## EE2211 Tutorial 12

Question 1: The convolutional neural network is particularly useful for applications related to image and text processing due to its dense connections. X

a) True

b) False

CNN -> image RNN & LSTM -> text

Ans: b).

dense connection: current > previous

tully connected

Question 2: In neural networks, nonlinear activation functions such as sigmoid, and ReLU

only

- a) speed up the gradient calculation in backpropagation, as compared to linear units 🗡
- b) are applied only to the output units x all layers
- c) help to introduce non-linearity into the model /

d) always output values between 0 and 1 X

aptimisation & quality

Ans: c.

Question 3: A fully connected network of 2 layers has been constructed as

$$F_{\mathbf{w}}(\mathbf{X}) = f(f(\mathbf{X}\mathbf{W}_1)\mathbf{W}_2)$$

where 
$$\mathbf{X} = \begin{bmatrix} 1 & 1 & 3.0 \\ 1 & 2 & 2.5 \end{bmatrix}$$
,  $\mathbf{W}_1 = \mathbf{W}_2 = \begin{bmatrix} -1 & 0 & 1 \\ 0 & -1 & 0 \\ 1 & 0 & 1 \end{bmatrix}$ . Relu:  $\sigma(a) = \max(o, a)$ 

Suppose the Rectified Linear Unit (ReLU) has been used as the activation function (f) for all the nodes. Compute the network output matrix  $F_{\mathbf{w}}(\mathbf{X})$  (up to 1 decimal place for each entry) based on the given network weights and data.

$$\mathbf{F_{w}(X)} = \begin{bmatrix} blank1 & blank2 & blank3 \\ blank4 & blank5 & blank6 \end{bmatrix}$$

Answer:

$$f(\mathbf{X}\mathbf{W}_{1}) = f \begin{pmatrix} \begin{bmatrix} 1 & 1 & 3.0 \\ 1 & 2 & 2.5 \end{bmatrix} \begin{bmatrix} -1 & 0 & 1 \\ 0 & -1 & 0 \\ 1 & 0 & 1 \end{bmatrix} \end{pmatrix}$$

$$= f \begin{pmatrix} \begin{bmatrix} 2 & -1 & 4.0 \\ 1.5 & -2 & 3.5 \end{bmatrix} \end{pmatrix}$$

$$= \begin{bmatrix} 2 & 0 & 4.0 \\ 1.5 & 0 & 3.5 \end{bmatrix}$$

$$f(f(\mathbf{X}\mathbf{W}_{1})\mathbf{W}_{2}) = f \begin{pmatrix} \begin{bmatrix} 2 & 0 & 4.0 \\ 1.5 & 0 & 3.5 \end{bmatrix} \begin{bmatrix} -1 & 0 & 1 \\ 0 & -1 & 0 \\ 1 & 0 & 1 \end{bmatrix} \end{pmatrix}$$

$$= f \begin{pmatrix} \begin{bmatrix} 2 & 0 & 6 \\ 2 & 0 & 5 \end{bmatrix} \end{pmatrix}$$

$$= \begin{bmatrix} 2 & 0 & 6 \\ 2 & 0 & 5 \end{bmatrix}$$

**Matlab codes:** 

Question 4: A fully connected network of 3 layers has been constructed as

$$F_{\mathbf{w}}(\mathbf{X}) = f([\mathbf{1}, f([\mathbf{1}, f(\mathbf{X}\mathbf{W}_{1})]\mathbf{W}_{2})]\mathbf{W}_{3}) \quad \text{Signoid} \quad \text{or } (\mathbf{a}) = \frac{1}{1 - 1} \quad \text{or } ($$

Suppose the **Sigmoid** has been used as the activation function (f) for all the nodes. Compute the network output matrix  $F_{\mathbf{w}}(\mathbf{X})$  (up to 1 decimal place for each entry) based on the given network weights and data.

$$F_{\mathbf{w}}(\mathbf{X}) = \begin{bmatrix} blank1 & blank2 & blank3 \\ blank4 & blank5 & blank6 \end{bmatrix}$$

Answer:

$$f(\mathbf{X}\mathbf{W}_{1}) = f\begin{pmatrix} \begin{bmatrix} 1 & 2 & 1 \\ 1 & 5 & 1 \end{bmatrix} \begin{bmatrix} -1 & 0 & 1 \\ 0 & -1 & 0 \\ 1 & 0 & -1 \end{bmatrix} \end{pmatrix}$$

$$= f\begin{pmatrix} \begin{bmatrix} 0 & -2 & 0 \\ 0 & -5 & 0 \end{bmatrix} \end{pmatrix}$$

$$= \begin{bmatrix} 0.5 & 0.1192 & 0.5 \\ 0.5 & 0.0067 & 0.5 \end{bmatrix}$$

$$f([\mathbf{1}, f(\mathbf{X}\mathbf{W}_{1})]\mathbf{W}_{2}) = f\begin{pmatrix} \begin{bmatrix} 1 & 0.5 & 0.1192 & 0.5 \\ 1 & 0.5 & 0.0067 & 0.5 \end{bmatrix} \begin{bmatrix} -1 & 0 & 1 \\ 0 & -1 & 0 \\ 1 & 0 & 1 \\ 1 & -1 & 1 \end{bmatrix} \end{pmatrix}$$

$$= f\begin{pmatrix} \begin{bmatrix} -0.3808 & -1.0000 & 1.6192 \\ -0.4933 & -1.0000 & 1.5067 \end{bmatrix} \end{pmatrix}$$

$$= \begin{bmatrix} 0.4059 & 0.2689 & 0.8347 \\ 0.3791 & 0.2689 & 0.8186 \end{bmatrix}$$

```
f([\mathbf{1}, f([\mathbf{1}, f(\mathbf{X}\mathbf{W}_1)]\mathbf{W}_2)]\mathbf{W}_3) = f \begin{pmatrix} \begin{bmatrix} 1 & 0.4059 & 0.2689 & 0.8347 \\ 1 & 0.3791 & 0.2689 & 0.8186 \end{bmatrix} \begin{bmatrix} -1 & 0 & 1 \\ 0 & -1 & 0 \\ 1 & 0 & 1 \\ 1 & -1 & 1 \end{bmatrix} \end{pmatrix}= \begin{bmatrix} 0.5259 & 0.2243 & 0.8913 \\ 0.5219 & 0.2319 & 0.8897 \end{bmatrix}
```

# **Matlab Codes:**

```
X = [1 2 1; 1 5 1]
W1 = [-1 0 1; 0 -1 0; 1 0 -1]
W2 = [-1 0 1; 0 -1 0; 1 0 1; 1 -1 1]
W3 = W2;
F = sigmoid([ones(2,1),sigmoid([ones(2,1),sigmoid(X*W1)]*W2)]*W3)
function y = sigmoid(x)
y = 1./(1+exp(-x));
end
```

(MLP classifier, find the best hidden node size, assuming same hidden layer size in each layer, based on cross-validation on the training set and then use it for testing)

## **Question 5:**

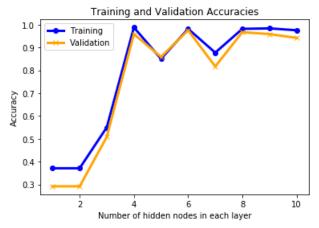
Obtain the data set "from sklearn.datasets import load iris".

- (a) Split the database into two sets: 80% of samples for training, and 20% of samples for testing using random state=0
- (b) Perform a 5-fold Cross-validation using only the training set to determine the best 3-layer MLPClassifier (from sklearn.neural\_network import MLPClassifier with hidden\_layer\_sizes=(Nhidd, Nhidd, Nhidd) for Nhidd in range (1,11))\* for prediction. In other words, partition the training set into two sets, 4/5 for training and 1/5 for validation; and repeat this process until each of the 1/5 has been validated. Provide a plot of the average 5-fold training and validation accuracies over the different network sizes
- (c) Find the size of Nhidd that gives the best validation accuracy for the training set.
- (d) Use this Nhidd in the MLPClassifier with hidden\_layer\_sizes=(Nhidd, Nhidd, Nhidd) to compute the prediction accuracy based on the 20% of samples for testing in part (a).
- \* The assumption of hidden\_layer\_sizes=(Nhidd, Nhidd, Nhidd) is to reduce the search space in this exercise. In field applications, the search should take different sizes for each hidden layer.

#### **Answer:**

```
## load data from scikit
import numpy as np
import pandas as pd
print("pandas version: {}".format(pd.__version__))
import sklearn
print("scikit-learn version: {}".format(sklearn.__version__))
from sklearn.datasets import load_iris
from sklearn.model_selection import train_test_split
from sklearn.neural_network import MLPClassifier # neural network
from sklearn import metrics
```

```
def find network size(X train, y train):
   acc train array = []
   acc_valid_array = []
   for Nhidd in range (1,11):
      acc_train_array_fold = []
      acc_valid_array_fold = []
      ## Random permutation of data
      Idx = np.random.RandomState(seed=8).permutation(len(y train))
      ## Tuning: perform 5-fold cross-validation on the training set to determine the best network
size
      for k in range (0,5):
          N = np.around((k+1)*len(y_train)/5)
          N = N.astype(int)
          Xvalid = X train[Idx[N-24:N]] # validation features
          Yvalid = y_train[Idx[N-24:N]] # validation targets
          Idxtrn = np.setdiff1d(Idx, Idx[N-24:N])
          Xtrain = X train[Idxtrn] # training features in tuning loop
          Ytrain = y train[Idxtrn] # training targets in tuning loop
          ## MLP Classification with same size for each hidden-layer (specified in question)
          clf = MLPClassifier(solver='lbfgs', alpha=1e-5, hidden layer sizes=(Nhidd,Nhidd,Nhidd),
random state=1)
         clf.fit(Xtrain, Ytrain)
          ## trained output
          y est p = clf.predict(Xtrain)
          acc train array fold += [metrics.accuracy score(y est p,Ytrain)]
          ## validation output
          yt est p = clf.predict(Xvalid)
          acc valid array fold += [metrics.accuracy score(yt est p, Yvalid)]
      acc train array += [np.mean(acc train array fold)]
      acc_valid_array += [np.mean(acc_valid_array_fold)]
   ## find the size that gives the best validation accuracy
   Nhidden = np.argmax(acc_valid_array,axis=0)+1
   ## plot.t.ing
   import matplotlib.pyplot as plt
   hiddensize = [x \text{ for } x \text{ in range}(1,11)]
   plt.plot(hiddensize, acc_train_array, color='blue', marker='o', linewidth=3, label='Training')
   plt.plot(hiddensize,
                            acc valid array,
                                                  color='orange',
                                                                     marker='x', linewidth=3,
label='Validation')
   plt.xlabel('Number of hidden nodes in each layer')
   plt.ylabel('Accuracy')
   plt.title('Training and Validation Accuracies')
   plt.legend()
   plt.show()
   return Nhidden
## load data
iris dataset = load iris()
## split dataset into training and test sets
X_train, X_test, y_train, y_test = train_test_split(iris_dataset['data'],
                                               iris dataset['target'],
                                               test size=0.20,
                                               random state=0)
## find the best hidden node size using only the training set
Nhidden = find network size(X train, y train)
print('best hidden node size =', Nhidden, 'based on 5-fold cross-validation on training set')
## perform evaluation
clf = MLPClassifier(solver='lbfgs', alpha=1e-5, hidden layer sizes=(Nhidden, Nhidden, Nhidden),
random_state=1)
clf.fit(X_train, y_train)
## trained output
y test predict = clf.predict(X test)
test accuracy = metrics.accuracy score(y test predict, y test)
print('test accuracy =', test_accuracy)
```



>> best hidden node size = 6 based on 5-fold cross-validation on training set >> test accuracy = 1.0

(An example of handwritten digit image classification using CNN)

# **Question 6:**

Please go through the baseline example in the following link to get a feel of how the Convolutional Neural Network (CNN) can be used for handwritten digit image classification.

https://machinelearningmastery.com/how-to-develop-a-convolutional-neural-network-from-scratch-for-mnist-handwritten-digit-classification/

**Note:** This example assumes that you are using standalone Keras running on top of TensorFlow with Python 3 (you might need conda install -c conda-forge keras tensorflow to get the Keras library installed).

The following codes might be useful for warnings suppression if you find them annoying:

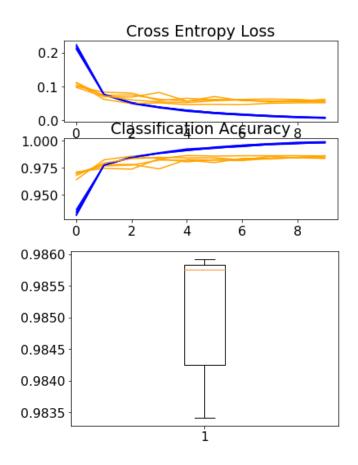
```
import warnings
```

```
warnings.filterwarnings("ignore", category=UserWarning)
```

As the data size and the network size are relatively large comparing with previous assignments, the codes can take quite some time to run (e.g., several minutes running on the latest notebook).

## **Results:**

```
Accuracy for each fold:
> 98.583
> 98.425
> 98.342
> 98.575
> 98.592
Accuracy: mean=98.503 std=0.102, n=5
```



Improved version (network of larger size):
Accuracy for each fold:

> 98.992

> 98.717

> 98.925

> 99.233

> 98.875

Accuracy: mean=98.948 std=0.169, n=5

