

answers to these 100

1. Basic Probability and Events

1. Probability of even number on dice = $3/6 = 1/2$
2. Probability exactly 1 head in two coin flips = $2/4 = 1/2$
3. Probability of blue ball = $5/10 = 1/2$
4. Probability spinner lands on 3 = $1/4$
5. Probability of two tails = $1/4$
6. Probability of heart card = $13/52 = 1/4$
7. Probability no rain = $1 - 0.3 = 0.7$
8. Probability not chocolate = $(8+7)/20 = 15/20 = 3/4$
9. Complement of spade = $1 - 13/52 = 39/52 = 3/4$
10. Probability face card or 10 = $(12 \text{ face cards} + 4 \text{ tens})/52 = 16/52 = 4/13$

2. Combined and Independent Events

11. Sum is 7: Outcomes = $6/36 = 1/6$
12. Both red without replacement: $(6/10)*(5/9)=30/90=1/3$
13. Two tails = $(1/2)*(1/2)=1/4$
14. Both dice show same: $6/36 = 1/6$
15. Dice 3 and heart card: $(1/6)*(1/4)=1/24$
16. Both kings without replacement: $(4/52)*(3/51)=1/221$
17. Independent events: $P(A \text{ and } B) = 0.3*0.5 = 0.15$
18. Sum 6 two dice: $5/36$
19. $P(\text{face } 6) = 0$ if faces 1-5 given probabilities
20. Both green without replacement: $(\text{number green}/\text{total})*(\text{number green}-1/\text{total}-1)$

3. Conditional Probability and Bayes' Theorem

- 21. Total walking = girls walking + boys walking. $P(\text{Boy}|\text{Walk}) = \text{boys walking} / \text{total walking}$
- 22. Probability two tails = $(1 - 0.4)^2 = 0.6^2 = 0.36$
- 23. $P(\text{First green} | \text{Second green}) = P(\text{green then green}) / [P(\text{green then green}) + P(\text{blue then green})]$
- 24. $P(A|B) = P(A \text{ and } B) / P(B)$
- 25. $P(\text{two heads}) = 0.16$. So $P(\text{head}) = \sqrt{0.16} = 0.4$; $P(\text{tail}) = 0.6$; $P(\text{two tails}) = 0.6^2 = 0.36$
- 26. Use binomial formula with $p=0.5$, calculate $P(4 \text{ correct}) = C(5,4)(0.5)^4(0.5)^1 = 5 \cdot 1/32 = 5/32$
- 27. Probability one red one blue: $P = 2 \cdot (n/12) \cdot (12-n)/11$
- 28. Use counts and conditional probability formulas to calculate given gender and sport choice
- 29. Use Venn diagram numbers to calculate conditional probabilities
- 30. $P(\text{wins at least one}) = 1 - P(\text{loses both}) = 1 - (0.4)^2 = 0.84$

4. Tree Diagrams and Sequential Events

- 31. Multiply number of choices: $232=12$
- 32. Expected winners = total * probability
- 33. Probability wins at least one = $1 - P(\text{loses both}) = 1 - (0.4)^2 = 0.84$
- 34. Use tree diagram branches and multiply probabilities on branches
- 35. Probability sector = given probability directly
- 36. Number of girls / total students = $12/30 = 2/5$
- 37. Count letters and divide: $\#A / \text{total letters}$
- 38. Sum to 7 outcomes = $6/36 = 1/6$
- 39. Find all sequence probabilities using product rule
- 40. Total marbles and color counts determine probabilities of each sequence

5. Experimental, Theoretical and Expected Probability

41. Experimental probability = frequency/total trials = $15/60=0.25$
42. Theoretical P(divisible by 3) on 12-sided die = $4/12=1/3$
43. Compare experimental outcomes with theoretical probability
44. Expected value = (probability success×win amount) + (probability fail×loss amount)
45. Expected number = total draws × probability of event
46. Multiply expected value per game by number of plays
47. Experimental vs theoretical probability deviation analysis
48. Relative frequency = ratio of times event occurs to total trials
49. Expected profit = $(p \times \text{win}) - (1-p) \times \text{cost}$
50. Calculate distributions for multiple trials using binomial or multinomial formulae

6. Binomial Probability and Distributions

51. $P(3 \text{ heads in } 5 \text{ tosses}) = C(5,3)(0.5)^3(0.5)^2=10/32=5/16$
52. $P(x \text{ successes}) = C(n,x) p^x (1-p)^{(n-x)}$
53. $P(X=4) = C(5,4) 0.6^4 0.4^1 = 5 \times 0.1296 \times 0.4=0.2592$
54. Binomial expansion gives coefficients for probability formula
55. Expected heads = $n \times p = 8 \times 0.5=4$
56. $P(\text{exactly } 2 \text{ tails})= C(5,2) (0.3)^2(0.7)^3=10 \times 0.09 \times 0.343=0.3087$
57. Sum $P(X \leq 3)$ by adding probabilities $P(0), P(1), P(2), P(3)$
58. Mean = np , Variance = $np(1-p)$
59. Increasing n makes binomial distribution approach normal curve
60. Use binomial table or formula to find $P(X \geq 1)=1-P(0)$

7. Venn Diagrams and Set Events

61. $P(A \cup B) = P(A) + P(B) - P(A \cap B)$
62. $P(A \cap B)$ from given data or formula

- 63. Use inclusion-exclusion principle
- 64. Complement $P(\text{not } A \text{ or } B) = 1 - P(A \cup B)$
- 65. Use counts in Venn diagram parts to calculate only one set probability
- 66. Mutually exclusive means $P(A \cap B) = 0$, independent means $P(A \cap B) = P(A) \times P(B)$
- 67. $P(\text{neither } A \text{ nor } B) = 1 - P(A \cup B)$
- 68. No, mutually exclusive and independent cannot both be true except trivial case
- 69. Apply Bayes' theorem: $P(A|B) = P(B|A)P(A) / P(B)$
- 70. Use three set Venn diagram and known probabilities to calculate unknowns

8. Word Problems and Real-Life Applications

- 71. Use sequential probability multiplication considering replacement or not
- 72. Use combined probabilities for multiple conditions
- 73. Probability first occurrence on n th trial in geometric distribution
- 74. Multiply probabilities of required wins in sequence
- 75. Multiply choices for independent meal selection events
- 76. Multiply success probability by number of trials for expectation
- 77. Expected value based on payoffs weighted by probabilities
- 78. Calculate probabilities of winning sequences in independent games
- 79. Multiply probabilities to find none defective in sequence
- 80. Use combined and conditional probabilities from partial knowledge

9. Practice with Probability Equations

- 81. Form equation from sum of probabilities = 1, solve for unknown n
- 82. Write probability expressions for combined events, solve algebraically
- 83. Use total outcomes to express probabilities with unknowns
- 84. Form quadratic from probability equations and solve

- 85. Create probabilities from tree diagram branches and solve equations
- 86. Express complement probabilities; solve for unknowns
- 87. Use known and unknown probabilities to find totals
- 88. Expected values expressed with unknowns, solve linear equations
- 89. Use data to calculate probabilities as equations and solve unknowns
- 90. Balance probability distributions by forming and solving equations

10. Mixed Practice and Exam-style Questions

- 91. Probability sum 7 or 11 with two dice = $P(7) + P(11) = \frac{6}{36} + \frac{2}{36} = \frac{8}{36} = \frac{2}{9}$
- 92. Sum 7 with two spinners 1-5 = $P(2,5) + P(3,4) + P(4,3) + P(5,2) = \frac{4}{25}$
- 93. Probability red card or face card = $P(\text{red}) + P(\text{face}) - P(\text{red face}) = \frac{26}{52} + \frac{12}{52} - \frac{6}{52} = \frac{32}{52} = \frac{8}{13}$
- 94. Probability 3 heads in 4 tosses = $C(4,3)(0.5)^4 = 4 \times 0.0625 = 0.25$
- 95. Probability both same color from known proportions = sum products of color probabilities
- 96. Compound probabilities: multiply respective event probabilities
- 97. Use multiplication rule for stages and sums for alternative paths
- 98. Difference due to independence replacement affects total outcomes
- 99. Analyze branches of tree diagram to find overall probabilities
- 100. $(0.5+0.5)^2 - 2(0.5)(0.5) = 1 - 0.5 = 0.5$