

# GCSE Maths Practice: Geometry and Measures

Here is a curated list of **100 practice questions** covering these GCSE topics: *Geometry fundamentals, Measurements, Trigonometry, Circles, Quadrilaterals, Polygons, and Vectors*. These questions include varied difficulty levels suitable for revision and exam preparation.

## Geometry Fundamentals & Measurements

1. Calculate the perimeter of a rectangle with length 12 cm and width 7 cm.
2. Find the area of a triangle with base 10 cm and height 6 cm.
3. What is the volume of a cuboid with dimensions 5 cm  $\times$  3 cm  $\times$  4 cm?
4. Find the missing angle in a straight line where the known angle is  $115^\circ$ .
5. Calculate the length of the hypotenuse in a right-angled triangle with legs 9 cm and 12 cm.
6. Determine the surface area of a cube with side length 8 cm.
7. Convert  $45^\circ$  to radians.
8. If a circle has a diameter of 14 cm, find its circumference.
9. A triangle has sides 7 cm, 24 cm, and 25 cm. Is it right-angled?
10. Find the area of a parallelogram with base 8 cm and height 5 cm.

## Trigonometry

11. Find the sine of a  $30^\circ$  angle.
12. Use Pythagoras' theorem to find the length of the missing side if the other two sides are 6 cm and 10 cm.
13. Calculate the angle in a right triangle if the opposite side is 5 cm and adjacent side is 12 cm.
14. Find the length of the side opposite a  $45^\circ$  angle in an isosceles right triangle with hypotenuse 10 cm.
15. What is  $\cos(60^\circ)$ ?
16. Calculate the height of a tree if a 20 m shadow forms a  $30^\circ$  angle with the ground.
17. Determine the area of a triangle using two sides and the included angle of  $60^\circ$ .

18. Using sine rule, find the unknown side given an angle of  $40^\circ$  opposite side 7 cm, and the adjacent angle  $70^\circ$ .
19. Apply cosine rule to find the third side of a triangle with sides 8 cm and 6 cm enclosing a  $60^\circ$  angle.
20. Calculate the missing angle in a triangle when two angles are  $50^\circ$  and  $60^\circ$ .

## Circles

21. Find the area of a circle with radius 5 cm.
22. Calculate the length of an arc with a central angle of  $90^\circ$  in a circle with radius 8 cm.
23. What is the area of a sector with angle  $45^\circ$  and radius 12 cm?
24. Find the perimeter of a semicircle with diameter 10 cm.
25. Calculate the volume of a cylinder with radius 4 cm and height 10 cm.
26. Find the length of the tangent from a point 13 cm from the center of the circle with radius 5 cm.
27. Calculate the angle between two tangents drawn from an external point to a circle.
28. Find the radius of a circle whose circumference is 31.4 cm (approximate  $\pi$  as 3.14).
29. Calculate the length of a chord that subtends a right angle at the center of a circle with radius 7 cm.
30. Find the equation of a circle with center at (3, -2) and radius 5.

## Quadrilaterals

31. Find the interior angles of a square.
32. Calculate the sum of interior angles of any quadrilateral.
33. Find the area of a rhombus with diagonals 12 cm and 10 cm.
34. Calculate the lengths of the sides of a rectangle with perimeter 36 cm if the length is twice the width.
35. Find the missing angle in a parallelogram if one angle is  $70^\circ$ .
36. Determine the coordinates of the midpoint of the diagonal of a rectangle with corners at (1,2) and (7,10).
37. Prove that the diagonals of a square are equal.
38. Find the area of a trapezium with parallel sides 10 cm and 6 cm and height 5 cm.
39. Calculate the perimeter of a kite with sides of length 7 cm and 10 cm.
40. Prove that the diagonals of a parallelogram bisect each other.

## Polygons

41. How many sides does a polygon have if the sum of interior angles is  $1260^\circ$ ?
42. Find the size of each interior angle in a regular hexagon.
43. Calculate the exterior angle of a regular octagon.
44. Determine the total number of diagonals in a decagon.
45. Calculate the sum of the exterior angles of any polygon.
46. Find the size of an exterior angle in a regular polygon with 15 sides.
47. Calculate the size of each interior angle in a regular pentagon.
48. If one exterior angle is  $40^\circ$ , how many sides does the polygon have?
49. Find the number of sides of a polygon where each interior angle is  $140^\circ$ .
50. Calculate the number of diagonals drawn from one vertex in a 12-sided polygon.

## Vectors

51. Given vectors  $\vec{a} = (3, -2)$  and  $\vec{b} = (-1, 4)$ , find  $\vec{a} + \vec{b}$ .
52. Calculate  $2\vec{a} - 3\vec{b}$  for vectors  $\vec{a} = (1, 5)$  and  $\vec{b} = (4, -2)$ .
53. Find the magnitude of vector  $(6, 8)$ .
54. Find the direction of vector  $(5, 5)$  measured anti-clockwise from the positive x-axis.
55. If vector  $\vec{a} = (2, 3)$ , find a unit vector in the same direction.
56. Find the scalar product of vectors  $\vec{a} = (3, 4)$  and  $\vec{b} = (2, -1)$ .
57. Determine if vectors  $(3, 5)$  and  $(6, 10)$  are parallel.
58. Find vector  $\vec{AB}$  given  $A(2, 3)$  and  $B(7, 9)$ .
59. Determine the midpoint between points  $A(1, 4)$  and  $B(5, 10)$ .
60. Find the resultant vector when a force of 5 N acts at  $30^\circ$  and 8 N acts at  $120^\circ$ .

## Mixed Problems

61. Find the volume of a cone with radius 3 cm and height 7 cm.
62. The radius of a circle is increasing at a rate of 0.1 cm/s. Find the rate at which the area is increasing when radius is 5 cm.
63. Find the distance between the points  $(3, 4)$  and  $(7, 1)$ .

64. Calculate the vector perpendicular to  $(3, 2)$ .
65. Find the length and angle of the vector  $(4, 4\sqrt{3})$ .
66. A triangle has sides 5 cm, 7 cm, and 10 cm. Determine if the triangle is obtuse.
67. Find the equation of a line perpendicular to the vector  $(2, -3)$ .
68. Calculate the volume of a sphere with diameter 10 cm.
69. Find the length of the diagonal of a rectangular prism  $3 \text{ cm} \times 4 \text{ cm} \times 12 \text{ cm}$ .
70. Calculate the height of a trapezium given bases 8 cm, 5 cm and area  $52.5 \text{ cm}^2$ .

### Challenge Problems

71. Given vectors  $a = (1, 2)$  and  $b = (3, -1)$ , find the angle between them.
72. Find the shortest distance between the point  $(3, 4)$  and the line  $y = 2x + 1$ .
73. Calculate the area of a triangle formed by points  $A(3, 2)$ ,  $B(7, 4)$ , and  $C(5, 7)$ .
74. Prove that the diagonals of a rhombus are perpendicular.
75. A polygon has 20 sides. Find the measure of each exterior and interior angle.
76. Find the center and radius of the circle given by the equation  $x^2 + y^2 - 4x + 6y - 12 = 0$ .
77. Use sine rule to solve a triangle where side  $a = 8 \text{ cm}$ , angle  $A = 45^\circ$ , and angle  $B = 60^\circ$ .
78. Calculate the area of the sector formed by a  $120^\circ$  angle in a circle radius 10 cm.
79. Find the equation of the line through points  $(1, 3)$  and  $(4, 7)$ .
80. Calculate the length of the segment joining  $(4, 1)$  to the midpoint of  $(8, 3)$  and  $(2, 7)$ .

### Applied Geometry

81. Find the height of an equilateral triangle with side length 10 cm.
82. Calculate the bearing from point A at  $(2, 3)$  to point B at  $(6, 7)$ .
83. Find the sum of the interior angles of a polygon with  $n$  sides if each exterior angle is  $30^\circ$ .
84. Calculate the side length of a square whose diagonal is  $10\sqrt{2} \text{ cm}$ .
85. Determine the vector from point  $C(3, 5)$  to point  $D(7, 1)$ .
86. Find the perimeter of a regular pentagon with side length 8 cm.
87. Calculate the volume of a prism with triangular base area of  $24 \text{ cm}^2$  and length 15 cm.
88. Find the equation of reflection line that maps point  $P(3, 1)$  to  $Q(3, -5)$ .

89. Calculate the angle between vectors  $(2, 0)$  and  $(1, \sqrt{3})$ .
90. Find the radius of a circle inscribed in a square of side 10 cm.

### Exam-style Questions

91. Prove that the diagonals of a rectangle are equal in length.
92. Find the number of sides of a polygon if each interior angle measures  $156^\circ$ .
93. Calculate the missing angle in the quadrilateral where three angles are  $85^\circ$ ,  $95^\circ$ , and  $75^\circ$ .
94. Find the magnitude of vector  $3\mathbf{i} + 4\mathbf{j}$ .
95. Calculate the area of a trapezium with parallel sides of 12 cm and 8 cm and height 6 cm.
96. Find the shortest distance from the point  $(5, 5)$  to the x-axis.
97. Determine the volume of a cylinder with height 12 cm and radius 3 cm.
98. Calculate the exterior angle of a regular polygon with 18 sides.
99. Find the sum of interior angles of a polygon formed by joining 7 triangles.
100. Given a vector  $\mathbf{v} = (4, -3)$ , find the vector  $-2\mathbf{v}$ .