

# Lecture 7: Topic Modeling

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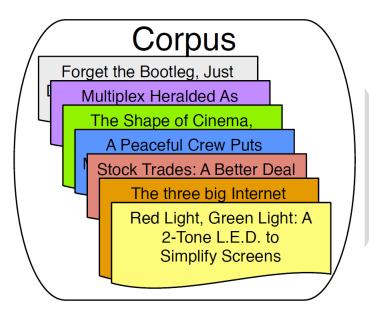
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# AGENDA

01	Topic Modeling
02	Probabilistic Latent Semantic Analysis
03	LDA: Document Generation Process
04	LDA Inference: Gibbs Sampling
05	LDA Evaluation

### Topic Model: Conceptual Approach

- Topic Model
  - ✓ From an input corpus and the number of topics  $K \rightarrow$  words to topics
  - ✓ From an input corpus and the number of topics  $K \rightarrow words$  to topics



#### TOPIC 1

computer, technology, system, service, site, phone, internet, machine

#### TOPIC 2

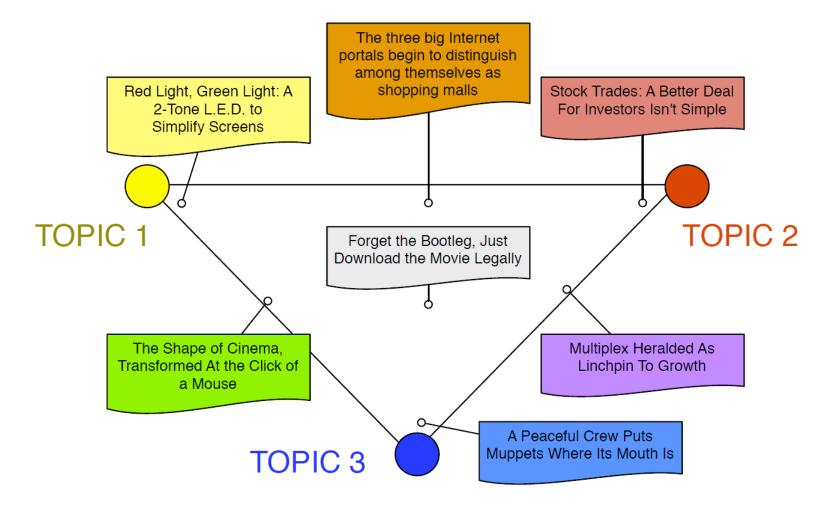
sell, sale, store, product, business, advertising, market, consumer

#### TOPIC 3

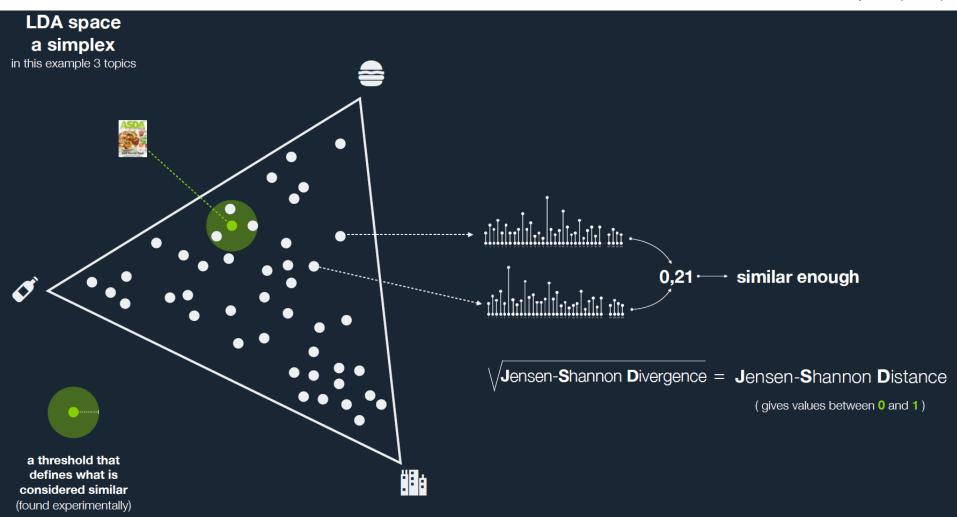
play, film, movie, theater, production, star, director, stage

## Topic Model: Conceptual Approach

- Topic Model
  - √ For each document, what topics are expressed by that document?



# Topic Model: Conceptual Approach



# Topic Models: Topic Extraction

Kim et al. (2016)

#### • Topic Extraction

√ 30 Topics discovered for "Deep Learning"

ault detection wi th DBN	Convolutional neural network	Network Learning	Representation learning	Face Recognition	Speech Recognition	Acoustic Modeling	Extreme Learning	Deep learning architecture	Image Segmentation
deep	neural	layer input	feature	face 	speaker	speech 	deep	deep	image
belief	convolutional	output	level	recognition	speech	recognition 	learn	architecture	scene
network	pool	unit	extract	estimation	noise	acoustic	algorithm	neural	scale
dbn	convolution	hide	learn	facial	adaptation	hmm	structure	standard	segmentatio
fault	convnet	function	extraction	shape	source	neural	extreme	explore	pixel
Long-short term memory	Predictive analytics	Signal processing	Classification models	Large-scale computing	Image quality assessment	Visual recognition	NLP	Detection using CNN	Action recognition
term	data	analysis	classification	application	domain	pattern	word	cnn	video
recurrent	prediction	filter	classifier	implementation	state	process	text	detection	human
long	technique	signal	class	efficient	quality	compute	language	convolutional	temporal
lstm	information	component	vector	process	resolution	visual	representation	neural	action
network	research	audio	support	power	relationship	field	semantic	detect	track
lmage retrieval	Medical image di agnosis	Reinforcement learning	Parameter optimization	Auto encoder	RBM and variations	Learning with few labeled data	Fast learning complexity reduction	Applications for vehicles & robots	Character recognition
image	image	learn	train	representation	machine	train	fast	time	recognition
visual	segmentation	question	algorithm	learn	boltzmann	data	reduce	real	system
retrieval	disease 	state	gradient	sparse	rbm	label	parameter	application	character
descriptor	cell	answer	sample	encode	restrict	few	weight	drive	network
attribute	medical	reinforcement	optimization	stack	distribution	transfer	complexity	Vehicle	neural

# Topic Models: Topic Extraction

#### • Topic Extraction

#### √ 50 Topics discovered for "Ultrasound/Ultrasonography"

Vascular	Prostate	heart	CAD	MSK	nerve	tumor	ОВ	surgery	intervention
plaque	biopsy	artery	image	joint	block	case	ultrasound	surgery	guide
ivus	prostate	carotid	ultrasound	patient	nerve	lesion	fetal	patient	patient
coronary	cancer	patient	method	disease	ultrasound	diagnosis	infant	intraoperative	complication
intravascular	patient	stenosis	base	score	guide	ultrasound	abnormality	preoperative	treatment
stent	transrectal	plaque	propose	arthritis	patient	cyst	prenatal	surgical	percutaneous
patient	trus	ultrasound	feature	ultrasound	pain	mass	case	ultrasound	ultrasound
lesion	guide	cardiac	algorithm	clinical	anesthesia	tumor	fetus	localization	drainage
mm.	core	dus	segmentation	inflammatory	surgery	finding	anomaly	operative	month
ultrasound	ultrasound	stroke	analysis	activity	plexus	ultrasonography	diagnosis	resection	rate
area	rate	arterial	result	study	technique	present	congenital	surgeon	procedure

osteoporosis	cerebral	ER&ICU	cancer	Lab test	US general	vein	lymph node	lung	Healthcare
age	brain	patient	cancer	extraction	ultrasound	vein	node	lung	patient
ultrasound	dog	emergency	patient	assist	imaging	venous	lymph	chest	risk
child	fus	care	tumor	ultrasound	technique	patient	patient	ultrasound	ultrasound
bone	bbb	ultrasound	stage	method	clinical	internal	biopsy	patient	year
year	ultrasound	department	eus	liquid	review	ultrasound	metastasis	pulmonary	study
study	blood	bedside	gastric	sample	application	jugular	ultrasound	lus	follow
fat	study	perform	ovarian	time	diagnostic	thrombosis	cancer	pleural	clinical
qus	day	physician	endoscopic	solvent	disease	central	guide	line	factor
body	follicle	point	ultrasonography	determination	article	dvt	negative	radiography	month
measure	barrier	cardiac	invasion	extract	role	femoral	positive	diagnosis	age

# Topic Models: Topic Extraction

#### • Topic Extraction

√ 10 Topics discovered for "Insider Threat"

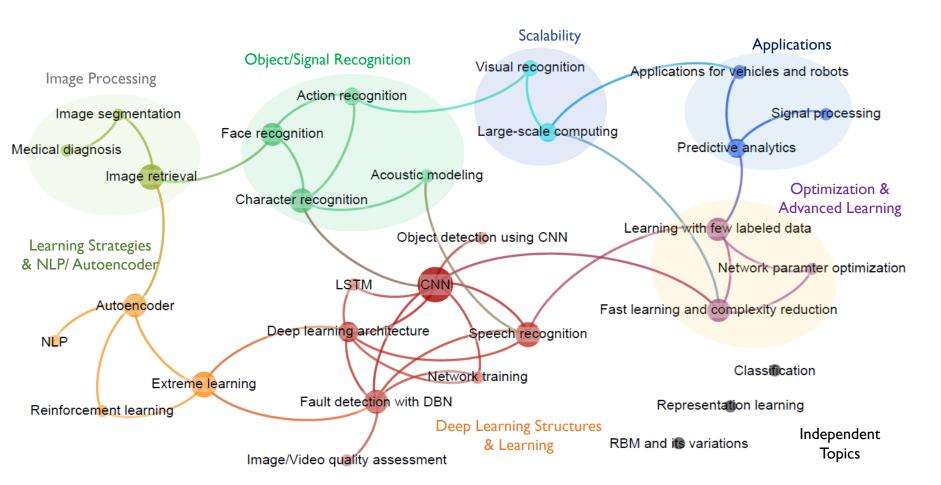
No.	Insider threat in relational database	Assessment of insider threat	Insider attacks on Communication protocol	Modeling and system framework for insider threat	Masquerade detection
ı	data	measure	attack	insider	user
2	information	assess	agent	threat	behavior
3	database	security	scheme	social	detect
4	leakage	behavior	protocol	analysis	activity
5	access	analysis	monitor	framework	malicious
6	detect	management	mitigation	mitigate	masquerade
7	transaction	privacy	fraud	monitor	attack
8	confidential	policy	damage	factor	legitimate
9	document	risk	psychological	technical	abnormal
10	file	threat	financial	business	decoy

No.	Access control for insider threat mitigation	Network intrusion detection systems	Feature selection for intrusion detection	Miscellaneous	Malicious domain detection
1	insider	network	detection	software	attack
2	access	detection	algorithm	security	malicious
3	user	intrusion	feature	system	domain
4	control	malicious	classification	device	event
5	cloud	traffic	accuracy	server	scenario
6	misuse	log	dataset	malicious	human
7	trust	event	performance	protect	knowledge
8	risk	packet	pattern	web	ontology
9	abuse	internet	learning	architecture	represent
10	attacker	resource	random	electronic	generate

## Topic Models: Relation between Topics

Kim et al. (2016)

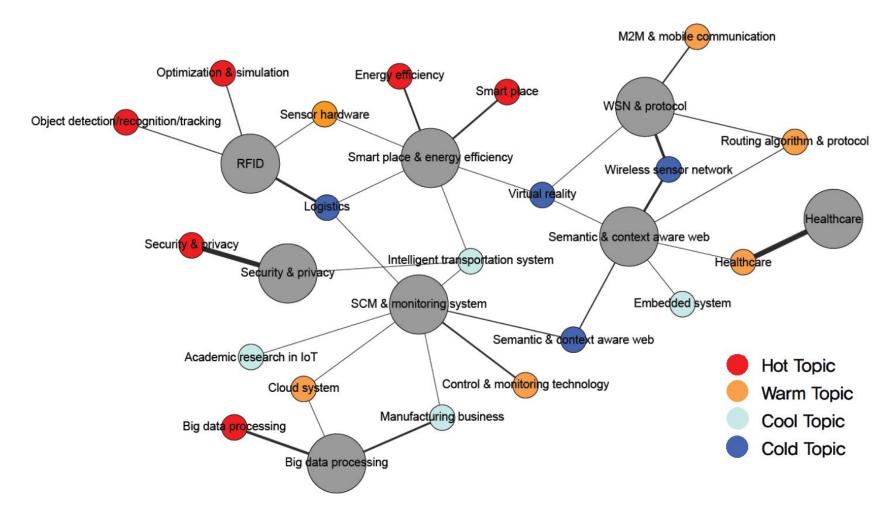
Relation between Topics: Deep Learning



### Topic Models: Relation between Topics

Kim and Kang (2018+)

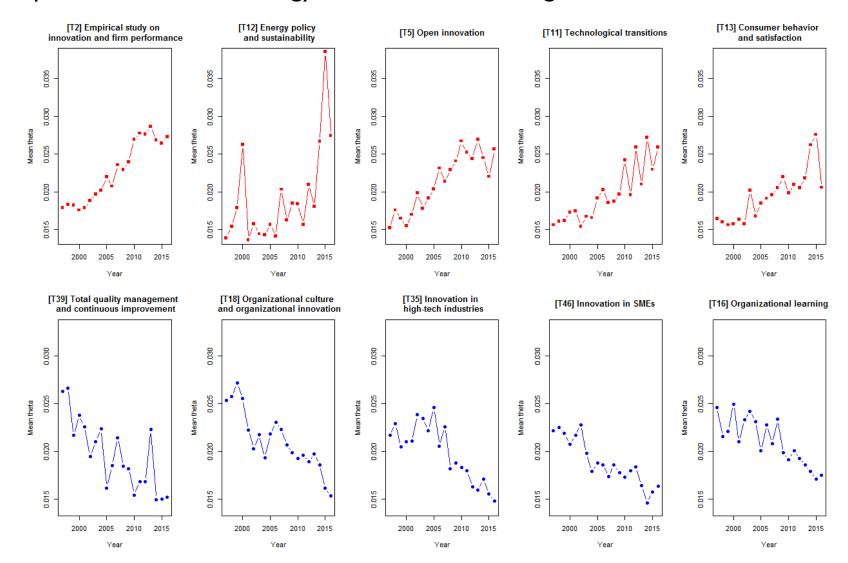
Relation between Topics: Internet of Things



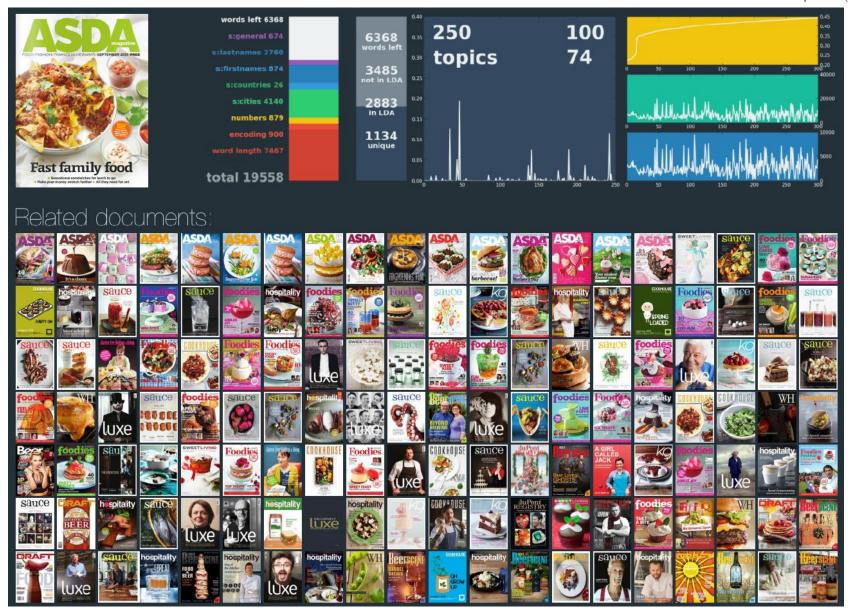
### Topic Models: Trend Analysis

Lee and Kang (2017)

• Topic trends for "technology and innovation management"



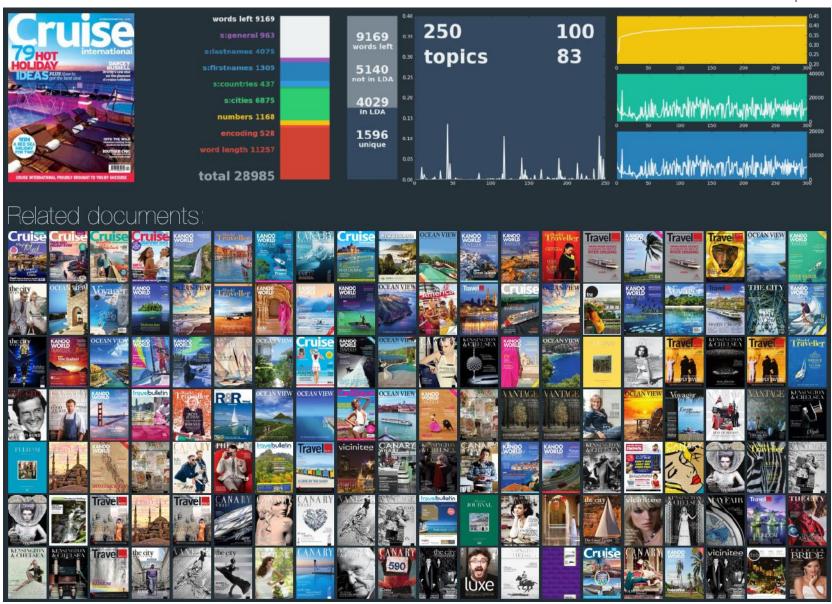
# Topic Model: Document Retrieval



### Topic Model: Document Retrieval

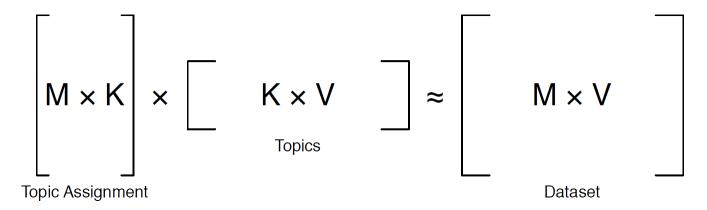


### Topic Model: Document Retrieval

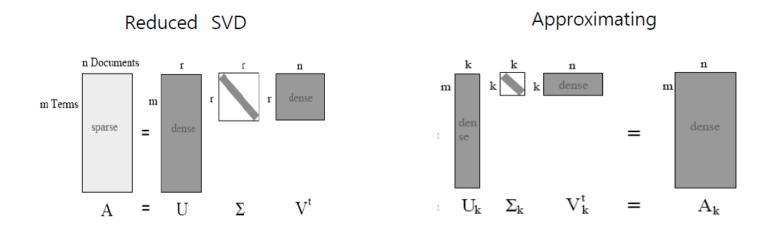


### Topic Model

Matrix Factorization Approach



✓ If we use singular value decomposition (SVD), it is called latent semantic analysis (LSA)

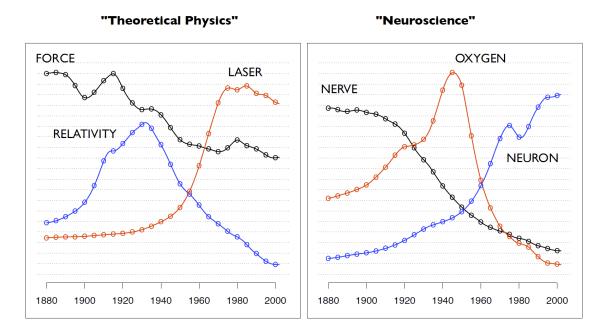


# Topic Model

- Disadvantage of LSA
  - ✓ Statistical foundation is missing
  - ✓ SVD assumes normally distributed data
  - √ Term occurrence is not normally distributed
  - √ Still, often it works remarkably good because matrix entries are weighted (e.g. tf-idf)
    and those weighted entries may be normally distributed

## Topic Model

- Probabilistic Topic Model: Generative Approach
  - ✓ Each document is a probability distribution over topics
  - ✓ Distribution over topics represents the essence of a given document
  - ✓ Each topic is a probability distribution over words
    - Topic "Education": school, students, education, university,...
    - Topic "Budget": million, finance, tax, program, ...



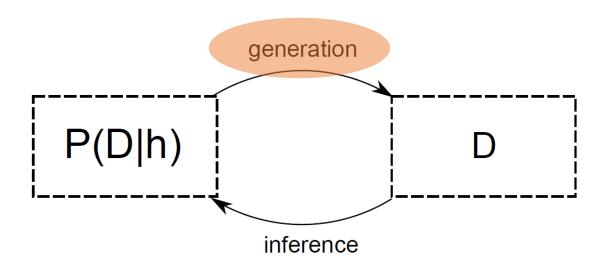
#### Model-based methods

- ✓ Statistical inference is based on fitting a probabilistic model of data
- √ The idea is based on a probabilistic or generative model
- √ Such models assign a probability for observing specific data examples
  - Observing words in a text document
- ✓ Generative models are powerful method to encode specific assumptions of how unknown parameters interact to create data

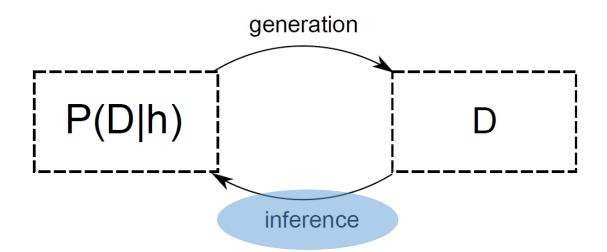
#### How it work?

- $\checkmark$  It defines a conditional probability distribution over data given a hypothesis P(D|h)
- $\checkmark$  Given h, we generate data from the conditional distribution P(D|h)
- ✓ Has many advantages but the main disadvantage is that fitting the model can be more complicated than an algorithmic approach

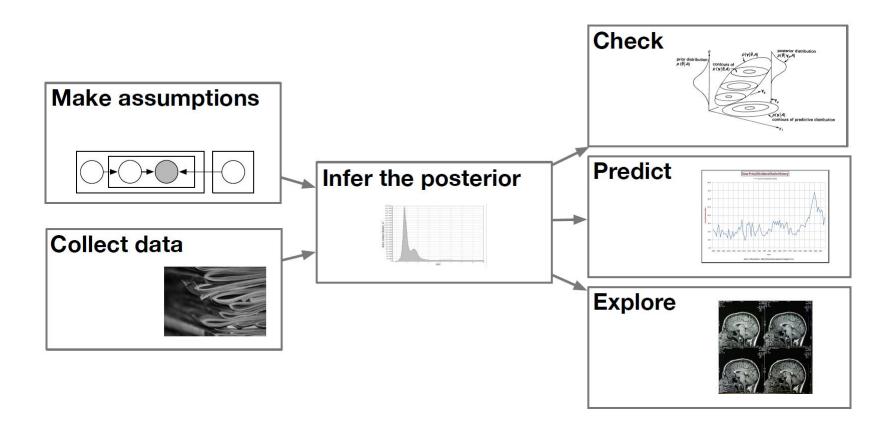
- How it work?
  - $\checkmark$  It defines a conditional probability distribution over data given a hypothesis P(D|h)
  - $\checkmark$  Given h, we generate data from the conditional distribution P(D|h)
  - ✓ Has many advantages but the main disadvantage is that fitting the model can be more complicated than an algorithmic approach



- (Statistical) inference is the reverse of the generation process
  - ✓ We are given some data D, e.g. a collection of documents
  - √ We want to estimate the model, or more precisely the parameters of the hypothesis
    h that are most likely to have generated data



Process of generative model



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#### Latent Structure

 Given a matrix that "encodes" data (e.g. term-document matrix), we have following potential problems

- √ Too large
- √ Too complicated
- ✓ Lack of structure
- √ Missing Entries
- ✓ Noisy Entries, ...

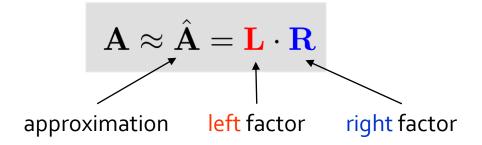
	$\int a_{11}$	• • •	$a_{1j}$	• • •	$a_{1m}$
$\mathbf{A} =$	$a_{i1}$	• • •	$a_{ij}$	• • •	$a_{im}$
	$\backslash a_{n1}$		$a_{nj}$		$a_{nm}$

#### Questions

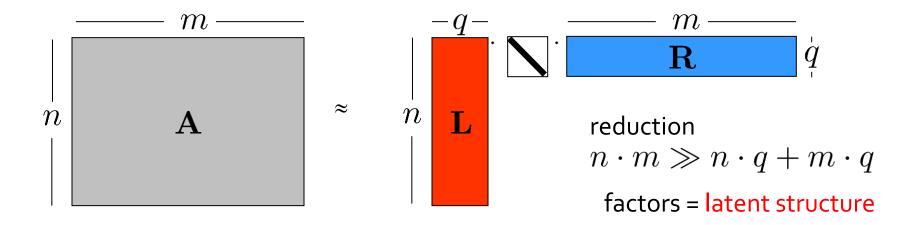
- ✓ Is there a simpler way to explain entities?
- ✓ There might be a latent structure underlying the data
- √ How can we reveal or discover this structure?

### Matrix Decomposition

Common approach: approximately factorize matrix

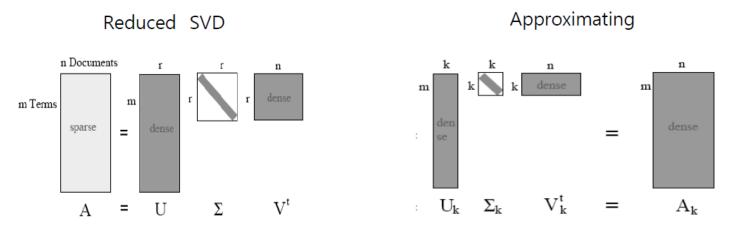


Factors are typically constrained to be "thin"



## LSA Decomposition (revisited)

Reduce the dimensions using SVD



✓ Step I) Construct the approximated matrix  $A_k$  from the original term-document matrix A using SVD

$$\mathbf{A} \approx \mathbf{A}_k = \mathbf{U}_k \mathbf{\Sigma}_k \mathbf{V}_k^T$$

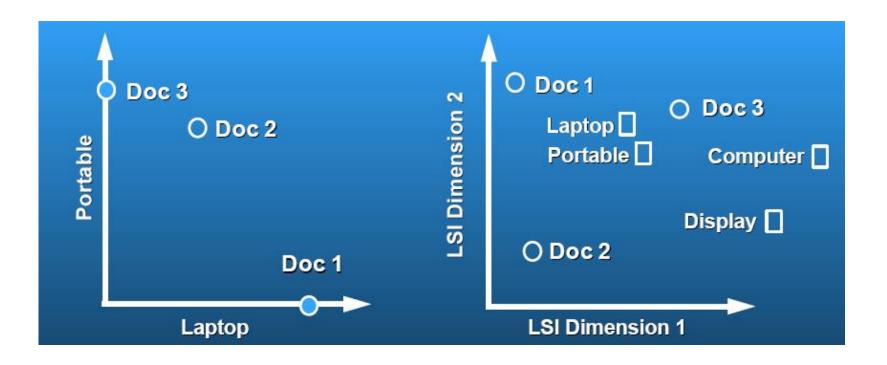
 $\checkmark$  Step 2) Multiply the transpose of  $U_k$  to obtain k (<<m) by n term-document matrix

$$\mathbf{U}_k^T \mathbf{A}_k = \mathbf{U}_k^T \mathbf{U}_k \mathbf{\Sigma}_k \mathbf{V}_k^T = \mathbf{I} \mathbf{\Sigma}_k \mathbf{V}_k^T = \mathbf{\Sigma}_k \mathbf{V}_k^T$$

✓ Step 3: Apply data mining algorithms

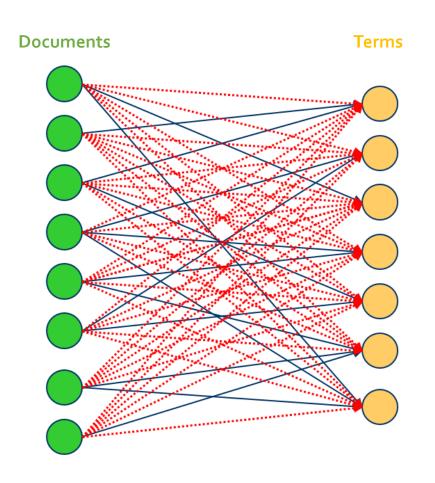
### LSA Decomposition

Illustrative Example



## Language Model: Naïve Approach

Maximum likelihood estimation (MLE)



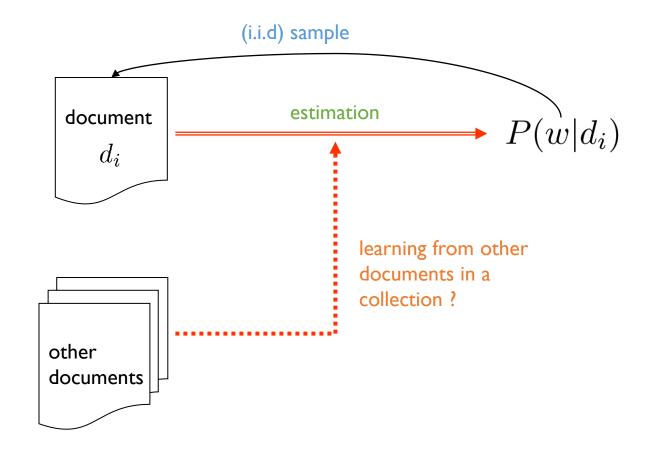
Number of occurrences of term w in document d

$$\hat{P}_{\text{ML}}(w|d) = \frac{n(d, w)}{\sum_{w'} n(d, w')}$$

Zero frequency problem: terms not occurring in a document get zero probability

### Language Model: Estimation Problem Hofmann (2005)

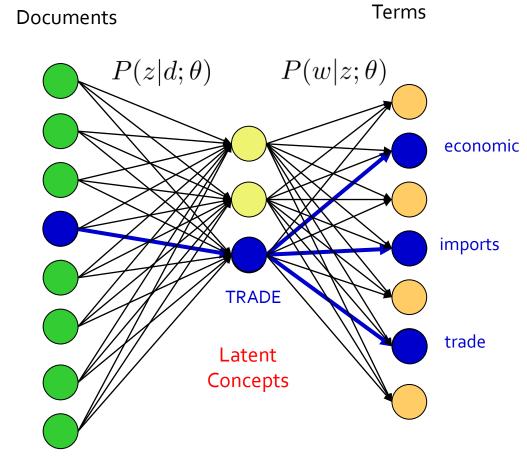
- Crucial question
  - ✓ In which way can the document collection be utilized to improve estimates?



### Probabilistic Latent Semantic Analysis (pLSA)

Hofmann (2005)

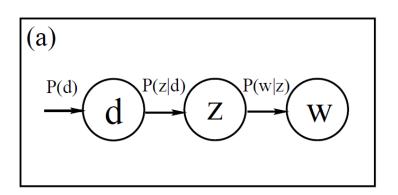
- Concept expression probability
  - ✓ Estimated based on all documents that are dealing with a concept
  - "Unmixing" of superimposed concepts is achieved by statistical learning algorithm
  - ✓ No prior knowledge about concepts required, context and term co-occurrences are exploited

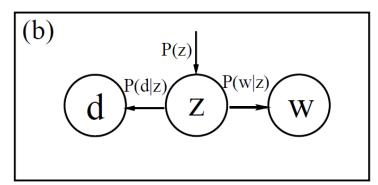


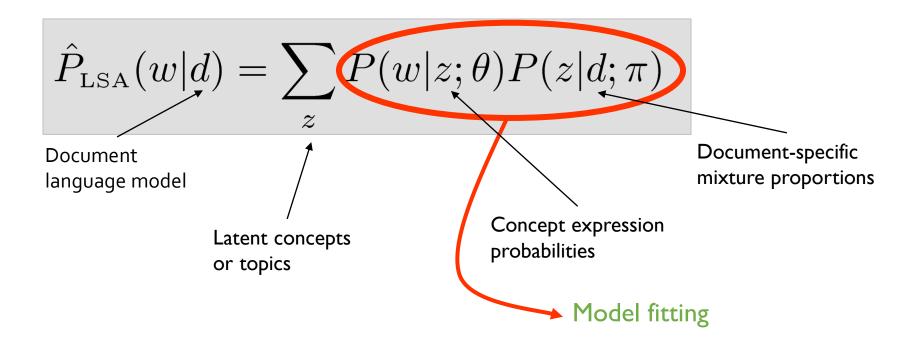
#### pLSA: Latent Variable Model

Hofmann (2005)

Structural modeling assumption (mixture model)





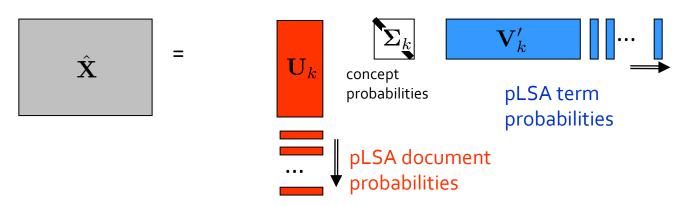


#### pLSA: Matrix Decomposition

Hofmann (2005)

Mixture model can be written as a matrix factorization

$$\hat{P}_{LSA}(d, w) = \sum_{z} \frac{P(d|z)}{P(d|z)} P(z) \frac{P(w|z)}{P(w|z)} = P(d) \sum_{z} P(w|z) P(z|d)$$

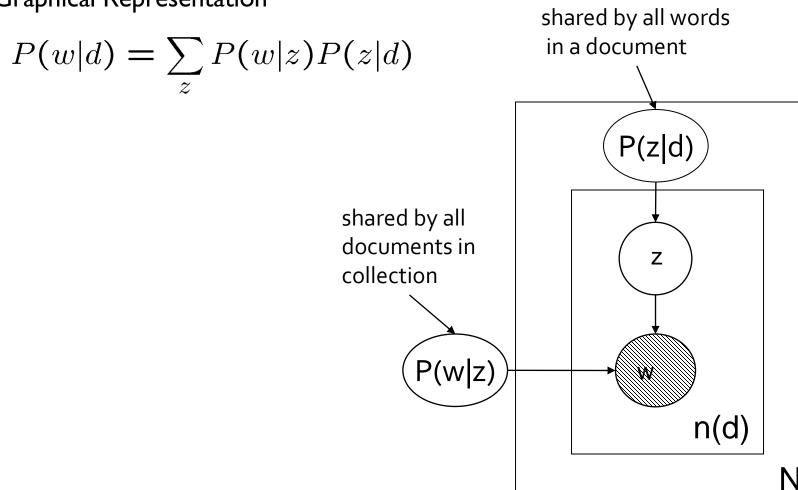


- Contrast to LSA
  - √ Non-negativity: every element in U & V is non-negative.
  - ✓ Normalization: Each document vector in U and each term vector in V has sum I

### pLSA: Graphical Model

Hofmann (2005)

Graphical Representation



### pLSA: Parameter Inference

#### Parameter inference

- √ We will infer parameters using Maximum Likelihood Estimator (MLE)
- ✓ First, we need to write down the likelihood function
- $\checkmark$  Let  $n(w_i, d_j)$  be the number of occurrences of word  $w_i$  in document  $d_j$
- $\checkmark p(w_i,d_j)$  is the probability of observing a single occurrence word  $w_i$  in document  $d_j$
- $\checkmark$  Then, the probability of observing  $n(w_i,d_j)$  occurrence of word  $w_i$  in document  $d_j$  is give by:

$$p(w_i, d_j)^{n(w_i, d_j)}$$

### pLSA: Parameter Inference

#### Parameter Inference

- ✓ The probability of observing the compete document collection is then given by the product of probabilities of observing every single word in every document with corresponding number of occurrences
- ✓ Then, the likelihood function becomes

$$L = \prod_{i=1}^{m} \prod_{j=1}^{n} p(w_i, d_j)^{n(w_i, d_j)}$$

√ The log-likelihood function becomes

$$\mathcal{L} = \sum_{i=1}^{m} \sum_{j=1}^{n} n(w_i, d_j) log(p(w_i, d_j))$$

$$= \sum_{i=1}^{m} \sum_{j=1}^{n} n(w_i, d_j) log(\sum_{l=1}^{k} p(w_i|z_l) p(z_l) p(d_j|z_l))$$

#### pLSA: Parameter Inference

Helic (2014)

#### Parameter Inference

- √ We can not maximize the likelihood analytically because of the logarithm of the sum
- ✓ A standard procedure is to use an algorithm called Expectation-Maximization (EM)
- ✓ This is an iterative method to estimate parameters of the models with latent variables
- $\checkmark$  Each iteration consists of two steps: expectation step (E) and maximization step (M)

### pLSA: EM Algorithm

• E-Step: Posterior probability of latent variables (concepts)

$$p(z|d, w) = \frac{P(z)P(d|z)P(w|z)}{\sum_{z' \in Z} P(z')P(d|z')P(w|z')}$$

Probability that the occurence of term w in document d can be "explained" by concept z

• M-Step: Parameter estimation based on "completed" statistics

$$P(w|z) = \frac{\sum_{d \in D} n(d, w) P(z|d, w)}{\sum_{d \in D, w' \in W} n(d, w') P(z|d, w')}$$

how often is term w associated with concept z ?

$$P(d|z) = \frac{\sum_{w \in W} n(d, w) P(z|d, w)}{\sum_{d' \in D, w \in W} n(d', w) P(z|d', w)}$$

how often is document d associated with concept z ?

$$P(z) = \frac{\sum_{d \in D, w \in W} n(d, w) P(z|d, w)}{\sum_{d \in D, w \in W} n(d, w)}$$

how prevalent is the concept z?

#### • Raw Data

	Doc 1	Doc 2	Doc 3	Doc 4	Doc 5	Doc 6
Baseball	1	2	0	0	0	0
Basketball	3	1	0	0	0	0
Boxing	2	0	0	0	0	0
Money	3	3	2	3	2	4
Interest	0	0	3	2	0	0
Rate	0	0	4	1	0	0
Democrat	0	0	0	0	4	3
Republican	0	0	0	0	2	1
Cocus	0	0	0	0	3	2
President	0	0	1	0	2	3

#### • Parameter Initialization

#### P(z)

Topic 1	Topic 2	Topic 3
0.525	0.407	0.068

#### P(d|z)

	Topic 1	Topic 2	Topic 3
Doc 1	0.020	0.008	0.048
Doc 2	0.294	0.255	0.329
Doc 3	0.204	0.138	0.178
Doc 4	0.200	0.146	0.007
Doc 5	0.186	0.196	0.233
Doc 6	0.096	0.257	0.205

#### P(w|z)

	Topic 1	Topic 2	Topic 3
Term 1	0.022	0.016	0.010
Term 2	0.018	0.133	0.166
Term 3	0.242	0.058	0.133
Term 4	0.123	0.088	0.145
Term 5	0.016	0.030	0.044
Term 6	0.020	0.167	0.056
Term 7	0.147	0.129	0.201
Term 8	0.188	0.156	0.039
Term 9	0.146	0.114	0.008
Term 10	0.077	0.110	0.199

#### • After I EM step

#### Initialization

Topic 1	Topic 2	Topic 3
0.525	0.407	0.068

	Topic 1	Topic 2	Topic 3
Doc 1	0.020	0.008	0.048
Doc 2	0.294	0.255	0.329
Doc 3	0.204	0.138	0.178
Doc 4	0.200	0.146	0.007
Doc 5	0.186	0.196	0.233
Doc 6	0.096	0.257	0.205

#### After I EM step

Topic 1	Topic 2	Topic 3
0.459	0.430	0.111

	Topic 1	Topic 2	Topic 3
Doc 1	0.180	0.077	0.382
Doc 2	0.124	0.089	0.091
Doc 3	0.147	0.213	0.149
Doc 4	0.125	0.110	0.004
Doc 5	0.266	0.204	0.167
Doc 6	0.158	0.308	0.207

#### • After I EM step

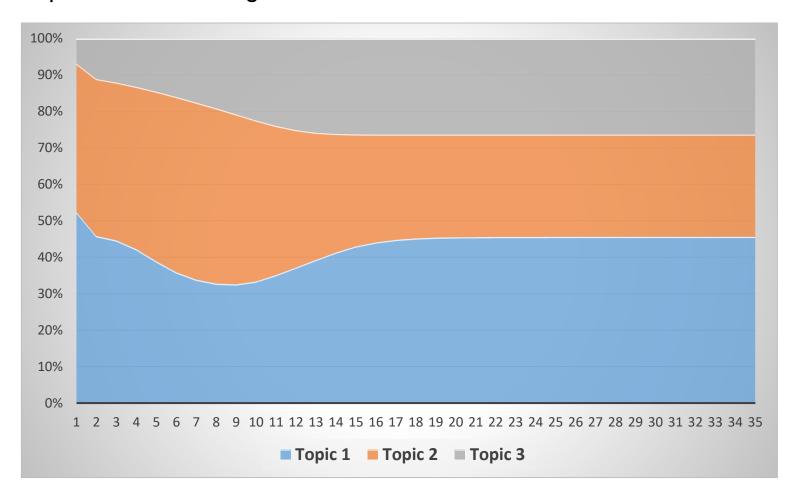
#### Initialization

	Topic 1	Topic 2	Topic 3
Term 1	0.022	0.016	0.010
Term 2	0.018	0.133	0.166
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Term 8	0.188	0.156	0.039
Term 9	0.146	0.114	0.008
Term 10	0.077	0.110	0.199

#### After I EM step

	Topic 1	Topic 2	Topic 3
Term 1	0.077	0.033	0.028
Term 2	0.024	0.074	0.245
Term 3	0.061	0.005	0.043
Term 4	0.370	0.222	0.295
Term 5	0.088	0.093	0.065
Term 6	0.033	0.159	0.035
Term 7	0.115	0.129	0.129
Term 8	0.058	0.058	0.010
Term 9	0.099	0.098	0.004
Term 10	0.073	0.129	0.146

- Topic Distribution
  - √ Topic distribution changes w.r.t. the EM iterations



#### • Final result

	Doc 1	Doc 2	Doc 3	Doc 4	Doc 5	Doc 6
Baseball	1	2	0	0	0	0
Basketball	3	1	0	0	0	0
Boxing	2	0	0	0	0	0
Money	3	3	2	3	2	4
Interest	0	0	3	2	0	0
Rate	0	0	4	1	0	0
Democrat	0	0	0	0	4	3
Republican	0	0	0	0	2	1
Cocus	0	0	0	0	3	2
President	0	0	1	0	2	3

Topic 1	Topic 2	Topic 3
0.456	0.281	0.263

	Topic 1	Topic 2	Topic 3
Doc 1	0.000	0.000	0.600
Doc 2	0.000	0.000	0.400
Doc 3	0.000	0.625	0.000
Doc 4	0.000	0.375	0.000
Doc 5	0.500	0.000	0.000
Doc 6	0.500	0.000	0.000

	Topic 1	Topic 2	Topic 3			
Baseball	0.000	0.000	0.200			
Basketball	0.000	0.000	0.267			
Boxing	0.000	0.000	0.133			
Money	0.231	0.313	0.400			
Interest	0.000	0.312	0.000			
Rate	0.000	0.312	0.000			
Democrat	0.269	0.000	0.000			
Republican	0.115	0.000	0.000			
Cocus	0.192	0.000	0.000			
President	0.192	0.063	0.000			

# pLSA: Example

#### • Concepts extracted from Science Magazine articles

	universe	0.0439	drug	0.0672	cells	0.0675	sequence	0.0818	years	0.156
<b>A</b>	galaxies	0.0375	patients	0.0493	stem	0.0478	sequences	0.0493	million	0.0556
	clusters	0.0279	drugs	0.0444	human	0.0421	genome	0.033	ago	0.045
(Z	matter	0.0233	clinical	0.0346	cell	0.0309	dna	0.0257	time	0.0317
P(w z)	galaxy	0.0232	treatment	0.028	gene	0.025	sequencing	0.0172	age	0.0243
	cluster	0.0214	trials	0.0277	tissue	0.0185	map	0.0123	year	0.024
	cosmic	0.0137	therapy	0.0213	cloning	0.0169	genes	0.0122	record	0.0238
•	dark	0.0131	trial	0.0164	transfer	0.0155	chromosome	0.0119	early	0.0233
	light	0.0109	disease	0.0157	blood	0.0113	regions	0.0119	billion	0.0177
	density	0.01	medical	0.00997	embryos	0.0111	human	0.0111	history	0.0148
					_					
	bacteria	0.0983	male	0.0558	theory	0.0811	immune	0.0909	stars	0.0524
•	-		male females	0.0558 0.0541	theory physics	0.0811 0.0782	immune response	0.0909 0.0375		
<b>†</b>	bacteria	0.0983			1				stars	0.0524
$\frac{1}{2}$	bacteria bacterial	0.0983 0.0561	females	0.0541	physics	0.0782	response	0.0375	stars star	0.0524 0.0458
(w z)	bacteria bacterial resistance	0.0983 0.0561 0.0431	females female	0.0541 0.0529	physics physicists	0.0782 0.0146	response system	0.0375 0.0358	stars star astrophys	0.0524 0.0458 0.0237
P(w z)	bacteria bacterial resistance coli	0.0983 0.0561 0.0431 0.0381	females female males	0.0541 0.0529 0.0477 0.0339	physics physicists einstein	0.0782 0.0146 0.0142	response system responses	0.0375 0.0358 0.0322	stars star astrophys mass	0.0524 0.0458 0.0237 0.021
P(w z)	bacterial bacterial resistance coli strains	0.0983 0.0561 0.0431 0.0381 0.025	females female males sex	0.0541 0.0529 0.0477 0.0339	physics physicists einstein university	0.0782 0.0146 0.0142 0.013	response system responses antigen	0.0375 0.0358 0.0322 0.0263	stars star astrophys mass disk	0.0524 0.0458 0.0237 0.021 0.0173
P(w z)	bacterial bacterial resistance coli strains microbiol	0.0983 0.0561 0.0431 0.0381 0.025 0.0214	females female males sex reproductive	0.0541 0.0529 0.0477 0.0339 0.0172	physics physicists einstein university gravity	0.0782 0.0146 0.0142 0.013 0.013	response system responses antigen antigens	0.0375 0.0358 0.0322 0.0263 0.0184	stars star astrophys mass disk black	0.0524 0.0458 0.0237 0.021 0.0173 0.0161
P(w z)	bacteria bacterial resistance coli strains microbiol microbial	0.0983 0.0561 0.0431 0.0381 0.025 0.0214 0.0196	females female males sex reproductive offspring	0.0541 0.0529 0.0477 0.0339 0.0172 0.0168 0.0166	physics physicists einstein university gravity black	0.0782 0.0146 0.0142 0.013 0.013 0.0127	response system responses antigen antigens immunity	0.0375 0.0358 0.0322 0.0263 0.0184 0.0176	stars star astrophys mass disk black gas	0.0524 0.0458 0.0237 0.021 0.0173 0.0161 0.0149

### pLSA: Example

#### • Example

# ✓ Polysemy: a word may have multiple senses and multiple types of usage in different context

"segment 1"	"segment 2"	"matrix 1"	"matrix 2"	"line 1"	"line 2"	"power 1"	power 2"
imag SEGMENT texture color tissue brain slice cluster mri	speaker speech recogni signal train hmm source speakerind. SEGMENT	robust MATRIX eigenvalu uncertainti plane linear condition perturb root	manufactur cell part MATRIX cellular famili design machinepart format	constraint LINE match locat imag geometr impos segment fundament	alpha redshift LINE galaxi quasar absorp high ssup densiti	POWER spectrum omega mpc hsup larg redshift galaxi standard	load memori vlsi POWER systolic input complex arrai present
volume	sound	suffici	group	recogn	veloc	model	implement

```
Document 1, P\{z_k|d_1, w_j = \text{`segment'}\} = (0.951, 0.0001, ...)
P\{w_j = \text{`segment'}|d_1\} = 0.06
```

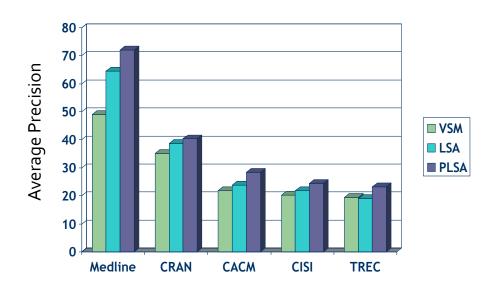
SEGMENT medic imag challeng problem field imag analysi diagnost base proper SEGMENT digit imag SEGMENT medic imag need applic involv estim boundari object classif tissu abnorm shape analysi contour detec textur SEGMENT despit exist techniqu SEGMENT specif medic imag remain crucial problem [...]

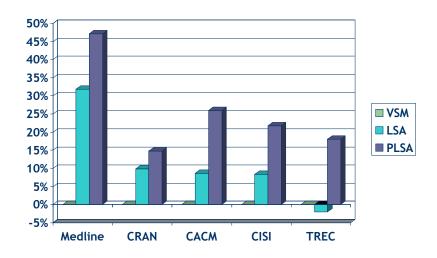
```
Document 2, P\{z_k|d_2, w_j = \text{`segment'}\} = (0.025, 0.867,...)
P\{w_j = \text{`segment'}|d_2\} = 0.010
```

consid signal origin sequenc sourc specif problem **SEGMENT** signal relat **SEGMENT** sourc address issu wide applic field report describ resolu method ergod hidden markov model hmm hmm state correspond signal sourc signal sourc sequenc determin decod procedur viterbi algorithm forward algorithm observ sequenc baumwelch train estim hmm paramet train materi applic multipl signal sourc identif problem experi perform unknown speaker identif [...]

### pLSA: Example

#### • Experimental Evaluation





- √ Consistent improvements of retrieval accuracy
- √ Relative improvement of average precision: I5-45%

