

EE2211 Introduction to Machine Learning

Lecture 10

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Course Contents



- Introduction and Preliminaries (Xinchao)
 - Introduction
 - Data Engineering
 - Introduction to Linear Algebra, Probability and Statistics
- Fundamental Machine Learning Algorithms I (Yueming)
 - Systems of linear equations
 - Least squares, Linear regression
 - Ridge regression, Polynomial regression
- Fundamental Machine Learning Algorithms II (Yueming)
 - Over-fitting, bias/variance trade-off
 - Optimization, Gradient descent
 - Decision Trees, Random Forest
- Performance and More Algorithms (Xinchao)
 - Performance Issues

[Important] In the Final, no coding questions for Xinchao's part!

- K-means Clustering
- Despite you will see some in the tutorial, they won't be testsed.

Neural Networks

EE2211: Learning Outcome A Summary of Module Content



- I am able to understand the formulation of a machine learning task
 - Lecture 1 (feature extraction + classification)
 - Lecture 4 to Lecture 9 (regression and classification)
 - Lecture 11 and Lecture 12 (clustering and neural network)
- I am able to relate the fundamentals of linear algebra and probability to machine learning
 - Lecture 2 (recap of probability and linear algebra)
 - Lecture 4 to Lecture 8 (regression and classification)
 - Lecture 12 (neural network)
- I am able to prepare the data for supervised learning and unsupervised learning
 - Lecture 1 (feature extraction) [For supervised and unsupervised]
 - Lecture 2 (data wrangling) [For supervised and unsupervised]
 - Lecture 10 (Training/Validation/Test) [For supervised]
 - Programming Exercises in tutorials
- I am able to evaluate the performance of a machine learning algorithm
 - Lecture 5 to Lecture 9 (evaluate the difference between labels and predictions)
 - Lecture 10 (evaluation metrics)
- · I am able to implement regression and classification algorithms
 - Lecture 5 to Lecture 9

Outline



- Dataset Partition:
 - Training/Validation/Testing
- Cross Validation
- Evaluation Metrics
 - Evaluating the quality of a trained classifier

We will talk about many metrics: It is OK you can't memorize them all But intuition is important!



 We would like to train a Random Forest for face classification (i.e., to tell an image is a human face or not)



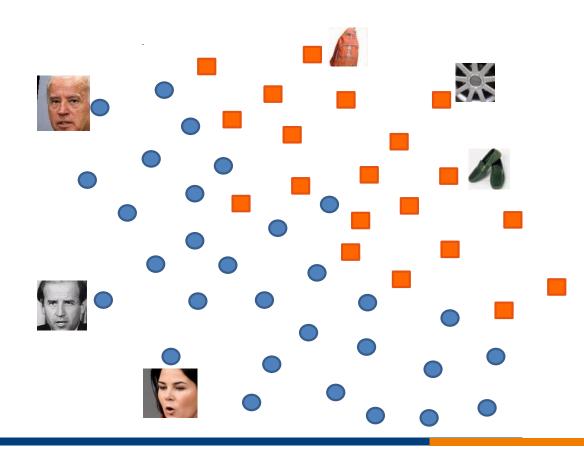
Faces



Non-faces



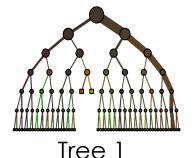
- We would like to train a Random Forest for face classification (i.e., to tell an image is a human face or not)
 - We will have <u>one dataset</u> to train the Random Forest

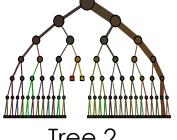


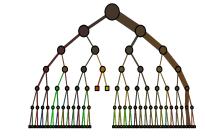


- We would like to train a Random Forest for face classification (i.e., to tell an image is a human face or not)
 - We will have one dataset to train the Random Forest
 - We will have tunable (<u>hyper)parameters</u> for the Random Forest. For example, *the number of trees* in the Random Forest
 - Shall we use 100 trees?
 - Shall we use 200 trees?

We need to decide on the parameter









- We would like to train a Random Forest for face classification (i.e., to tell an image is a human face or not)
 - We will have one dataset to train the Random Forest
 - We will have tunable (<u>hyper)parameters</u> for the Random Forest.
 For example, *the number of trees* in the Random Forest
 - Shall we use 100 trees?
 - Shall we use 200 trees?
 - ...

We need to decide on the parameter

Once we decide the number of trees, we will the Random Forest with the <u>selected parameter</u> on <u>unseen</u> test data.

Test Data



Yes!



No!

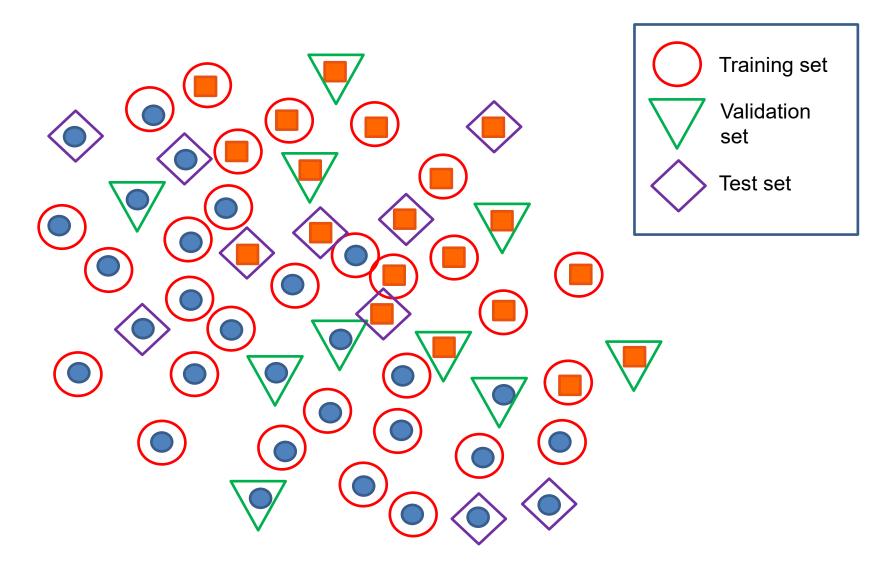


- In real-world application,
 - We don't have test data, since they are unseen
 - Imagine you develop a face detector app, you don't know whom you will test on
- In lab practice,
 - We divide the dataset into three parts

| Training set | Validation set | Test set | Hidden from Training! |
|----------------------------|--|--|--------------------------|
| For training the ML models | For validation: choosing the parameter or model | For testing the "re performance and generalization | |

– NEVER touch test data during training!!!







| Training set | Validation set | Test set |
|----------------------------|---|---|
| For training the ML models | For validation: choosing the parameter or model | For testing the "real" performance and generalization |

Example: Assume I want to build a Random Forest. I have a parameter to decide: shall I have

- 100 Trees?
- 200 Trees?

What we do next is to use the training set to train two classifiers,

1) C_1 : Random Forest with 100 trees, and 2) C_2 : Random Forest with 200 trees

They have the following accuracy:

- 1. C₁: Random Forest with 100 trees: validation accuracy 90%
- 2. C₂: Random Forest with 200 trees: validation accuracy 88%

Which one to choose for real application, i.e., testing?

The one with higher validation accuracy, i.e., Random Forest with 100 trees!

Python Demo: lec10.ipynb



Load Dataset Split it into Train:Val:Test = 100:25:25

| Training set | Validation set | Test set |
|----------------------------|--|---|
| For training the ML models | For validation: choosing the parameter or model | For testing the "real" performance and generalization |

[76]: ##--- load data from scikit ---## import numpy as np import pandas as pd print("pandas version: {}".format(pd.__version__)) print("scikit-learn version: {}".format(sklearn.__version__)) from sklearn.datasets import load iris ## Set Seed seed = 20## Load dataset iris dataset = load iris() X = np.array(iris_dataset['data']) y = np.array(iris_dataset['target']) ## one-hot encoding Y = list()for i in y: letter = [0, 0, 0]letter[i] = 1Y.append(letter) Y = np.array(Y)## Random shuffle data and train-test split test Idx = np.random.RandomState(seed=seed).permutation(Y.shape[0]) X_test = X[test_Idx[:25]] Y_test = Y[test_Idx[:25]] X = X[test Idx[25:]] $Y = Y[test_Idx[25:]]$

Problem Setup

- Dataset used: IRISdataset
 - Link: https://scikit-learn.org/stable/datasets/toy_dataset.html#iris-dataset
- Training/Validation/Test: 100/25/25
- Machine Learning Task and Model: Polynomial regression
- Parameters to select: Order 1 to 10

In the Final, no coding questions for Xinchao's part!



In practice, we do the k-fold cross validation

4-fold cross validation

Test

Step 1: take out *test set* from the dataset



In practice, we do the k-fold cross validation

4-fold cross validation

Test



Step 2: We partition the *remaining part of the dataset* (after taking out the test set), into *k* equal parts (equal in terms of number of samples).



In practice, we do the k-fold cross validation

4-fold cross validation

Test

| Fold 1 | Train | Train | Train | Validation |
|--------|------------|------------|------------|------------|
| Fold 2 | Train | Train | Validation | Train |
| Fold 3 | Train | Validation | Train | Train |
| Fold 4 | Validation | Train | Train | Train |

Step 3: We run *k folds* (i.e., k times) of experiments.

Within each fold, we use *one part* as *validation set*, and the *k-1 remaining parts* as *training set*. We use different validation sets for different folds.



In practice, we do the k-fold cross validation

4-fold cross validation

Classifiers Trained

| Fold 1 | Train | Train | Train | Validation | (|
|--------|------------|------------|------------|------------|---|
| Fold 2 | Train | Train | Validation | Train | (|
| Fold 3 | Train | Validation | Train | Train | (|
| Fold 4 | Validation | Train | Train | Train | (|

 $C_1^1 \ C_2^1$ $C_1^2 \ C_2^2$

 $C_1^3 \ C_2^3$

 $C_1^4 C_2^4$

1) C_1 : Random Forest with 100 trees

2) C_2 : Random Forest with 200 trees

Step 3.1: Within each fold, if we have n parameter/model candidates, we will train n models, and we check their validation performance.

Test



In practice, we do the k-fold cross validation

4-fold cross validation

Classifiers Trained

| Fold 1 | Train | Train | Train | Validation | C_1^1 C_2^1 |
|--------|------------|------------|------------|------------|-----------------|
| Fold 2 | Train | Train | Validation | Train | C_1^2 C_2^2 |
| Fold 3 | Train | Validation | Train | Train | $C_1^3 \ C_2^3$ |
| Fold 4 | Validation | Train | Train | Train | $C_1^4 \ C_2^4$ |

Example: which one to select for test?

Test

| | Fold 1 Accuracy on Validation Set 1 | Fold 2 Accuracy on Validation Set 2 | Fold 3 Accuracy on Validation Set 3 | Fold 4 Accuracy on Validation Set 4 | Average Accuracy on All Validation Sets |
|---|-------------------------------------|---|---|-------------------------------------|---|
| Classifier with Param1 (e.g. 100 trees) | 88% C_1^1 | 89% C_1^2 | 93% C_1^3 | 92% C_1^4 | 90.5% |
| Classifier with Param2 (e.g. 200 trees) | 90% C_2^1 | C_2^2 | 91% C_2^3 | 91% C_2^4 | 90% |

Step 4: We select the parameter/model with best average validation performance over k folds.

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Other common partitioning:

- 10-Fold CV
- 5-Fold CV
- 3-Fold CV

We may decide on the size of the test set, for example, 15%, 20%, 30% of the whole dataset, the rest for training/validation.



- The test set contains the examples that the learning algorithm has never seen before,
- So test performance shows how well our model generalizes.

 Example:

Xinchao uses k-fold cross validation to obtain an optimal parameter for his model (e.g., decision tree). This parameter, on the test set, achieves accuracy of 0.8.

Yueming uses uses k-fold cross validation to obtain an optimal parameter for her model (e.g., random forest). This parameter, on the test set, achieves accuracy of 0.9.

We can say, Yueming's model generalizes better than Xinchao's model.

Take home message:

Validation performance -> Selecting parameters!

Test performance -> The "real" performance of a model with selected parameter!



- Validation is however not always used:
 - Validation is used when you need to <u>pick parameters or models</u>
 - If you have no models or parameters to compare, you may consider partition the data into only training and test

Outline



- Dataset Partition:
 - Training/Validation/Testing
- Cross Validation
- Evaluation Metrics
 - Evaluating the quality of a trained classifier

We will talk about many metrics: It is OK you can't memorize them all But intuition is important!



Regression

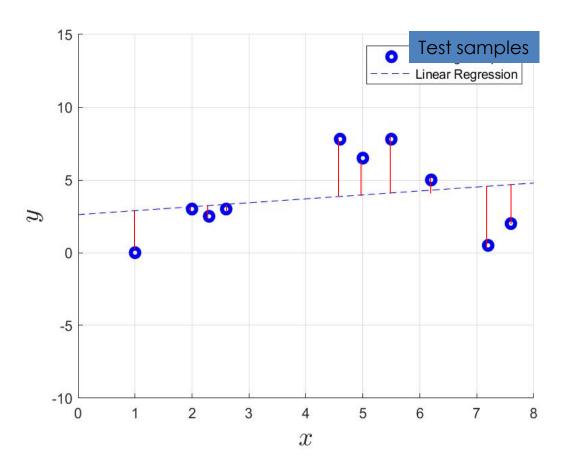
Mean Square Error

$$(MSE = \frac{\sum_{i=1}^{n} (y_i - \hat{y}_i)^2}{n})$$

Mean Absolute Error

$$(\mathsf{MAE} = rac{\Sigma_{i=1}^n |y_i - \hat{y}_i|}{n})$$

where y_i denotes the target output and \hat{y}_i denotes the predicted output for sample i.



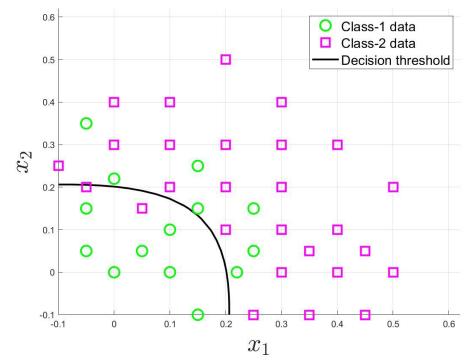


Classification

Class-1: Positive Class Class-2: Negative Class

Confusion Matrix

| | Class-1 (predicted) | Class-2 (predicted) |
|---------------------|------------------------|------------------------|
| Class-1 (actual) | 7 (TP) | 7 (FN) |
| Class-2 (actual) | 2 (FP) | 25 (TN) |



TP: True Positive

FN: False Negative (i.e., Type II Error)

FP: False Positive (i.e., Type I Error)

TN: True Negative

| Class-1 | Class-2 |
|------------|-------------|
| predicted) | (predicted) |

Classification

 How many samples in the dataset have the real label of Class-2?

| 103 | (predicted) | (predicted) |
|---------------------|-------------|-------------|
| Class-1 (actual) | 7 (TP) | 7 (FN) |
| Class-2 (actual) | 2 (FP) | 25 (TN) |

- How many samples are there in total?
- How many sample are correctly classified? How many are incorrectly classified?



Classification

Confusion Matrix for Binary Classification

| | $\widehat{\mathbf{P}}$ (predicted) | $\widehat{\mathbf{N}}$ (predicted) | |
|---------------|------------------------------------|------------------------------------|------------------------------|
| P (actual) | TP | FN | Recall TP/(TP+FN) |
| N (actual) | FP | TN | |
| | Precision TP/(TP+FP) | (TP+TN | Accuracy I)/(TP+TN+FP+FN) |



Classification

Cost Matrix for Binary Classification

| | $\widehat{\mathbf{P}}$ (predicted) | $\widehat{\mathbf{N}}$ (predicted) |
|---------------|------------------------------------|------------------------------------|
| P (actual) | $C_{p,p}$ * TP | $C_{p,n}$ * FN |
| N (actual) | $C_{n,p}$ * FP | $C_{n,n}$ * TN |

Total cost: $C_{p,p}$ * TP + $C_{p,n}$ * FN + $C_{n,p}$ * FP +

 $C_{n,n}$ * TN

Main Idea: To assign different *penalties* for different entries. Higher penalties for more severe results.

Usually, $C_{p,p}$ and $C_{n,n}$ are set to 0; $C_{n,p}$ and $C_{p,n}$ may and may not equal



- Example of cost matrix
 - Assume we would like to develop a self-driving car system
 - We have an ML system that detects the pedestrians using camera,
 by conducing a binary classification
 - When it detects a person (positive class), the car should stop
 - · When no person is detected (negative class), the car keeps going

<u>True Positive</u> (cost $C_{p,p}$)

There is person, ML detects person and car stops

<u>True Negative</u> (cost $C_{n,n}$)

There is no person, car keeps going

False Positive (cost $C_{n,v}$)

There is no person, ML detects person and car stops

False Negative (cost $C_{p,n}$)

There is person, ML fails to detect person and car keeps going

$$C_{n,p}$$
 ? $C_{p,n}$ (>, <, or =)



Credit: automotiveworld.com



- Handling unbalanced data
 - Assume we have 1000 samples, of which 10 are <u>positive</u> and 990 are <u>negative</u>
 - Accuracy = 990/1000=0.99!
 - Yet, half of the Class-1 are Classified to Class-2!

| | Class-1 (predicted) | Class-2 (predicted) |
|---------------------|------------------------|------------------------|
| Class-1 (actual) | 5 (TP) | 5 (FN) |
| Class-2 (actual) | 5 (FP) | 985 (TN) |

The goal is to highlight the problems of the results!

In this case, we shall

- 1) Use cost matrix, assign different costs for each entry
- 2) Use Precision and Recall! Precision = 0.5 and Recall = 0.5



Classification

```
(True Positive Rate) TPR = TP/(TP+FN) Recall (False Negative Rate) FNR = FN/(TP+FN)
```

(True Negative Rate) TNR = TN/(FP+TN) (False Positive Rate) FPR = FP/(FP+TN)

| TPR + FNR = 1 (100% of positive-class data) | |
|---|---|
| TNR + FPR = 1 (100% of negative-class data) |) |

| | P (predicted) | N (predicted) |
|---------------|---------------|---------------|
| P (actual) | TP | FN |
| N (actual) | FP | TN |



Classification

Prediction function y = f(x)

| sample | N1 | N2 | P1 | N3 | P2 | Р3 |
|-----------------|------|------|------|-----|------|------|
| input x | -4 | -3 | -2.5 | -2 | -1.5 | -0.5 |
| Prediction y | -1.1 | -0.5 | -0.1 | 0.2 | 0.6 | 0.9 |
| Actual Label | -1 | -1 | 1 | -1 | 1 | 1 |

If threshold set to be y=0, N3, P2, P3 will be taken as +1 P1, N2, N1 will be taken as -1

| | P (predicted) | Ñ (predicted) |
|---------------|---------------|------------------|
| P (actual) | TP = 2 | FN = 1 |
| N (actual) | FP = 1 | TN = 2 |



Classification

Prediction function y = f(x)

We can change the threshold!

| sample | N1 | N2 | P1 | N3 | P2 | P3 |
|-----------------|------|------|------|-----|------|------|
| input x | -4 | -3 | -2.5 | -2 | -1.5 | -0.5 |
| Prediction y | -1.1 | -0.5 | -0.1 | 0.2 | 0.6 | 0.9 |
| Actual Label | -1 | -1 | 1 | -1 | 1 | 1 |

If threshold set to be y=0.4, P2, P3 will be taken as +1 N3, P1, N2, N1 will be taken as -1

| | P (predicted) | Ñ (predicted) |
|---------------|---------------|------------------|
| P (actual) | TP = 2 | FN = 1 |
| N (actual) | FP = 0 | TN = 3 |



Classification:

TP, FP, FN, TN will change wrt thresholds!

If threshold set to be y=0, N3, P2, P3 will be taken as +1 P1, N2, N1 will be taken as -1

| | P (predicted) | $\widehat{\mathbf{N}}$ (predicted) |
|---------------|---------------|------------------------------------|
| P (actual) | TP = 2 | FN = 1 |
| N (actual) | FD — 1 | TN-2 |

If threshold set to be y=0.4, P2, P3 will be taken as +1 N3, P1, N2, N1 will be taken as -1

| | P (predicted) | Ñ (predicted) |
|---------------|---------------|------------------|
| P (actual) | TP = 2 | FN = 1 |
| N (actual) | FP = 0 | TN = 3 |



Classification

Confusion Matrix for Multicategory Classification

| | $P_{\widehat{1}}$ (predicted) | $P_{\widehat{2}}$ (predicted) | | $P_{\widehat{\mathbb{C}}}$ (predicted) |
|------------------|-------------------------------|-------------------------------|------|--|
| P_1 (actual) | $P_{1,\widehat{1}}$ | $P_{1,\widehat{2}}$ | ••• | $P_{1,\widehat{\mathbb{C}}}$ |
| P_2 (actual) | $P_{2,\widehat{1}}$ | $P_{2,\widehat{2}}$ | ••• | $P_{2,\widehat{\mathbb{C}}}$ |
| | | | **** | |
| P_{C} (actual) | $P_{C,\widehat{1}}$ | $P_{C,\widehat{2}}$ | | $P_{C,\widehat{C}}$ |

Other Issues



- Computational speed and memory consumptions are also important factors
 - Especially for mobile or edge devices
- Other factors
 - Parallelable, Modularity, Maintainability
- Not focus of this module

Practice Question



Suppose we have a dataset of 550 samples. We take out *n* samples as test set, and run k-fold cross validation on the remaining samples.

Within each fold, we know that, the number of training samples is **three times as large as** the number of validation samples, and **two times as large as** the number of test samples.

- 1. What is *k***?**
- 2. What is *n*?



