```
from google.colab import drive
drive.mount('/content/drive', force remount=True)
# 输入daseCV所在的路径
# 'daseCV' 文件夹包括 '.py', 'classifiers' 和'datasets'文件夹
# 例如 'CV/assignments/assignment1/daseCV/'
FOLDERNAME = '/content/drive/MyDrive/assignment1/daseCV'
assert FOLDERNAME is not None, "[!] Enter the foldername."
%cd drive/My\ Drive
%cp -r $FOLDERNAME ../../
%cd ../../
%cd daseCV/datasets/
!bash get datasets.sh
%cd ../../
    Go to this URL in a browser: https://accounts.google.com/o/oauth2/auth?client id:
    Enter your authorization code:
    4/1AX4XfWi2wPPT9CbPQtHGvsbR5x3M1te9M0JwAu1i02tDh4iEk-cpYohPTpM
    Mounted at /content/drive
    /content/drive/My Drive
    /content
    /content/daseCV/datasets
    --2021-10-17 02:32:14-- http://www.cs.toronto.edu/~kriz/cifar-10-python.tar.gz
    Resolving www.cs.toronto.edu (www.cs.toronto.edu)... 128.100.3.30
    Connecting to www.cs.toronto.edu (www.cs.toronto.edu) | 128.100.3.30 | :80... connec
    HTTP request sent, awaiting response... 200 OK
    Length: 170498071 (163M) [application/x-gzip]
    Saving to: 'cifar-10-python.tar.gz'
    in 2.9s
    2021-10-17 02:32:17 (56.7 MB/s) - 'cifar-10-python.tar.gz' saved [170498071/1704
    cifar-10-batches-py/
    cifar-10-batches-py/data batch 4
    cifar-10-batches-py/readme.html
    cifar-10-batches-py/test batch
    cifar-10-batches-py/data batch 3
    cifar-10-batches-py/batches.meta
    cifar-10-batches-py/data batch 2
    cifar-10-batches-py/data batch 5
    cifar-10-batches-py/data batch 1
    /content
```

# → Softmax 练习

补充并完成本练习。

本练习类似于SVM练习, 你要完成的事情包括:

- 为Softmax分类器实现完全矢量化的损失函数
- 实现其解析梯度(analytic gradient)的完全矢量化表达式
- 用数值梯度检查你的代码
- 使用验证集调整学习率和正则化强度
- 使用SGD优化损失函数
- 可视化最终学习的权重

```
import random
import numpy as np
from daseCV.data utils import load CIFAR10
import matplotlib.pyplot as plt
%matplotlib inline
plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
plt.rcParams['image.interpolation'] = 'nearest'
plt.rcParams['image.cmap'] = 'gray'
# for auto-reloading extenrnal modules
# see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipython
%load ext autoreload
%autoreload 2
def get CIFAR10 data(num training=49000, num validation=1000, num test=1000, num dev=5
    11 11 11
    Load the CIFAR-10 dataset from disk and perform preprocessing to prepare
    it for the linear classifier. These are the same steps as we used for the
    SVM, but condensed to a single function.
    # Load the raw CIFAR-10 data
    cifar10 dir = 'daseCV/datasets/cifar-10-batches-py'
    # Cleaning up variables to prevent loading data multiple times (which may cause me
    try:
       del X train, y train
       del X test, y test
       print('Clear previously loaded data.')
    except:
       pass
    X_train, y_train, X_test, y_test = load_CIFAR10(cifar10_dir)
    # subsample the data
    mask = list(range(num_training, num_training + num_validation))
    X val = X train[mask]
    y val = y train[mask]
    mask = list(range(num training))
```

```
X_train = X_train[mask]
   y_train = y_train[mask]
   mask = list(range(num test))
   X_{\text{test}} = X_{\text{test}}[mask]
   y_test = y_test[mask]
   mask = np.random.choice(num training, num dev, replace=False)
   X dev = X train[mask]
   y dev = y train[mask]
   # Preprocessing: reshape the image data into rows
    X_train = np.reshape(X_train, (X_train.shape[0], -1))
   X_val = np.reshape(X_val, (X_val.shape[0], -1))
    X test = np.reshape(X test, (X test.shape[0], -1))
    X_dev = np.reshape(X_dev, (X_dev.shape[0], -1))
    # Normalize the data: subtract the mean image
   mean image = np.mean(X train, axis = 0)
    X train -= mean image
    X_val -= mean_image
    X test -= mean image
    X dev -= mean_image
   # add bias dimension and transform into columns
   X_train = np.hstack([X_train, np.ones((X_train.shape[0], 1))])
   X val = np.hstack([X val, np.ones((X val.shape[0], 1))])
   X test = np.hstack([X test, np.ones((X test.shape[0], 1))])
    X dev = np.hstack([X dev, np.ones((X dev.shape[0], 1))])
    return X_train, y_train, X_val, y_val, X_test, y_test, X_dev, y_dev
# Invoke the above function to get our data.
X_train, y_train, X_val, y_val, X_test, y_test, X_dev, y_dev = get_CIFAR10_data()
print('Train data shape: ', X train.shape)
print('Train labels shape: ', y train.shape)
print('Validation data shape: ', X_val.shape)
print('Validation labels shape: ', y val.shape)
print('Test data shape: ', X test.shape)
print('Test labels shape: ', y_test.shape)
print('dev data shape: ', X dev.shape)
print('dev labels shape: ', y dev.shape)
    Train data shape: (49000, 3073)
    Train labels shape: (49000,)
    Validation data shape: (1000, 3073)
    Validation labels shape: (1000,)
    Test data shape: (1000, 3073)
    Test labels shape: (1000,)
    dev data shape: (500, 3073)
    dev labels shape: (500,)
```

# ▼ Softmax 分类器

请在daseCV/classifiers/softmax.py中完成本节的代码。

```
# 首先使用嵌套循环实现简单的softmax损失函数。
# 打开文件 daseCV/classifiers/softmax.py 并补充完成
# softmax loss naive 函数.
from daseCV.classifiers.softmax import softmax loss naive
import time
# 生成一个随机的softmax权重矩阵,并使用它来计算损失。
W = np.random.randn(3073, 10) * 0.0001
loss, grad = softmax loss naive(W, X dev, y dev, 0.0)
# As a rough sanity check, our loss should be something close to -\log(0.1).
print('loss: %f' % loss)
print('sanity check: %f' % (-np.log(0.1)))
    loss: 2.305535
    sanity check: 2.302585
问题 1
为什么我们期望损失接近-log(0.1)?简要说明。
答:因为有十个类,期望的损失为0.1
# 完成softmax loss naive, 并实现使用嵌套循环的梯度的版本(naive)。
loss, grad = softmax_loss_naive(W, X_dev, y_dev, 0.0)
# 就像SVM那样,请使用数值梯度检查作为调试工具。
# 数值梯度应接近分析梯度。
from daseCV.gradient check import grad check sparse
f = lambda w: softmax loss naive(w, X dev, y dev, 0.0)[0]
grad numerical = grad check sparse(f, W, grad, 10)
# 与SVM情况类似,使用正则化进行另一个梯度检查
loss, grad = softmax loss naive(W, X dev, y dev, 5e1)
f = lambda w: softmax loss naive(w, X dev, y dev, 5e1)[0]
grad numerical = grad check sparse(f, W, grad, 10)
    numerical: -0.092313 analytic: -0.092313, relative error: 7.848583e-07
    numerical: 1.186202 analytic: 1.186202, relative error: 2.666723e-09
    numerical: -1.058982 analytic: -1.058982, relative error: 4.874924e-09
    numerical: 1.913691 analytic: 1.913691, relative error: 1.297657e-08
    numerical: -1.460689 analytic: -1.460689, relative error: 8.856265e-09
    numerical: 3.023018 analytic: 3.023018, relative error: 2.030259e-08
    numerical: -0.421117 analytic: -0.421117, relative error: 2.074646e-07
```

```
numerical: 1.896211 analytic: 1.896211, relative error: 5.072040e-09
    numerical: -0.908376 analytic: -0.908376, relative error: 1.670384e-08
    numerical: 0.220471 analytic: 0.220470, relative error: 2.823862e-07
    numerical: -0.416161 analytic: -0.416162, relative error: 2.992578e-07
    numerical: 2.751280 analytic: 2.751280, relative error: 7.537741e-09
    numerical: -0.374107 analytic: -0.374107, relative error: 8.300424e-08
    numerical: 1.934267 analytic: 1.934267, relative error: 8.725618e-09
    numerical: -0.606299 analytic: -0.606299, relative error: 4.275726e-08
    numerical: 4.369015 analytic: 4.369015, relative error: 1.835455e-08
    numerical: 2.482823 analytic: 2.482823, relative error: 3.152160e-08
    numerical: -0.216057 analytic: -0.216057, relative error: 2.245926e-07
    numerical: 2.899489 analytic: 2.899489, relative error: 8.623744e-09
    numerical: 2.490563 analytic: 2.490563, relative error: 1.614791e-09
# 现在,我们有了softmax损失函数及其梯度的简单实现,
# 接下来要在 softmax loss vectorized 中完成一个向量化版本.
# 这两个版本应计算出相同的结果,但矢量化版本应更快。
tic = time.time()
loss naive, grad naive = softmax loss naive(W, X dev, y dev, 0.000005)
toc = time.time()
print('naive loss: %e computed in %fs' % (loss naive, toc - tic))
from daseCV.classifiers.softmax import softmax loss vectorized
tic = time.time()
loss_vectorized, grad_vectorized = softmax_loss_vectorized(W, X_dev, y_dev, 0.000005)
toc = time.time()
print('vectorized loss: %e computed in %fs' % (loss vectorized, toc - tic))
# 正如前面在SVM练习中所做的一样,我们使用Frobenius范数比较两个版本梯度。
grad difference = np.linalg.norm(grad naive - grad vectorized, ord='fro')
print('Loss difference: %f' % np.abs(loss naive - loss vectorized))
print('Gradient difference: %f' % grad_difference)
    naive loss: 2.305535e+00 computed in 0.221637s
    vectorized loss: 2.305535e+00 computed in 0.023503s
    Loss difference: 0.000000
    Gradient difference: 0.000000
# 使用验证集调整超参数(正则化强度和学习率)。您应该尝试不同的学习率和正则化强度范围;
# 如果您小心的话, 您应该能够在验证集上获得超过0.35的精度。
from daseCV.classifiers import Softmax
results = {}
best val = -1
best softmax = None
learning rates = [1e-7, 5e-7]
regularization strengths = [2.5e4, 5e4]
# 需要完成的事:
```

- # 对验证集设置学习率和正则化强度。
- # 这与之前SVM中做的类似;
- # 保存训练效果最好的softmax分类器到best softmax中。

```
# *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)****
for lr in learning rates:
    for reg in regularization strengths:
       softmax = Softmax()
       loss hist = softmax.train(X train, y train, learning rate=lr, reg=reg,
                     num iters=1500, verbose=True)
       y train pred = softmax.predict(X train)
       y_val_pred = softmax.predict(X_val)
       y train acc = np.mean(y train pred==y train)
       y_val_acc = np.mean(y_val_pred==y_val)
       results[(lr,reg)] = [y_train_acc, y_val_acc]
       if y val acc > best val:
           best_val = y_val_acc
           best softmax = softmax
# pass
# *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)*****
# Print out results.
for lr, reg in sorted(results):
   train accuracy, val_accuracy = results[(lr, reg)]
   print('lr %e reg %e train accuracy: %f val accuracy: %f' % (
               lr, reg, train accuracy, val accuracy))
print('best validation accuracy achieved during cross-validation: %f' % best val)
    iteration 0 / 1500: loss 387.887396
    iteration 100 / 1500: loss 234.265144
    iteration 200 / 1500: loss 142.444479
    iteration 300 / 1500: loss 86.723143
    iteration 400 / 1500: loss 53.350264
    iteration 500 / 1500: loss 33.032353
    iteration 600 / 1500: loss 20.762014
    iteration 700 / 1500: loss 13.331908
    iteration 800 / 1500: loss 8.807347
    iteration 900 / 1500: loss 6.143814
    iteration 1000 / 1500: loss 4.560600
    iteration 1100 / 1500: loss 3.519878
    iteration 1200 / 1500: loss 2.984078
    iteration 1300 / 1500: loss 2.527354
    iteration 1400 / 1500: loss 2.365570
    iteration 0 / 1500: loss 778.842106
    iteration 100 / 1500: loss 285.855298
    iteration 200 / 1500: loss 105.761081
    iteration 300 / 1500: loss 40.045934
    iteration 400 / 1500: loss 15.935950
    iteration 500 / 1500: loss 7.161054
    iteration 600 / 1500: loss 3.967596
    iteration 700 / 1500: loss 2.663295
    iteration 800 / 1500: loss 2.321994
    iteration 900 / 1500: loss 2.161244
    iteration 1000 / 1500: loss 2.106063
    iteration 1100 / 1500: loss 2.187975
```

```
iteration 1200 / 1500: loss 2.115550
    iteration 1300 / 1500: loss 2.102174
    iteration 1400 / 1500: loss 2.099187
    iteration 0 / 1500: loss 389.787534
    iteration 100 / 1500: loss 32.823125
    iteration 200 / 1500: loss 4.441475
    iteration 300 / 1500: loss 2.244465
    iteration 400 / 1500: loss 2.050659
    iteration 500 / 1500: loss 1.999261
    iteration 600 / 1500: loss 2.006276
    iteration 700 / 1500: loss 2.055902
    iteration 800 / 1500: loss 2.006492
    iteration 900 / 1500: loss 2.030486
    iteration 1000 / 1500: loss 2.006163
    iteration 1100 / 1500: loss 2.051063
    iteration 1200 / 1500: loss 2.007585
    iteration 1300 / 1500: loss 2.074801
    iteration 1400 / 1500: loss 2.040214
    iteration 0 / 1500: loss 777.098820
    iteration 100 / 1500: loss 6.925512
    iteration 200 / 1500: loss 2.182330
    iteration 300 / 1500: loss 2.025547
    iteration 400 / 1500: loss 2.029821
    iteration 500 / 1500: loss 2.090553
    iteration 600 / 1500: loss 2.083437
    iteration 700 / 1500: loss 2.018833
    iteration 800 / 1500: loss 2.081464
    iteration 900 / 1500: loss 2.041466
    iteration 1000 / 1500: loss 2.126551
    iteration 1100 / 1500: loss 2.101511
    iteration 1200 / 1500: loss 2.073027
    iteration 1300 / 1500: loss 2.127412
# 在测试集上评估
# 在测试集上评估最好的softmax
y test pred = best softmax.predict(X test)
```

```
test_accuracy = np.mean(y_test == y_test_pred)
print('softmax on raw pixels final test set accuracy: %f' % (test accuracy, ))
```

softmax on raw pixels final test set accuracy: 0.360000

### 问题 2 - 对或错

假设总训练损失定义为所有训练样本中每个数据点损失的总和。可能会有新的数据点添加到训练集 中、同时SVM损失保持不变、但是对于Softmax分类器的损失而言,情况并非如此。

#### 你的回答:正确

你的解释:对于softmax分类器,当增加新的数据点时,正确类别和错误类别输出分数差距越大,损 失函数越小。

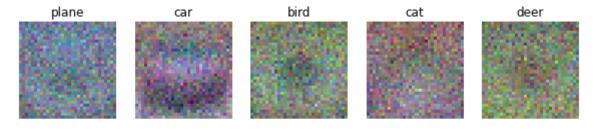
```
# 可视化每个类别的学习到的权重
w = best softmax.W[:-1,:] # strip out the bias
```

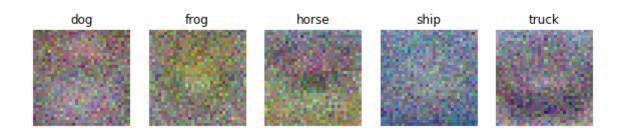
```
w = w.reshape(32, 32, 3, 10)
```

```
w_min, w_max = np.min(w), np.max(w)

classes = ['plane', 'car', 'bird', 'cat', 'deer', 'dog', 'frog', 'horse', 'ship', 'tru
for i in range(10):
    plt.subplot(2, 5, i + 1)

# Rescale the weights to be between 0 and 255
    wimg = 255.0 * (w[:, :, :, i].squeeze() - w_min) / (w_max - w_min)
    plt.imshow(wimg.astype('uint8'))
    plt.axis('off')
    plt.title(classes[i])
```





## ▼ 重要

### 防止作业被吞

这里是作业的结尾处, 请执行以下步骤:

- 1. 点击 File -> Save 或者用 control+s 组合键,确保你最新的的notebook的作业已经保存到谷歌云。
- 2. 执行以下代码确保 .py 文件保存回你的谷歌云。

```
import os

FOLDER_TO_SAVE = os.path.join('drive/My Drive/', FOLDERNAME)
FILES_TO_SAVE = ['daseCV/classifiers/softmax.py']
```

```
for files in FILES_TO_SAVE:
   with open(os.path.join(FOLDER_TO_SAVE, '/'.join(files.split('/')[1:])), 'w') as f:
    f.write(''.join(open(files).readlines()))
```

✓ 0秒 完成时间: 上午11:05

×