# 차원 축소

### 1.환경준비

### (1) 라이브러리 로딩

```
In [1]: !pip install plotly
         import plotly graph objects as go
         Requirement already satisfied: plotly in c:\users\user\anaconda3\lib\site-packages (5.9.0)
         Requirement already satisfied: tenacity>=6.2.0 in c:\users\user\anaconda3\lib\site-packages (f
         rom plotly) (8.2.2)
In [2]: # 기본 라이브러리 가져오기
         import pandas as pd
         import numpy as np
         import matplotlib.pyplot as plt
         import seaborn as sns
         from sklearn.model selection import train test split
         from sklearn.neighbors import KNeighborsClassifier
         from sklearn.metrics import *
         from sklearn.datasets import load_breast_cancer, load_digits, load_iris, make_swiss_roll
         from sklearn.preprocessing import MinMaxScaler
         from sklearn.decomposition import PCA
```

### (2) 샘플 데이터 생성하기

```
In [3]: # 럭비공 형태의 샘플 데이터 생성 함수

def generate_rugby_data(n_points=1000, a=1, b=1.5, c=2):
    phi = np.random.uniform(0, np.pi, n_points)
    theta = np.random.uniform(0, 2*np.pi, n_points)
    x = a * np.sin(phi) * np.cos(theta)
    y = b * np.sin(phi) * np.sin(theta)
    z = c * np.cos(phi)
    X = np.column_stack((x, y, z))
    return X

rugby = generate_rugby_data()

# 스위스를 데이터
swiss_roll, _ = make_swiss_roll(n_samples=1000, noise=0.2)
```

# 2.PCA 개념이해

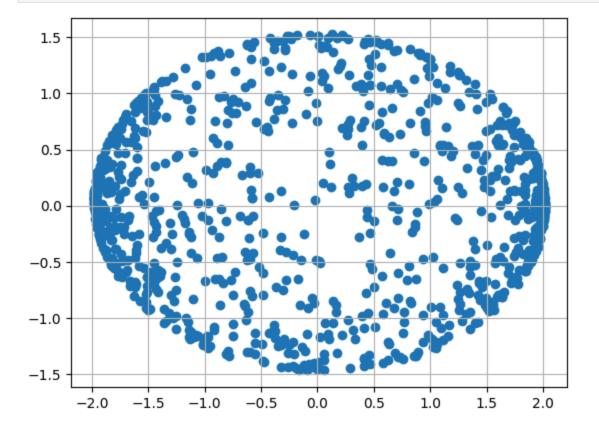
- (1) 럭비공 형태의 데이터 차원 축소
  - 원본 데이터 둘러보기

```
In [5]: my_3d_Scatter(rugby)
```

• 차원 축소

```
In [6]: # PCA를 이용하여 2개의 주성분으로 차원 축소
pca = PCA(n_components=2)
X_pca = pca.fit_transform(rugby)
# PCA 축소 데이터 조회
```

```
plt.scatter(X_pca[:, 0], X_pca[:, 1])
plt.grid()
plt.show()
```



In [ ]:

# (2) 스위스롤 형태의 데이터 차원 축소

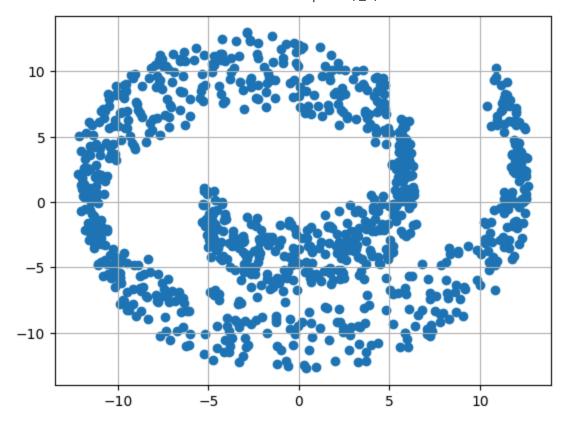
• 원본 데이터 둘러보기

In [7]: my\_3d\_Scatter(swiss\_roll)

#### • 차원 축소

```
In [8]: # PCA를 이용하여 2개의 주성분으로 차원 축소
pca = PCA(n_components=2)
X_pca = pca.fit_transform(swiss_roll)

# PCA 축소 데이터 조회
plt.scatter(X_pca[:, 0], X_pca[:, 1])
plt.grid()
plt.show()
```



# 3.PCA 사용해보기

### (1) 데이터 준비

• 데이터 로딩

```
iris = pd.read_csv("https://raw.githubusercontent.com/DA4BAM/dataset/master/iris.csv")
target = 'Species'
x = iris.drop(target, axis = 1)
y = iris.loc[:, target]
```

In [54]: x.head()

Out[54]:		Sepal.Length	Sepal.Width	Petal.Length	Petal.Width
	0	5.1	3.5	1.4	0.2
	1	4.9	3.0	1.4	0.2
	2	4.7	3.2	1.3	0.2
	3	4.6	3.1	1.5	0.2
	4	5.0	3.6	1.4	0.2

• 스케일링

```
In [55]: scaler = MinMaxScaler()
x2 = scaler.fit_transform(x)

# (옵션)데이터프레임 변환
x2 = pd.DataFrame(x2, columns= x.columns)
```

#### (2) 주성분 분석

```
In [56]: from sklearn.decomposition import PCA
         # feature 수
In [57]:
         x2.shape[1]
Out[57]:
           • 주 성분 분석 수행
In [58]: # 주성분 수 2개
         n = 2
         pca = PCA(n_components = n) # 2차원으로 축소
         # 만들고, 적용하기(결과는 넘파이 어레이)
         x2_pc = pca.fit_transform(x2)
In [59]: # 2개의 주성분
         x2_pc[:5]
         array([[-0.63070293, 0.10757791],
Out[59]:
                [-0.62290494, -0.10425983],
                [-0.6695204, -0.05141706],
                [-0.65415276, -0.10288487],
                [-0.64878806, 0.13348758]])
In [60]: # (옵션) 데이터프레임으로 변환
         x2 pc = pd.DataFrame(x2 pc, columns = ['PC1', 'PC2'])
         x2_pc.head()
                PC1
                          PC2
Out[60]:
         0 -0.630703 0.107578
         1 -0.622905 -0.104260
         2 -0.669520 -0.051417
         3 -0.654153 -0.102885
         4 -0.648788 0.133488
```

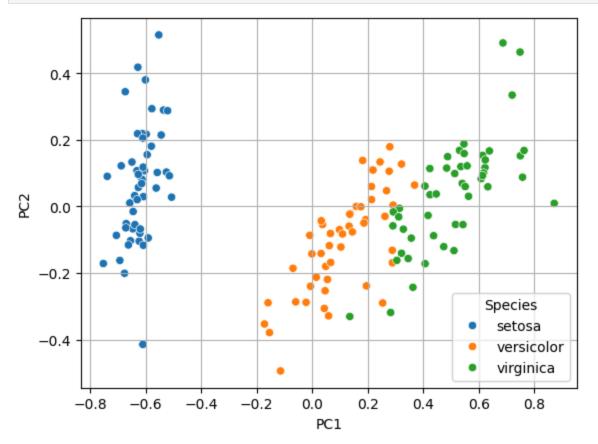
• 기존 데이터에 차원 축소된 데이터를 붙여 봅시다.

```
In [61]: pd.concat([iris, x2_pc], axis = 1).head()
```

Out[61]:		Sepal.Length	Sepal.Width	Petal.Length	Petal.Width	Species	PC1	PC2
	0	5.1	3.5	1.4	0.2	setosa	-0.630703	0.107578
	1	4.9	3.0	1.4	0.2	setosa	-0.622905	-0.104260
	2	4.7	3.2	1.3	0.2	setosa	-0.669520	-0.051417
	3	4.6	3.1	1.5	0.2	setosa	-0.654153	-0.102885
	4	5.0	3.6	1.4	0.2	setosa	-0.648788	0.133488

• 두개의 주성분 시각화

```
In [62]: sns.scatterplot(x = 'PC1', y = 'PC2', data = x2_pc, hue = y)
plt.grid()
plt.show()
```



# 4.고차원 데이터 차원축소

- (1) 데이터 준비
- 1) 데이터 로딩

```
In [63]: # breast_cancer 데이터 로딩
cancer=load_breast_cancer()
x = cancer.data
y = cancer.target
```

x = pd.DataFrame(x, columns=cancer.feature\_names)

x.shape

Out[63]:

(569, 30)

In [20]:

x.head()

Out[20]:

•		mean radius	mean texture	mean perimeter	mean area	mean smoothness	mean compactness	mean concavity	mean concave points	mean symmetry	dime
	0	17.99	10.38	122.80	1001.0	0.11840	0.27760	0.3001	0.14710	0.2419	0.
	1	20.57	17.77	132.90	1326.0	0.08474	0.07864	0.0869	0.07017	0.1812	0.
	2	19.69	21.25	130.00	1203.0	0.10960	0.15990	0.1974	0.12790	0.2069	0.
	3	11.42	20.38	77.58	386.1	0.14250	0.28390	0.2414	0.10520	0.2597	0.
	4	20.29	14.34	135.10	1297.0	0.10030	0.13280	0.1980	0.10430	0.1809	0.

5 rows × 30 columns

In [21]: x.info()

<class 'pandas.core.frame.DataFrame'>
RangeIndex: 569 entries, 0 to 568
Data columns (total 30 columns):

#	Column	Non-Null Count	Dtype
0	mean radius	569 non-null	float64
1	mean texture	569 non-null	float64
2	mean perimeter	569 non-null	float64
3	mean area	569 non-null	float64
4	mean smoothness	569 non-null	float64
5	mean compactness	569 non-null	float64
6	mean concavity	569 non-null	float64
7	mean concave points	569 non-null	float64
8	mean symmetry	569 non-null	float64
9	mean fractal dimension	569 non-null	float64
10	radius error	569 non-null	float64
11	texture error	569 non-null	float64
12	perimeter error	569 non-null	float64
13	area error	569 non-null	float64
14	smoothness error	569 non-null	float64
15	compactness error	569 non-null	float64
16	concavity error	569 non-null	float64
17	concave points error	569 non-null	float64
18	symmetry error	569 non-null	float64
19	fractal dimension error	569 non-null	float64
20	worst radius	569 non-null	float64
21	worst texture	569 non-null	float64
22	worst perimeter	569 non-null	float64
23	worst area	569 non-null	float64
24	worst smoothness	569 non-null	float64
25	worst compactness	569 non-null	float64
26	worst concavity	569 non-null	float64
27	worst concave points	569 non-null	float64
28	worst symmetry	569 non-null	float64
29	worst fractal dimension	569 non-null	float64
dtyp	es: float64(30)		

dtypes: float64(30) memory usage: 133.5 KB

In [22]: x.describe().T

Out[22]:

	count	mean	std	min	25%	50%	75%	r
mean radius	569.0	14.127292	3.524049	6.981000	11.700000	13.370000	15.780000	28.11
mean texture	569.0	19.289649	4.301036	9.710000	16.170000	18.840000	21.800000	39.28
mean perimeter	569.0	91.969033	24.298981	43.790000	75.170000	86.240000	104.100000	188.50
mean area	569.0	654.889104	351.914129	143.500000	420.300000	551.100000	782.700000	2501.00
mean smoothness	569.0	0.096360	0.014064	0.052630	0.086370	0.095870	0.105300	0.16
mean compactness	569.0	0.104341	0.052813	0.019380	0.064920	0.092630	0.130400	0.34
mean concavity	569.0	0.088799	0.079720	0.000000	0.029560	0.061540	0.130700	0.42
mean concave points	569.0	0.048919	0.038803	0.000000	0.020310	0.033500	0.074000	0.20
mean symmetry	569.0	0.181162	0.027414	0.106000	0.161900	0.179200	0.195700	0.30
mean fractal dimension	569.0	0.062798	0.007060	0.049960	0.057700	0.061540	0.066120	0.09
radius error	569.0	0.405172	0.277313	0.111500	0.232400	0.324200	0.478900	2.87
texture error	569.0	1.216853	0.551648	0.360200	0.833900	1.108000	1.474000	4.88
perimeter error	569.0	2.866059	2.021855	0.757000	1.606000	2.287000	3.357000	21.98
area error	569.0	40.337079	45.491006	6.802000	17.850000	24.530000	45.190000	542.20
smoothness error	569.0	0.007041	0.003003	0.001713	0.005169	0.006380	0.008146	0.03
compactness error	569.0	0.025478	0.017908	0.002252	0.013080	0.020450	0.032450	0.13
concavity error	569.0	0.031894	0.030186	0.000000	0.015090	0.025890	0.042050	0.39
concave points error	569.0	0.011796	0.006170	0.000000	0.007638	0.010930	0.014710	0.05
symmetry error	569.0	0.020542	0.008266	0.007882	0.015160	0.018730	0.023480	0.07
fractal dimension error	569.0	0.003795	0.002646	0.000895	0.002248	0.003187	0.004558	0.02
worst radius	569.0	16.269190	4.833242	7.930000	13.010000	14.970000	18.790000	36.04
worst texture	569.0	25.677223	6.146258	12.020000	21.080000	25.410000	29.720000	49.54
worst perimeter	569.0	107.261213	33.602542	50.410000	84.110000	97.660000	125.400000	251.20

	count	mean	std	min	25%	50%	75%	r
worst area	569.0	880.583128	569.356993	185.200000	515.300000	686.500000	1084.000000	4254.00
worst smoothness	569()	0.132369	0.022832	0.071170	0.116600	0.131300	0.146000	0.22
worst compactness	569.0	0.254265	0.157336	0.027290	0.147200	0.211900	0.339100	1.05
worst concavity	569.0	0.272188	0.208624	0.000000	0.114500	0.226700	0.382900	1.25
worst concave points	569.0	0.114606	0.065732	0.000000	0.064930	0.099930	0.161400	0.29
worst symmetry	569.0	0.290076	0.061867	0.156500	0.250400	0.282200	0.317900	0.66
worst fractal	569.0	0.083946	0.018061	0.055040	0.071460	0.080040	0.092080	0.20

#### 2) 스케일링

• 거리계산 기반 차원축소이므로 스케일링 필요

```
In [64]: scaler = MinMaxScaler()
x = scaler.fit_transform(x)

# (옵션)데이터프레임 변환
x = pd.DataFrame(x, columns=cancer.feature_names)
```

### 3) 데이터 분할

• train, validation 분할

```
In [65]: x_train, x_val, y_train, y_val = train_test_split(x, y, test_size = .3, random_state = 20)
```

### (2) 주성분 만들기

```
In [66]: from sklearn.decomposition import PCA

In [67]: # feature 수  
x_train.shape[1]

Out[67]: 30
```

• 주 성분 분석 수행

```
In [68]: # 주성분을 몇개로 할지 결정(최대값 : 전체 feature 수)
n = x_train.shape[1] # feautre 수
# 주성분 분석 선언
```

```
pca = PCA(n_components=n)

# 만들고, 적용하기

x_train_pc = pca.fit_transform(x_train)

x_val_pc = pca.transform(x_val)
```

• 편리하게 사용하기 위해 데이터프레임으로 변환

```
In [69]: # 칼럼이름 생성
          column_names = [ 'PC'+str(i+1) for i in range(n) ]
          column_names
          ['PC1',
Out[69]:
           'PC2',
           'PC3',
            'PC4',
           'PC5',
            'PC6',
            'PC7',
           'PC8',
            'PC9',
           'PC10',
           'PC11',
           'PC12',
           'PC13',
            'PC14',
           'PC15',
           'PC16',
           'PC17',
           'PC18',
           'PC19',
           'PC20',
           'PC21',
           'PC22',
           'PC23',
           'PC24',
           'PC25',
           'PC26',
            'PC27',
           'PC28',
           'PC29',
           'PC30']
In [70]: # 데이터프레임으로 변환하기
          x_train_pc = pd.DataFrame(x_train_pc, columns = column_names)
          x_val_pc = pd.DataFrame(x_val_pc, columns = column_names)
          x_train_pc
```

```
localhost:8888/lab/tree/chapter 2. 차원축소.ipynb
```

24. 4. 3. 오후 5:09 chapter 2. 차원축소

Out[70]:		PC1	PC2	PC3	PC4	PC5	PC6	PC7	PC8	PC9
	0	0.215422	0.112002	-0.208768	-0.293000	-0.032626	-0.135166	-0.022526	-0.032558	0.047827
	1	0.869455	0.174561	-0.277555	-0.177606	0.142633	-0.032379	0.224845	0.131471	0.013562
	2	-0.298314	0.259637	0.090626	0.118568	-0.017034	0.139689	-0.001580	0.037095	-0.016287
	3	0.862285	0.165837	0.061614	0.199085	0.347577	-0.180729	0.228333	-0.067238	-0.069730
	4	-0.229030	0.149323	-0.483832	0.331190	-0.096083	-0.016467	-0.082057	0.026775	0.036597
	•••									
	393	0.741352	-0.388231	0.040183	0.074092	-0.068445	0.075507	0.024218	0.060493	-0.133940
	394	0.336910	0.050769	-0.187677	-0.248374	-0.064661	0.098182	0.056833	0.054760	0.031554
	395	-0.467700	0.063227	0.217000	-0.247931	-0.060940	-0.031664	-0.024826	-0.024798	-0.032136
	396	-0.320752	0.297598	0.063923	-0.290258	0.132390	-0.028911	0.168774	-0.034643	-0.047127
	397	-0.186368	0.088527	0.156500	0.234542	0.190558	-0.095791	-0.097599	0.019651	0.044739
	398 r	ows × 30 c	olumns							

-연합문제-

- 문1) 다음의 조건으로 주성분을 추출해 봅시다.
  - 주성분 1개로 선언하고, x train을 이용해서 주성분 추출
  - 주성분 2개로 선언하고, x train을 이용해서 주성분 추출
  - 주성분 3개로 선언하고, x train을 이용해서 주성분 추출

```
In [47]: # 주성분 1개짜리
n = 1
pca = PCA(n_components = n)
# 만들고, 적용하기(결과는 넘파이 어레이)
x_train_pc_1 = pca.fit_transform(x_train)

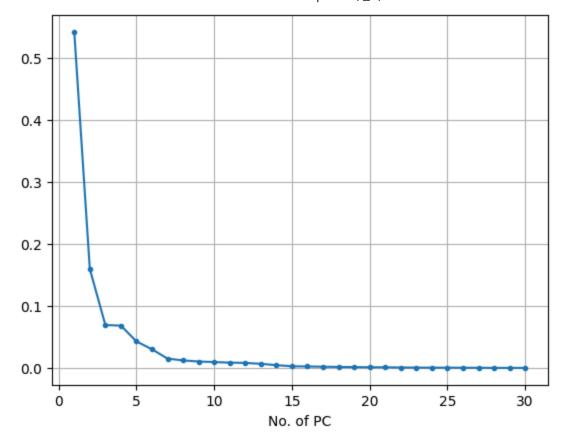
In [48]: # 주성분 2개짜리
n = 2
pca = PCA(n_components = n)
# 만들고, 적용하기(결과는 넘파이 어레이)
x_train_pc_2 = pca.fit_transform(x_train)

In [49]: # 주성분 3개짜리
n = 3
pca = PCA(n_components = n)
# 만들고, 적용하기(결과는 넘파이 어레이)
x_train_pc_3 = pca.fit_transform(x_train)
```

• 문2) 각 주성분 결과에서 상위 3개 행씩 조회하여 비교해 봅시다.

```
x_train_pc_1[:3]
In [33]:
         array([[ 0.21542202],
Out[33]:
                [ 0.86945519],
                [-0.29831397]])
         x_train_pc_2[:3]
In [34]:
          array([[ 0.21542202, 0.11200241],
Out[34]:
                [ 0.86945519, 0.1745606 ],
                [-0.29831397, 0.25963695]])
         x_train_pc_3[:2]
In [35]:
         array([[ 0.21542202, 0.11200241, -0.20876766],
Out[35]:
                [ 0.86945519, 0.1745606 , -0.27755476]])
          print(x_train_pc_1[:3])
In [36]:
          print()
          print(x train pc 2[:3])
          print()
          print(x_train_pc_3[:3])
          [[ 0.21542202]
          [ 0.86945519]
          [-0.29831397]]
          [[ 0.21542202  0.11200241]
          [ 0.86945519  0.1745606 ]
          [-0.29831397 0.25963695]]
          [[ 0.21542202  0.11200241 -0.20876766]
          [ 0.86945519  0.1745606  -0.27755476]
          [-0.29831397 0.25963695 0.09062589]]
         (3) 주성분 누적 분산 그래프
           • 그래프를 보고 적절한 주성분의 개수를 지정(elbow method!)
           • x축: PC 수
           • y축: 전체 분산크기 - 누적 분산크기
In [41]: # 주성분을 몇개로 할지 결정(최대값 : 전체 feature 수)
          n = x_{train.shape[1]}
          # 주성분 분석 선언
          pca = PCA(n_components=n)
          # 만들고, 적용하기
          x_train_pc = pca.fit_transform(x_train)
          x val pc = pca.transform(x val)
         plt.plot(range(1,n+1), pca.explained_variance_ratio_, marker = '.')
In [38]:
          plt.xlabel('No. of PC')
          plt.grid()
```

plt.show()



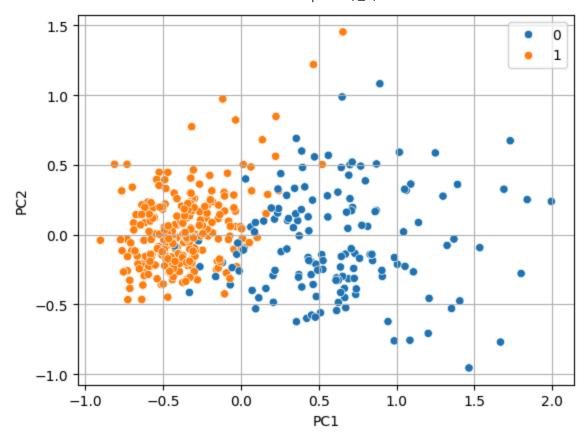
주성분 개수 몇개면 충분할까요?

In [ ]:

## (4) 시각화

• 주 성분 중 상위 2개를 뽑아 시각화 해 봅시다.

```
In [71]: sns.scatterplot(x = 'PC1', y = 'PC2', data = x_train_pc, hue = y_train)
   plt.grid()
   plt.show()
```



## 5.지도학습으로 연계하기

- (1) 원본데이터로 모델 생성하기
  - knn 알고리즘으로 분류 모델링을 수행합니다.
  - k: 기본값으로 지정
  - 학습

In [72]: model0 = KNeighborsClassifier()
model0.fit(x\_train, y\_train)

Out[72]: • KNeighborsClassifier

KNeighborsClassifier()

• 예측 및 평가

In [73]: x\_val = np.array(x\_val)

In [74]: # 원본데이터 모델의 성능
pred0 = model0.predict(x\_val)
print(confusion\_matrix(y\_val, pred0))

```
print(accuracy_score(y_val, pred0))
print(classification_report(y_val, pred0))
```

C:\Users\User\anaconda3\Lib\site-packages\sklearn\base.py:464: UserWarning:

X does not have valid feature names, but KNeighborsClassifier was fitted with feature names

```
[[ 62 2]
[ 3 104]]
```

0.9707602339181286

	precision	recall	f1-score	support
0	0.95	0.97	0.96	64
1	0.98	0.97	0.98	107
accuracy			0.97	171
macro avg	0.97	0.97	0.97	171
weighted avg	0.97	0.97	0.97	171

#### (2) 실습

- 다음의 조건으로 모델을 만들고 성능을 확인해 봅시다.
  - 알고리즘 : KNN
- 1) 주성분 상위 1개로 모델 만들기

• 주성분 1개로 만든 모델 Vs. 전체 변수로 만든 모델

```
In [78]: x_train_pc1.shape[1]
Out[78]:

In [79]: # KNW 모델링, 주성분 1개로 모델링
model1 = KNeighborsClassifier()
model1.fit(x_train, y_train)

Out[79]: KNeighborsClassifier
KNeighborsClassifier()
```

```
# 원본데이터 모델의 성능
In [80]:
          pred1 = model1.predict(x_val)
          print(confusion matrix(y val, pred1))
          print(accuracy_score(y_val, pred1))
          print(classification_report(y_val, pred1))
          [[ 62 2]
          [ 3 104]]
          0.9707602339181286
                       precision
                                  recall f1-score
                                                       support
                    0
                            0.95
                                      0.97
                                                0.96
                                                           64
                    1
                            0.98
                                      0.97
                                                0.98
                                                          107
                                                0.97
                                                          171
             accuracy
                            0.97
                                      0.97
                                                0.97
                                                          171
             macro avg
          weighted avg
                            0.97
                                      0.97
                                                0.97
                                                          171
```

C:\Users\User\anaconda3\Lib\site-packages\sklearn\base.py:464: UserWarning:

X does not have valid feature names, but KNeighborsClassifier was fitted with feature names

#### 2) 주성분 2개로 모델링

```
In [81]: n = 2
# 데이터 준비
cols = column_names[:n]
x_train_pc_n = x_train_pc.loc[:, cols]
x_val_pc_n = x_val_pc.loc[:, cols]
# 모델링
model_n = KNeighborsClassifier()
model_n.fit(x_train_pc_n, y_train)

Out[81]: 

* KNeighborsClassifier
KNeighborsClassifier()
```

```
In [84]: # 예측 pred_n = model_n.predict(x_val_pc_n)

# 평가 print(confusion_matrix(y_val, pred_n)) print(accuracy_score(y_val, pred_n)) print(classification_report(y_val, pred_n))
```

```
[[ 63 1]
[ 5 102]]
0.9649122807017544
              precision
                         recall f1-score
                                              support
           0
                   0.93
                             0.98
                                       0.95
                                                   64
           1
                   0.99
                             0.95
                                       0.97
                                                  107
    accuracy
                                       0.96
                                                  171
                   0.96
                             0.97
                                       0.96
                                                  171
   macro avg
weighted avg
                   0.97
                             0.96
                                       0.97
                                                  171
```

# 6.[추가]t-SNE

### (1) 학습(차원축소)

```
In []: from sklearn.manifold import TSNE

In []: # 2차원으로 축소하기
tsne = TSNE(n_components = 2, random_state=20)
x_tsne = tsne.fit_transform(x)

# 사용의 편리함을 위해 DataFrame으로 변환
x_tsne = pd.DataFrame(x_tsne, columns = ['T1','T2'])

In []: x_tsne.shape
```

#### (2) 시각화

```
In [ ]: plt.figure(figsize=(6,6))
    sns.scatterplot(x = 'T1', y = 'T2', data = x_tsne, hue = y)
    plt.grid()
```

### (3) 실습

- 1) 데이터 준비
  - 샘플데이터 로딩

```
In [ ]: digits = load_digits()
    x = digits.data
    y = digits.target

    y = pd.Categorical(y)
In [ ]: x.shape
```

• 둘러보기

```
In [ ]: print(x[0].reshape(8,8))

In [ ]: # f, axes = plt.subplots(5, 2, sharey=True, figsize=(16,6))
    plt.figure(figsize=(10, 4))
    for i in range(10):
        plt.subplot(2, 5, i + 1)
        plt.imshow(x[i,:].reshape([8,8]), cmap='gray');
```

• 스케일링

```
In []: # 최대, 최소값 np.min(x), np.max(x)

In []: # 최대값으로 나누면 Min Max 스케일링이 됩니다.
```

In [ ]: #  $\frac{1}{x} = \frac{1}{x} = \frac{1}$ 

#### 2) PCA

- 주성분 2개로 차원을 축소하고
- 시각화 합니다.

```
In []: # 차원 축소
pca = PCA(n_components=2)
x_pca = pca.fit_transform(x)

# 데이터프레임으로 변환(옵션)
x_pca = pd.DataFrame(x_pca, columns = ['PC1', 'PC2'])
```

```
In []: # 시각화
plt.figure(figsize=(8, 8))
sns.scatterplot(x = 'PC1', y = 'PC2', data = x_pca, hue = y)
plt.grid()
plt.show()
```

#### 3) tSNE

- 2차원으로 축소하고
- 시각화 합니다.

```
In []: tsne = TSNE(n_components = 2, random_state=20)
x_tsne = tsne.fit_transform(x)

# 데이터프레임으로 변환(옵션)
x_tsne = pd.DataFrame(x_tsne, columns = ['T1', 'T2'])
```

```
In []: # 시 각화
plt.figure(figsize=(8, 8))
sns.scatterplot(x = 'T1', y = 'T2', data = x_tsne, hue = y)
plt.grid()
plt.show()
```

In [ ]: