epochs):
        for i in range(0, 60000, batch):
            X = train_data.data[i:i + batch]
            Y = train_data.targets[i:i + batch]
            # 前向传播过程
            predict = conv1.forward(X)
            predict = relu1.forward(predict)
            predict = pool1.forward(predict)
            predict = conv2.forward(predict)
            predict = relu2.forward(predict)
            predict = pool2.forward(predict)
            predict = predict.reshape(batch, -1)
            predict = nn.forward(predict)
            # 误差计算
            loss, delta = softmax.cal_loss(predict, Y)
            # 反向传播过程
            delta = nn.backward(delta, lr)
            delta = delta.reshape(batch, 4, 4, 16)
            delta = pool2.backward(delta)
            delta = relu2.backward(delta)
            delta = conv2.backward(delta, lr)
            delta = pool1.backward(delta)
            delta = relu1.backward(delta)
            conv1.backward(delta, lr)
```





# 代码分享

前向:  $w^{(L)} = w^{(L)} a^{(L-1)} + b^{(L)}$

全连接层 (前向传播)

## 全连接层

class Linear(object):

```
def __init__(self, inChannel, outChannel):
    scale = np.sqrt(inChannel / 2)
    self.W = np.random.standard_normal((inChannel, outChannel)) / scale
    self.b = np.random.standard_normal(outChannel) / scale
    self.W_gradient = np.zeros((inChannel, outChannel))
    self.b_gradient = np.zeros(outChannel)
```

```
def forward(self, x):
```

"""前向过程"""

## 补全代码 ##  $(32 \times 256)$

self.x=x

return np.dot(self.x,self.W)+self.b

```
def backward(self, delta, learning_rate):
```

"""反向过程"""

## 梯度计算

batch\_size = self.x.shape[0]

## 补全代码 ##

self.W\_gradient = np.dot(self.x.transpose(), delta)

self.b\_gradient = np.sum(delta,axis=0)

delta\_backward = np.dot(delta,self.W.transpose())

## 反向传播

self.W -= learning\_rate/batch\_size\*self.W\_gradient

self.b -= learning\_rate/batch\_size\*self.b\_gradient

return delta\_backward

```
def train(batch=32, lr=0.01, epochs=10):
```

# Mnist手写数字集

dataset\_path = "../datasets/mnist"

train\_data = torchvision.datasets.MNIST(root=dataset\_path, train=True

train\_data.data = train\_data.data.numpy() # [60000,28,28]

train\_data.targets = train\_data.targets.numpy() # [60000]

train\_data.data = train\_data.data.reshape(60000, 28, 28, 1) / 255.

train\_data.targets = onehot(train\_data.targets, 60000) # 标签one-hot

# [28,28] 卷积 6x[5,5] -> 6x[24,24]

conv1 = Conv(kernel\_shape=(5, 5, 1, 6))

relu1 = Relu()

# 6x[24,24] -> 6x[12,12]

pool1 = Pool()

# 6x[12,12] 卷积 16x(6x[12,12]) -> 16x[8,8]

conv2 = Conv(kernel\_shape=(5, 5, 6, 16)) # 8x8x16

relu2 = Relu()

# 16x[8,8] -> 16x[4,4]

pool2 = Pool()

# 在这里可以尝试增加网络的深度, 再实例化conv3和pool3, 记得后面的前向传播过程

# 和反向传播过程也要有对应的过程

nn = Linear(256, 10)

softmax = Softmax()

for epoch in range(epochs):

for i in range(0, 60000, batch):

X = train\_data.data[i:i + batch]

Y = train\_data.targets[i:i + batch]

# 前向传播过程

predict = conv1.forward(X)

predict = relu1.forward(predict)

predict = pool1.forward(predict)

predict = conv2.forward(predict)

predict = relu2.forward(predict)

predict = pool2.forward(predict)

predict = predict.reshape(batch, -1)

predict = nn.forward(predict)

$(32 \times 10)$

$(32 \times 256)$



# 代码分享

$$\delta_i^{(L)} = -(y_i - a_i^{(L)}) f'(z_i^{(L)}) \quad \text{全连接层(反向传播)}$$

$$\delta_i^{(L)} = \left( \sum_{j=1}^{n_{i+1}} \delta_j^{(L+1)} \theta_{ji}^{(L+1)} \right) f'(z_i^{(L)})$$



```
## 全连接层
class Linear(object):

    def __init__(self, inChannel, outChannel):
        scale = np.sqrt(inChannel / 2)
        self.W = np.random.standard_normal((inChannel, outChannel)) / scale
        self.b = np.random.standard_normal(outChannel) / scale
        self.W_gradient = np.zeros((inChannel, outChannel))
        self.b_gradient = np.zeros(outChannel)

    def forward(self, x):
        """前向过程"""
        ## 补全代码 ##
        self.x=x
        return np.dot(self.x,self.W)+self.b

    def backward(self, delta, learning_rate):
        """反向过程"""
        ## 梯度计算 ##
        batch_size = self.x.shape[0]
        ## 补全代码 ##
        self.W_gradient = np.dot(self.x.transpose(), delta)
        self.b_gradient = np.sum(delta, axis=0)
        delta_backward = np.dot(delta, self.W.transpose())
        ## 反向传播 ##
        self.W -= learning_rate / batch_size * self.W_gradient
        self.b -= learning_rate / batch_size * self.b_gradient
        return delta_backward
```

256x10  
10  
batchsize: 32  
input: 256  
output: 10  
(32x10)  
32x256  
(256x32) (32x10)  
(32x10) (10x256)  
(32x256)

```
## Softmax 函数
class Softmax(object):
    def cal_loss(self, predict, label):
        batchsize, classes = predict.shape
        self.predict(predict)
        loss = 0
        delta = np.zeros(predict.shape)
        for i in range(batchsize):
            delta[i] = self.softmax[i] - label[i]
            loss -= np.sum(np.log(self.softmax[i]) * label[i])
        loss /= batchsize
        return loss, delta

    def predict(self, predict):
        batchsize, classes = predict.shape
        self.softmax = np.zeros(predict.shape)
        for i in range(batchsize):
            predict_tmp = predict[i] - np.max(predict[i])
            predict_tmp = np.exp(predict_tmp)
            self.softmax[i] = predict_tmp / np.sum(predict_tmp)
        return self.softmax
```

(32x10)  
(32x10)

$$\frac{\partial E}{\partial \theta_{ji}^{(L)}} = \delta_i^{(L)} \theta_{ji}^{(L-1)}$$

$$\frac{\partial E}{\partial b_i^{(L)}} = \delta_i^{(L)}$$

$$\Rightarrow \delta_i^{(L)} = \left( \sum_{j=1}^{n_{i+1}} \delta_j^{(L+1)} \theta_{ji}^{(L+1)} \right)$$

# 代码分享

## 卷积层(前向传播)

```
class Conv(object):
    def __init__(self, kernel_shape, step=1, pad=0):
        # [w, h, d]
        width, height, in_channel, out_channel = kernel_shape
        self.step = step
        self.pad = pad
        scale = np.sqrt(3 * in_channel * width * height / out_channel)
        self.k = np.random.standard_normal(kernel_shape) / scale
        self.b = np.random.standard_normal(out_channel) / scale
        self.k_gradient = np.zeros(kernel_shape)
        self.b_gradient = np.zeros(out_channel)

    def forward(self, x):
        self.x = x
        if self.pad != 0:
            self.x = np.pad(self.x, ((0, 0), (self.pad, self.pad), ...
                                (self.pad, self.pad), (0, 0)), 'constant')
            # x batch, width, height, channel
        bx, wx, hx, cx = self.x.shape
        # kernel的宽、高、通道数、个数
        wk, hk, ck, nk = self.k.shape
        feature_w = (wx - wk) // self.step + 1 # 返回的特征图尺寸
        feature = np.zeros((bx, feature_w, feature_w, nk))

        self.image_col = []
        # kernel也进行了reshape, 便于卷积加速, 只保留通道维度, 是个二维的矩阵
        kernel = self.k.reshape(-1, nk)
        ## 补全代码 ##
        for i in range(bx):
            image_col = img2col(self.x[i], wk, self.step)
            feature[i] = (np.dot(image_col, kernel) + self.b).reshape(feature_w, feature_w, nk)
            self.image_col.append(image_col)
        return feature
```

① 图像转化为矩阵

②  $Net^t = Conv(W^t, a^{t-1}) + W_b$

①  
②  
③

kernel重新排列



# 代码分享

## 池化层(前向传播)

```
## Max Pooling层
class Pool(object):
    def forward(self, x):
        b, w, h, c = x.shape
        feature_w = w // 2
        feature = np.zeros((b, feature_w, feature_w, c))
        self.feature_mask = np.zeros((b, w, h, c)) # 记录最大池化时最大值的位置信息用于反向传播
        for bi in range(b):
            for ci in range(c):
                for i in range(feature_w):
                    for j in range(feature_w):
                        ## 补全代码
                        feature[bi, i, j, ci] = np.max(x[bi, i*2:i*2+2, j*2:j*2+2, ci])
                        index = np.argmax(x[bi, i*2:i*2+2, j*2:j*2+2, ci])
                        self.feature_mask[bi, i*2 + index // 2, j*2 + index % 2, ci] = 1
        return feature

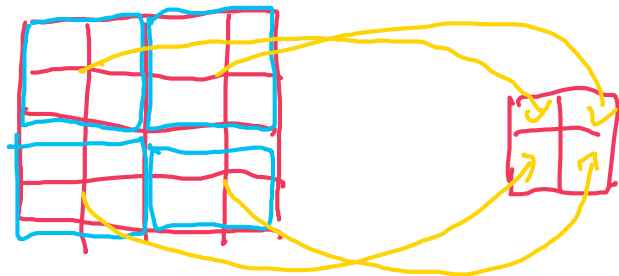
    def backward(self, delta):
        return np.repeat(np.repeat(delta, 2, axis=1), 2, axis=2) * self.feature_mask
```

```
>>> a
array([[ -1.28095222, -1.78081359],
       [ 0.6110716 ,  0.33153531]])
>>> np.argmax(a)
```

→ 构建 feature map

→ 记录最大值的位置

→ 将最大值位置处置为1





# 代码分享.

## 卷积层(反向传播)

```
def backward(self, delta, learning_rate):
    bx, wx, hx, cx = self.x.shape # batch, 14, 14, inchannel 32, 12, 12, 6
    wk, hk, ck, nk = self.k.shape # 5, 5, inChannel, outChannel 5, 5, 6, 16
    bd, wd, hd, cd = delta.shape # batch, 10, 10, outChannel 32, 8, 8, 16
    # 计算self.k gradient, self.b_gradient
    # 参数更新过程
    ## 补全代码 ##
    delta_col = delta.reshape(bd, -1, cd)
    for i in range(bx):
        self.k_gradient += np.dot(self.image_col[i].transpose(), ...
                                delta_col[i]).reshape(self.k.shape)
    self.k_gradient /= bx
    self.b_gradient += np.sum(delta_col, axis=(0, 1))
    self.b_gradient /= bx

    # 计算delta backward
    # 误差的反向传递
    delta_backward = np.zeros(self.x.shape)
    # numpy矩阵 (对应kernel) 旋转180度
    ## 补全代码 ##
    k_180 = self.k
    k_180 = k_180[::-1, ::-1]
    k_180_col = k_180.reshape(-1, ck)
    if hd - hk + 1 != hx:
        pad = (hx - hd + hk - 1) // 2
        pad_delta = np.pad(delta, ((0, 0), ...
                                (pad, pad), (pad, pad), (0, 0)), 'constant')
    else:
        pad_delta = delta

    for i in range(bx):
        pad_delta_col = img2col(pad_delta[i], wk, self.step)
        delta_backward[i] = np.dot(pad_delta_col, k_180_col).reshape(wx, hx, ck)

    # 反向传播
    self.k -= self.k_gradient * learning_rate
    self.b -= self.b_gradient * learning_rate

    return delta_backward
```

以 COV2 为例:

conv2(5, 5, 6, 16)

k\_shape: 5x6

inchannel: 6

outchannel: 16

step=1 Depth=6 Filter=16

$$\begin{cases} \frac{\partial E_d}{\partial w_{ij}} = \sum_k w_k \cdot h_k \cdot \delta^L \cdot a^{L-1} \\ \frac{\partial E_d}{\partial w_{ij}} = \sum_i \sum_j \delta_{w_{ij}}^L \end{cases}$$

$$\begin{bmatrix} w_{11} & w_{12} \\ w_{21} & w_{22} \end{bmatrix} \xrightarrow{\text{flip, pad}} \begin{bmatrix} w_{22} & w_{21} \\ w_{12} & w_{11} \end{bmatrix}$$

```
>>> a
array([[0, 1],
       [2, 3]])
>>> a[::-1, ::-1]
array([[3, 2],
       [1, 0]])
```

(旋转180°)

# 代码分享. 池化层 (反向传播)

```
## Max Pooling层
class Pool(object):
    def forward(self, x):
        b, w, h, c = x.shape
        feature_w = w // 2
        feature = np.zeros((b, feature_w, feature_w, c))
        self.feature_mask = np.zeros((b, w, h, c)) # 记录最大池化时最大值的位置信息用于反向传播
        for bi in range(b):
            for ci in range(c):
                for i in range(feature_w):
                    for j in range(feature_w):
                        ## 补全代码
                        feature[bi, i, j, ci] = np.max(x[bi, i*2:i*2+2, j*2:j*2+2, ci])
                        index = np.argmax(x[bi, i*2:i*2+2, j*2:j*2+2, ci])
                        self.feature_mask[bi, i*2 + index // 2, j*2 + index % 2, ci] = 1
        return feature

    def backward(self, delta):
        return np.repeat(np.repeat(delta, 2, axis=1), 2, axis=2) * self.feature_mask
```

以pool2为例:

$\text{delta}(32, 4, 4, 16)$

```
>>> a
array([[0, 1],
       [2, 3]])
>>> np.repeat(np.repeat(a, 2, axis=0), 2, axis=1)
array([[0, 0, 1, 1],
       [0, 0, 1, 1],
       [2, 2, 3, 3],
       [2, 2, 3, 3]])
```

after repeat

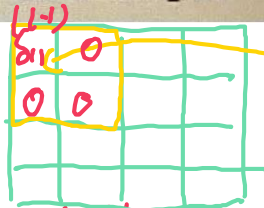
feature\_mask

① 无学习的参数

$\text{axis}=1$   $\text{axis}=2$

② 将误差项传递到上一层, 没有梯度计算

③ 对于 Max pooling, 下一层的误差项的值传递到上一层对应区中最大值对应的神经元, 其它神经元误差项为0.





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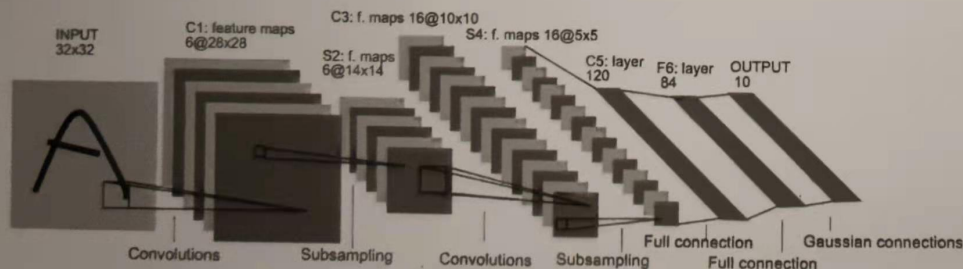
感谢各位聆听 !  
Thanks for Listening





# 作业讲解

1. 对比卷积神经网络与全连接神经网络，在图像分类任务中，原始图像大小的变化将会怎样影响模型可训练参数个数？
2. 卷积神经网络是通过什么方式来完成可训练参数的减少？
3. 如图是LeNet-5的示意图，试着写出每一层的参数个数。



	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
0	X				X	X	X		X	X	X	X	X	X	X	X
1	X	X			X		X	X		X	X	X	X	X	X	X
2	X	X	X				X	X	X		X		X	X	X	X
3		X	X	X			X	X	X	X		X	X	X	X	X
4			X	X	X			X	X	X	X		X	X	X	X
5				X	X	X			X	X	X	X		X	X	X

# 作业讲解

Input:  $32 \times 32$

$\Rightarrow$  kernel\_size:  $5 \times 5$

$C_1$ : feature\_map:  $6 \times (28 \times 28)$

$C_1$ 层参数:  $k: 6 \times (1 \times 25) = 150$      $b: 6 \times (1 \times 1) = 6$      $k + b = 156$

$S_2$ : pooling\_size:  $2 \times 2$

{ 若采样采用 max, mean 方法不需要参数训练

{ 若采用一个训练参数,则需要:  $k: 6 \times 1 = 6$      $b: 6 \times 1 = 6$      $k + b = 12$

# 作业讲解

$C_3$ : 根据右图的输入方式: 共需要:

$$\begin{aligned} & \overset{\rightarrow \text{相邻3个神经元}}{6 \times (3 \times 25 + 1)} + \overset{\rightarrow \text{相邻4个神经元}}{6 \times (4 \times 25 + 1)} + \overset{\rightarrow \text{间隔两个}}{3 \times (2 \times 25 + 1)} + \overset{\rightarrow \text{间隔一个}}{3 \times (2 \times 25 + 1)} \\ & + \overset{\rightarrow \text{所有神经元}}{1 \times (6 \times 25 + 1)} = 1516 \end{aligned}$$

$S_4$ 层: { 若采用 max, mean 则不需要参数

若采用 训练参数, 共需要  $16 \times (1 + 1) = 32$

$C_5$ 层: 共有 120 个特征图, 每个特征图与  $S_4$  层 16 个单元相连。  
由于  $S_4$  层的 16 个单元都为  $5 \times 5$ , 特征图也为  $5 \times 5$ 。

故  $C_5$  特征图大小为  $(5 - 5 + 1) = 1$



# 作业讲解

$C_5$ 层参数为:  $120 \times (16 \times 5 \times 5 + 1) = 48120$

$F_6$ 层: 与 $C_5$ 层全相连.

$$84 \times (120 \times (1 \times 1) + 1) = 10164$$

↓  
 $C_5$ 特征图