

1) linear probing

$$h(k, i) = (h(k) + i) \% m$$

$$hash(k) = (2k + 1) \% 8$$

Index	Element
0	10
1	13
2	77
3	70
4	54
5	41
6	52
7	25

$$hash(10) = 0$$

$$hash(41) = 5$$

$$hash(52) = 6$$

$$hash(25) = 5, h(25, 1) = 6, h(25, 2) = 7$$

$$hash(13) = 1$$

$$hash(77) = 1, h(77, 1) = 2$$

$$hash(54) = 4$$

$$hash(70) = 4, h(70, 1) = 5$$

2) Quadratic probing

$$h(k, i) = (h(k) + i^2) \% m$$

$$h(k) = (3k + 2) \% 8$$

Index	element
0	10
1	25
2	13
3	35
4	42
5	41
6	52
7	92

$$h(10) = 0$$

$$h(41) = 5$$

$$h(52) = 6$$

$$h(25) = 5, h(25, 1) = 6, h(25, 2) = 1$$

$$h(13) = 1, h(13, 1) = 2$$

$$h(42) = 0, h(42, 1) = 1, h(42, 2) = 4$$

$$h(35) = 3$$

$$h(92) = 6, h(92, 1) = 7$$

3) Double hashing

$$h(k, i) = (h_1(k) + i \cdot h_2(k)) \% m$$

$$h_1(k) = k \% 8$$

$$h_2 = ((5k + 3) \% 7) + 1$$

Index	Element
0	80
1	49
2	14
3	53
4	50
5	23
6	22
7	39

$$h_1(22) = 6$$

$$h_1(14) = 6, h(14, 1) = 2$$

$$h_1(39) = 7$$

$$h_1(23) = 7, h(23, 1) = 6, h(23, 2) = 5$$

$$h_1(80) = 0$$

$$h_1(53) = 5, h(53, 1) = 0, h(53, 2) = 3$$

$$h_1(49) = 1$$

$$h_1(50) = 2, h(50, 1) = 3, h(50, 2) = 4$$

4) cuckoo hashing

$$h_1(k) = (3k + 1) \% 7$$

$$h_2(k) = (\lfloor 5k/2 \rfloor + 3) \% 7$$

Index	Element
0	23
1	
2	47
3	87
4	15
5	20
6	

Index	Element
0	24
1	
2	
3	
4	9
5	12
6	

$$h_1(9) = 0$$

$$h_1(23) = 0, h_2(9) = 4$$

$$h_1(24) = 3$$

$$h_1(15) = 4$$

$$h_1(87) = 3, h_2(24) = 0$$

$$h_1(20) = 5$$

$$h_1(12) = 2$$

$$h_1(47) = 2, h_2(12) = 5$$