Assignment 5 - Kaggle Competition and Unsupervised Learning

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Note: this assignment falls under collaboration Mode 2: Individual Assignment – Collaboration Permitted. Please refer to the syllabus for additional information.

Instructions for all assignments can be found here, and is also linked to from the course syllabus.

Total points in the assignment add up to 90; an additional 10 points are allocated to presentation quality.

Learning objectives

Through completing this assignment you will be able to...

- Apply the full supervised machine learning pipeline of preprocessing, model selection, model performance evaluation and comparison, and model application to a real-world scale dataset
- Apply clustering techniques to a variety of datasets with diverse distributional properties, gaining an understanding of their strengths and weaknesses and how to tune model parameters
- 3. Apply PCA and t-SNE for performing dimensionality reduction and data visualization

1

[40 points] Kaggle Classification Competition

You've learned a great deal about supervised learning and now it's time to bring together all that you've learned. You will be competing in a Kaggle Competition along with the rest of the class! Your goal is to predict hotel reservation cancellations based on a number of potentially related factors such as lead time on the booking, time of year, type of room, special requests made, number of children, etc. While you will be asked to take certain steps along the way to your submission, you're encouraged to try creative solutions to this problem and your choices are wide open for you to make your decisions on how to best make the predictions.

IMPORTANT: Follow the link posted on Ed to register for the competition

You can view the public leaderboard anytime here

The Data. The dataset is provided as a5_q1.pkl which is a pickle file format, which allows you to load the data directly using the code below; the data can be downloaded from the Kaggle competition website. A data dictionary for the project can be found here and the original paper that describes the dataset can be found here. When you load the data, 5 matrices are provided X_train_original, y_train, and X_test_original, which are the original, unprocessed features and labels for the training set and the test features (the test labels are not provided - that's what you're predicting). Additionally, X_train_ohe and X_test_ohe are provided which are one-hot-encoded (OHE) versions of the data. The OHE versions OHE processed every categorical variable. This is provided for convenience if you find it helpful, but you're welcome to reprocess the original data other ways if your prefer.

Scoring. You will need to achieve a minimum acceptable level of performance to demonstrate proficiency with using these supervised learning techniques. Beyond that, it's an open competition and scoring in the top three places of the *private leaderboard* will result in **5 bonus points in this assignment** (and the pride of the class!). Note: the Kaggle leaderboard has a public and private component. The public component is viewable throughout the competition, but the private leaderboard is revealed at the end. When you make a submission, you immediately see your submission on the public leaderboard, but that only represents scoring on a fraction of the total collection of test data, the rest remains hidden until the end of the competition to prevent overfitting to the test data through repeated submissions. You will be be allowed to hand-select two eligible submissions for private score, or by default your best two public scoring submissions will be selected for private scoring.

Requirements:

- **(a) Explore your data.** Review and understand your data. Look at it; read up on what the features represent; think through the application domain; visualize statistics from the paper data to understand any key relationships. **There is no output required for this question**, but you are encouraged to explore the data personally before going further.
- **(b) Preprocess your data.** Preprocess your data so it's ready for use for classification and describe what you did and why you did it. Preprocessing may include: normalizing data, handling missing or erroneous values, separating out a validation dataset, preparing categorical variables through one-hot-encoding, etc. To make one step in this process easier, you're provided with a one-hot-encoded version of the data already.
 - Comment on each type of preprocessing that you apply and both how and why you apply it.
- **(c) Select, train, and compare models.** Fit at least 5 models to the data. Some of these can be experiments with different hyperparameter-tuned versions of the same model, although all 5

should not be the same type of model. There are no constraints on the types of models, but you're encouraged to explore examples we've discussed in class including:

- 1. Logistic regression
- 2. K-nearest neighbors
- 3. Random Forests
- 4. Neural networks
- 5. Support Vector Machines
- 6. Ensembles of models (e.g. model bagging, boosting, or stacking). Scikit-learn offers a number of tools for assisting with this including those for bagging, boosting, and stacking. You're also welcome to explore options beyond the sklean universe; for example, some of you may have heard of XGBoost which is a very fast implementation of gradient boosted decision trees that also allows for parallelization.

When selecting models, be aware that some models may take far longer than others to train. Monitor your output and plan your time accordingly.

Assess the classification performance AND computational efficiency of the models you selected:

- Plot the ROC curves and PR curves for your models in two plots: one of ROC curves and one of PR curves. For each of these two plots, compare the performance of the models you selected above and trained on the training data, evaluating them on the validation data. Be sure to plot the line representing random guessing on each plot. You should plot all of the model's ROC curves on a single plot and the PR curves on a single plot. One of the models should also be your BEST performing submission on the Kaggle public leaderboard (see below). In the legends of each, include the area under the curve for each model (limit to 3 significant figures). For the ROC curve, this is the AUC; for the PR curve, this is the average precision (AP).
- As you train and validate each model time how long it takes to train and validate in each case and create a plot that shows both the training and prediction time for each model included in the ROC and PR curves.
- Describe:
 - Your process of model selection and hyperparameter tuning
 - Which model performed best and your process for identifying/selecting it
- **(d) Apply your model "in practice".** Make *at least* 5 submissions of different model results to the competition (more submissions are encouraged and you can submit up to 5 per day!). These do not need to be the same that you report on above, but you should select your *most competitive* models.
 - Produce submissions by applying your model on the test data.
 - Be sure to RETRAIN YOUR MODEL ON ALL LABELED TRAINING AND VALIDATION DATA before making your predictions on the test data for submission. This will help to maximize your performance on the test data.
 - In order to get full credit on this problem you must achieve an AUC on the Kaggle public leaderboard above the "Benchmark" score on the public leaderboard.

Guidance:

- 1. Preprocessing. You may need to preprocess the data for some of these models to perform well (scaling inputs or reducing dimensionality). Some of this preprocessing may differ from model to model to achieve the best performance. A helpful tool for creating such preprocessing and model fitting pipelines is the sklearn pipeline module which lets you group a series of processing steps together.
- 2. Hyperparameters. Hyperparameters may need to be tuned for some of the model you use. You may want to perform hyperparameter tuning for some of the models. If you experiment with different hyperparameters that include many model runs, you may want to apply them to a small subsample of your overall data before running it on the larger training set to be time efficient (if you do, just make sure to ensure your selected subset is representative of the rest of your data).
- 3. **Validation data**. You're encouraged to create your own validation dataset for comparing model performance; without this, there's a significant likelihood of overfitting to the data. A common choice of the split is 80% training, 20% validation. Before you make your final predictions on the test data, be sure to retrain your model on the entire dataset.
- 4. **Training time**. This is a larger dataset than you've worked with previously in this class, so training times may be higher that what you've experienced in the past. Plan ahead and get your model pipeline working early so you can experiment with the models you use for this problem and have time to let them run.

Starter code

Below is some code for (1) loading the data and (2) once you have predictions in the form of confidence scores for those classifiers, to produce submission files for Kaggle.

```
In [ ]: import pandas as pd
      import numpy as np
      import pickle
      # Load the data
      data = pickle.load( open( "F:/Duke MIDS/705 ML/"
                          "Assignment/05/a5 q1.pkl", "rb" ) )
      y_train = data['y_train']
      X_train_original = data['X_train'] # Original dataset
      X_train_ohe = data['X_train_ohe'] # One-hot-encoded dataset
      X test original = data['X test']
      X_test_ohe = data['X_test_ohe']
      # Produce submission
      def create_submission(confidence_scores, save_path):
```

```
Parameters
------
confidence_scores : list or numpy array
    Confidence scores (from predict_proba methods from classifiers) or
    binary predictions (only recommended in cases when predict_proba is
    not available)
save_path : string
    File path for where to save the submission file.

Example:
create_submission(my_confidence_scores, './data/submission.csv')

'''
import pandas as pd

submission = pd.DataFrame({"score":confidence_scores})
submission.to_csv(save_path, index_label="id")
```

ANSWER

```
In [ ]: import numpy as np
        import pandas as pd
        import matplotlib.pyplot as plt
        import seaborn as sns
        from imblearn.over sampling import SMOTE
        from sklearn.model_selection import train_test_split
        from sklearn.model_selection import PredefinedSplit
        from sklearn.preprocessing import StandardScaler
        from sklearn.decomposition import PCA
        from sklearn.linear model import LogisticRegression
        from sklearn.neighbors import KNeighborsClassifier
        from sklearn.tree import DecisionTreeClassifier
        from sklearn.ensemble import RandomForestClassifier
        from sklearn.neural_network import MLPClassifier
        from sklearn.svm import SVC
        from xgboost import XGBClassifier
        from sklearn.model_selection import GridSearchCV
        from sklearn.model_selection import RandomizedSearchCV
        from sklearn.metrics import f1_score, roc_auc_score, \
            roc_curve, precision_recall_curve, average_precision_score
        from time import time
```

(a) Explore the data

```
In [ ]: X_train_original.head()
```

Out[]:		hotel	lead_time	arrival_date_year	arrival_date_month	$arrival_date_week_number$	arrival_date_day
	0	Resort Hotel	342	2015	July	27	
	2	Resort Hotel	7	2015	July	27	
	3	Resort Hotel	13	2015	July	27	
	4	Resort Hotel	14	2015	July	27	
	5	Resort Hotel	14	2015	July	27	

5 rows × 29 columns

In []: X_train_original.info()

<class 'pandas.core.frame.DataFrame'>
Int64Index: 95512 entries, 0 to 119389
Data columns (total 29 columns):

0hotel95512 non-nullobject1lead_time95512 non-nullint642arrival_date_year95512 non-nullint643arrival_date_month95512 non-nullobject4arrival_date_week_number95512 non-nullint645arrival_date_day_of_month95512 non-nullint646stays_in_weekend_nights95512 non-nullint647stays_in_week_nights95512 non-nullint648adults95512 non-nullint649children95510 non-nullfloat6410babies95512 non-nullobject11meal95512 non-nullobject12country95117 non-nullobject13market_segment95512 non-nullobject14distribution_channel95512 non-nullobject15is_repeated_guest95512 non-nullint6416previous_cancellations95512 non-nullint6417previous_bookings_not_canceled95512 non-nullobject19assigned_room_type95512 non-nullobject20booking_changes95512 non-nullint6421deposit_type95512 non-nullobject22agent82431 non-nullfloat6423company5453 non-nullfloat64	#	Column	Non-Null Count	Dtype
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26 adr 95512 non-null float64		adr	95512 non-null	float64
27 required_car_parking_spaces 95512 non-null int64				
28 total_of_special_requests 95512 non-null int64				int64

dtypes: float64(4), int64(15), object(10)

memory usage: 21.9+ MB

Label is slightly imbalanced, sampling method is needed

	There are 10 categorical variables and 15 humene variables								
n []:	<pre>X_train_original.describe()</pre>	. T							
Out[]:		count	mean	std	min	25%	50%	75%	
	lead_time	95512.0	103.849768	106.722804	0.00	18.00	69.0	160.0	
	arrival_date_year	95512.0	2016.157205	0.707470	2015.00	2016.00	2016.0	2017.0	i
	arrival_date_week_number	95512.0	27.152902	13.611204	1.00	16.00	27.0	38.0	
	arrival_date_day_of_month	95512.0	15.823038	8.786777	1.00	8.00	16.0	23.0	
	stays_in_weekend_nights	95512.0	0.928491	0.999940	0.00	0.00	1.0	2.0	
	stays_in_week_nights	95512.0	2.503288	1.918017	0.00	1.00	2.0	3.0	
	adults	95512.0	1.855746	0.596925	0.00	2.00	2.0	2.0	
	children	95510.0	0.103696	0.397763	0.00	0.00	0.0	0.0	
	babies	95512.0	0.007748	0.093348	0.00	0.00	0.0	0.0	
	is_repeated_guest	95512.0	0.031598	0.174929	0.00	0.00	0.0	0.0	
	previous_cancellations	95512.0	0.087235	0.844491	0.00	0.00	0.0	0.0	
	previous_bookings_not_canceled	95512.0	0.140035	1.532968	0.00	0.00	0.0	0.0	
	booking_changes	95512.0	0.220621	0.653900	0.00	0.00	0.0	0.0	
	agent	82431.0	86.893778	110.839209	1.00	9.00	14.0	229.0	
	company	5453.0	188.237117	131.459182	6.00	62.00	178.0	269.0	
	days_in_waiting_list	95512.0	2.316348	17.651287	0.00	0.00	0.0	0.0	
	adr	95512.0	101.679313	50.906371	-6.38	69.29	94.5	126.0	
	required_car_parking_spaces	95512.0	0.062673	0.246274	0.00	0.00	0.0	0.0	
	total_of_special_requests	95512.0	0.571310	0.792712	0.00	0.00	0.0	1.0	
	Label distribution:								
[]:	<pre>y_train.value_counts()</pre>								
t[]:	<pre>0 60123 1 35389 Name: is_canceled, dtype: int64</pre>								
[]:	<pre>print(f"Percentage of positive class: {y_train.value_counts()[1]\ /y_train.shape[0]*100:.2f}%") print(f"Percentage of negative class: {y_train.value_counts()[0]\ /y_train.shape[0]*100:.2f}%")</pre>								
	Percentage of positive class: 37.05% Percentage of negative class: 62.95%								

```
In [ ]: for i in X train original.columns:
          if X_train_original[i].isnull().sum()/X_train_original.shape[0]*100 > 0:
             print(f"Missing value number of {i}: {X_train_original[i].isnull().sum()}")
             print(f"Missing value percentage of {i}: \
             {X train original[i].isnull().sum()/X train original.shape[0]*100:.2f}%")
             print('='*50)
      Missing value number of children: 2
      Missing value percentage of children: 0.00%
      _____
      Missing value number of country: 395
      Missing value percentage of country: 0.41%
      _____
      Missing value number of agent: 13081
      Missing value percentage of agent: 13.70%
      _____
      Missing value number of company: 90059
      Missing value percentage of company: 94.29%
      _____
```

children, country, agent, and compay have missing values.

(b) Preprocess the data

missing values

```
In [ ]: X_train_ohe_2 = X_train_ohe.copy()
    X_train_ohe_2.fillna(0, inplace=True)
    assert X_train_ohe_2.isnull().sum().sum() == 0
```

Resampling

The lable distribution is a little imbalanced. The percentage of negative class is 62.95% while the percentage of positive class is 37.05%. I use SMOTE to resample the data.

```
In [ ]: smote = SMOTE(random_state=42)
   X_train_resampled, y_train_resampled = smote.fit_resample(X_train_ohe_2, y_train)
```

train-test-split

After resampling, I split the data into 80% training and 20% validation.

normalize

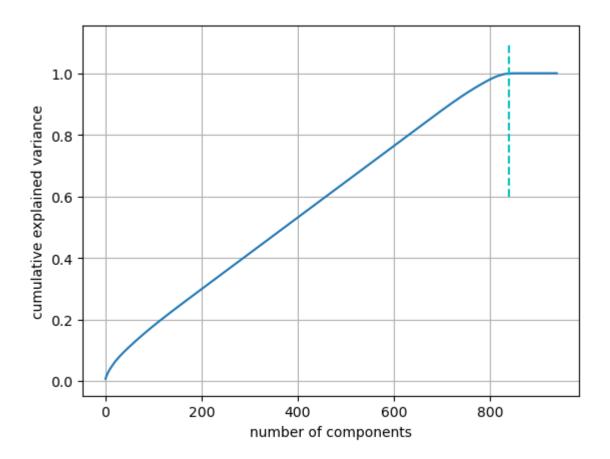
I used StandardScaler to normalize the data for dimension reduction.

```
In [ ]: stdscalar = StandardScaler()
    stdscalar.fit(Xtrain)
    Xtrain = stdscalar.transform(Xtrain)
    Xval = stdscalar.transform(Xval)

In [ ]: X_train_plus_val = np.concatenate((Xtrain, Xval), axis=0)
    y_train_plus_val = np.concatenate((ytrain, yval), axis=0)
```

Dimensionality reduction

First I plotted the cumulative explained variance ratio of all the features. I found that the first 800 features explained most of the variance. Then I applied a decision tree classifier on both the original data and the reduced data to check whether dimension reduction would affect the performance of the model.



```
In [ ]: pca= PCA(n components=840)
        pca.fit(Xtrain)
        Xtrain_pca = pca.transform(Xtrain)
        Xval_pca = pca.transform(Xval)
In [ ]: # test the effect of PCA on the performance of the model
        # decision tree
        dt = DecisionTreeClassifier(random_state=42)
        dt.fit(Xtrain, ytrain)
        print(f"Decision Tree score on training set: {dt.score(Xtrain, ytrain):.4f}")
        print(f"Decision Tree score on validation set: {dt.score(Xval, yval):.4f}")
        dt = DecisionTreeClassifier(random_state=42)
        dt.fit(Xtrain_pca, ytrain)
        print(f"Decision Tree score on training set after PCA: \
              {dt.score(Xtrain pca, ytrain):.4f}")
        print(f"Decision Tree score on validation set after PCA: \
              {dt.score(Xval_pca, yval):.4f}")
```

Decision Tree score on training set: 0.9967

Decision Tree score on validation set: 0.8756

Decision Tree score on training set after PCA: 0.9967

Decision Tree score on validation set after PCA: 0.8504

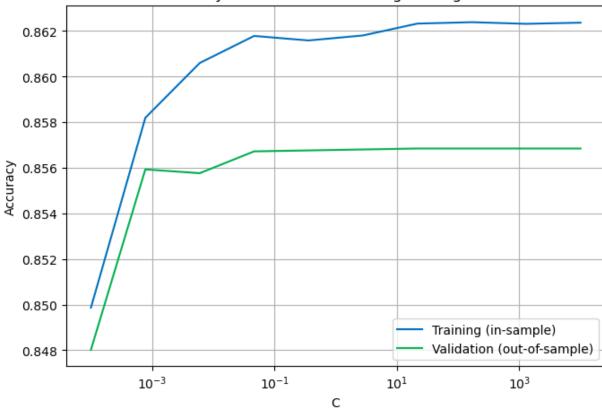
From the principal component analysis, I find that the first 800 principal components can explain most of the variance. Then I use the decision tree classifier to test the effect of dimensionality reduction. I find that the accuracy of the model is reduced from 87.56% to 85.04% on validation dataset after dimensionality reduction. So I decide **not to use pca in further analysis**.

(c) Model training

1. Logistic regression

```
In [ ]: start = time()
        LR = LogisticRegression(solver='liblinear', random state=42)
        LR.fit(Xtrain, ytrain)
        end = time()
        print(f"Time used: {end-start:.2f}s")
        print(f"Accuracy of validation set: {100*LR.score(Xval, yval):.2f}%")
        Time used: 79.60s
        Accuracy of validation set: 85.66%
In [ ]: # tuning C
        1_C = np.logspace(-4, 4, 10)
        acc_train_lr = []
        acc val lr = []
        for c in 1_C:
            LR = LogisticRegression(solver='liblinear', random_state=42, C=c)
            LR.fit(Xtrain, ytrain)
            acc train lr.append(LR.score(Xtrain, ytrain))
            acc_val_lr.append(LR.score(Xval, yval))
In [ ]: print(f"Best C: {1 C[np.argmax(acc val lr)]}")
        print(f"Best accuracy: {100*np.max(acc val lr):.2f}%")
        # plot the acc of validation set
        plt.figure(figsize=(7,5), dpi= 100)
        plt.semilogx(l_C, acc_train_lr, color = "#0070C0", label='Training (in-sample)')
        plt.semilogx(l_C, acc_val_lr, color = "#00B050", label='Validation (out-of-sample)')
        plt.legend()
        plt.grid('on')
        plt.xlabel('C')
        plt.ylabel('Accuracy')
        plt.legend()
        plt.title("Accuracy of validation set for logistic regression")
        plt.tight_layout() # Use this to maximize the use of space in the figure
        plt.show()
        Best C: 21.54434690031882
        Best accuracy: 85.68%
```

Accuracy of validation set for logistic regression



2. **KNN**

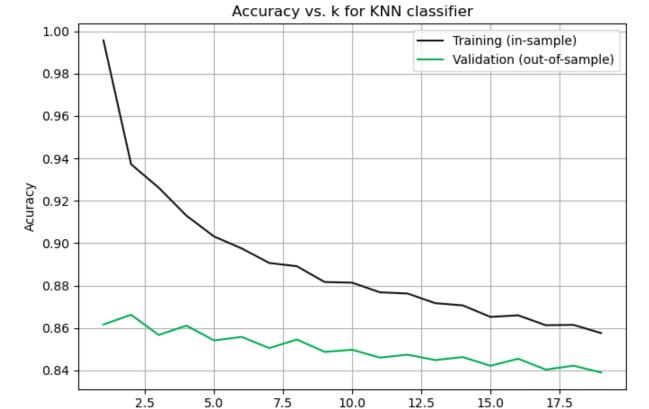
```
In []: # default setting
    start = time()
    knn = KNeighborsClassifier()
    knn.fit(Xtrain, ytrain)
    end = time()
    print(f"Accuracy of validation set: {100*knn.score(Xval, yval):.2f}%")
    print(f"Time used: {end-start:.2f}s")

Accuracy of validation set: 85.41%
    Time used: 0.52s
```

```
In []: # tuning n_neighbors
l_n_neighbors = np.arange(1, 20, 1)
acc_train_knn = []
acc_val_knn = []
for n in l_n_neighbors:
    knn = KNeighborsClassifier(n_neighbors=n)
    knn.fit(Xtrain, ytrain)
    acc_train_knn.append(knn.score(Xtrain, ytrain))
    acc_val_knn.append(knn.score(Xval, yval))
```

```
In [ ]: print(f"Best k: {l_n_neighbors[np.argmax(acc_val_knn)]}")
        print(f"Best accuracy: {100*np.max(acc_val_knn):.2f}%")
        # plot the error rate of training and test set
        plt.figure(figsize=(7,5), dpi= 100)
        plt.plot(l_n_neighbors, acc_train_knn, color = "#121619", \
                 label='Training (in-sample)')
        plt.plot(l_n_neighbors, acc_val_knn, color = '#00B050', \
                 label='Validation (out-of-sample)')
        plt.legend()
        plt.grid('on')
        plt.xlabel('k nearest neighbors')
        plt.ylabel('Acuracy')
        plt.legend()
        plt.title("Accuracy vs. k for KNN classifier")
        plt.tight_layout() # Use this to maximize the use of space in the figure
        plt.show()
```

Best k: 2
Best accuracy: 86.62%



k nearest neighbors

```
start = time()
best_knn = KNeighborsClassifier(n_neighbors=2).fit(Xtrain, ytrain)
end = time()
knn_train_time = end-start

# save the model
pickle.dump(best_knn, open('best_knn.pkl', 'wb'))

In []: start = time()
knn_pred_prob = best_knn.predict_proba(Xval)[:,1]
end = time()
knn_pred_time = end-start

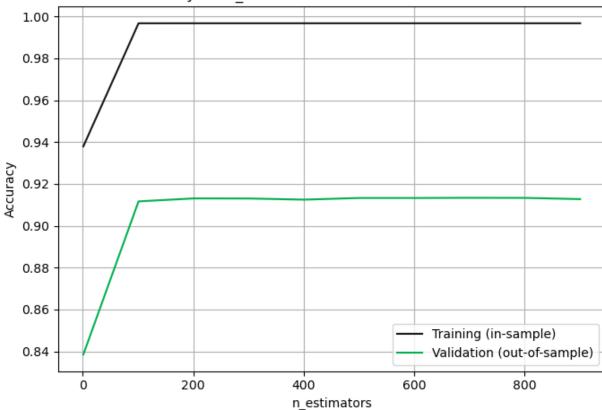
3. Random Forest

In []: # default setting
```

```
In [ ]: # default setting
        start = time()
        rfc = RandomForestClassifier(random state=42)
        rfc.fit(Xtrain, ytrain)
        end = time()
        print(f"Accuracy of validation set: {100*rfc.score(Xval, yval):.2f}%")
        print(f"Time used: {end-start:.2f}s")
        Accuracy of validation set: 91.20%
        Time used: 52.43s
In [ ]: # n_estimators
        l_n_{estimators} = np.arange(1, 1000, 100)
        acc_train_rfc = []
        acc_val_rfc = []
        for n in l_n_estimators:
            rfc = RandomForestClassifier(n estimators=n, random state=42)
            rfc.fit(Xtrain, ytrain)
            acc_train_rfc.append(rfc.score(Xtrain, ytrain))
            acc val rfc.append(rfc.score(Xval, yval))
In [ ]: | print(f"Best n_estimators: {l_n_estimators[np.argmax(acc_val_rfc)]}")
        print(f"Best accuracy: {100*np.max(acc_val_rfc):.2f}%")
        # plot the error rate of training and test set
        plt.figure(figsize=(7,5), dpi= 100)
        plt.plot(l_n_estimators, acc_train_rfc, color = "#121619",\
                  label='Training (in-sample)')
        plt.plot(l_n_estimators, acc_val_rfc, color = '#00B050',\
                  label='Validation (out-of-sample)')
        plt.legend()
        plt.grid('on')
        plt.xlabel('n_estimators')
        plt.ylabel('Accuracy')
        plt.legend()
        plt.title("Accuracy vs. n estimators for Random Forest classifier")
        plt.tight_layout() # Use this to maximize the use of space in the figure
        plt.show()
        Best n estimators: 701
```

Best n_estimators: 701 Best accuracy: 91.33%

Accuracy vs. n estimators for Random Forest classifier

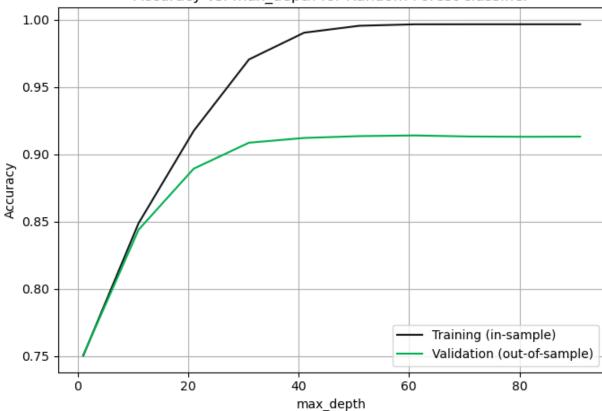


```
rfc_best = RandomForestClassifier(n_estimators=701, random_state=42)
        rfc best.fit(Xtrain, ytrain)
        print(f"Accuracy of validation set: {100*rfc_best.score(Xval, yval):.2f}%")
        Accuracy of validation set: 91.33%
In [ ]: # tunnig max_depth
        l_max_depth = np.arange(1, 100, 10)
        acc_train_rfc = []
        acc_val_rfc = []
        for n in l_max_depth:
            rfc = RandomForestClassifier(n_estimators=701, max_depth=n, random_state=42)
            rfc.fit(Xtrain, ytrain)
            acc train rfc.append(rfc.score(Xtrain, ytrain))
            acc_val_rfc.append(rfc.score(Xval, yval))
In [ ]: print(f"Best max_depth: {1_max_depth[np.argmax(acc_val_rfc)]}")
        print(f"Best accuracy: {100*np.max(acc_val_rfc):.2f}%")
        # plot the learning curve of training and test set
        plt.figure(figsize=(7,5), dpi= 100)
        plt.plot(l_max_depth, acc_train_rfc, color = "#121619",\
                  label='Training (in-sample)')
        plt.plot(l_max_depth, acc_val_rfc, color = '#00B050',\
                 label='Validation (out-of-sample)')
        plt.legend()
        plt.grid('on')
        plt.xlabel('max_depth')
        plt.ylabel('Accuracy')
        plt.legend(loc = "best")
        plt.title("Accuracy vs. max_depth for Random Forest classifier")
```

```
plt.tight_layout() # Use this to maximize the use of space in the figure
plt.show()
```

Best max_depth: 61
Best accuracy: 91.40%

Accuracy vs. max depth for Random Forest classifier



4. Neural Networks

```
In []: # default setting
    start = time()
    mlp = MLPClassifier(max_iter=500, random_state=42)
    mlp.fit(Xtrain, ytrain)
    end = time()
    mlp_train_time = end-start
    print(f"Accuracy of validation set: {100*mlp.score(Xval, yval):.2f}%")
```

```
print(f"Time used: {end-start:.2f}s")

# save the model
pickle.dump(mlp, open('mlp.pkl', 'wb'))

Accuracy of validation set: 89.27%
Time used: 1372.23s

In []: start = time()
mlp_pred_prob = mlp.predict_proba(Xval)[:,1]
end = time()
mlp_pred_time = end-start
```

Training time is too long on local machine and the accuracy is not as high as random forest classifier, so I decided not to use neural networks in further analysis.

5. Support Vector Machine

```
In []: start = time()
    svc = SVC(random_state=42, probability=True)
    svc.fit(Xtrain, ytrain)
    end = time()
    svc_train_time = end-start

    print(f"Accuracy of validation set: {100*svc.score(Xval, yval):.2f}%")
    print(f"Time used: {end-start:.2f}s")

# save the model
    pickle.dump(svc, open('svc.pkl', 'wb'))

Accuracy of validation set: 86.59%
    Time used: 19736.57s

In []: start = time()
    svc_pred_prob = svc.predict_proba(Xval)[:,1]
    end = time()
    svc_pred_time = end-start
```

It requires a long time to train the model. So I didn't decide to use it as the final model.

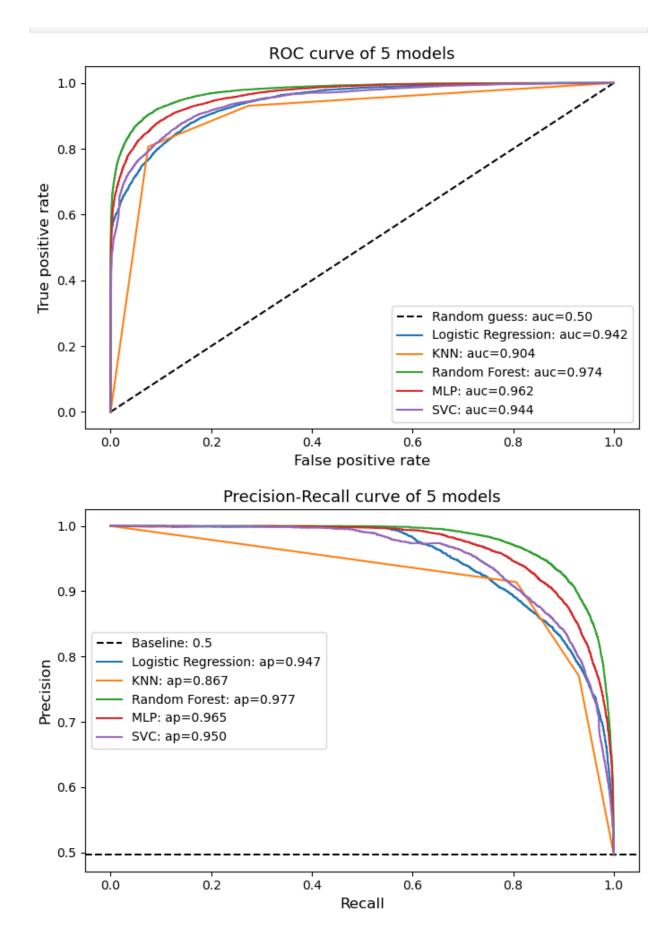
```
In [ ]:
```

Assess the classification performance AND computational efficiency of the models you selected:

• Plot the ROC curves and PR curves for your models in two plots: one of ROC curves and one of PR curves. For each of these two plots, compare the performance of the models you selected above and trained on the training data, evaluating them on the validation data. Be sure to plot the line representing random guessing on each plot. You should plot all of the model's ROC curves on a single plot and the PR curves on a single plot. One of the models should also be your BEST performing submission on the Kaggle public leaderboard (see below). In the legends of each, include the area under the curve for each model (limit to 3)

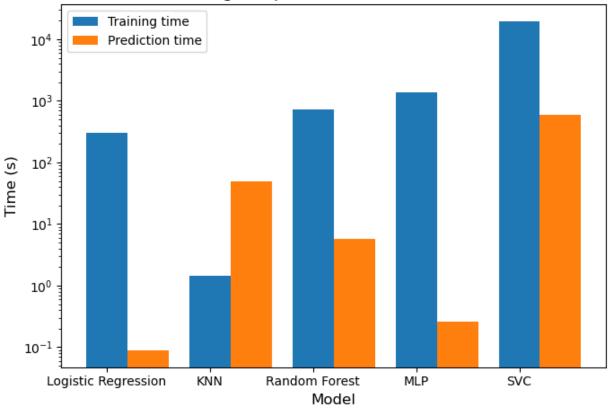
significant figures). For the ROC curve, this is the AUC; for the PR curve, this is the average precision (AP).

```
In [ ]: 1 model = [best LR, best knn, best rfc, mlp, svc]
        l_model_name = ['Logistic Regression', 'KNN', 'Random Forest', 'MLP', 'SVC']
        l_train_time = [LR_train_time, knn_train_time, \
                        rfc_train_time, mlp_train_time, svc_train_time]
        l_pred_time = [LR_pred_time, knn_pred_time, rfc_pred_time,\
                        mlp pred time, svc pred time]
        1_pred_prob = [LR_pred_prob, knn_pred_prob, rfc_pred_prob, \
                        mlp_pred_prob, svc_pred_prob]
In [ ]: # iterate through the 4 models and store info for plotting
        l_{fpr} = []
        1_tpr = []
        1 auc = []
        l precision = []
        l_recall = []
        1 ap = []
        for pred_prob in l_pred_prob:
            fpr_, tpr_, _ = roc_curve(yval, pred_prob)
            1_fpr.append(fpr_)
            1_tpr.append(tpr_)
            auc_ = roc_auc_score(yval, pred_prob)
            1_auc.append(auc_)
            # store info for plotting pr curve
            precision, recall, _ = precision_recall_curve(yval, pred_prob)
            1_precision.append(precision)
            1 recall.append(recall)
            1_ap.append(average_precision_score(yval, pred_prob))
In [ ]: plt.figure(figsize=(7, 5), dpi=100)
        plt.plot([0, 1], [0, 1], 'k--', label='Random guess: auc=0.50')
        for fpr, tpr, auc, model_name in zip(l_fpr, l_tpr, l_auc,l_model_name):
            plt.plot(fpr, tpr, label=f"{model_name}: auc={auc:.3f}")
            plt.xlabel('False positive rate', fontsize=12)
            plt.ylabel('True positive rate', fontsize=12)
            plt.title('ROC curve of 5 models', fontsize=13)
            plt.legend()
        plt.tight_layout()
        plt.show()
        # pr curve
        plt.figure(figsize=(7, 5), dpi=100)
        pr_baseline = (yval==1).sum() / len(yval)
        plt.axhline(pr_baseline, ls='--', color='k', \
                    label=f"Baseline: {round(pr_baseline,2)}")
        for precision, recall, ap, model_name in \
                             zip(l_precision, l_recall, l_ap, l_model_name):
            plt.plot(recall, precision, label=f"{model_name}: ap={ap:.3f}")
            plt.xlabel('Recall', fontsize=12)
            plt.ylabel('Precision', fontsize=12)
            plt.title('Precision-Recall curve of 5 models', fontsize=13)
            plt.legend()
        plt.tight layout()
        plt.show()
```



• As you train and validate each model time how long it takes to train and validate in each case and create a plot that shows both the training and prediction time for each model

Training and prediction time of 5 models



- Describe:
 - Your process of model selection and hyperparameter tuning
 - Which model performed best and your process for identifying/selecting it

First of all, I selected five models: logistic regression, KNN, random forest, neural networks, and support vector machine. I began with using default setting to see the performance of each model. Then I performed hyperparameter training on each model. Since I ran the training locally, I didn't use grid search or random search, just to save time. For logistic regression, I tuned the regularization parameter C. For KNN, I tuned the number of neighbors. For random

forest, I tuned the number of trees and the maximum depth of each tree. For neural network and support vector machine, it took more time than I expected to train one set of hyperparameters, and the accuracy didn't improve much compared to random forest classifier. So I didn't tune the hyperparameters for these two models.

Among the five models, **random forest classifier** has the best performance on validation dataset. The AUC is 0.974, AP is 0.977, and the accuracy is 91.40%, which are the highest among the five. It is also above the benchmark score on the public leaderboard on Kaggle. The training time is about 10 minutes and the prediction takes 5 seconds, which is not long compared to other models. So I decided to use random forest classifier as the final model.

- **(d) Apply your model "in practice".** Make *at least* 5 submissions of different model results to the competition (more submissions are encouraged and you can submit up to 5 per day!). These do not need to be the same that you report on above, but you should select your *most competitive* models.
 - Produce submissions by applying your model on the test data.
 - Be sure to RETRAIN YOUR MODEL ON ALL LABELED TRAINING AND VALIDATION DATA before making your predictions on the test data for submission. This will help to maximize your performance on the test data.
 - In order to get full credit on this problem you must achieve an AUC on the Kaggle public leaderboard above the "Benchmark" score on the public leaderboard.

```
In []: # fill missing values with 0
X_test_ohe.fillna(0, inplace=True)
assert X_test_ohe.isnull().sum().sum() == 0

# standardize the test set
X_test_ohe = stdscalar.transform(X_test_ohe)

# fit on the whole training set
best_rfc.fit(X_train_plus_val, y_train_plus_val)

# create submission file
rfc_fit_all_pred_prob = best_rfc.predict_proba(X_test_ohe)[:, 1]
create_submission(rfc_fit_all_pred_prob, 'submit.csv')
```

In []:

[25 points] Clustering

Clustering can be used to reveal structure between samples of data and assign group membership to similar groups of samples. This exercise will provide you with experience applying clustering algorithms and comparing these techniques on various datasets to experience the pros and cons of these approaches when the structure of the data being clustered varies. For this exercise, we'll explore clustering in two dimensions to make the results more tangible, but in practice these approaches can be applied to any number of dimensions.

Note: For each set of plots across the five datasets, please create subplots within a single figure (for example, when applying DBSCAN - please show the clusters resulting from DBSCAN as a single figure with one subplot for each dataset). This will make comparison easier.

- (a) Run K-means and choose the number of clusters. Five datasets are provided for you below and the code to load them below.
 - Scatterplot each dataset
 - For each dataset run the k-means algorithm for values of k ranging from 1 to 10 and for each plot the "elbow curve" where you plot dissimilarity in each case. Here, you can measure dissimilarity using the within-cluster sum-of-squares, which in sklean is known as "inertia" and can be accessed through the inertia attribute of a fit KMeans class instance.
 - For each dataset, where is the elbow in the curve of within-cluster sum-of-squares and why? Is the elbow always clearly visible? When it's not clear, you will have to use your judgment in terms of selecting a reasonable number of clusters for the data. There are also other metrics you can use to explore to measure the quality of cluster fit (but do not have to for this assignment) including the silhouette score, the Calinski-Harabasz index, and the Davies-Bouldin, to name a few within sklearn alone. However, assessing the quality of fit without "preferred" cluster assignments to compare against (that is, in a truly unsupervised manner) is challenging because measuring cluster fit quality is typically poorly-defined and doesn't generalize across all types of inter- and intra-cluster variation.
 - Plot your clustered data (different color for each cluster assignment) for your best k-means
 fit determined from both the elbow curve and your judgment for each dataset and your
 inspection of the dataset.
- **(b) Apply DBSCAN**. Vary the eps and min_samples parameters to get as close as you can to having the same number of clusters as your choices with K-means. In this case, the black points are points that were not assigned to clusters.
- (c) Apply Spectral Clustering. Select the same number of clusters as selected by k-means.

(d) Comment on the strengths and weaknesses of each approach. In particular, mention:

- Which technique worked "best" and "worst" (as defined by matching how human intuition would cluster the data) on each dataset?
- How much effort was required to get good clustering for each method (how much parameter tuning needed to be done)?

Note: For these clustering plots in this question, do NOT include legends indicating cluster assignment; instead, just make sure the cluster assignments are clear from the plot (e.g. different colors for each cluster)

Code is provided below for loading the datasets and for making plots with the clusters as distinct colors

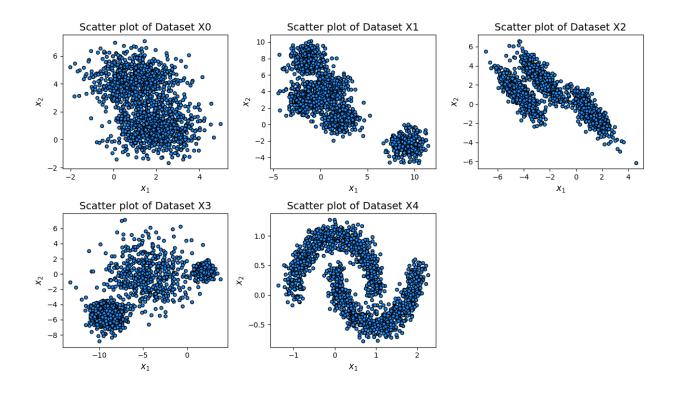
```
# Load the data
       import os
       import pandas as pd
       import numpy as np
       import matplotlib.pyplot as plt
       from sklearn.datasets import make_blobs, make_moons
       # Create / Load the datasets:
       n \text{ samples} = 1500
       X0, _ = make_blobs(n_samples=n_samples, centers=2, n_features=2, random_state=0)
       X1, _ = make_blobs(n_samples=n_samples, centers=5, n_features=2, random_state=0)
       random state = 170
       X, y = make_blobs(n_samples=n_samples, random_state=random_state, cluster_std=1.3)
       transformation = [[0.6, -0.6], [-0.2, 0.8]]
       X2 = np.dot(X, transformation)
       X3, _ = make_blobs(n_samples=n_samples, cluster_std=[1.0, 2.5, 0.5], \
                         random state=random state)
       X4, _ = make_moons(n_samples=n_samples, noise=.12)
       X = [X0, X1, X2, X3, X4]
       # The datasets are X[i], where i ranges from 0 to 4
```

```
clusters = np.unique(cluster_assignments)
n_clusters = len(clusters)
for ca in clusters:
   kwargs = \{\}
   if ca == -1:
        # if samples are not assigned to a cluster
        # (have a cluster assignment of -1, color them gray)
        kwargs = {'color':'gray'}
        n clusters = n clusters - 1
    ax.scatter(data[cluster assignments==ca, 0], \
               data[cluster_assignments==ca, 1],s=5,alpha=0.5, **kwargs)
   ax.set_xlabel('feature 1')
   ax.set_ylabel('feature 2')
   ax.set_title(f'No. Clusters = {n_clusters}')
   ax.axis('equal')
```

ANSWER

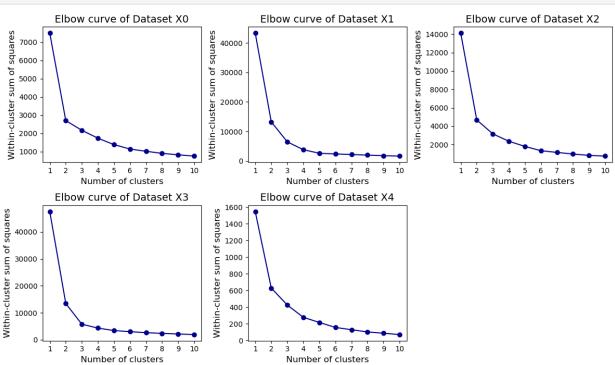
- (a) Run K-means and choose the number of clusters.

```
(i) Scatterplot each dataset
In [ ]: # plot the training data by class
        def plot_scatter(axis, X, title):
            Plot a scatter plot of the data X
            Parameters:
            axis: a matplotlib axis
            X: a pandas dataframe of size [N \times 2]
            title: a string for the title of the plot
            Return:
            None
             1.1.1
            axis.scatter(X[:, 0], X[:, 1], edgecolors='black', s=20, c='dodgerblue')
            axis.set_xlabel('$x_1$', fontsize=12)
            axis.set_ylabel('$x_2$', fontsize=12)
            axis.set_title(title, fontsize=14)
In [ ]: fig, axes = plt.subplots(2, 3, figsize=(12, 7))
        for i in range(2):
            for j in range(3):
                if i*3+j == 5:
                     break
                plot_scatter(axes[i, j], X[i*3+j], \
                              title="Scatter plot of Dataset X{}".format(i*3+j))
                axes[1, 2].axis('off')
                plt.tight_layout()
```



(ii) Run k-means algorithm for values of k ranging from 1 to 10 and for each plot the "elbow curve".

```
In [ ]: from sklearn.cluster import KMeans
        import warnings
        warnings.filterwarnings("ignore")
In [ ]: def plot_elbow(axis, X, title):
            Plot the elbow curve for KMeans clustering
            Parameters
            axis : matplotlib axis, Axis to plot on
            X : list or numpy array of size [N \times 2], Data to cluster
            title : string, Title of the plot
            WSCC = []
            for i in range(10):
                kmeans = KMeans(n_clusters=i+1, random_state=42).fit(X)
                wscc.append(kmeans.inertia_)
            # Plot the elbow curve
            axis.plot(range(1, 11), wscc, marker='o', linestyle='-', color='darkblue')
            axis.set_xticks(range(1, 11))
            axis.set_xlabel('Number of clusters', fontsize=12)
            axis.set_ylabel('Within-cluster sum of squares', fontsize=12)
            axis.set_title(title, fontsize=14)
In [ ]: # plot clustered data
        fig, axes = plt.subplots(2, 3, figsize=(12, 7))
        for i in range(2):
            for j in range(3):
                if i*3+j == 5:
                     break
```



(iii) For each dataset, where is the elbow in the curve of withincluster sum-of-squares and why? Is the elbow always clearly visible? When it's not clear, you will have to use your judgment in terms of selecting a reasonable number of clusters for the data.

- For Dataset **X0**, the best k is **2** from the elbow curve because the decrease in WCSS begins to level off after k=2
- For Dataset **X1**, the best k is not very clear from the elbow curve, but I choose k=4 using my judgement because adding more clusters to the model no longer leads to significant improvements in the clustering quality after k=4
- For Dataset **X2**, the best k is not very clear from the elbow curve, but I choose k=3 using my judgement. After the number of clusters reaches four (k=3), further increases in the number of clusters do not result in significant decrease in WCSS.
- For Dataset **X3**, the best k is **3** from the elbow curve since the level of decrease in WCSS is much less after k=3
- For Dataset **X4**, the best k is not very clear from the elbow curve, but I choose k=2 using my judgement. The decrease of WCSS begins to slow down after k=2.

(iv) Plot your clustered data (different color for each cluster assignment) for your best \$k\$-means fit determined from both the elbow curve and your judgment for each dataset and your inspection of the dataset.

```
In [ ]: def pred_y(X, n_clusters):
             Parameters
             X : list or numpy array of size [N x 2]
             n_clusters : int, Number of clusters to use for KMeans clustering
             Returns
             y_pred : list or numpy array [N]'''
             kmeans = KMeans(n_clusters=n_clusters, random_state=42).fit(X)
             return kmeans.predict(X)
In [ ]: # store cluster assignments for each dataset to a list
         l_cluster_assginments = []
         1 cluster assginments.append(pred y(X[0], 2))
         l_cluster_assginments.append(pred_y(X[1], 4))
         1_cluster_assginments.append(pred_y(X[2], 3))
         1_cluster_assginments.append(pred_y(X[3], 3))
         1_cluster_assginments.append(pred_y(X[4], 2))
In [ ]: # plot clustered data
         fig, axes = plt.subplots(2, 3, figsize=(12, 8))
         for i in range(2):
             for j in range(3):
                 if i*3+j == 5:
                      break
                 plot_cluster(axes[i,j], X[i*3+j], \
                                cluster_assignments=l_cluster_assginments[i*3+j])
                 axes[1, 2].axis('off')
                  plt.tight_layout()
                     No. Clusters = 2
                                                     No. Clusters = 4
                                                                                    No. Clusters = 3
                                           10
            0
                                            -5.0 -2.5
                                                               7.5
                                                    0.0
                                                           5.0
                                                     No. Clusters = 2
                     No. Clusters = 3
           7.5
                                           2.0
           5.0
                                           1.5
                                           1.0
           2.5
           0.0
                                           0.0
                                          -0.5
           -5.0
                                          -1.0
                                          -1.5
                        feature 1
```

After choosing the best k from both the elbow curve and my judgement, KMeans clustering

performs well on dataset X0, X1, X3, but it struggles with correctly clustering datasets X2 and X4, leading to some confusion.

(b) Apply DBSCAN. Vary the eps and min_samples parameters to get as close as you can to having the same number of clusters as your choices with K-means. In this case, the black points are points that were not assigned to clusters.

```
In [ ]: from sklearn.cluster import DBSCAN
```

Dataset X0

```
def dbscan_learning_curve(eps_range, min_samples_range, X):
    Parameters
    eps_range : list, Range of eps to use
   min_samples_range : list, Range of min_samples to use
   X: dataset to fit
    l_n_clusters = []
    l n noise = []
    for eps in eps_range:
        for min_samples in min_samples_range:
            db = DBSCAN(eps=eps, min samples=min samples).fit(X)
            labels = db.labels
            n_clusters_ = len(set(labels)) - (1 if -1 in labels else 0)
            n_noise_ = list(labels).count(-1)
            l_n_clusters.append(n_clusters_)
            l_n_noise.append(n_noise_)
            print('eps = {}, min_samples = {}'.format(eps, min_samples))
            print("Estimated number of clusters: %d" % n clusters )
            print("Estimated number of noise points: %d" % n_noise_)
```

```
In [ ]: dbscan_learning_curve(np.linspace(0.01, 1, 10), range(1, 80, 20), X[0])
```

```
eps = 0.01, min samples = 1
Estimated number of clusters: 1482
Estimated number of noise points: 0
eps = 0.01, min samples = 21
Estimated number of clusters: 0
Estimated number of noise points: 1500
eps = 0.01, min samples = 41
Estimated number of clusters: 0
Estimated number of noise points: 1500
eps = 0.01, min samples = 61
Estimated number of clusters: 0
Estimated number of noise points: 1500
eps = 0.12, min samples = 1
Estimated number of clusters: 388
Estimated number of noise points: 0
eps = 0.12, min samples = 21
Estimated number of clusters: 0
Estimated number of noise points: 1500
eps = 0.12, min samples = 41
Estimated number of clusters: 0
Estimated number of noise points: 1500
eps = 0.12, min samples = 61
Estimated number of clusters: 0
Estimated number of noise points: 1500
eps = 0.23, min_samples = 1
Estimated number of clusters: 79
Estimated number of noise points: 0
eps = 0.23, min samples = 21
Estimated number of clusters: 5
Estimated number of noise points: 1072
eps = 0.23, min_samples = 41
Estimated number of clusters: 0
Estimated number of noise points: 1500
eps = 0.23, min samples = 61
Estimated number of clusters: 0
Estimated number of noise points: 1500
eps = 0.34, min_samples = 1
Estimated number of clusters: 29
Estimated number of noise points: 0
eps = 0.34, min samples = 21
Estimated number of clusters: 2
Estimated number of noise points: 362
eps = 0.34, min samples = 41
Estimated number of clusters: 2
Estimated number of noise points: 967
eps = 0.34, min samples = 61
Estimated number of clusters: 0
Estimated number of noise points: 1500
eps = 0.45, min_samples = 1
Estimated number of clusters: 12
Estimated number of noise points: 0
eps = 0.45, min samples = 21
Estimated number of clusters: 1
Estimated number of noise points: 129
eps = 0.45, min samples = 41
Estimated number of clusters: 2
Estimated number of noise points: 380
```

```
eps = 0.45, min samples = 61
Estimated number of clusters: 2
Estimated number of noise points: 742
eps = 0.56, min samples = 1
Estimated number of clusters: 5
Estimated number of noise points: 0
eps = 0.56, min samples = 21
Estimated number of clusters: 1
Estimated number of noise points: 54
eps = 0.56, min samples = 41
Estimated number of clusters: 1
Estimated number of noise points: 145
eps = 0.56, min samples = 61
Estimated number of clusters: 2
Estimated number of noise points: 304
eps = 0.67, min samples = 1
Estimated number of clusters: 3
Estimated number of noise points: 0
eps = 0.67, min samples = 21
Estimated number of clusters: 1
Estimated number of noise points: 22
eps = 0.67, min samples = 41
Estimated number of clusters: 1
Estimated number of noise points: 70
eps = 0.67, min_samples = 61
Estimated number of clusters: 1
Estimated number of noise points: 118
eps = 0.78, min samples = 1
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.78, min_samples = 21
Estimated number of clusters: 1
Estimated number of noise points: 9
eps = 0.78, min samples = 41
Estimated number of clusters: 1
Estimated number of noise points: 29
eps = 0.78, min_samples = 61
Estimated number of clusters: 1
Estimated number of noise points: 59
eps = 0.89, min samples = 1
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.89, min samples = 21
Estimated number of clusters: 1
Estimated number of noise points: 2
eps = 0.89, min samples = 41
Estimated number of clusters: 1
Estimated number of noise points: 11
eps = 0.89, min_samples = 61
Estimated number of clusters: 1
Estimated number of noise points: 25
eps = 1.0, min samples = 1
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 1.0, min samples = 21
Estimated number of clusters: 1
Estimated number of noise points: 0
```

```
eps = 1.0, min_samples = 41
Estimated number of clusters: 1
Estimated number of noise points: 4
eps = 1.0, min_samples = 61
Estimated number of clusters: 1
Estimated number of noise points: 11
```

When eps = 0.56, min_samples = 61, estimated number of clusters is 2, and the estimated number of noise points is the smallest (304).

 $\mathsf{Dataset}\ X1$

```
In [ ]: dbscan_learning_curve(np.linspace(0.01, 2, 10), range(1, 80, 10), X[1])
```

```
eps = 0.01, min samples = 1
Estimated number of clusters: 1492
Estimated number of noise points: 0
eps = 0.01, min samples = 11
Estimated number of clusters: 0
Estimated number of noise points: 1500
eps = 0.01, min samples = 21
Estimated number of clusters: 0
Estimated number of noise points: 1500
eps = 0.01, min samples = 31
Estimated number of clusters: 0
Estimated number of noise points: 1500
eps = 0.01, min samples = 41
Estimated number of clusters: 0
Estimated number of noise points: 1500
eps = 0.01, min samples = 51
Estimated number of clusters: 0
Estimated number of noise points: 1500
eps = 0.01, min samples = 61
Estimated number of clusters: 0
Estimated number of noise points: 1500
eps = 0.01, min samples = 71
Estimated number of clusters: 0
Estimated number of noise points: 1500
eps = 0.23111111111111113, min_samples = 1
Estimated number of clusters: 217
Estimated number of noise points: 0
eps = 0.231111111111111113, min samples = 11
Estimated number of clusters: 18
Estimated number of noise points: 1216
eps = 0.231111111111111113, min samples = 21
Estimated number of clusters: 0
Estimated number of noise points: 1500
Estimated number of clusters: 0
Estimated number of noise points: 1500
eps = 0.231111111111111113, min samples = 41
Estimated number of clusters: 0
Estimated number of noise points: 1500
eps = 0.231111111111111113, min samples = 51
Estimated number of clusters: 0
Estimated number of noise points: 1500
eps = 0.231111111111111113, min samples = 61
Estimated number of clusters: 0
Estimated number of noise points: 1500
eps = 0.231111111111111113, min samples = 71
Estimated number of clusters: 0
Estimated number of noise points: 1500
eps = 0.4522222222222225, min samples = 1
Estimated number of clusters: 33
Estimated number of noise points: 0
eps = 0.452222222222225, min samples = 11
Estimated number of clusters: 4
Estimated number of noise points: 164
eps = 0.4522222222222225, min samples = 21
Estimated number of clusters: 4
Estimated number of noise points: 492
```

```
eps = 0.452222222222225, min samples = 31
Estimated number of clusters: 8
Estimated number of noise points: 986
eps = 0.4522222222222225, min samples = 41
Estimated number of clusters: 1
Estimated number of noise points: 1448
eps = 0.452222222222225, min samples = 51
Estimated number of clusters: 0
Estimated number of noise points: 1500
eps = 0.4522222222222225, min samples = 61
Estimated number of clusters: 0
Estimated number of noise points: 1500
eps = 0.45222222222225, min samples = 71
Estimated number of clusters: 0
Estimated number of noise points: 1500
Estimated number of clusters: 11
Estimated number of noise points: 0
Estimated number of clusters: 2
Estimated number of noise points: 33
Estimated number of clusters: 2
Estimated number of noise points: 93
eps = 0.6733333333333333, min_samples = 31
Estimated number of clusters: 3
Estimated number of noise points: 174
Estimated number of clusters: 4
Estimated number of noise points: 339
Estimated number of clusters: 4
Estimated number of noise points: 517
Estimated number of clusters: 5
Estimated number of noise points: 791
Estimated number of clusters: 3
Estimated number of noise points: 1279
eps = 0.89444444444445, min samples = 1
Estimated number of clusters: 6
Estimated number of noise points: 0
eps = 0.894444444444445, min samples = 11
Estimated number of clusters: 2
Estimated number of noise points: 8
eps = 0.894444444444445, min samples = 21
Estimated number of clusters: 2
Estimated number of noise points: 18
eps = 0.89444444444445, min samples = 31
Estimated number of clusters: 2
Estimated number of noise points: 32
eps = 0.894444444444445, min samples = 41
Estimated number of clusters: 3
Estimated number of noise points: 59
eps = 0.89444444444445, min samples = 51
Estimated number of clusters: 3
Estimated number of noise points: 90
```

```
eps = 0.894444444444445, min samples = 61
Estimated number of clusters: 3
Estimated number of noise points: 161
eps = 0.8944444444444445, min samples = 71
Estimated number of clusters: 4
Estimated number of noise points: 212
eps = 1.1155555555555556, min samples = 1
Estimated number of clusters: 4
Estimated number of noise points: 0
eps = 1.11555555555555556, min samples = 11
Estimated number of clusters: 2
Estimated number of noise points: 2
eps = 1.1155555555555556, min samples = 21
Estimated number of clusters: 2
Estimated number of noise points: 4
eps = 1.1155555555555556, min samples = 31
Estimated number of clusters: 2
Estimated number of noise points: 9
eps = 1.1155555555555556, min samples = 41
Estimated number of clusters: 2
Estimated number of noise points: 11
eps = 1.1155555555555556, min samples = 51
Estimated number of clusters: 2
Estimated number of noise points: 19
eps = 1.1155555555555556, min_samples = 61
Estimated number of clusters: 2
Estimated number of noise points: 30
eps = 1.1155555555555556, min samples = 71
Estimated number of clusters: 3
Estimated number of noise points: 44
eps = 1.3366666666666667, min_samples = 1
Estimated number of clusters: 3
Estimated number of noise points: 0
eps = 1.33666666666666667, min samples = 11
Estimated number of clusters: 2
Estimated number of noise points: 1
eps = 1.3366666666666667, min_samples = 21
Estimated number of clusters: 2
Estimated number of noise points: 1
eps = 1.3366666666666667, min samples = 31
Estimated number of clusters: 2
Estimated number of noise points: 1
eps = 1.33666666666666667, min_samples = 41
Estimated number of clusters: 2
Estimated number of noise points: 2
eps = 1.3366666666666667, min samples = 51
Estimated number of clusters: 2
Estimated number of noise points: 3
eps = 1.33666666666666667, min_samples = 61
Estimated number of clusters: 2
Estimated number of noise points: 6
eps = 1.33666666666666667, min samples = 71
Estimated number of clusters: 2
Estimated number of noise points: 9
eps = 1.5577777777778, min samples = 1
Estimated number of clusters: 2
Estimated number of noise points: 0
```

```
eps = 1.5577777777778, min samples = 11
Estimated number of clusters: 2
Estimated number of noise points: 0
eps = 1.55777777777778, min samples = 21
Estimated number of clusters: 2
Estimated number of noise points: 0
eps = 1.5577777777778, min samples = 31
Estimated number of clusters: 2
Estimated number of noise points: 0
eps = 1.5577777777778, min samples = 41
Estimated number of clusters: 2
Estimated number of noise points: 0
eps = 1.5577777777778, min samples = 51
Estimated number of clusters: 2
Estimated number of noise points: 0
eps = 1.5577777777778, min samples = 61
Estimated number of clusters: 2
Estimated number of noise points: 0
eps = 1.5577777777778, min samples = 71
Estimated number of clusters: 2
Estimated number of noise points: 0
eps = 1.77888888888889, min samples = 1
Estimated number of clusters: 2
Estimated number of noise points: 0
eps = 1.77888888888889, min_samples = 11
Estimated number of clusters: 2
Estimated number of noise points: 0
eps = 1.77888888888889, min samples = 21
Estimated number of clusters: 2
Estimated number of noise points: 0
eps = 1.77888888888889, min samples = 31
Estimated number of clusters: 2
Estimated number of noise points: 0
eps = 1.77888888888889, min samples = 41
Estimated number of clusters: 2
Estimated number of noise points: 0
eps = 1.77888888888889, min samples = 51
Estimated number of clusters: 2
Estimated number of noise points: 0
eps = 1.77888888888889, min samples = 61
Estimated number of clusters: 2
Estimated number of noise points: 0
eps = 1.77888888888889, min_samples = 71
Estimated number of clusters: 2
Estimated number of noise points: 0
eps = 2.0, min samples = 1
Estimated number of clusters: 2
Estimated number of noise points: 0
eps = 2.0, min_samples = 11
Estimated number of clusters: 2
Estimated number of noise points: 0
eps = 2.0, min samples = 21
Estimated number of clusters: 2
Estimated number of noise points: 0
eps = 2.0, min samples = 31
Estimated number of clusters: 2
Estimated number of noise points: 0
```

```
eps = 2.0, min_samples = 41
Estimated number of clusters: 2
Estimated number of noise points: 0
eps = 2.0, min_samples = 51
Estimated number of clusters: 2
Estimated number of noise points: 0
eps = 2.0, min_samples = 61
Estimated number of clusters: 2
Estimated number of noise points: 0
eps = 2.0, min_samples = 71
Estimated number of clusters: 2
Estimated number of clusters: 2
Estimated number of noise points: 0
```

When eps = 0.89, min_samples = 71, estimated number of clusters is 4, and the estimated number of noise points is 212.

Dataset X2

```
In [ ]: dbscan_learning_curve(np.linspace(0.01, 1, 10), range(1, 40, 10), X[2])
```

```
eps = 0.01, min samples = 1
Estimated number of clusters: 1479
Estimated number of noise points: 0
eps = 0.01, min samples = 11
Estimated number of clusters: 0
Estimated number of noise points: 1500
eps = 0.01, min samples = 21
Estimated number of clusters: 0
Estimated number of noise points: 1500
eps = 0.01, min samples = 31
Estimated number of clusters: 0
Estimated number of noise points: 1500
eps = 0.12, min samples = 1
Estimated number of clusters: 378
Estimated number of noise points: 0
eps = 0.12, min samples = 11
Estimated number of clusters: 7
Estimated number of noise points: 1413
eps = 0.12, min samples = 21
Estimated number of clusters: 0
Estimated number of noise points: 1500
eps = 0.12, min samples = 31
Estimated number of clusters: 0
Estimated number of noise points: 1500
eps = 0.23, min_samples = 1
Estimated number of clusters: 92
Estimated number of noise points: 0
eps = 0.23, min samples = 11
Estimated number of clusters: 6
Estimated number of noise points: 367
eps = 0.23, min_samples = 21
Estimated number of clusters: 7
Estimated number of noise points: 1063
eps = 0.23, min samples = 31
Estimated number of clusters: 1
Estimated number of noise points: 1460
eps = 0.34, min_samples = 1
Estimated number of clusters: 28
Estimated number of noise points: 0
eps = 0.34, min samples = 11
Estimated number of clusters: 4
Estimated number of noise points: 127
eps = 0.34, min samples = 21
Estimated number of clusters: 3
Estimated number of noise points: 322
eps = 0.34, min samples = 31
Estimated number of clusters: 3
Estimated number of noise points: 537
eps = 0.45, min_samples = 1
Estimated number of clusters: 9
Estimated number of noise points: 0
eps = 0.45, min samples = 11
Estimated number of clusters: 2
Estimated number of noise points: 49
eps = 0.45, min samples = 21
Estimated number of clusters: 3
Estimated number of noise points: 128
```

```
eps = 0.45, min samples = 31
Estimated number of clusters: 3
Estimated number of noise points: 225
eps = 0.56, min samples = 1
Estimated number of clusters: 4
Estimated number of noise points: 0
eps = 0.56, min samples = 11
Estimated number of clusters: 1
Estimated number of noise points: 23
eps = 0.56, min samples = 21
Estimated number of clusters: 3
Estimated number of noise points: 45
eps = 0.56, min samples = 31
Estimated number of clusters: 3
Estimated number of noise points: 87
eps = 0.67, min samples = 1
Estimated number of clusters: 4
Estimated number of noise points: 0
eps = 0.67, min samples = 11
Estimated number of clusters: 1
Estimated number of noise points: 16
eps = 0.67, min samples = 21
Estimated number of clusters: 1
Estimated number of noise points: 21
eps = 0.67, min_samples = 31
Estimated number of clusters: 2
Estimated number of noise points: 41
eps = 0.78, min samples = 1
Estimated number of clusters: 4
Estimated number of noise points: 0
eps = 0.78, min_samples = 11
Estimated number of clusters: 1
Estimated number of noise points: 10
eps = 0.78, min samples = 21
Estimated number of clusters: 1
Estimated number of noise points: 14
eps = 0.78, min_samples = 31
Estimated number of clusters: 1
Estimated number of noise points: 22
eps = 0.89, min samples = 1
Estimated number of clusters: 3
Estimated number of noise points: 0
eps = 0.89, min samples = 11
Estimated number of clusters: 1
Estimated number of noise points: 5
eps = 0.89, min samples = 21
Estimated number of clusters: 1
Estimated number of noise points: 10
eps = 0.89, min_samples = 31
Estimated number of clusters: 1
Estimated number of noise points: 15
eps = 1.0, min samples = 1
Estimated number of clusters: 3
Estimated number of noise points: 0
eps = 1.0, min samples = 11
Estimated number of clusters: 1
Estimated number of noise points: 3
```

```
eps = 1.0, min_samples = 21
Estimated number of clusters: 1
Estimated number of noise points: 6
eps = 1.0, min_samples = 31
Estimated number of clusters: 1
Estimated number of noise points: 11
```

When eps = 0.56, min_samples = 31, estimated number of clusters is 3, and the estimated number of noise points is 87.

 $\mathsf{Dataset}\ X3$

```
In [ ]: dbscan_learning_curve(np.linspace(0.01, 1, 10), range(1, 40, 10), X[3])
```

```
eps = 0.01, min samples = 1
Estimated number of clusters: 1480
Estimated number of noise points: 0
eps = 0.01, min samples = 11
Estimated number of clusters: 0
Estimated number of noise points: 1500
eps = 0.01, min samples = 21
Estimated number of clusters: 0
Estimated number of noise points: 1500
eps = 0.01, min samples = 31
Estimated number of clusters: 0
Estimated number of noise points: 1500
eps = 0.12, min samples = 1
Estimated number of clusters: 708
Estimated number of noise points: 0
eps = 0.12, min samples = 11
Estimated number of clusters: 3
Estimated number of noise points: 1246
eps = 0.12, min samples = 21
Estimated number of clusters: 1
Estimated number of noise points: 1421
eps = 0.12, min samples = 31
Estimated number of clusters: 0
Estimated number of noise points: 1500
eps = 0.23, min_samples = 1
Estimated number of clusters: 351
Estimated number of noise points: 0
eps = 0.23, min samples = 11
Estimated number of clusters: 5
Estimated number of noise points: 821
eps = 0.23, min_samples = 21
Estimated number of clusters: 1
Estimated number of noise points: 1088
eps = 0.23, min samples = 31
Estimated number of clusters: 1
Estimated number of noise points: 1175
eps = 0.34, min_samples = 1
Estimated number of clusters: 164
Estimated number of noise points: 0
eps = 0.34, min samples = 11
Estimated number of clusters: 2
Estimated number of noise points: 616
eps = 0.34, min samples = 21
Estimated number of clusters: 3
Estimated number of noise points: 750
eps = 0.34, min samples = 31
Estimated number of clusters: 2
Estimated number of noise points: 1002
eps = 0.45, min_samples = 1
Estimated number of clusters: 90
Estimated number of noise points: 0
eps = 0.45, min samples = 11
Estimated number of clusters: 9
Estimated number of noise points: 424
eps = 0.45, min samples = 21
Estimated number of clusters: 2
Estimated number of noise points: 609
```

```
eps = 0.45, min samples = 31
Estimated number of clusters: 2
Estimated number of noise points: 693
eps = 0.56, min samples = 1
Estimated number of clusters: 53
Estimated number of noise points: 0
eps = 0.56, min samples = 11
Estimated number of clusters: 5
Estimated number of noise points: 263
eps = 0.56, min samples = 21
Estimated number of clusters: 2
Estimated number of noise points: 535
eps = 0.56, min samples = 31
Estimated number of clusters: 2
Estimated number of noise points: 582
eps = 0.67, min samples = 1
Estimated number of clusters: 40
Estimated number of noise points: 0
eps = 0.67, min samples = 11
Estimated number of clusters: 4
Estimated number of noise points: 142
eps = 0.67, min samples = 21
Estimated number of clusters: 4
Estimated number of noise points: 431
eps = 0.67, min_samples = 31
Estimated number of clusters: 2
Estimated number of noise points: 528
eps = 0.78, min samples = 1
Estimated number of clusters: 27
Estimated number of noise points: 0
eps = 0.78, min_samples = 11
Estimated number of clusters: 4
Estimated number of noise points: 100
eps = 0.78, min samples = 21
Estimated number of clusters: 4
Estimated number of noise points: 261
eps = 0.78, min_samples = 31
Estimated number of clusters: 2
Estimated number of noise points: 507
eps = 0.89, min samples = 1
Estimated number of clusters: 21
Estimated number of noise points: 0
eps = 0.89, min samples = 11
Estimated number of clusters: 3
Estimated number of noise points: 64
eps = 0.89, min samples = 21
Estimated number of clusters: 3
Estimated number of noise points: 151
eps = 0.89, min_samples = 31
Estimated number of clusters: 5
Estimated number of noise points: 327
eps = 1.0, min samples = 1
Estimated number of clusters: 11
Estimated number of noise points: 0
eps = 1.0, min samples = 11
Estimated number of clusters: 1
Estimated number of noise points: 46
```

```
eps = 1.0, min_samples = 21
Estimated number of clusters: 3
Estimated number of noise points: 106
eps = 1.0, min_samples = 31
Estimated number of clusters: 3
Estimated number of noise points: 179
```

When eps = 0.89, min_samples = 11, estimated number of clusters is 3, and the estimated number of noise points is 64.

Dataset X4

```
In [ ]: dbscan_learning_curve(np.linspace(0.01, 1, 10), range(1, 40, 5), X[4])
```

```
eps = 0.01, min samples = 1
Estimated number of clusters: 1381
Estimated number of noise points: 0
eps = 0.01, min samples = 6
Estimated number of clusters: 0
Estimated number of noise points: 1500
eps = 0.01, min samples = 11
Estimated number of clusters: 0
Estimated number of noise points: 1500
eps = 0.01, min samples = 16
Estimated number of clusters: 0
Estimated number of noise points: 1500
eps = 0.01, min samples = 21
Estimated number of clusters: 0
Estimated number of noise points: 1500
eps = 0.01, min samples = 26
Estimated number of clusters: 0
Estimated number of noise points: 1500
eps = 0.01, min samples = 31
Estimated number of clusters: 0
Estimated number of noise points: 1500
eps = 0.01, min samples = 36
Estimated number of clusters: 0
Estimated number of noise points: 1500
eps = 0.12, min_samples = 1
Estimated number of clusters: 7
Estimated number of noise points: 0
eps = 0.12, min samples = 6
Estimated number of clusters: 1
Estimated number of noise points: 14
eps = 0.12, min_samples = 11
Estimated number of clusters: 2
Estimated number of noise points: 30
eps = 0.12, min samples = 16
Estimated number of clusters: 2
Estimated number of noise points: 62
eps = 0.12, min_samples = 21
Estimated number of clusters: 2
Estimated number of noise points: 106
eps = 0.12, min samples = 26
Estimated number of clusters: 2
Estimated number of noise points: 186
eps = 0.12, min_samples = 31
Estimated number of clusters: 9
Estimated number of noise points: 393
eps = 0.12, min samples = 36
Estimated number of clusters: 10
Estimated number of noise points: 868
eps = 0.23, min_samples = 1
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.23, min samples = 6
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.23, min samples = 11
Estimated number of clusters: 1
Estimated number of noise points: 0
```

```
eps = 0.23, min samples = 16
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.23, min samples = 21
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.23, min samples = 26
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.23, min samples = 31
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.23, min samples = 36
Estimated number of clusters: 1
Estimated number of noise points: 1
eps = 0.34, min samples = 1
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.34, min samples = 6
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.34, min samples = 11
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.34, min_samples = 16
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.34, min samples = 21
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.34, min_samples = 26
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.34, min samples = 31
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.34, min_samples = 36
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.45, min samples = 1
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.45, min samples = 6
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.45, min samples = 11
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.45, min_samples = 16
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.45, min samples = 21
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.45, min samples = 26
Estimated number of clusters: 1
Estimated number of noise points: 0
```

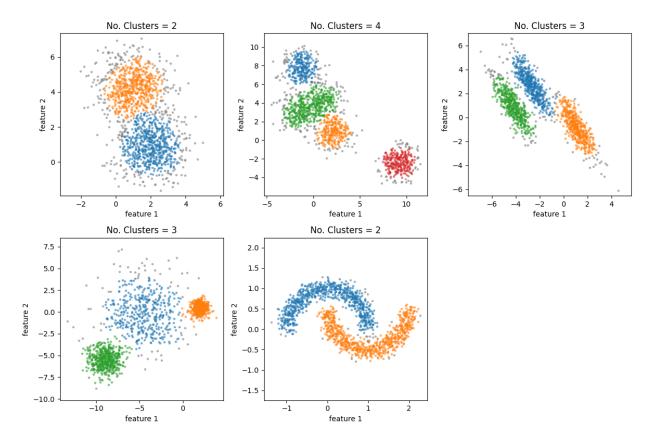
```
eps = 0.45, min samples = 31
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.45, min samples = 36
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.56, min samples = 1
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.56, min samples = 6
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.56, min samples = 11
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.56, min samples = 16
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.56, min samples = 21
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.56, min samples = 26
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.56, min_samples = 31
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.56, min samples = 36
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.67, min_samples = 1
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.67, min samples = 6
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.67, min_samples = 11
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.67, min samples = 16
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.67, min_samples = 21
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.67, min samples = 26
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.67, min_samples = 31
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.67, min samples = 36
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.78, min samples = 1
Estimated number of clusters: 1
Estimated number of noise points: 0
```

```
eps = 0.78, min samples = 6
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.78, min samples = 11
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.78, min samples = 16
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.78, min samples = 21
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.78, min samples = 26
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.78, min samples = 31
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.78, min samples = 36
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.89, min samples = 1
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.89, min_samples = 6
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.89, min samples = 11
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.89, min_samples = 16
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.89, min samples = 21
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.89, min_samples = 26
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.89, min samples = 31
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 0.89, min samples = 36
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 1.0, min samples = 1
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 1.0, min samples = 6
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 1.0, min samples = 11
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 1.0, min samples = 16
Estimated number of clusters: 1
Estimated number of noise points: 0
```

```
eps = 1.0, min_samples = 21
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 1.0, min_samples = 26
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 1.0, min_samples = 31
Estimated number of clusters: 1
Estimated number of noise points: 0
eps = 1.0, min_samples = 36
Estimated number of clusters: 1
Estimated number of clusters: 1
Estimated number of noise points: 0
```

When eps = 0.12, min_samples = 11, estimated number of clusters is 3, and the estimated number of noise points is 30.

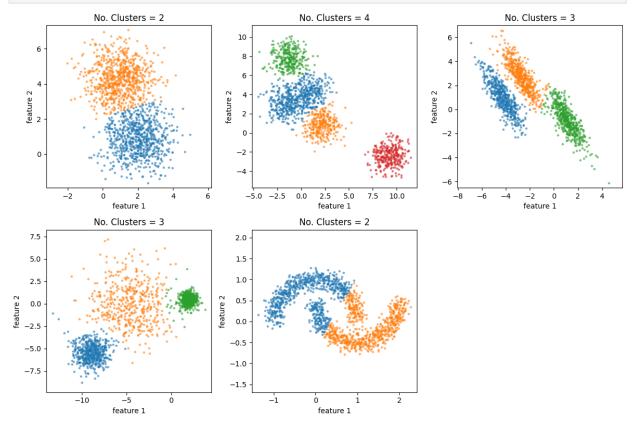
```
In [ ]: # final DBSCAN clustering for each dataset
        db x0 = DBSCAN(eps=0.56, min samples=61).fit(X[0])
        clusters_x0 = db_x0.fit_predict(X[0])
        db x1 = DBSCAN(eps=0.89, min samples=71).fit(X[1])
        clusters_x1 = db_x1.fit_predict(X[1])
        db x2 = DBSCAN(eps=0.56, min samples=31).fit(X[2])
        clusters_x2 = db_x2.fit_predict(X[2])
        db x3 = DBSCAN(eps=0.89, min samples=11).fit(X[3])
        clusters_x3 = db_x3.fit_predict(X[3])
        db_x4 = DBSCAN(eps=0.12, min_samples=11).fit(X[4])
        clusters_x4 = db_x4.fit_predict(X[4])
In [ ]: # plot the clustering results
        fig, axes = plt.subplots(2, 3, figsize=(12, 8))
        plot_cluster(axes[0,0], X[0], cluster_assignments=clusters_x0)
        plot_cluster(axes[0,1], X[1], cluster_assignments=clusters_x1)
        plot_cluster(axes[0,2], X[2], cluster_assignments=clusters_x2)
        plot_cluster(axes[1,0], X[3], cluster_assignments=clusters_x3)
        plot_cluster(axes[1,1], X[4], cluster_assignments=clusters_x4)
        axes[1, 2].axis('off')
        plt.tight layout()
        plt.show()
```



(c) Apply Spectral Clustering. Select the same number of clusters as selected by k-means.

```
In [ ]: from sklearn.cluster import SpectralClustering
In [ ]: def pred_y(X, n_clusters):
            Parameters
            X : list or numpy array of size [N x 2]
            n_clusters : int, Number of clusters to use for KMeans clustering
            Returns
            y_pred : list or numpy array [N]'''
            Sclustering = SpectralClustering(n_clusters=n_clusters, random_state=42).fit(X)
            return Sclustering.labels_
In [ ]: # store cluster assignments for each dataset to a list
        l_cluster_assginments = []
        1_cluster_assginments.append(pred_y(X[0], 2))
        l_cluster_assginments.append(pred_y(X[1], 4))
        l_cluster_assginments.append(pred_y(X[2], 3))
        1_cluster_assginments.append(pred_y(X[3], 3))
        1_cluster_assginments.append(pred_y(X[4], 2))
In [ ]: # plot clustered data
        fig, axes = plt.subplots(2, 3, figsize=(12, 8))
        for i in range(2):
            for j in range(3):
                if i*3+j == 5:
                    break
                plot_cluster(axes[i,j], X[i*3+j], \
                             cluster_assignments=l_cluster_assginments[i*3+j])
```

axes[1, 2].axis('off')
plt.tight_layout()



(d) Comment on the strengths and weaknesses of each approach. In particular, mention:

- Which technique worked "best" and "worst" (as defined by matching how human intuition would cluster the data) on each dataset?
- How much effort was required to get good clustering for each method (how much parameter tuning needed to be done)?

Comparing with KMeans, DBSCAN, and spectral clustering, DBSCAN worked best on the five datasets while KMeans worked the worst. DBSCAN achieved good performance on all datasets, spectral clustering had some trouble clustering dataset X4, and KMeans struggles on both dataset X2 and dataset X4.

KMeans:

- Strengths:
 - 1. It converges very quickly.
 - 2. It excels with clusters of equal variance.
 - 3. Ituitive, easy to understand and implement.

Weaknesses:

- 1. It is sensitive to initialization of means.
- 2. It requires specifying number of clusters.
- 3. It struggles in situations with variation in cluster variance and correlation between features. It also struggles when there are nonlinear boundaries between clusters. Worked 'worst' on the five datasets.

DBSCAN:

- Strengths:
 - 1. No need to pre-define number of clusters.
 - 2. Can find arbitrarily shaped clusters. Worked 'best' on the five datasets.
 - 3. It is robust to outliers.
- Weaknesses:
 - 1. It requires the most effort to train. Need to perform hyperparameter tuning (eps and min_samples).
 - 2. It cannot handle significant variation in cluster density.
 - 3. It is not entirely deterministic.

Spectral clustering:

- Strengths:
 - 1. It can capture the global structure of the data and often produces good clustering results
 - 2. No need to perform hyperparameter tuning, easy to implement
 - 3. It is robust to noise and outliers.
- Weaknesses:
 - 1. It requires specifying number of clusters.
 - 2. It can be computationally expensive for large datasets

In []:

3

[25 points] Dimensionality reduction and visualization of digits with PCA and t-SNE

- (a) Reduce the dimensionality of the data with PCA for data visualization. Load the scikit-learn digits dataset (code provided to do this below). Apply PCA and reduce the data (with the associated cluster labels 0-9) into a 2-dimensional space. Plot the data with labels in this two dimensional space (labels can be colors, shapes, or using the actual numbers to represent the data definitely include a legend in your plot).
- **(b)** Create a plot showing the cumulative fraction of variance explained as you incorporate from 1 through all D principal components of the data (where D is the dimensionality of the data).
 - What fraction of variance in the data is UNEXPLAINED by the first two principal components of the data?
 - Briefly comment on how this may impact how well-clustered the data are.

You can use the <code>explained_variance_</code> attribute of the PCA module in <code>scikit-learn</code> to assist with this question

- (c) Reduce the dimensionality of the data with t-SNE for data visualization. T-distributed stochastic neighborhood embedding (t-SNE) is a nonlinear dimensionality reduction technique that is particularly adept at embedding the data into lower 2 or 3 dimensional spaces. Apply t-SNE using the scikit-learn implementation to the digits dataset and plot it in 2-dimensions (with associated cluster labels 0-9). You may need to adjust the parameters to get acceptable performance. You can read more about how to use t-SNE effectively here.
- **(d)** Briefy compare/contrast the performance of these two techniques.
 - Which seemed to cluster the data best and why?
 - Notice that while t-SNE has a fit method and a fit_transform method, these
 methods are actually identical, and there is no transform method. Why is this? What
 implications does this imply for using this method?

Note: Remember that you typically will not have labels available in most problems.

Code is provided for loading the data below.

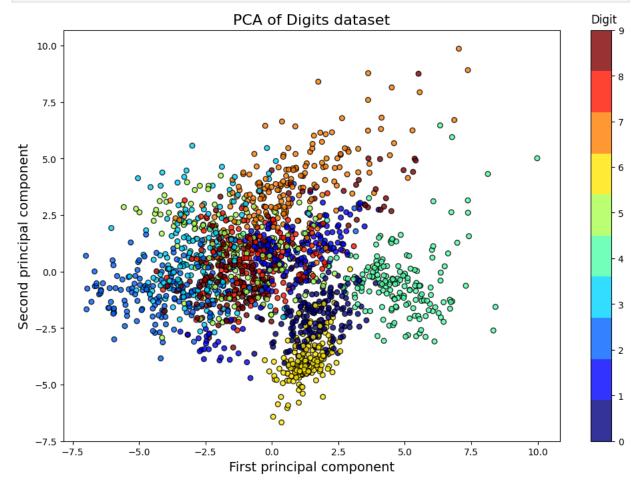
ANSWER

(a) Reduce the dimensionality of the data with PCA for data visualization. Apply PCA and reduce the data (with the associated cluster labels 0-9) into a 2-dimensional space. Plot the data with labels in this two dimensional space (labels can be colors, shapes, or using the actual numbers to represent the data - definitely include a legend in your plot).

```
In []: # standardize the data
    from sklearn.preprocessing import StandardScaler
    X_digits_std = StandardScaler().fit_transform(X_digits)

In []: # fit PCA and get transformed X
    pca = PCA(n_components=2, random_state=42).fit(X_digits_std)
    X_pca = pca.transform(X_digits_std)

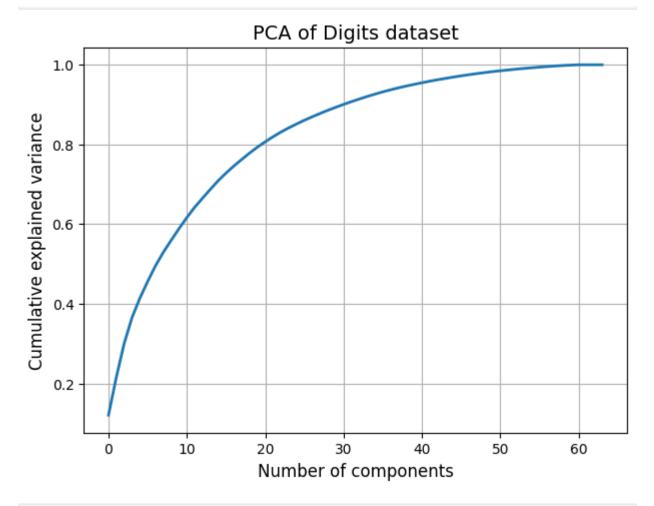
# plotting
    plt.figure(figsize=(12,8), dpi=100)
```



- **(b)** Create a plot showing the cumulative fraction of variance explained as you incorporate from 1 through all D principal components of the data (where D is the dimensionality of the data).
 - What fraction of variance in the data is UNEXPLAINED by the first two principal components of the data?
 - Briefly comment on how this may impact how well-clustered the data are.

You can use the <code>explained_variance_</code> attribute of the PCA module in <code>scikit-learn</code> to assist with this question

```
In [ ]: pca = PCA().fit(X_digits_std)
    plt.figure(figsize=(7, 5), dpi=100)
    plt.grid('on')
    plt.plot(np.cumsum(pca.explained_variance_ratio_), linewidth=2)
    plt.xlabel('Number of components', fontsize=12)
    plt.ylabel('Cumulative explained variance', fontsize=12)
    plt.title('PCA of Digits dataset', fontsize=14)
    plt.show()
```



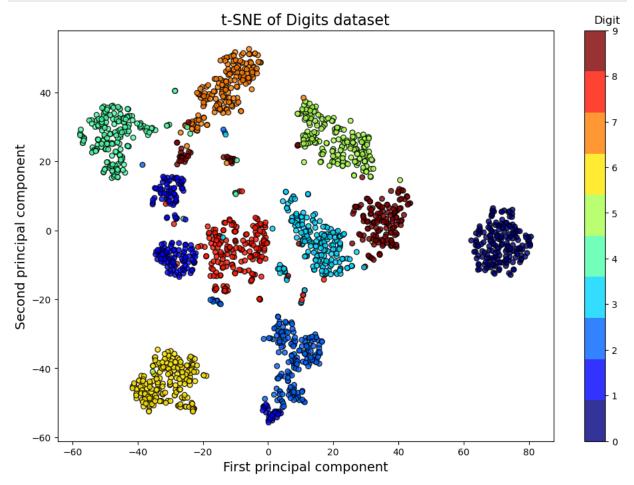
```
In [ ]: pca_two = PCA(n_components=2, random_state=42).fit(X_digits_std)
    var_exp_1, var_exp_2 = pca_two.explained_variance_ratio_
    print(f"Fraction of variance that is UNEXPLAINED by the first two \
        principal components: {(1 - var_exp_1 - var_exp_2)*100:.2f}%")
```

Fraction of variance that is UNEXPLAINED by the first two principal components: 78.4 1%

From the plot of cumulative fraction of variance explained, we can see that as the number of components increase, more variance is explained. The fraction of variance that is unexplained by the first two components reach 78.41%, which means that the first two principal components may not be sufficient to capture all the important characteristics of the data. This can result in clusters that are less well-separated and less distinct, as the remaining variability may be contributing to overlaps between the clusters

(c) Reduce the dimensionality of the data with t-SNE for data visualization. T-distributed stochastic neighborhood embedding (t-SNE) is a nonlinear dimensionality reduction technique that is particularly adept at embedding the data into lower 2 or 3 dimensional spaces. Apply t-SNE using the scikit-learn implementation to the digits dataset and plot it in 2-dimensions (with associated cluster labels 0-9). You may need to adjust the parameters to get acceptable performance. You can read more about how to use t-SNE effectively here.

```
In [ ]: X_digits_tsne = TSNE(n_components=2, random_state=42).fit_transform(X_digits_std)
```



(d) Briefy compare/contrast the performance of these two techniques.

- Which seemed to cluster the data best and why?
- Notice that while t-SNE has a fit method and a fit_transform method, these methods are actually identical, and there is no transform method. Why is this? What implications does this imply for using this method?

From the two-dimensional plots, it seems that t-SNE performs better than PCA in clustering the data. There is less overlapping between clusters after t-SNE dimentionality reduction. This is becaue t-SNE uses a probabilistic approach to embed the data in a lower-dimensional space while preserving the local structure of the data. Therefore, it is particularly well-suited for visualizing complex relationships between variables and clusters that may be difficult to separate in high-dimensional space. On the other hand, PCA is a linear method, so it may struggle with non-linear relationships between the variables.

The reason why t-SNE has *fit* and *fit_transform* method without *transform* method is due to the fact that when mapping high-dimensional data to a lower-dimensional space, the mapping is not a linear transformation, and the reduced representation of the data cannot be computed directly from a pre-defined transformation matrix.

The t-SNE algorithm uses the *fit* method to start an iterative optimization process that updates the locations of the data points until it reaches a minimum. The *fit_transform* method performs the same optimization process as *fit*, but it also returns the reduced representation of the data in a lower-dimensional space. Since there is no pre-defined transformation matrix for t-SNE, it doesn't make sense to have a separate *transform* method to apply a pre-defined transformation to new data points.