

## Geometric Modeling for Computer Graphics



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GeometricModeling.pptx

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1

## What do we mean by “Modeling”?

How we model geometry depends on what we would like to use the geometry for:

- Looking at its appearance
- Will we need to interact with its shape?
- How does it interact with its environment?
- How does it interact with other objects?
- What is its surface area and volume?
- Will it need to be 3D-printed?
- Etc.



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2

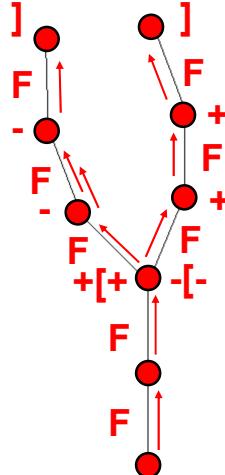
## L-Systems as a Special Way to Model 3D Geometry

3

Introduced and developed in 1968 by Aristid Lindenmayer, L-systems are a way to apply grammar rules for generating fractal (self-similar) geometric shapes. For example, take the string:

“FF+[+F-F-F]-[-F+F+F]”

F move forward one step  
+ turn right  
- turn left  
[ push state  
] pop state



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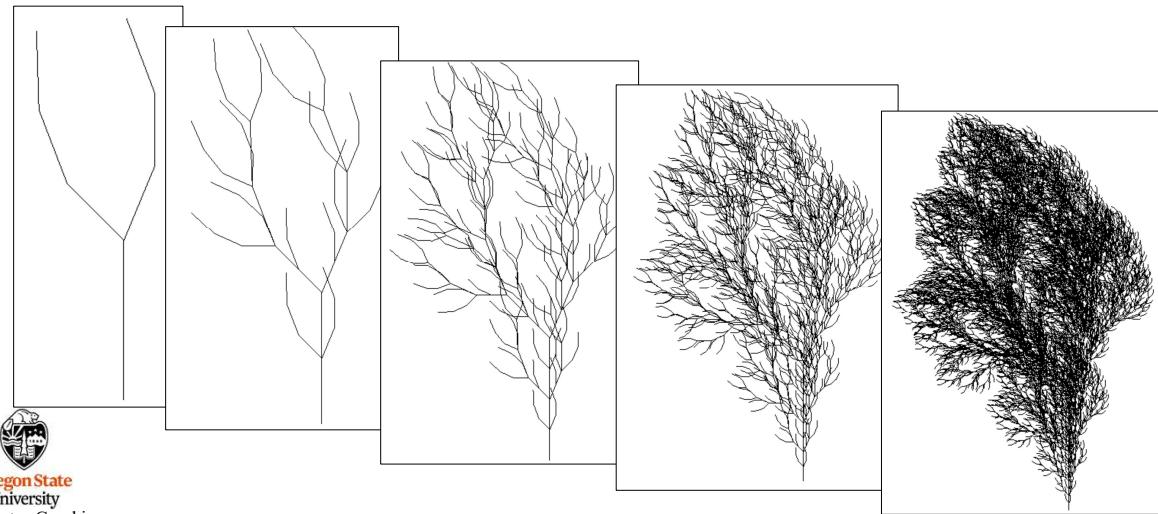
3

## L-Systems as a Special Way to Model 3D Geometry

4

But the *real* fun comes when you call that string recursively. For every **F**, replicate that string but with smaller geometry:

“F → FF+[+F-F-F]-[-F+F+F]”



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4

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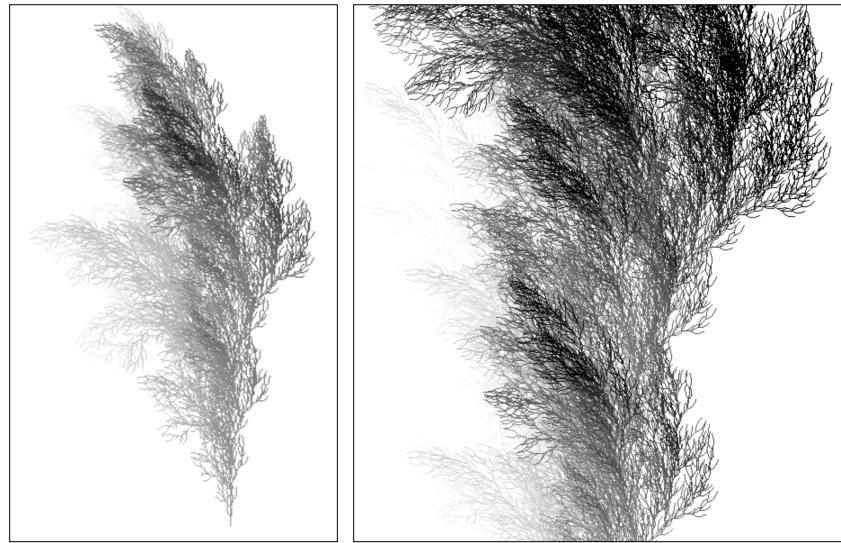
## L-Systems as a Special Way to Model 3D Geometry

5

And, of course we can introduce more grammar to swing it into 3D

$$\text{“F} \rightarrow \text{FF+ [+F- <F->F]- [-F+ ^F+vF]”}$$

+	rotate + about Z
-	rotate - about Z
<	rotate + about Y
>	rotate - about Y
v	rotate + about X
^	rotate - about X



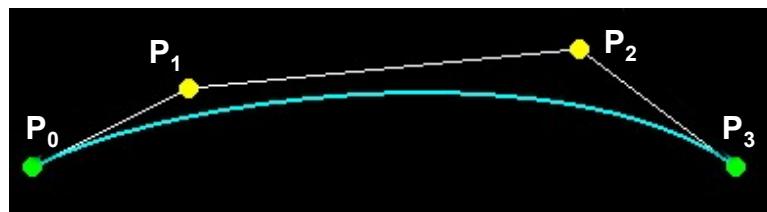
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## Another way to Model: Curve Sculpting – Bézier Curve Sculpting

6



$$P(t) = (1-t)^3 P_0 + 3t(1-t)^2 P_1 + 3t^2(1-t) P_2 + t^3 P_3$$

$$0. \leq t \leq 1.$$

where  $P$  represents  $\begin{Bmatrix} x \\ y \\ z \end{Bmatrix}$

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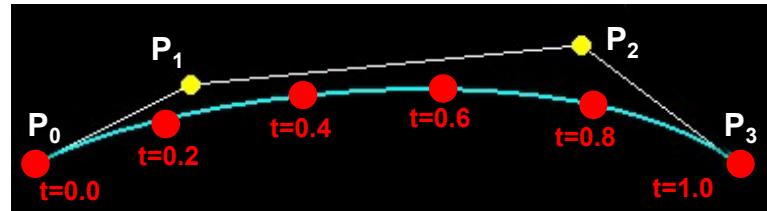
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$t$  goes from 0.0 to 1.0 in whatever increment you'd like

7

$$0. \leq t \leq 1.$$

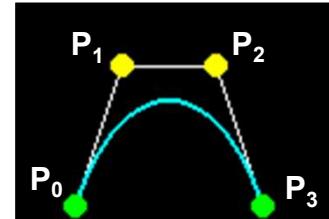
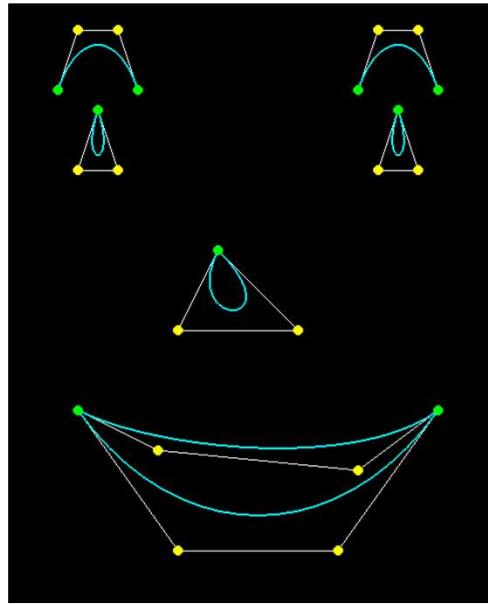


You draw the curve as a series of lines

**GL\_LINE\_STRIP** is a good topology for this

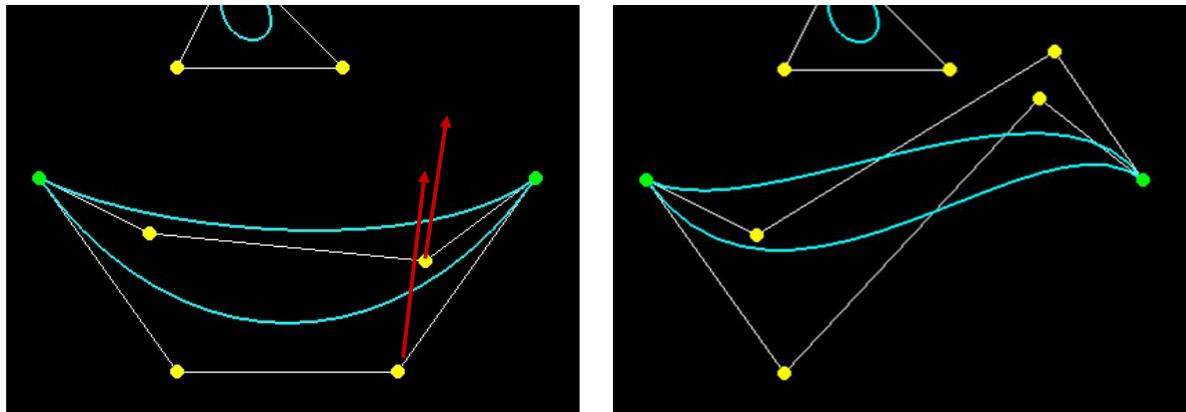
### Curve Sculpting – Bézier Curve Sculpting Example

8



## Curve Sculpting – Bézier Curve Sculpting Example

9



Moving a *single* control point moves its *entire* curve



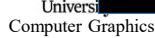
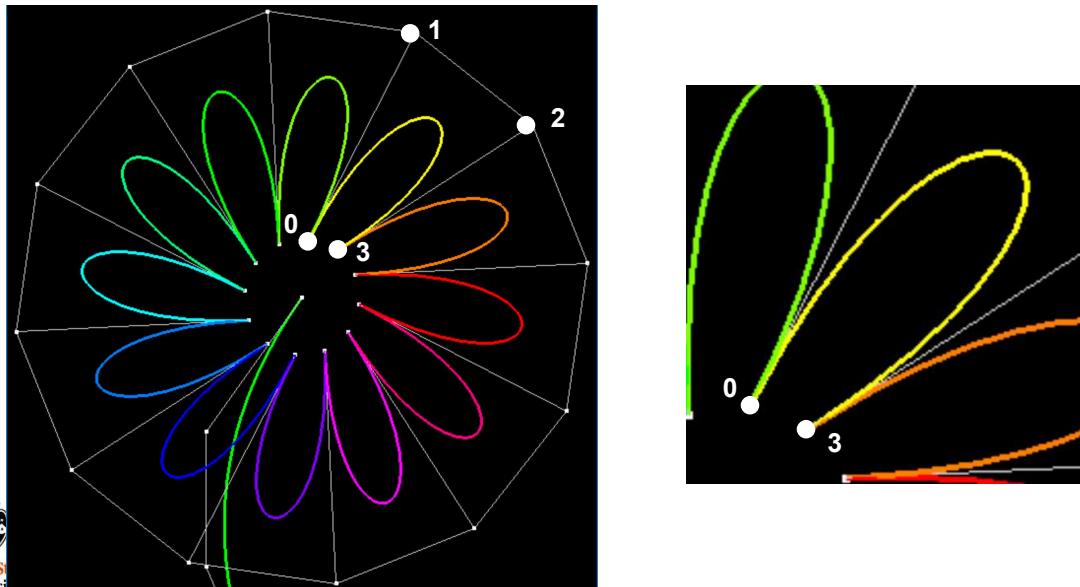
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## The Yellow 4-Point Bézier Curve

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## Another way to Model: Curve Sculpting – Catmull-Rom Curve Sculpting

11

The Catmull-Rom curve consists of any number of points.

The first point influences how the curve starts.

The last point influences how the curve ends.

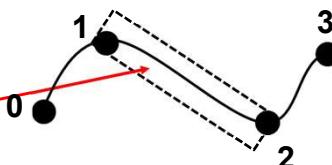
The overall curve goes smoothly through all other points.

To draw the curve, grab points 0, 1, 2, and 3, call them  $P_0, P_1, P_2$ , and  $P_3$ , and loop through the following equation, varying t from 0. to 1. in an increment of your own choosing:

$$P(t) = 0.5 * [2 * P_1 + t * (-P_0 + P_2) + t^2(2 * P_0 - 5.* P_1 + 4P_2 - P_3) + t^3(-P_0 + 3P_1 - 3P_2 + P_3)]$$

$$0. \leq t \leq 1.$$

where  $P$  represents  $\begin{cases} x \\ y \\ z \end{cases}$



For each set of 4 points, this equation just draws the line between the second and third points. That's why you keep having to use subsequent sets of 4 points

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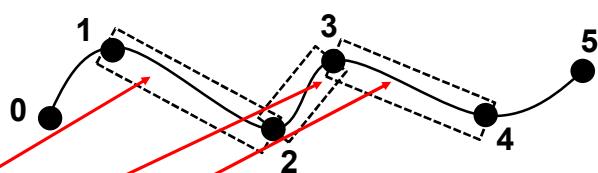
11

## Another way to Model: Curve Sculpting – Catmull-Rom Curve Sculpting

12

For each set of 4 points, this equation just draws the line between the second and third points.

That's why you keep having to use subsequent sets of 4 points



To draw the curve, grab points 0, 1, 2, and 3, call them  $P_0, P_1, P_2$ , and  $P_3$ , and loop through the equation, varying t from 0. to 1. in an increment of your own choosing.

Then, grab points 1, 2, 3, and 4, call them  $P_0, P_1, P_2$ , and  $P_3$ , and loop through the same equation.

Then, grab points 2, 3, 4, and 5, call them  $P_0, P_1, P_2$ , and  $P_3$ , and loop through the same equation

And so on...

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**A Small Amount of Input Change Results in a Large Amount of Output Change**

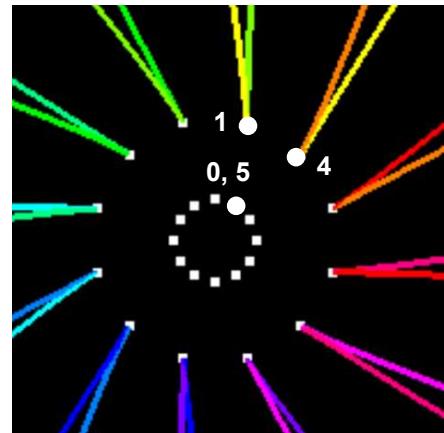
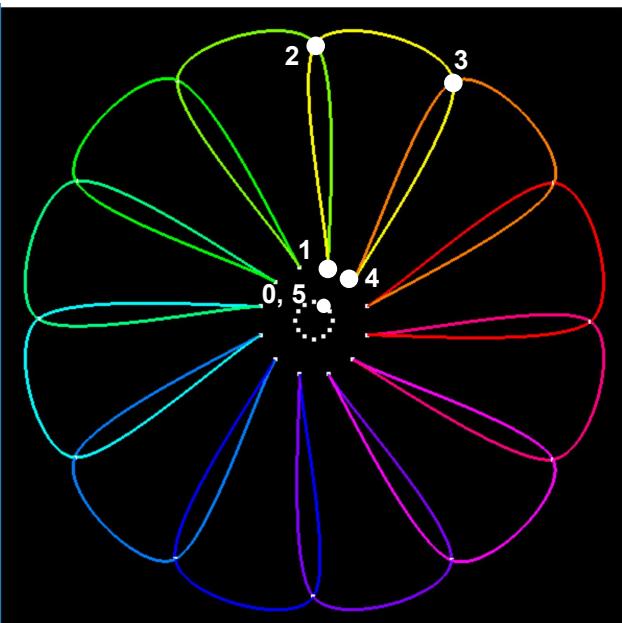
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12

6

### The Yellow 6-Point Catmull-Rom Curve

13



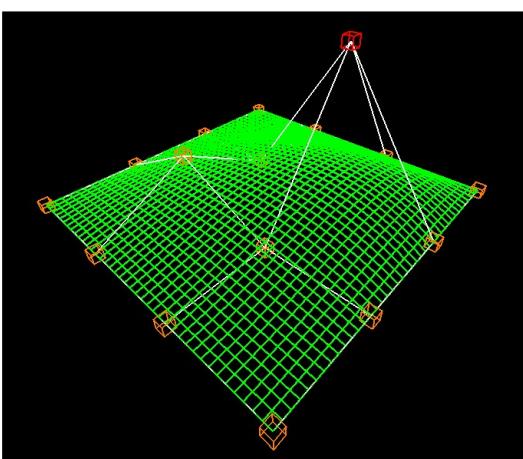
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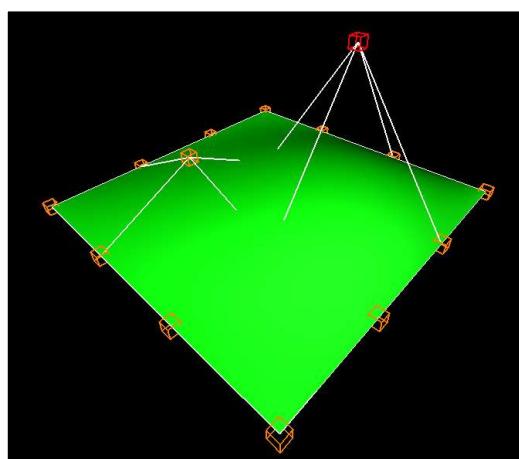
13

### Another way to Model: Bézier Surface Sculpting

14



Wireframe



Surface

Moving a single point moves its entire surface

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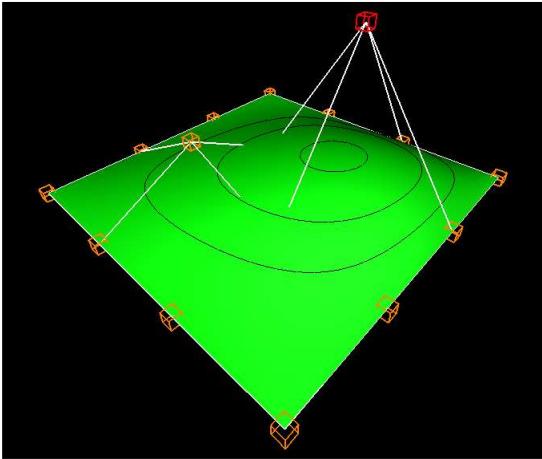
**A Small Amount of Input Change Results in a Large Amount of Output Change**

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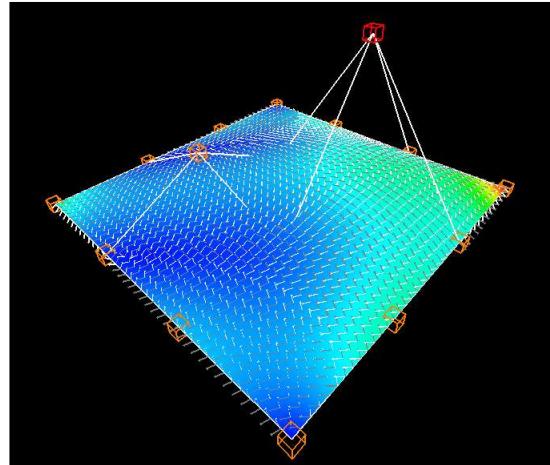
14

## Surface Equations can also be used for Analysis

15



Showing Contour Lines



Showing Curvature



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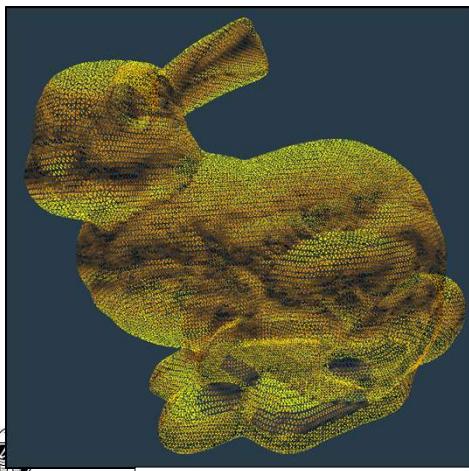
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15

## Explicitly Listing Geometry and Topology

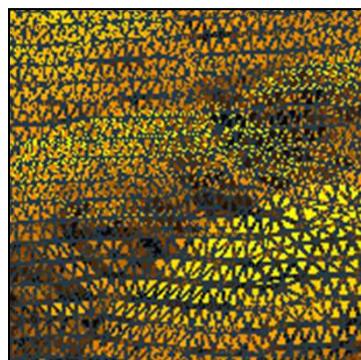
16

Models can consist of thousands of vertices and faces – we need some way to list them efficiently



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<http://graphics.stanford.edu/data/3Dscanrep>



This is called a **Mesh**.

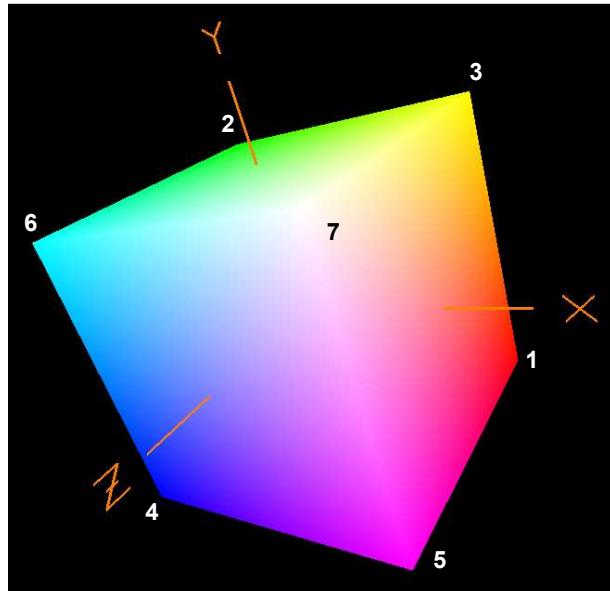
If it's in nice neat rows like this, it is called a **Regular Mesh**.

If it's not, it is called an **Irregular Mesh**, or oftentimes called a **Triangular Irregular Network**, or **TIN**.

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16

### Cube Example



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17

### Explicitly Listing Geometry and Topology

```
static GLfloat CubeVertices[ ][3] = {
{
    { -1., -1., -1. },
    { 1., -1., -1. },
    { -1., 1., -1. },
    { 1., 1., -1. },
    { -1., -1., 1. },
    { 1., -1., 1. },
    { -1., 1., 1. },
    { 1., 1., 1. }
};
```

```
GLuint CubeTriangleIndices[ ][3] = {
{
    { 0, 2, 3 },
    { 0, 3, 1 },
    { 4, 5, 7 },
    { 4, 7, 6 },
    { 1, 3, 7 },
    { 1, 7, 5 },
    { 0, 4, 6 },
    { 0, 6, 2 },
    { 2, 6, 7 },
    { 2, 7, 3 },
    { 0, 1, 5 },
    { 0, 5, 4 }
};
```

```
static GLfloat CubeColors[ ][3] = {
{
    { 0., 0., 0. },
    { 1., 0., 0. },
    { 0., 1., 0. },
    { 1., 1., 0. },
    { 0., 0., 1. },
    { 1., 0., 1. },
    { 0., 1., 1. },
    { 1., 1., 1. }
};
```

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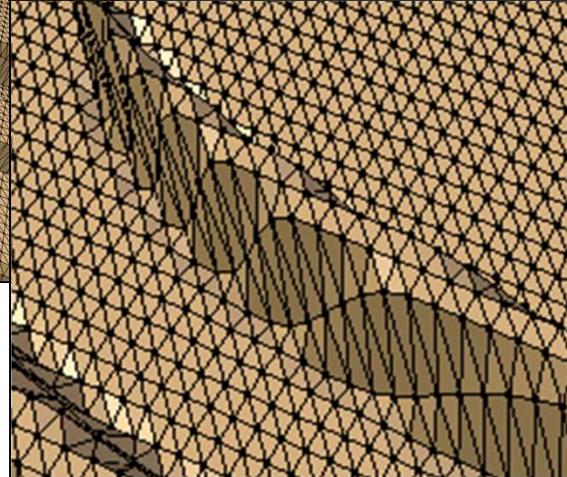
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18

9

### 3D Printing uses an Irregular Triangular Mesh Data Format

19



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19

### 3D Printing uses an Irregular Triangular Mesh Data Format

20



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10

Go Beavs – mmmmmmm! ☺

21



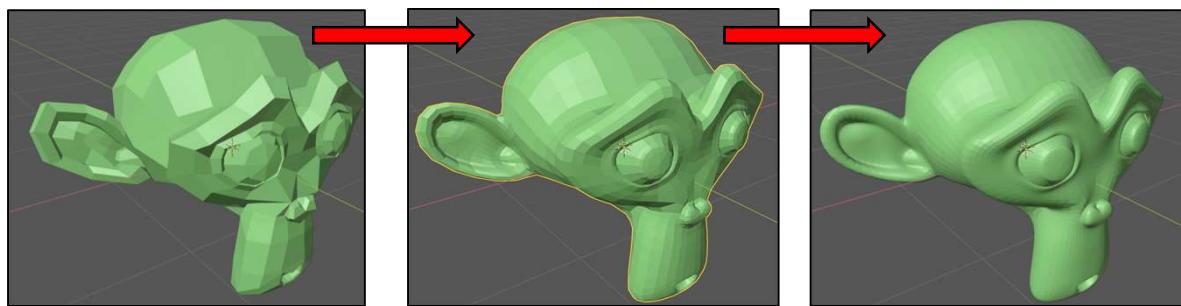
  
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21

Meshes Can Be Smoothed

22



  
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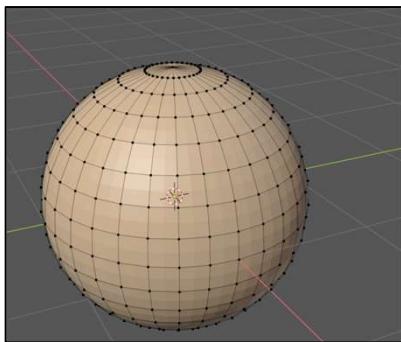
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22

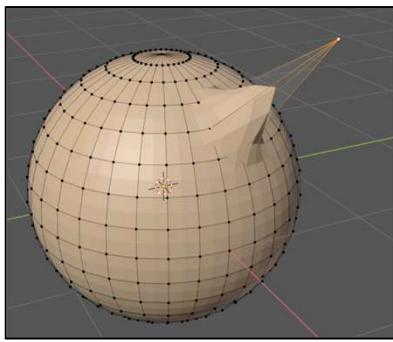
11

### Meshes Can Be Edited

23

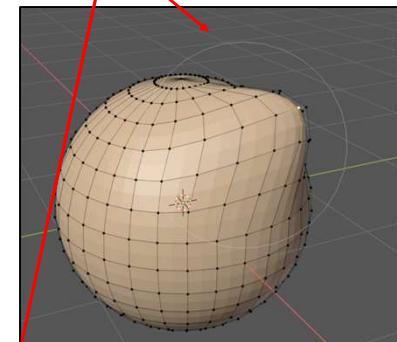


Original

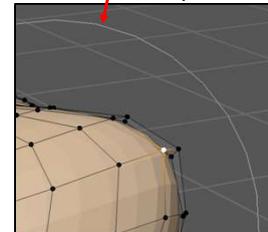


Pulling on a single Vertex

"Circle of Influence"



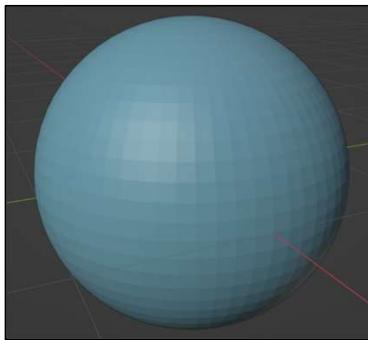
Pulling on a Vertex with  
Proportional Editing Turned On



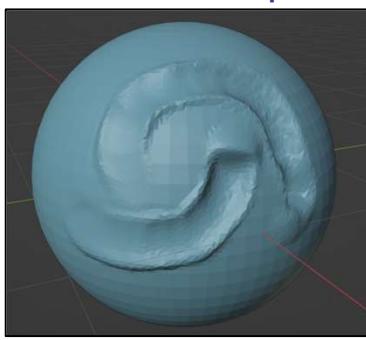
23

### Meshes Can Be Sculpted

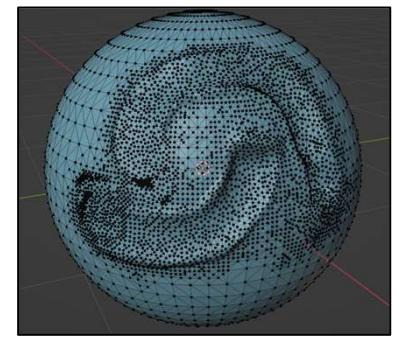
24



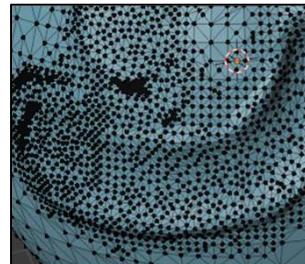
Original



"Clay Thumb" Sculpting

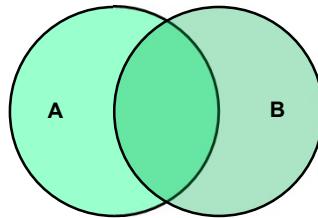


Sculpting Can Produce Additional  
Mesh Vertices

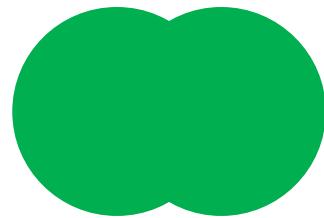


24

### Remember Venn Diagrams (2D Boolean Operators) from High School?



Two Overlapping Shapes



Union:  $A \cup B$



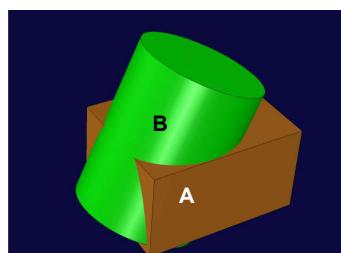
Intersection:  $A \cap B$



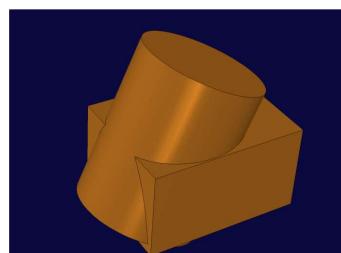
I thought I left Venn Diagrams behind in High School !

Difference:  $A - B$

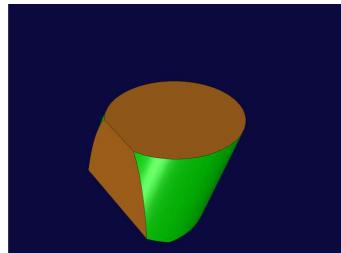
### Well, Welcome to Venn Diagrams in 3D



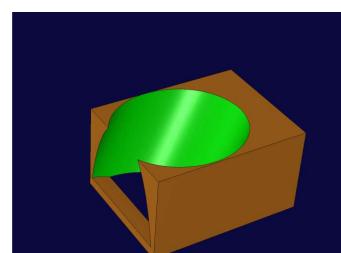
Two Overlapping Solids



Union:  $A \cup B$



Intersection:  $A \cap B$

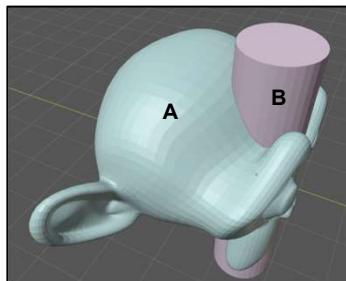


Difference:  $A - B$

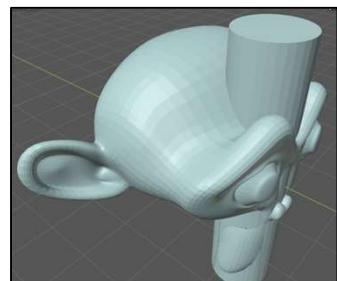
This is often called **Constructive Solid Geometry**, or CSG

## Geometric Modeling Using 3D Boolean Operators on Meshes

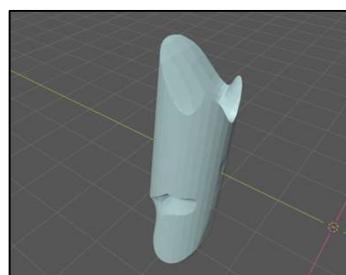
27



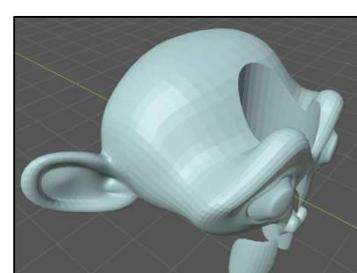
Two Overlapping Solids



Union:  $A \cup B$



Intersection:  $A \cap B$



Difference:  $A - B$

27

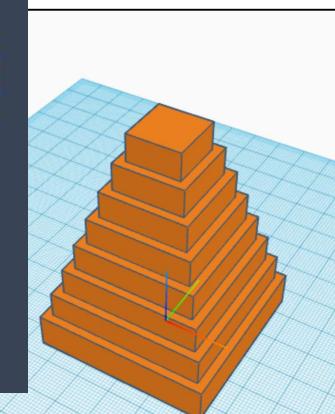
## Procedural Geometric Modeling Using TinkerCad/Codeblocks

28

```

Create New Object object0
Create Variable Xlength 50
Create Variable Ylength 50
Create Variable Zlength 10
Create Variable Zheight 5
Repeat (8) [
    Add Cube [Xlength] [Ylength] [Zlength] [edge 0 Edge Steps 10]
    Move [X: 0 Y: 0 Z: Zheight]
    Change Zheight by 8
    Change Xlength by -5
    Change Ylength by -5
    Change Zlength by 0
]
Create Group

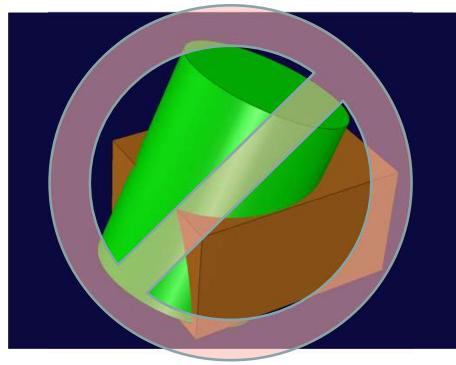
```



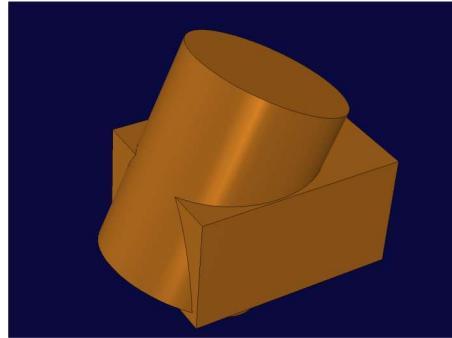
28

## 3D Boolean Operators are Important in 3D Printing as well as General Modeling

29



Two Overlapping Solids –  
Cannot Be 3D Printed

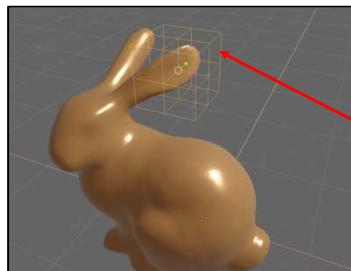


Two Overlapping Solids Unioned –  
Now Can Be 3D Printed

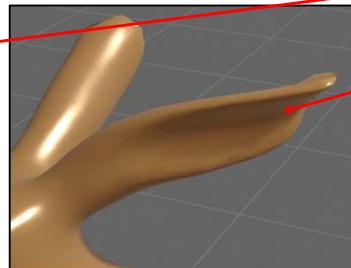
Intersected and Differenced Solids Can be 3D Printed as Well

## Another Way to Edit Meshes: Lattice Sculpting

30



This is often called a  
“Lattice” or a “Cage”.



Slip a simpler object (e.g., a subdivided cube) around some of the object's vertices. As you sculpt the simpler object, all those object vertices get sculpted too.

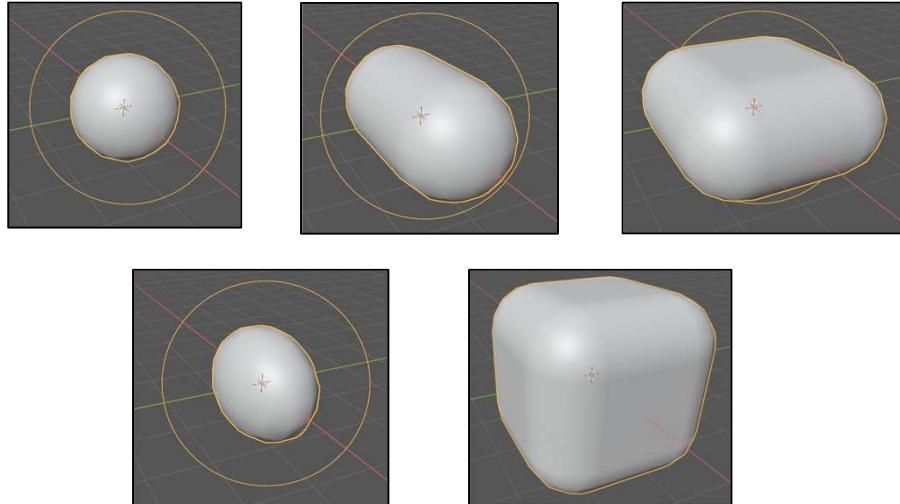


lattice.mp4

A Small Amount of Input Change Results in a  
Large Amount of Output Change

## Another Way to Model: Metaball Objects

31

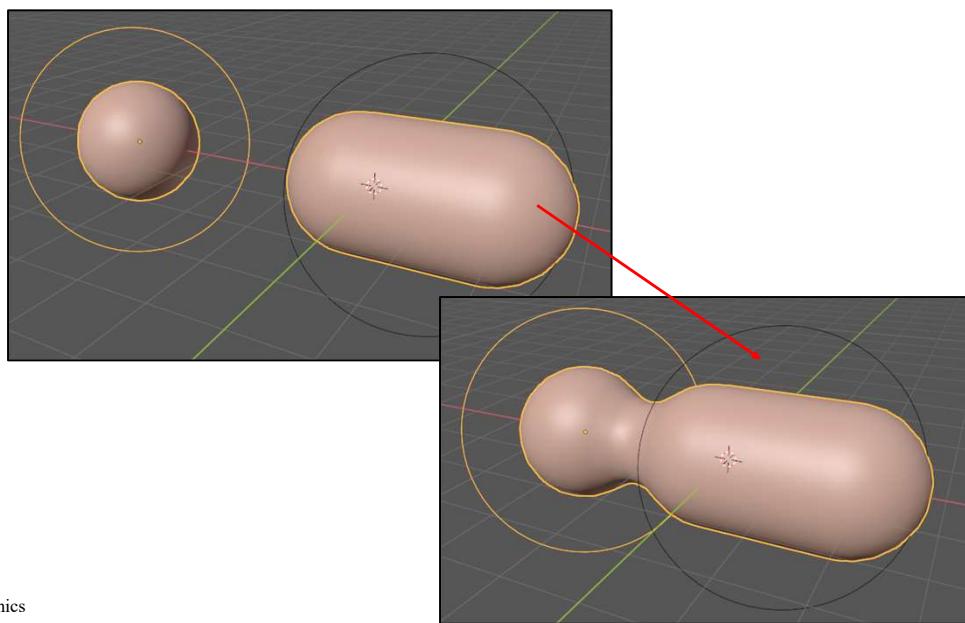


31

## Metaball Objects

32

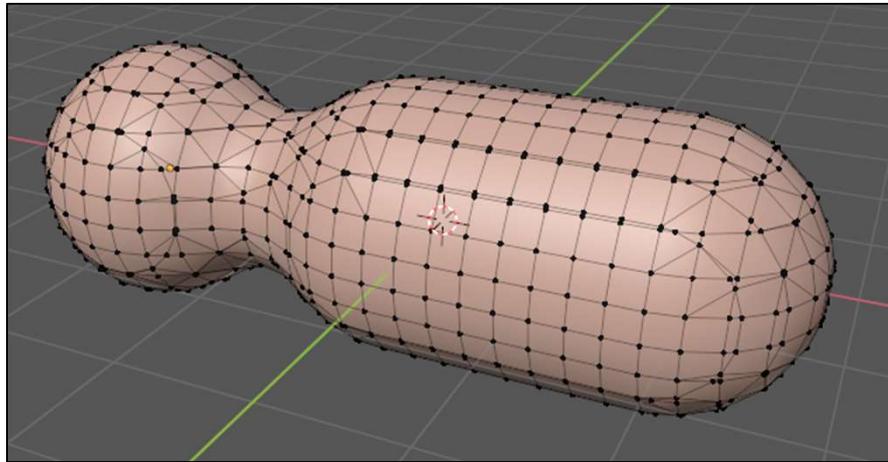
The cool thing is that, if you move them close enough together, they will “glom” into a single object



32

## Metaball Objects Can Be Turned into Meshes for Later Editing

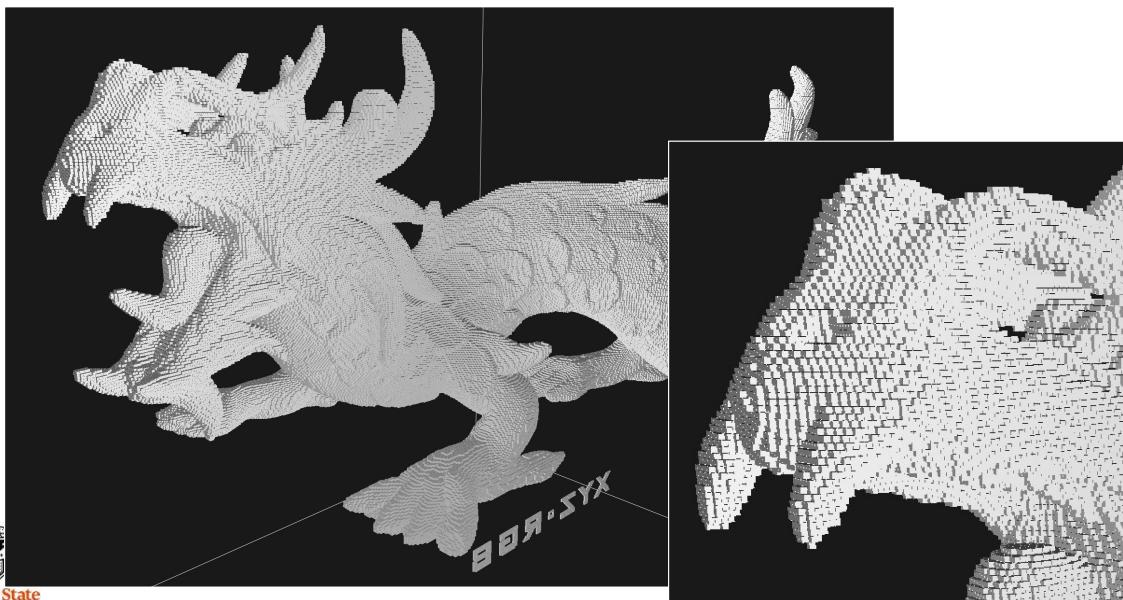
33



33

## Voxelization as a Special Way to Model 3D Geometry

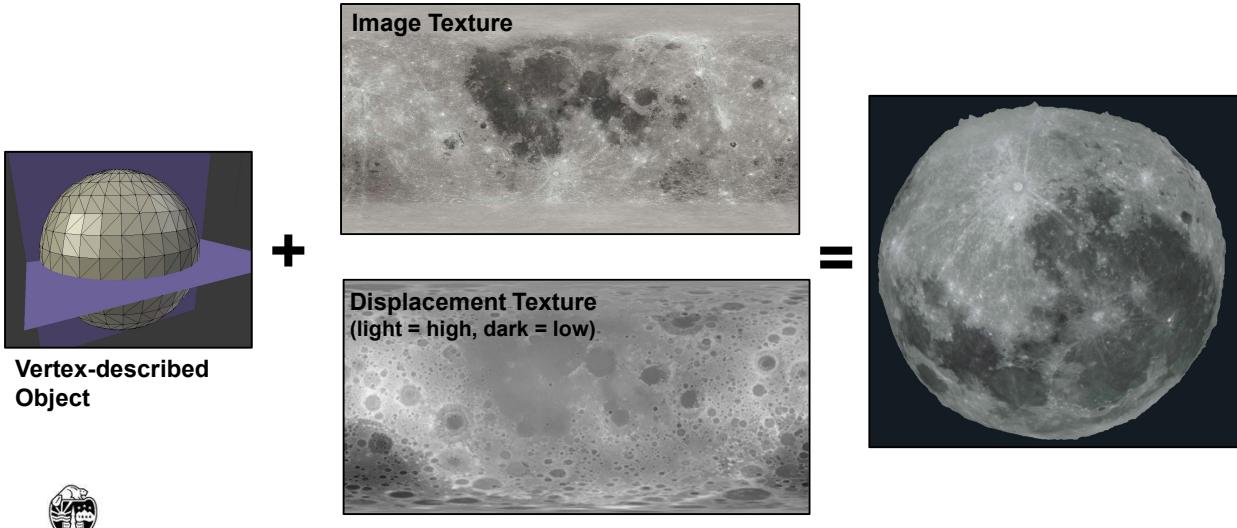
34



34

## Displacement Textures as a Special Way to Model 3D Geometry

35



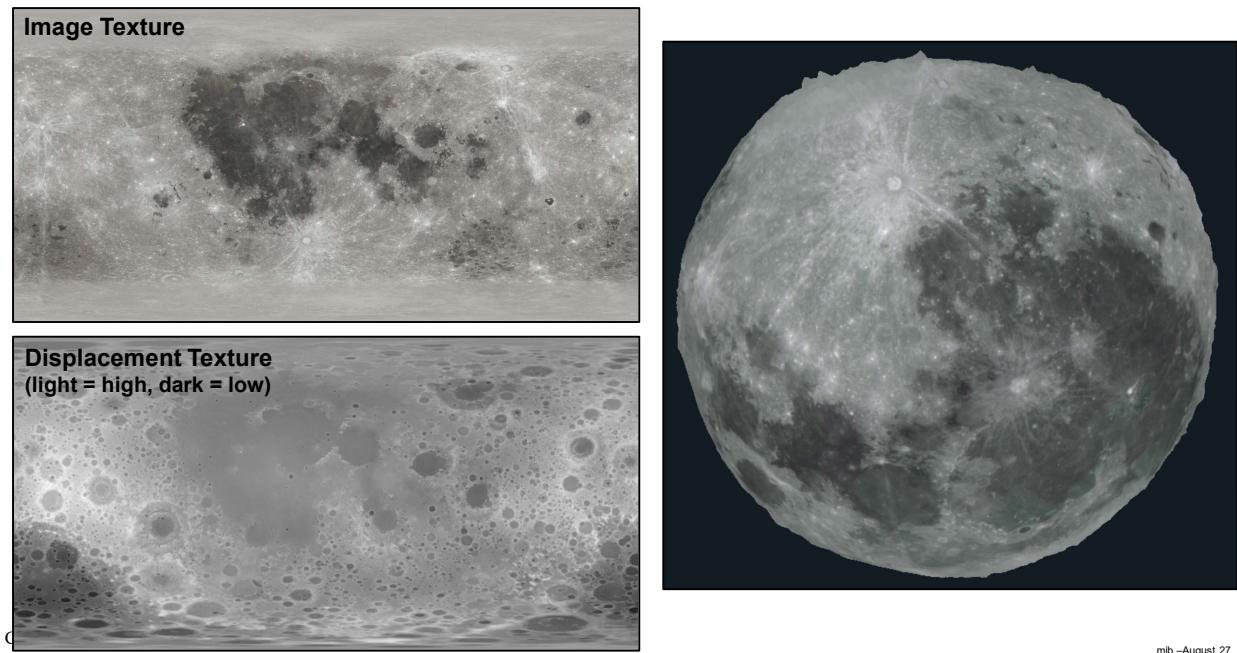
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35

## Displacement Textures as a Special Way to Model 3D Geometry

36



36

18

## Displacement Textures as a Special Way to Model 3D Geometry

37

**moondisp.vert**

```
#version 330 compatibility
uniform float uLightX, uLightY, uLightZ;
uniform float uHeightScale;
uniform float uSeaLevel;
uniform sampler2D uDispUnit;
uniform bool uDoElevations;

out vec2 vST;
out vec3 VN;           // normal vector
out vec3 VL;           // vector from point to light

void main( )
{
    vec2 st = gl_MultiTexCoord0.st;
    vST = st;

    vec3 norm = normalize(gl_NormalMatrix * gl_Normal);           // normal vector
    VN = norm;
    vec3 LightPos = normalize( vec3( uLightX, uLightY, uLightZ ) );
    vec4 ECposition = gl_ModelViewMatrix * gl_Vertex;           // eye coordinate position
    VL = LightPos - ECposition.xyz;                                // vector from the point to the light position

    vec3 vert = gl_Vertex.xyz;
    if( uDoElevations )
    {
        float disp = texture( uDispUnit, st ).r;
        disp -= uSeaLevel;
        disp *= uHeightScale;
        vert += normalize(gl_Normal) * disp;
    }

    gl_Position = gl_ModelViewProjectionMatrix * vec4( vert, 1. );
}
```



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37

## Displacement Textures as a Special Way to Model 3D Geometry

38

**moondisp.frag, I**

```
#version 330 compatibility
uniform bool uDoBumpMapping;
uniform float uKa, uKd;
uniform float uHeightScale;
uniform float uNormalScale;
uniform sampler2D uColorUnit;
uniform sampler2D uDispUnit;

in vec2 vST;
in vec3 VN;
in vec3 VL;
#define DELTA 0.01

void main()
{
    vec3 newColor = texture( uColorUnit, vST ).rgb;
    gl_FragColor = vec4( newColor, 1. );
    if( uDoBumpMapping )
    {
        ...
    }
}
```



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38

19

**moondisp.frag, II**

```

if( uDoBumpMapping )
{
    vec2 stp0 = vec2( DELTA, 0. );
    vec2 st0p = vec2( 0. , DELTA );
    float west = texture2D( uDispUnit, vST-stp0 ).r;
    float east = texture2D( uDispUnit, vST+stp0 ).r;
    float south = texture2D( uDispUnit, vST-st0p ).r;
    float north = texture2D( uDispUnit, vST+st0p ).r;
    vec3 tangent = vec3( 2.*DELTA, 0., uNormalScale * ( east - west ) );
    vec3 ttangent = vec3( 0., 2.*DELTA, uNormalScale * ( north - south ) );
    vec3 Normal = normalize( cross( tangent, ttangent ) );
    vec3 Light = normalize(vL);

    vec3 ambient = uKa * newColor;
    float d = 0.;
    if( dot(Normal,Light) > 0. ) // only do diffuse if the light can see the point
    {
        d = dot(Normal,Light);
    }
    vec3 diffuse = uKd * d * newColor;
    gl_FragColor = vec4( ambient+diffuse, 1. );
}
}

```

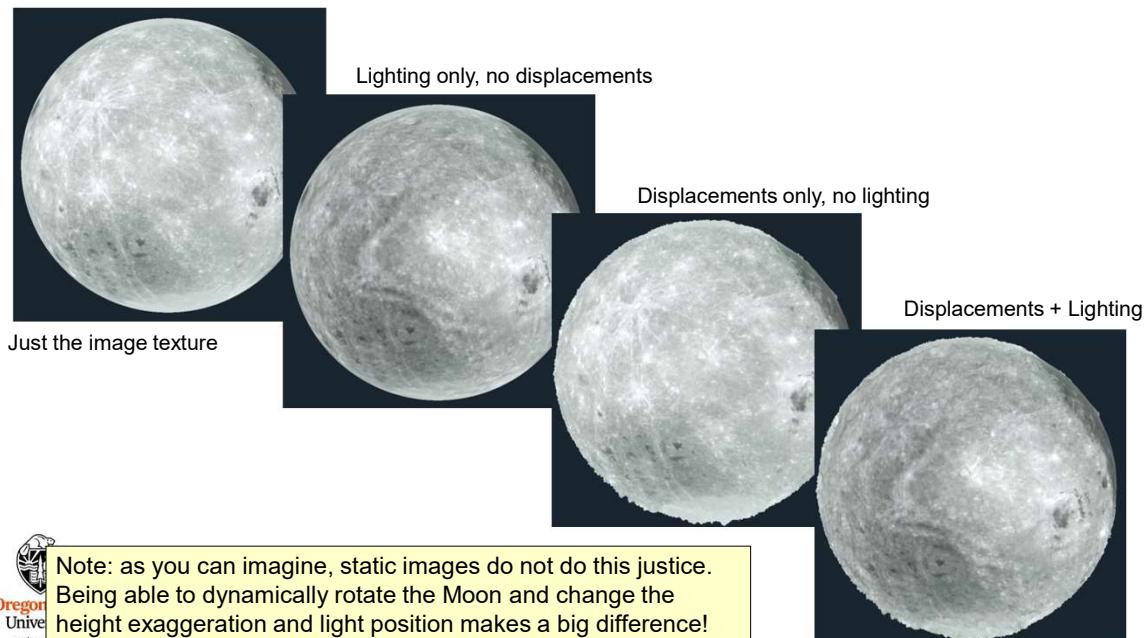


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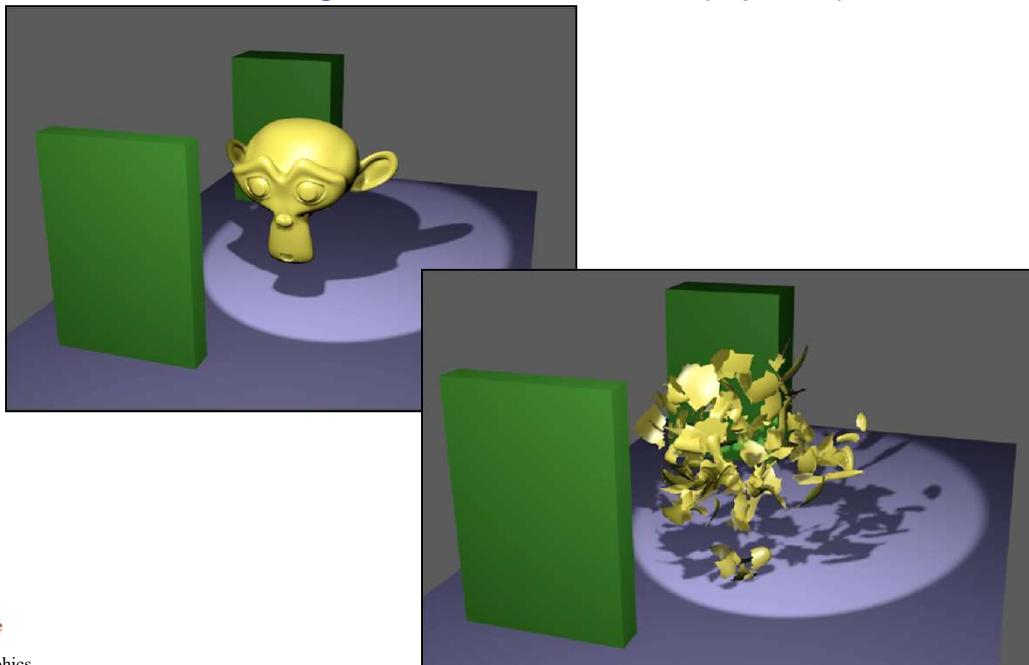
39



40

### Modeling as an Initial Step in Simulation (Explosion)

41

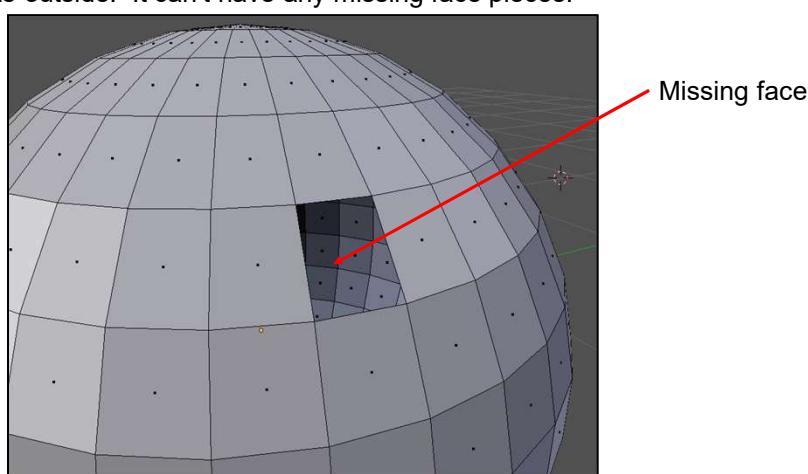


41

### Object Modeling Rules for 3D Printing

42

The object must be a legal solid. It must have a definite inside and a definite outside. It can't have any missing face pieces.

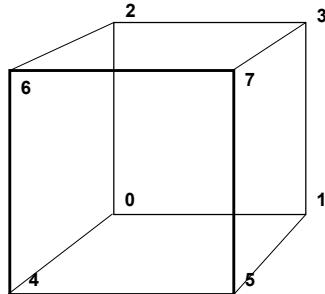


42

## The Simplified Euler's Formula\* for Legal Solids

43

\*sometimes called the Euler-Poincaré formula



$$F - E + V = 2$$

F      Faces  
E      Edges  
V      Vertices

For a cube,  $6 - 12 + 8 = 2$

We will talk more about this  
in the 3D Printing notes!



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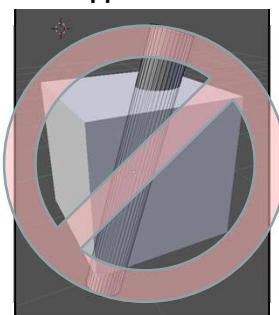
43

## Object Modeling Rules for 3D Printing

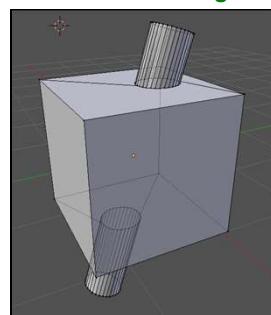
44

Objects cannot pass through other objects. If you want two shapes together, do a Boolean union on them so that they become one complete object.

Overlapped in 3D -- **bad**



Boolean union -- **good**



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44

## The OpenGL Mathematics (GLM) Library



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GLM.pptx

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### What is GLM?

GLM is a set of C++ classes and functions that fill in the programming gaps in writing the basic vector and matrix mathematics for computer graphics applications.

GLM isn't a *library* – it is all specified in \*.hpp header files that get compiled in with your source code.

You can find GLM at:

<http://glm.g-truc.net/0.9.8.5/>

or you can get a zip file of it on our Class Resources page.

You typically use GLM by putting these lines at the top of your program:

```
#define GLM_FORCE_RADIANS
#include "glm/vec2.hpp"
#include "glm/vec3.hpp"
#include "glm/mat4x4.hpp"
#include "glm/gtc/matrix_transform.hpp"
#include "glm/gtc/matrix_inverse.hpp"
#include "glm/gtc/type_ptr.hpp"
```



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## Why are we even talking about this?

3

The OpenGL overlords have “deprecated” some of the OpenGL functions we have been using to perform transformations. In the desktop world, it means that the use of such functions is **discouraged**. In Vulkan and in the mobile world of OpenGL-ES, it means those functions are **gone**. You might as well become familiar with how to live without them. So, instead of saying:

```
gluLookAt( 0., 0., 3., 0., 0., 0., 0., 1., 0. );
glRotatef( (GLfloat)Yrot, 0., 1., 0. );
glRotatef( (GLfloat)Xrot, 1., 0., 0. );
glScalef( (GLfloat)Scale, (GLfloat)Scale, (GLfloat)Scale );
```

for OpenGL, you would now say:

```
glm::mat4 modelview;
glm::vec3 eye(0.,0.,3.);
glm::vec3 look(0.,0.,0.);
glm::vec3 up(0.,1.,0.);
modelview = glm::lookAt( eye, look, up );
modelview = glm::rotate( modelview, D2R*Yrot, glm::vec3(0.,1.,0.) );
modelview = glm::rotate( modelview, D2R*Xrot, glm::vec3(1.,0.,0.) );
modelview = glm::scale( modelview, glm::vec3(Scale,Scale,Scale) );
glMultMatrixf( glm::value_ptr( modelview ) );
```



Exactly the same concept, but a different expression of it. Read on for details ...

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## The Most Useful GLM Variables, Operations, and Functions

4

// constructor:

```
glm::mat4( 1. );                                // identity matrix
glm::vec4( );
glm::vec3( );
```

GLM recommends that you use the “**glm::**” syntax and not use “**using namespace**” syntax because they have not made any effort to create unique function names

// multiplications – the \* operator has been overloaded:

```
glm::mat4 * glm::mat4
glm::mat4 * glm::vec4
glm::mat4 * glm::vec4( glm::vec3, 1. )      // promote vec3 to a vec4 via a constructor
```

// emulating OpenGL transformations *with concatenation*:

```
glm::mat4 glm::rotate( glm::mat4 const & m, float angle, glm::vec3 const & axis );
glm::mat4 glm::scale( glm::mat4 const & m, glm::vec3 const & factors );
glm::mat4 glm::translate( glm::mat4 const & m, glm::vec3 const & translation );
```



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## The Most Useful GLM Variables, Operations, and Functions

5

```
// viewing volume (assign, not concatenate):
```

```
glm::mat4 glm::ortho( float left, float right, float bottom, float top, float near, float far );  
glm::mat4 glm::ortho( float left, float right, float bottom, float top );
```

```
glm::mat4 glm::frustum( float left, float right, float bottom, float top, float near, float far );  
glm::mat4 glm::perspective( float fovy, float aspect, float near, float far );
```

```
// viewing (assign, not concatenate):
```

```
glm::mat4 glm::lookAt( glm::vec3 const & eye, glm::vec3 const & look, glm::vec3 const & up );
```

```
// loading matrices into opengl:
```

```
glLoadMatrix( glm::value_ptr( glm::mat4 ) );
```

```
glUniformMatrix4fv( Location, 1, GL_FALSE, glm::value_ptr( glm::mat4 ) );
```

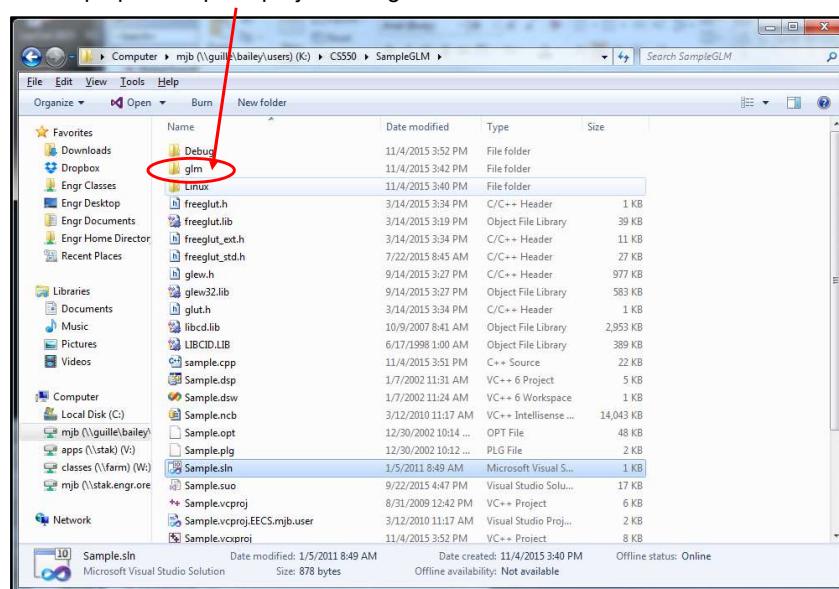


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## Installing GLM into your own space

6

I like to just put the whole thing under my Visual Studio project folder so I can zip up a complete project and give it to someone else.



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## Here's what that GLM folder looks like

7

The screenshot shows a Windows file explorer window with a red circle highlighting the 'glm' folder in the address bar. The folder contains 27 items, all of which are C/C++ Header files. The files include detail.hpp, gtc.hpp, glm.hpp, integer.hpp, mat2x2.hpp, mat3x3.hpp, matrix.hpp, vec2.hpp, vec3.hpp, vec4.hpp, vector.hpp, and vector\_relational.hpp. There is also a CMakelists.txt file. The file sizes range from 2 KB to 83 KB.

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## Telling Linux about where the GLM folder is

8

g++ ... -I ...

"minus-capital-eye-period" means "also look for the < > includes in this folder"

Instead of the period, you can list a full or relative pathname.

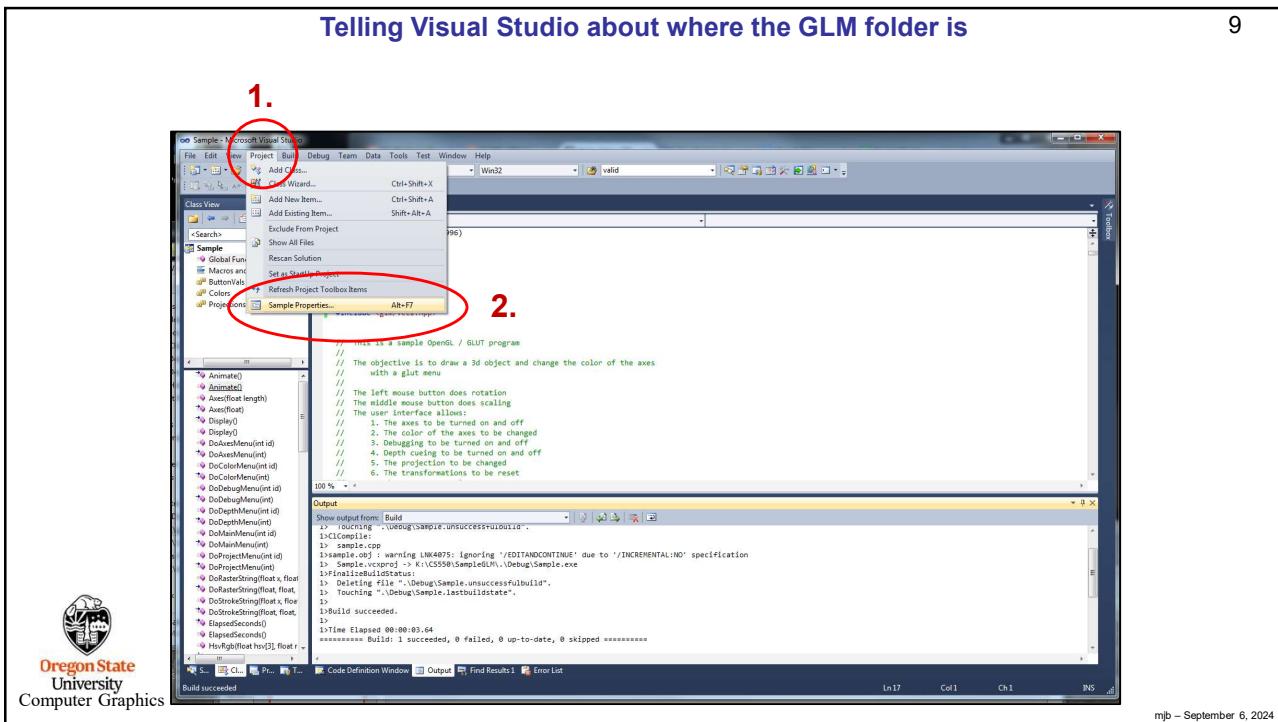
The screenshot shows a terminal window on a Linux system. A red arrow points to the '-I' option in the command line. The command is a g++ compiler command with various flags and source files listed. The '-I' option is used to specify the directory where the GLM header files are located.

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## Telling Visual Studio about where the GLM folder is

9

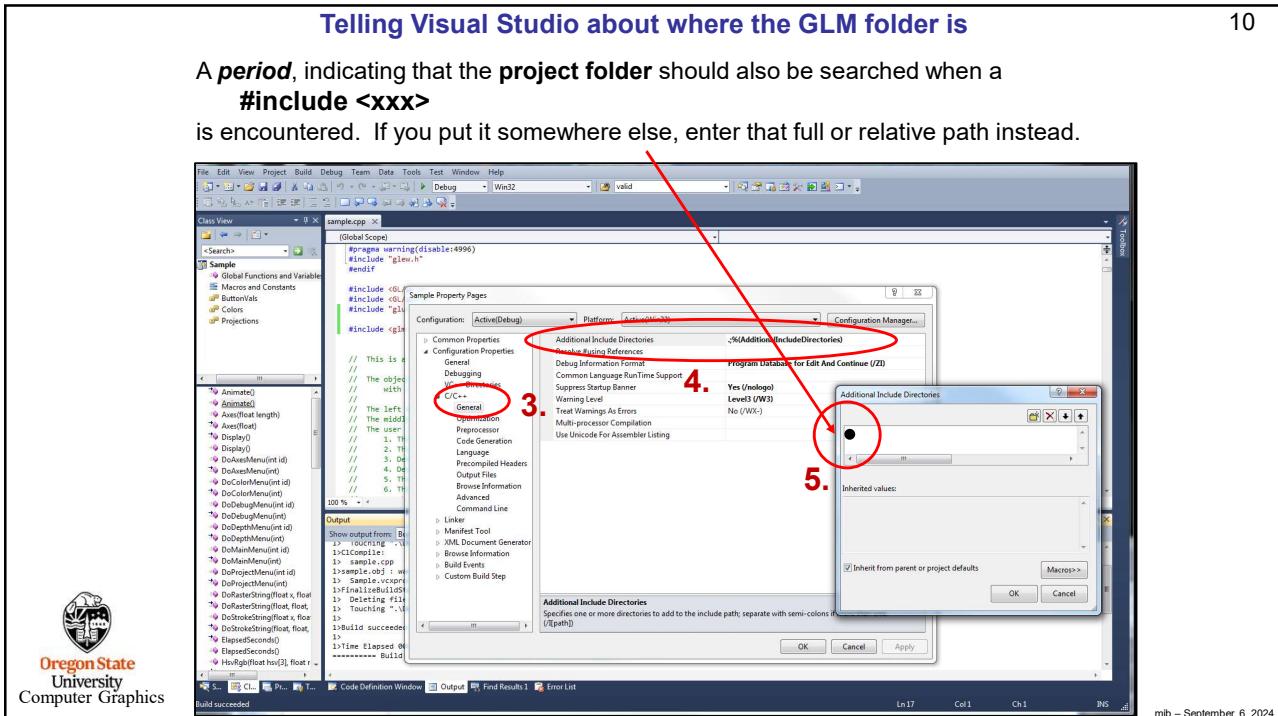


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## Telling Visual Studio about where the GLM folder is

10

A **period**, indicating that the **project folder** should also be searched when a  
**#include <xxx>**  
is encountered. If you put it somewhere else, enter that full or relative path instead.



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## Using Transformations, OpenGL-style, like in the sample.cpp Program

11

```
glMatrixMode( GL_PROJECTION );
glLoadIdentity();
if( WhichProjection == ORTHO )
    glOrtho( -3., 3., -3., 3., 0.1, 1000. );
else
    gluPerspective( 90., 1., 0.1, 1000. );

// place the objects into the scene:
glMatrixMode( GL_MODELVIEW );
glLoadIdentity();

// set the eye position, look-at position, and up-vector:
gluLookAt( 0., 0., 3., 0., 0., 0., 0., 1., 0. );

// rotate the scene:
glRotatef( (GLfloat)Yrot, 0., 1., 0. );
glRotatef( (GLfloat)Xrot, 1., 0., 0. );

// uniformly scale the scene:
if( Scale < MINSCALE )
    Scale = MINSCALE;
glScalef( (GLfloat)Scale, (GLfloat)Scale, (GLfloat)Scale );
```



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## Using Transformations, GLM-style, I

12

```
#include <glm/vec3.hpp>
#include <glm/mat4x4.hpp>
#include <glm/gtc/matrix_transform.hpp>
#include <glm/gtc/type_ptr.hpp>

...

// convert degrees to radians:
const float D2R = M_PI/180.f;           // 0.01745...

...

glMatrixMode( GL_PROJECTION );
glLoadIdentity();
glm::mat4 projection;

if( WhichProjection == ORTHO )
    projection = glm::ortho( -3., 3., -3., 3., 0.1, 1000. );
else
    projection = glm::perspective( D2R*90., 1., 0.1, 1000. );

// apply the projection matrix:
glMultMatrixf( glm::value_ptr( projection ) );
```



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## Using Transformations, GLM-style, II

13

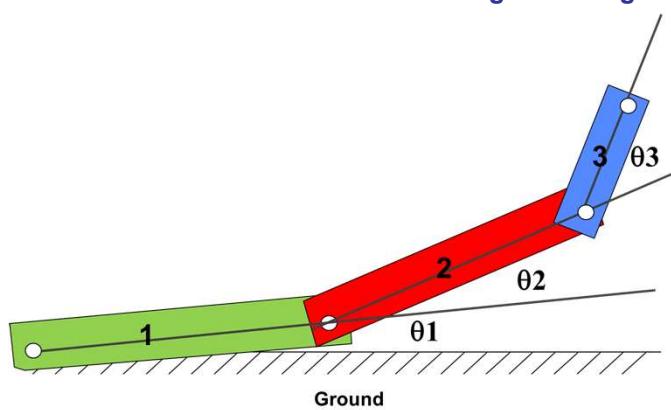
```
// place the objects into the scene:  
glMatrixMode( GL_MODELVIEW );  
glLoadIdentity();  
  
// set the eye position, look-at position, and up-vector:  
glm::vec3 eye(0.,0.,3.);  
glm::vec3 look(0.,0.,0.);  
glm::vec3 up(0.,1.,0.);  
glm::mat4 modelview = glm::lookAt( eye, look, up );  
  
// rotate the scene (warning -- unlike OpenGL's glRotatef,  
// GLM's rotate method takes angles in *radians*):  
modelview = glm::rotate( modelview, D2R*Yrot, glm::vec3(0.,1.,0.) );  
modelview = glm::rotate( modelview, D2R*Xrot, glm::vec3(1.,0.,0.) );  
  
// uniformly scale the scene:  
if( Scale < MINSCALE )  
    Scale = MINSCALE;  
modelview = glm::scale( modelview, glm::vec3(Scale,Scale,Scale) );  
  
// apply the modelview matrix:  
glMultMatrixf( glm::value_ptr( modelview ) );
```



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## Let's Re-work the Forward Kinematics Program Using GLM

14



$$[M_{3/G}] = [T_{1/G}] * [R_{\theta_1}] * [T_{2/1}] * [R_{\theta_2}] * [T_{3/2}] * [R_{\theta_3}]$$

$$[M_{3/G}] = [M_{1/G}] * [M_{2/1}] * [M_{3/2}]$$



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## Let's Re-work the Forward Kinematics Program Using GLM

15

### Standard OpenGL

```
void DrawMechanism( float θ1, float θ2, float θ3 )
{
    glPushMatrix();
    glRotatef(θ1, 0., 0., 1.);
    DrawLinkOne();

    glTranslatef(LENGTH_1, 0., 0.);
    glRotatef(θ2, 0., 0., 1.);
    DrawLinkTwo();

    glTranslatef(LENGTH_2, 0., 0.);
    glRotatef(θ3, 0., 0., 1.);
    DrawLinkThree();
    glPopMatrix();
}
```

### Using GLM

```
void DrawMechanism( float θ1, float θ2, float θ3 )
{
    glm::mat4 identity = glm::mat4(1.);
    glm::vec3 zaxis = glm::vec3(0., 0., 1.);
    glPushMatrix();
    glm::mat4 m1g = glm::rotate(identity, θ1, zaxis);
    glMultMatrixf( glm::value_ptr(m1g) );
    DrawLinkOne();

    glm::mat4 m21 = glm::translate(m1g, glm::vec3(LENGTH_1, 0., 0.));
    m21 = glm::rotate(m21, θ2, zaxis);
    glMultMatrixf( glm::value_ptr(m21) );
    DrawLinkTwo();

    glm::mat4 m32 = glm::translate(m21, glm::vec3(LENGTH_2, 0., 0.));
    m32 = glm::rotate(m32, θ3, zaxis);
    glMultMatrixf( glm::value_ptr(m32) );
    DrawLinkThree();
    glPopMatrix();
}
```

$$[M_{3/G}] = [M_{1/G}] * [M_{2/1}] * [M_{3/2}]$$

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## Passing GLM Matrices into a Vertex Shader

16

### In the shader:

```
uniform mat4 projectionMatrix;
uniform mat4 viewMatrix;
uniform mat4 modelMatrix;

mat4 PVM = projectionMatrix * viewMatrix * modelMatrix;
gl_Position = PVM * gl_Vertex;
```

### In the C/C++ program:

```
glm::mat4 projection = glm::perspective(D2R*90., 1., 0.1, 1000.);

glm::vec3 eye(0., 0., 3.);
glm::vec3 look(0., 0., 0.);
glm::vec3 up(0., 1., 0.);
glm::mat4 view = glm::lookAt(eye, look, up);

glm::mat4 model(1.); // identity
model = glm::rotate(model, D2R*Yrot, glm::vec3(0., 1., 0.));
model = glm::rotate(model, D2R*Xrot, glm::vec3(1., 0., 0.));

Pattern.Use();
Pattern.SetUniformVariable("projectionMatrix", projection);
Pattern.SetUniformVariable("viewMatrix", view);
Pattern.SetUniformVariable("modelMatrix", model);
```



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```
glm::mat4 projection = glm::perspective( D2R*90., 1., 0.1, 1000. );
projection[1][1] *= -1; // Vulkan's projected Y is inverted from OpenGL's

glm::vec3 eye(0.,0.,3.);
glm::vec3 look(0.,0.,0.);
glm::vec3 up(0.,1.,0.);
glm::mat4 view = glm::lookAt( eye, look, up );

glm::mat4 model( 1. ); // identity
model = glm::rotate( model, D2R*Yrot, glm::vec3(0.,1.,0.) );
model = glm::rotate( model, D2R*Xrot, glm::vec3(1.,0.,0.) );
```



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1

## Vertex Buffer Objects



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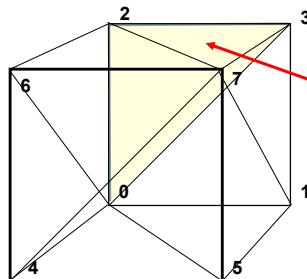
VertexBuffer.pptx

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1

### Remember this from the Geometric Modeling Notes?

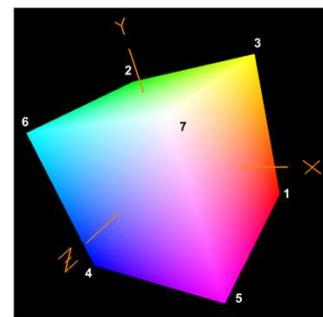
2



```
static GLfloat CubeVertices[ ][3] = {
{
    { -1., -1., -1. },
    { 1., -1., -1. },
    { -1., 1., -1. },
    { 1., 1., -1. },
    { -1., -1., 1. },
    { 1., -1., 1. },
    { -1., 1., 1. },
    { 1., 1., 1. }
};
```

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```
GLuint CubeTriangleIndices[ ][3] = {
{
    { 0, 2, 3 },
    { 0, 3, 1 },
    { 4, 5, 7 },
    { 4, 7, 6 },
    { 1, 3, 7 },
    { 1, 7, 5 },
    { 0, 4, 6 },
    { 0, 6, 2 },
    { 2, 6, 7 },
    { 2, 7, 3 },
    { 0, 1, 5 },
    { 0, 5, 4 }
};
```



```
static GLfloat CubeColors[ ][3] = {
{
    { 0., 0., 0. },
    { 1., 0., 0. },
    { 0., 1., 0. },
    { 1., 1., 0. },
    { 0., 0., 1. },
    { 1., 0., 1. },
    { 0., 1., 1. },
    { 1., 1., 1. }
};
```

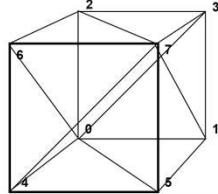
2

1

3

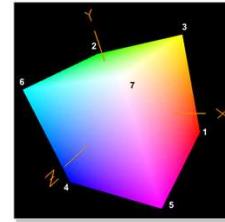
### Vertex Buffer Objects: The Big Idea

- Store vertex coordinates and vertex attributes on the **graphics card**.
- Optionally store the connections on the graphics card too.
- Every time you go to redraw, coordinates will be pulled from GPU memory instead of CPU memory, avoiding a significant amount of bus latency.



```
static GLfloat CubeVertices[ ][3] =
{
    { -1., -1., -1. },
    { 1., -1., -1. },
    { -1., 1., -1. },
    { 1., 1., -1. },
    { -1., -1., 1. },
    { 1., -1., 1. },
    { -1., 1., 1. },
    { 1., 1., 1. }
};
```

```
GLuint CubeTriangleIndices[ ][3] =
{
    { 0, 2, 3 },
    { 0, 3, 1 },
    { 4, 5, 7 },
    { 4, 7, 6 },
    { 1, 3, 7 },
    { 1, 7, 5 },
    { 0, 4, 6 },
    { 0, 6, 2 },
    { 2, 6, 7 },
    { 2, 7, 3 },
    { 0, 1, 5 },
    { 0, 5, 4 }
};
```



```
static GLfloat CubeColors[ ][3] =
{
    { 0., 0., 0. },
    { 1., 0., 0. },
    { 0., 1., 0. },
    { 1., 1., 0. },
    { 0., 0., 1. },
    { 1., 0., 1. },
    { 0., 1., 1. },
    { 1., 1., 1. }
};
```

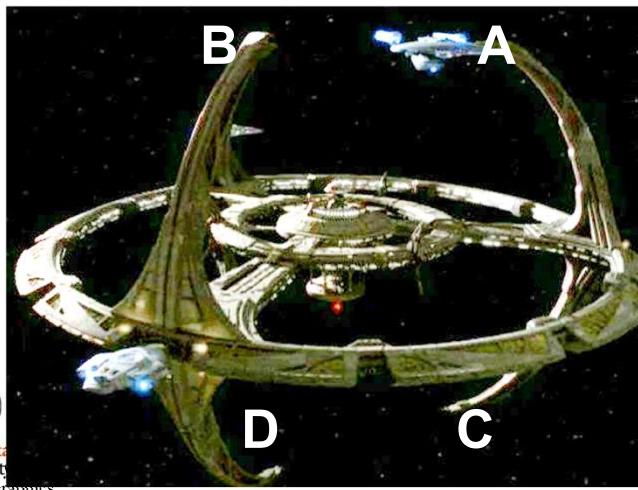
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3

### Did any of you ever watch Star Trek: Deep Space Nine?

4

It was about life aboard a space station. Ships docked at Deep Space Nine to unload cargo and pick up supplies. When a ship was docked at docking port "A", for instance, the supply-loaders didn't need to know what ship it was. They could just be told, "send these supplies out docking port A", and "bring this cargo in from docking port A".



Surprisingly, this actually has something to do with computer graphics! ☺



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4

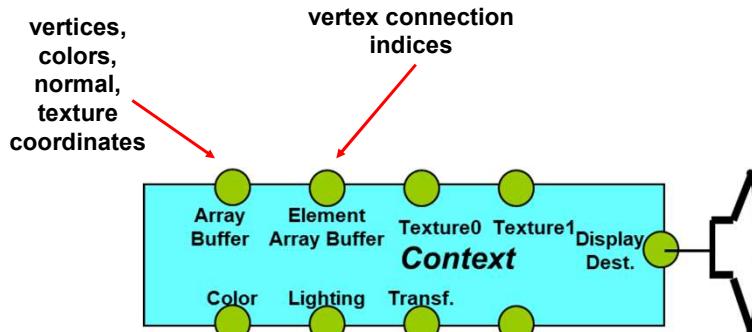
2

## The OpenGL Rendering Context

5

The OpenGL **Rendering Context** (also called “the **state**”) contains all the characteristic information necessary to produce an image from geometry. This includes the current transformation, color, lighting, textures, where to send the display, etc.

Each window (e.g., glutCreateWindow) has its own rendering context.



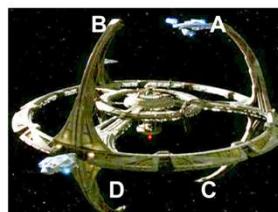
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5

## More Background – “Binding” to the Context

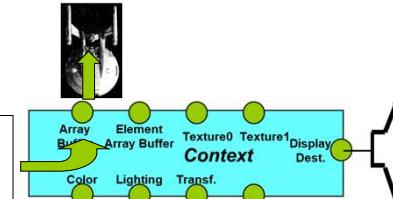
6

The OpenGL term “binding” refers to “attaching” or “docking” (a metaphor which I find to be more visually pleasing) an OpenGL object to the Context. You can then assign characteristics, and they will “flow in” through the Context into the object.



```
glBindBuffer( GL_ARRAY_BUFFER, bufA );
glBufferData( GL_ARRAY_BUFFER, numBytes, data, usage );
```

Vertex Buffer Object pointed to by bufA



Ships docked at Deep Space Nine to unload cargo and pick up supplies. When a ship was docked at docking port “A”, for instance, the supply-loaders didn’t need to know what ship it was. They could just be told, “send these supplies out docking port A”, and “pick up this cargo from docking port A”.

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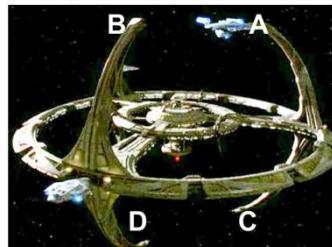
6

3

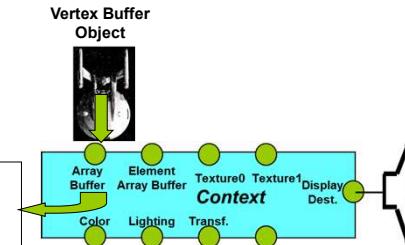
## More Background – “Binding” to the Context

7

When you want to *use* that Vertex Buffer Object, just bind it again. All of the characteristics will then be active, just as if you had specified them again. Its contents will “flow out” of the object into the Context.



```
glBindBuffer( GL_ARRAY_BUFFER, bufA );
glDrawArrays( GL_TRIANGLES, 0, numVertices );
```



## More Background – How do you Create an OpenGL “Buffer Object”?

8

When creating data structures in C++, objects are pointed to by their addresses.

In OpenGL, objects are pointed to by an unsigned integer “handle”. You can assign a value for this handle yourself (not recommended), or have OpenGL generate one for you that is guaranteed to be unique. For example:

How many “handles” to generate      The “array” to put them in

```
GLuint bufA;
glGenBuffers( 1, &bufA );
```

OpenGL then uses these handles to determine the actual GPU memory addresses to use.

## Loading data into the currently-bound Vertex Buffer Object

9

**glBufferData( type, numBytes, data, usage );**

*type* is the type of buffer object this is:

Use **GL\_ARRAY\_BUFFER** to store floating point vertices, normals, colors, and texture coordinates

*numBytes* is the number of bytes to store all together. It's not the number of numbers, not the number of coordinates, not the number of vertices, but the number of **bytes**!

*data* is the memory address of (i.e., pointer to) the data to be transferred from CPU memory to the graphics memory. (This is allowed to be NULL, indicating that you will transfer the data over later.)



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9

## Loading data into the currently-bound Vertex Buffer Object

10

**glBufferData( type, numBytes, data, usage );**

*usage* is a hint as to how the data will be used: GL\_xxx\_yyy

where xxx can be:

STATIC	this buffer will be re-written seldom
DYNAMIC	this buffer will be re-written often

and yyy can be:

DRAW	this buffer will be used for drawing
READ	this buffer will be copied into

For what we are doing, use **GL\_STATIC\_DRAW**



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10

11

### Step #1 – Fill the C/C++ Arrays with Drawing Data (vertices, colors, ...)

```
GLfloat Vertices[ ][3] =
{
    { 1., 2., 3. },
    { 4., 5., 6. },
    ...
};
```

### Step #2 – Transfer the Drawing Data

```
glGenBuffers( 1, &bufA );

 glBindBuffer( GL_ARRAY_BUFFER, bufA );
 glBufferData( GL_ARRAY_BUFFER, 3*sizeof(GLfloat)*numVertices, Vertices, GL_STATIC_DRAW );
```



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11

12

### Step #3 – Activate the Drawing Data Types That You Are Using

```
glEnableClientState( type );
```

where *type* can be any of:

```
GL_VERTEX_ARRAY
GL_COLOR_ARRAY
GL_NORMAL_ARRAY
GL_TEXTURE_COORD_ARRAY
```

- Call this as many times as you need to enable all the drawing data types that you are using.
- To deactivate a type, call:

```
glDisableClientState( type );
```



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12

13

#### Step #4 – To start the drawing process, bind the Buffer that holds the Drawing Data

```
glBindBuffer( GL_ARRAY_BUFFER, bufA );
```



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13

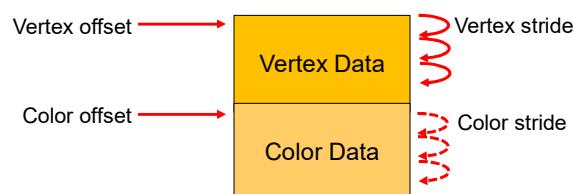
#### Step #5 – Then, specify how to get at each Data Type within that Buffer

14

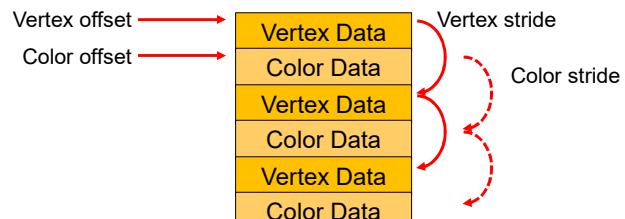
**offset** is the number of byte offsets from the start of the data array buffer to where the first element of this part of the data lives

**stride** is the number of bytes between the same type of data

Information can be stored as packed, like this:



Information can be stored as interleaved, like this:



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14

### Step #5 – Then, specify how to get at each Data Type within that Buffer

15

```
glVertexPointer( size, type, stride, offset);
glColorPointer( size, type, stride, offset);
glNormalPointer( type, stride, offset);
glTexCoordPointer( size, type, stride, offset);
```



vs.



*size* is the “how many numbers per vertex”, and can be: 2, 3, or 4

*type* can be:

GL\_SHORT  
GL\_INT  
GL\_FLOAT  
GL\_DOUBLE

*stride* is the byte offset between consecutive entries in the buffer (0 means tightly packed)



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15

### The Data Types in a vertex buffer object can be stored either as “packed” or “interleaved”

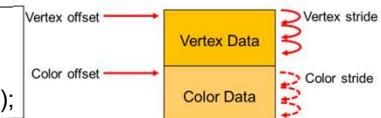
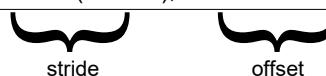
16

```
gl*Pointer( size, type, stride, offset);
```

Packed:

```
glVertexPointer( 3, GL_FLOAT, 3*sizeof(GLfloat), 0 );
```

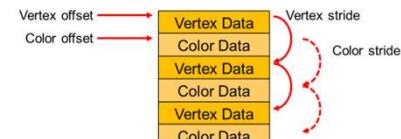
```
glColorPointer( 3, GL_FLOAT, 3*sizeof(GLfloat), 3*numVertices*sizeof(GLfloat));
```



Interleaved:

```
glVertexPointer( 3, GL_FLOAT, 6*sizeof(GLfloat), 0 );
```

```
glColorPointer( 3, GL_FLOAT, 6*sizeof(GLfloat), 3*sizeof(GLfloat) );
```



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16

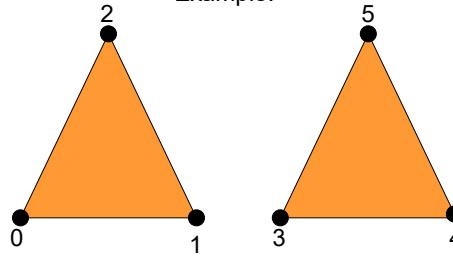
## Step #6 – Draw!

17

```
glDrawArrays( GL_TRIANGLES, first, numVertices );
```

This is how you do it if your vertices can be drawn in consecutive order

Example:



Start with vertex #0

```
glDrawArrays( GL_TRIANGLES, 0, 6 );
```

Draw 6 vertices



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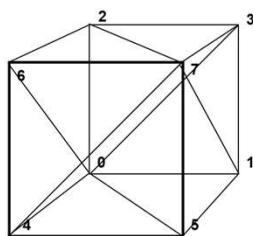
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17

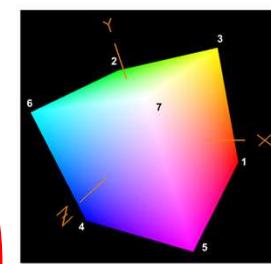
## What if your vertices need to be accessed in random order?

18



```
static GLfloat CubeVertices[ ][3] = {
    { -1., -1., -1. },
    { 1., -1., -1. },
    { -1., 1., -1. },
    { 1., 1., -1. },
    { -1., -1., 1. },
    { 1., -1., 1. },
    { -1., 1., 1. },
    { 1., 1., 1. }
};
```

```
GLuint CubeTriangleIndices[ ][3] = {
    { 0, 2, 3 },
    { 0, 3, 1 },
    { 4, 5, 7 },
    { 4, 7, 6 },
    { 1, 3, 7 },
    { 1, 7, 5 },
    { 0, 4, 6 },
    { 0, 6, 2 },
    { 2, 6, 7 },
    { 2, 7, 3 },
    { 0, 1, 5 },
    { 0, 5, 4 }
};
```



```
static GLfloat CubeColors[ ][3] = {
    { 0., 0., 0. },
    { 1., 0., 0. },
    { 0., 1., 0. },
    { 1., 1., 0. },
    { 0., 0., 1. },
    { 1., 0., 1. },
    { 0., 1., 1. },
    { 1., 1., 1. }
};
```



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18

19

### Cube Example

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19

20

```

glEnableClientState(GL_VERTEX_ARRAY);
glEnableClientState(GL_COLOR_ARRAY);
glVertexPointer(3, GL_FLOAT, 0, (GLchar*) 0 );
glColorPointer(3, GL_FLOAT, 0, (GLchar*)
    (3*sizeof(GLfloat)*numVertices) );
glBegin(GL_TRIANGLES);
    glArrayElement(0);
    glArrayElement(2);
    glArrayElement(3);
    glArrayElement(0);
    glArrayElement(3);
    glArrayElement(1);
    glArrayElement(4);
    glArrayElement(5);
    glArrayElement(7);
    glArrayElement(4);
    glArrayElement(7);
    glArrayElement(6);
    glArrayElement(1);
    glArrayElement(3);
    glArrayElement(7);
    glArrayElement(1);
    glArrayElement(7);
    glArrayElement(5);
    ...

```

**Vertex Data**  
**Color Data**

```

...
glArrayElement(0);
glArrayElement(4);
glArrayElement(6);
glArrayElement(0);
glArrayElement(6);
glArrayElement(2);
glArrayElement(2);
glArrayElement(6);
glArrayElement(7);
glArrayElement(2);
glArrayElement(7);
glArrayElement(3);
glArrayElement(0);
glArrayElement(1);
glArrayElement(5);
glArrayElement(0);
glArrayElement(5);
glArrayElement(4);
glEnd();

```

**But, this requires that all these glArrayElement() calls happen on the CPU and get transmitted across the bus to the GPU!**

```

GLuint CubeTriangleIndices[ ] = {
    {0, 2, 3},
    {0, 3, 1},
    {4, 5, 7},
    {4, 7, 6},
    {1, 3, 7},
    {1, 7, 5},
    {0, 4, 6},
    {0, 6, 2},
    {2, 6, 7},
    {2, 7, 3},
    {0, 1, 5},
    {0, 5, 4}
};

```

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20

It would be better if that index array was stored over on the GPU as well

21

```
glBindBuffer( GL_ARRAY_BUFFER, bufA );
glBufferData( GL_ARRAY_BUFFER, 3*sizeof(GLfloat)*numVertices, CubeVertices, GL_STATIC_DRAW );

glBindBuffer( GL_ELEMENT_ARRAY_BUFFER, bufB );
glBufferData( GL_ELEMENT_ARRAY_BUFFER, sizeof(GLuint)*numIndices, CubeTriangleIndices, GL_STATIC_DRAW );
```



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21

## The glDrawElements( ) call

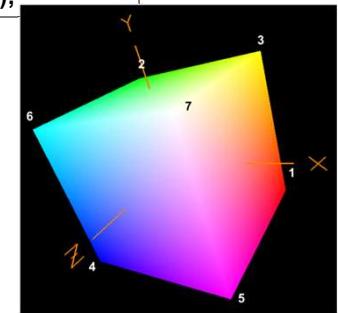
22

```
glBindBuffer( GL_ARRAY_BUFFER, bufA );
glBindBuffer( GL_ELEMENT_ARRAY_BUFFER, bufB );

glEnableClientState( GL_VERTEX_ARRAY );
glEnableClientState( GL_COLOR_ARRAY );

glVertexPointer( 3, GL_FLOAT, 0, (Gluchar*) 0 );
glColorPointer( 3, GL_FLOAT, 0, (Gluchar*)(3*sizeof(GLfloat)*numVertices) );

glDrawElements( GL_TRIANGLES, 36, GL_UNSIGNED_INT, (Gluchar*) 0 );
```



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22

## Writing Data into a Buffer Object, Treating it as a C/C++ Array of Structures

23

```
float * vertexArray = glMapBuffer( GL_ARRAY_BUFFER, usage );
```

*usage* is how the data will be accessed:

GL_READ_ONLY	the vertex data will be read from, but not written to
GL_WRITE_ONLY	the vertex data will be written to, but not read from
GL_READ_WRITE	the vertex data will be read from and written to

You can now use **vertexArray[ ]** like any other C/C++ floating-point array of structures.

When you are done, be sure to call:

```
glUnmapBuffer( GL_ARRAY_BUFFER );
```



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23

## glMapBuffer Example

24

```

struct Point
{
    float x, y, z;
    float nx, ny, nz;
    float r, g, b;
    float s, t;
};

...

glGenBuffers( 1, &pbuffer );
glBindBuffer( GL_ARRAY_BUFFER, pbuffer );
glBufferData( GL_ARRAY_BUFFER, numPoints * sizeof(struct Point), NULL, GL_STATIC_DRAW );
struct Point * paray = (struct Point *) glMapBuffer( GL_ARRAY_BUFFER, GL_WRITE_ONLY );
for( int i = 0; i < numPoints; i++ )
{
    paray[i].x = PointVec[i].x;
    paray[i].y = PointVec[i].y;
    paray[i].z = PointVec[i].z;
    paray[i].nx = PointVec[i].nx;
    paray[i].ny = PointVec[i].ny;
    paray[i].nz = PointVec[i].nz;
    paray[i].r = PointVec[i].r;
    paray[i].g = PointVec[i].g;
    paray[i].b = PointVec[i].b;
    paray[i].s = PointVec[i].s;
    paray[i].t = PointVec[i].t;
}
glUnmapBuffer( GL_ARRAY_BUFFER );

```



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24

## Using our Vertex Buffer Object C++ Class

25

### Declaring a Global:

```
VertexBufferObject VB;
```

### Filling:

```
VB.Init();
VB.glBegin( GL_TRIANGLES ); // can be any of the OpenGL topologies
for( int i = 0; i < 12; i++ )
{
    for( int j = 0; j < 3; j++ )
    {
        int k = CubeTriangleIndices[ i ][ j ];
        VB	glColor3fv( CubeColors[ k ] );
        VB glVertex3fv( CubeVertices[ k ] );
    }
}
VB.glEnd();
```

### Drawing:

```
VB.Draw();
```

This is available from our Class Resources page


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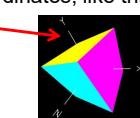
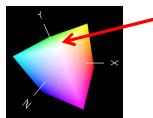
25

## Vertex Buffer Object Class Methods

26

```
void CollapseCommonVertices( bool );
```

*true* means to not replicate common vertices in the internal vertex table. This is good if all uses of a particular vertex will have the same normal, color, and texture coordinates, like this – instead of like this.



```
void Draw( );
```

Draw the primitive. If this is the first time Draw( ) is being called, it will setup all the proper buffer objects, etc. If it is a subsequent call, then it will just initiate the drawing.

```
void DrawInstanced( numInstances );
```

Same as Draw( ), but will draw multiple instances. Must be using shaders to make this worthwhile.

```
void glBegin( topology );
```

Begin the definition of a primitive.

```
void glColor3f( r, g, b);
void glColor3fv( rgb[ 3 ] );
```

Specify a vertex's color.

Ore  
Ur  
Compu

Terminate the definition of a primitive.

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26

## Vertex Buffer Object Class Methods

27

void glNormal3f( nx, ny, nz );	Specify a vertex's normal.
void glNormal3fv( nxyz[ 3 ] );	
void glTexCoord2f( s, t );	Specify a vertex's texture coordinates.
void glTexCoord2fv( st[ 2 ] );	
void glVertex3f( x, y, z);	Specify a vertex's coordinates.
void glVertex3fv( xyz[ 3 ] );	
void Print( char *text, FILE * );	Prints the vertex, normal, color, texture coordinate, and connection element information to a file, along with some preliminary text. If the file pointer is not given, standard error (i.e., the console) is used.
void RestartPrimitive( );	Causes the primitive to be restarted. This is useful when doing triangle strips or quad strips and you want to start another one without getting out of the current one. By doing it this way, all of the strips' vertices will end up in the same table, and you only need to have one <i>VertexBufferObject</i> class going.



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27

## Notes

28

- If you want to print the contents of your data structure to a file (for debugging or curiosity), do this:

```
FILE *fp = fopen( "debuggingfile.txt", "w" );
if( fp == NULL )
{
    fprintf( stderr, "Cannot create file 'debuggingfile.txt'\n" );
}
else
{
    VB.Print( "My Vertex Buffer :", fp );
    fclose( fp );
}
```
- You can call the *glBegin* method more than once. Each call will wipe out your original display information and start over from scratch. This is useful if you are interactively editing geometry, such as sculpting a curve.



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28

29

### A Caveat

Be judicious about collapsing common vertices! The good news is that it saves space and it might increase speed some (by having to transform fewer vertices). But, the bad news is that it takes much longer to create large meshes. Here's why.

Say you have a 1,000 x 1,000 point triangle mesh, drawn as 999 triangle strips, all in the same *VertexBufferObject* class (which you can do using the *RestartPrimitive* method).

When you draw the S<sup>th</sup> triangle strip, half of those points are coincident with points in the S-1<sup>st</sup> strip. But, to find those 1,000 coincident points, it must search through 1000\*S points first. There is no way to tell it to only look at the last 1,000 points. Even though the search is only O(log<sub>2</sub>N), where N is the number of points kept so far, it still adds up to a lot of time over the course of the entire mesh.

It starts out fast, but slows down as the number of points being held increases.

If you did have a 1,000 x 1,000 mesh, it might be better to not collapse vertices at all. Or, a compromise might be to collapse vertices, but break this mesh up into 50 *VertexBufferObjects*, each of size 20 x 1,000.



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Just a thought...

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29

30

### Drawing the Cube With Collapsing Identical Vertices

```
GLuint CubeTriangleIndices[] = [
{
    { 0, 2, 3 },
    { 0, 3, 1 },
    { 4, 5, 7 },
    { 4, 7, 6 },
    { 1, 3, 7 },
    { 1, 7, 5 },
    { 0, 4, 6 },
    { 0, 6, 2 },
    { 2, 6, 7 },
    { 2, 7, 3 },
    { 0, 1, 5 },
    { 0, 5, 4 }
};
```

#### Define 8 points

X	Y	Z
-1.00	-1.00	-1.00
-1.00	1.00	-1.00
1.00	1.00	-1.00
1.00	-1.00	-1.00
-1.00	-1.00	1.00
1.00	-1.00	1.00
1.00	1.00	1.00
-1.00	1.00	1.00

#### Define 8 colors

R	G	B
0.00	0.00	0.00
0.00	1.00	0.00
1.00	1.00	0.00
1.00	0.00	0.00
0.00	0.00	1.00
1.00	0.00	1.00
1.00	1.00	1.00
0.00	1.00	1.00

#### Draw 36 array indices:

0	2	3
0	3	1
4	5	7
4	7	6
1	3	7
1	7	5
0	4	6
0	6	2
2	6	7
2	7	3
0	1	5
0	5	4

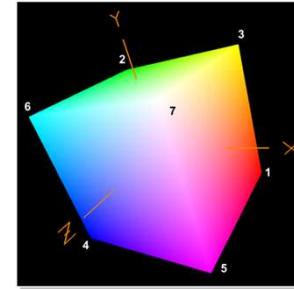
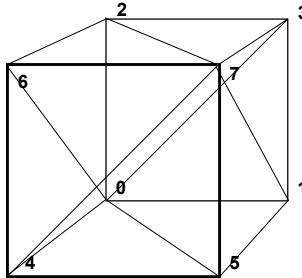
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30

## Drawing the Cube Without Collapsing Identical Vertices

31



Define 36 vertices and 36 colors

X	Y	Z
-1.	-1.	-1.
...		

R	G	B
0.	0.	0.
...		



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31

## Using Vertex Buffers with Shaders

32

Let's say that we have the following **vertex shader** and we want to supply the vertices from a Vertex Buffer Object.

```
in vec3 aVertex;
in vec3 aColor;

out vec3 vColor;

void
main( )
{
    vColor = aColor;
    gl_Position = gl_ModelViewProjectionMatrix * vec4( aVertex, 1. );
}
```

Let's also say that, at some time, we want to supply the colors from a Vertex Buffer Object as well, but for right now, the color will be uniform.



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32

## Using Vertex Buffers with Shaders

33

- We're assuming here that
- we already have the shader program setup in *program*
  - we already have the vertices in the *vertexBuffer*

```
glBindBuffer( GL_ARRAY_BUFFER, vertexBuffer );

glEnableClientState( GL_VERTEX_ARRAY );
glEnableClientState( GL_COLOR_ARRAY );

GLuint vertexLocation = glGetUniformLocation( program, "aVertex" );
GLuint colorLocation = glGetUniformLocation( program, "aColor" );

glVertexAttribPointer( vertexLocation, 3, GL_FLOAT, GL_FALSE, 0, (GLuchar *)0 );
glEnableVertexAttribArray( vertexLocation ); // dynamic attribute

glVertexAttrib3f( colorLocation, r, g, b ); // static attribute
glEnableVertexAttribArray( colorLocation );

glDrawArrays( GL_TRIANGLES, 0, 3*numTris );
```



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33

## Using Vertex Buffers with the Shaders C++ Class

34

- We're assuming here that
- we already have the vertices in the *vertexBuffer*
  - we have already created a C++ GLSLProgram class object called *Pattern*

```
glBindBuffer( GL_ARRAY_BUFFER, vertexBuffer );

glEnableClientState( GL_VERTEX_ARRAY );
glEnableClientState( GL_COLOR_ARRAY );

Pattern.SetVertexAttributePointer3fv( "aVertex", (GLfloat *)0 );
Pattern.EnableVertexAttribArray( "aVertex" ); // dynamic attribute

Pattern.SetVertexAttributeVariable( "aColor", r, g, b ); // static attribute
Pattern.EnableVertexAttribArray( "aColor" );

glDrawArrays( GL_TRIANGLES, 0, 3*numTris );
```



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34