## **Answers to Probability Questions SET 4**

3. 
$$5/10 = 1/2$$

6. 
$$13/52 = 1/4$$

8. 
$$15/20 = 3/4$$

15. 
$$(1/6) \times (1/4) = 1/24$$

16. 
$$(4/52) \times (3/51) = 1/221$$

23. 
$$3/6 = 1/2$$

25. 
$$(12/52) \times (11/51) = 1/17$$

26. 
$$(5/12) \times (7/11) + (7/12) \times (5/11) = 70/132 = 35/66$$

29. 
$$(4/10) \times (4/10) = 4/25$$

31. 
$$(12/30) \times (11/29) = 132/870 = 22/145$$

32. 
$$(4/10) \times (4/10) = 16/100 = 4/25$$

33. 
$$(5/6)^3 = 125/216$$

34. Expected heads = 
$$5 \times 0.5 = 2.5$$

35. 
$$C(8,4) \times (0.5)^8 = 70 \times (1/256) \approx 0.273$$

$$36.\ 1 - (0.3)^3 = 1 - 0.027 = 0.973$$

$$37. (6+2)/36 = 8/36 = 2/9$$

38. 
$$P(\text{at least 2 passes}) = 0.896$$

$$40.(0.1)^2 = 0.01$$

42. 
$$C(8,4) \times (0.5)^8 \approx 0.273$$

43. Expected sixes = 
$$20 \times (1/6) \approx 3.33$$

44. 
$$C(10,3) \times (0.4)^3 \times (0.6)^7 \approx 0.2508$$

45. Sum of P(2 to 6) 
$$\approx 0.617$$

46. 
$$C(5,4) \times (0.75)^4 \times (0.25)^1 = 0.395$$

47. 
$$(0.4)^4 = 0.0256$$

51. 
$$1 - (0.02)^3 = 1 - 8e - 6 \approx 0.999992$$

**52.** Use binomial CDF, 
$$P(X > 5) \approx 0.02$$

53. Sum  $P(X \ge 4)$  using binomial formula with p=0.55

54. 
$$1 - (0.99)^30 \approx 0.26$$

- 56. Use Z-table, approx 15.87% below 60
- 57. Use normal approximation or Z-score for £350 threshold
- 58.  $C(20,3) \times (0.1)^3 \times (0.9)^17 \approx 0.057$
- 59. Use binomial distribution for  $P(X \ge 40)$  with p=0.6, n=60
- 60. 0.15
- 61.  $(3/5) \times (2/7) = 6/35$
- 62. Calculate complement population given intersection count
- $63. (5/8) \times (4/7) = 20/56 = 5/14$
- 64. Sampling variation, experiment vs theory
- 65. Use law of total probability
- 66. Add probabilities of outcomes with same color
- 67. Calculate using dice probability table
- 68. Solve using probability and proportion principles
- 69. 6 matching dice pairs (1,1), (2,2), ... (6,6)
- 70. Experimental estimates frequencies; theoretical uses model
- 71. Compute using algebra for unknown n
- 72. 1/36
- $73. \ 3/6 = 1/2$
- 74. Calculate experimental bias from frequency data
- 75. Add probabilities for red then blue and blue then red
- 76. Calculate total submit or total none probabilities
- 77. Apply inclusion-exclusion principle
- 78. Calculate with conditional probabilities
- 79. Intersection of independent events
- 80. Multiply along tree diagram branches

- 81. 12/30 = 2/5
- 82. 15/50 = 3/10
- 83. \$\frac{n(12-n)}{66} \$
- 84. Multiply branches probabilities
- 85. Apply multiplication rule for independents
- 86. Sum and subtract intersect probabilities
- 87. Use conditional probabilities formula
- 88. Multiply sequential probabilities
- 89. Add combined event probabilities
- 90. Use comparative analysis in dice events
- 91. Add P(sum=7) and P(sum=11)
- 92. 4 favorable pairs / 25 total
- 93. Combine probabilities of red and face cards minus overlap
- 94. Binomial coefficient × (prob powers)
- 95. Add probabilities for colors matching
- 96. Multiply independent weather probabilities
- 97. Multiply probabilities over event stages
- 98. Calculate samples with/without replacement
- 99. Sum products over tree paths
- 100. Multiply conditional probabilities