

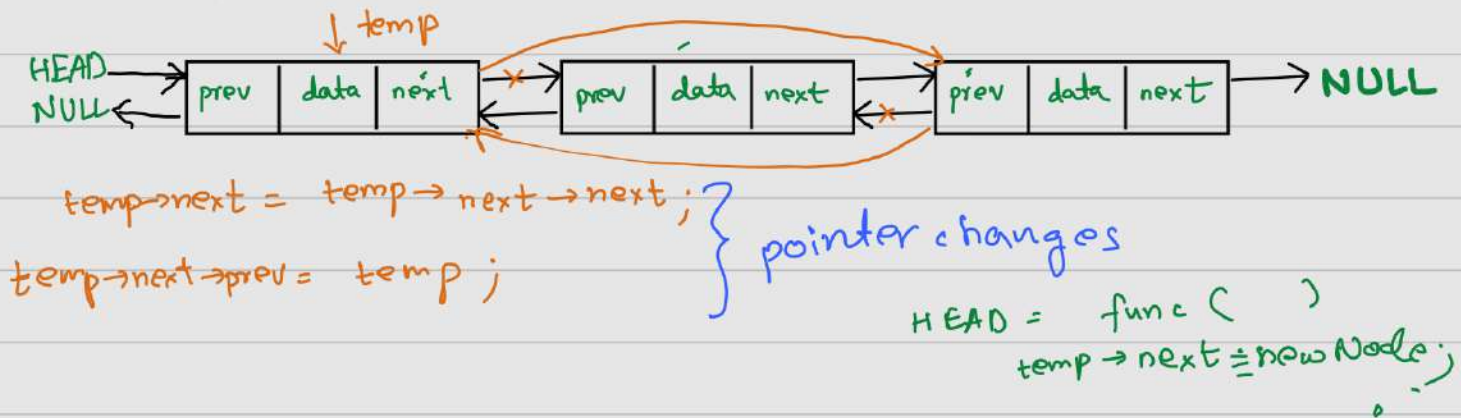
```

newNode → next = temp → next;
newNode → prev = temp;
temp → next → prev = newNode;
temp → next = newNode;

```

## DELETION

### Deletion of inner node



## STACK

Linear data structure following principle of (LIFO)  
(last-in First-out)



Putting an item on top is called "push" & removing is called "pop"

### Main Operations:

★ Push - adds element on top

- ★ Pop - Removes element from top
- ★ IsEmpty - check if stack is empty
- ★ Is Full - If stack is full
- ★ Top - returns the top element

## Working

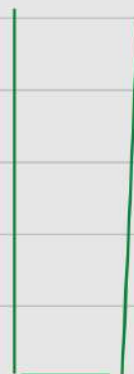
- A pointer **TOP** keeps track of top element
- When initialising the stack, we set **TOP** value to -1 so as to check for emptiness
- Pushing the value we increase the value of top & place new element at position pointed by **TOP**
- On popping remove the element from top.
- Before pushing check if it's full
- Before popping check if it's empty

Application → Used in function calls, Recursion expression evaluation.

## Balanced Brackets

consider a string "{ } { { } } { { } }". You need to check if all pairs of brackets "{}" are paired up & in-order.

Eg. " { } { } { { } } " not balanced  
 " { } } } { { } " not balanced



## Next bigger element.

Given an array find the next bigger element of every element & if there doesn't exist any mark it -1.

Original Ar: 6 7 4 5 1 2 10

Ans: 7 10 5 10 10 10 -1

idea: Use 2 loops, 1<sup>st</sup> iterate over all elements & then for each element find the next greater element.

```
for (int i = 0; i < n; ++i)
{
    for (int j = i + 1; j < n; ++j)
    {
        =;
    }
}
```

Time complexity:  $O(n^2)$

$$\begin{aligned} f(n) &= \sum_{i=0}^{n-1} (n-1) - (i+1) \\ &= (n-1)^2 - \sum_{i=0}^{n-1} (i+1) \\ &\approx O(n^2) \end{aligned}$$

Better idea: Using Stack: Time Complexity:  $O(n)$

Starting from end keep a stack of next greater possibilities  
element

you have answer till here, ←

6 7 4 5 1 2 10  
7 10 5 10 2 10 -1

could you ans. for this index?

if  $a[i] < a[i+1]$   $a[i+1]$  is the ans  
otherwise check if with ans. of  $a[i+1]$  is ans. or not & similarly move until you get the ans.



In other words you compare first with last possible ans.

6 7 4 5 1 2 10  
7 10 5 10 2 10 -1

7  
10

### Calculator problem

$$1 + (2 + 3 - (4 + 5) - 6) + 7$$

keep sum & sign variables extract number  
add them to sum variable acc. to their sign  
as soon as you encounter "(" put the current  
sum & sign as a pair in the stack. & set  
sum = 0. Then as you encounter ")"  
take out top of the stack & make the  
sum = Top.first + Top.second \* sum

Remember if you encounter '-' change the  
sign

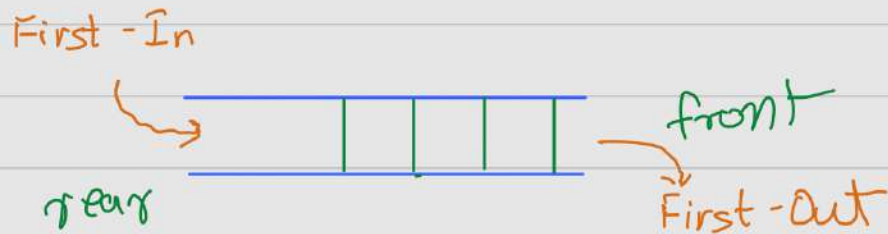
$$( \text{---} * ( \text{---} ) * \text{---} )$$

eval-val

$$\text{sum} + \text{sign} * \text{eval-val}$$

# QUEUE

Queue is a linear data structure following FIFO rule (First-In First-Out)



Putting items in queue is called "enqueue" & removing these items is called "dequeue"

## Basic Operations

- \* Enqueue → add element to the end
- \* Dequeue → Remove an element from front
- \* IsEmpty → If it's empty returns true else false
- \* IsFull → If it's full
- \* Front → returns you the front element

## Working

- two pointers FRONT & REAR.
- FRONT tracks first element
- REAR tracks last element
- Initially both set to -1.

## Enqueue

- Check if queue is full
- For 1<sup>st</sup> element i.e. if it had been empty set FRONT to 0



→ increase REAR by 1.

→ add element in position of REAR

## Dequeue

→ check if queue is empty

→ return value pointed by front

→ increase FRONT by 1 index

→ For last element, reset value of FRONT & REAR to -1.

## Shortest path in a maze

mxn grid



Idea: Inspired from water ripples

Starting from "start" travel like ripple & update the distance if it's not a obstacle & mark visited so that you don't visit it again for updation (1<sup>st</sup> updation) will give the min distance

Time complexity:  $O(mn)$

X: obstacles

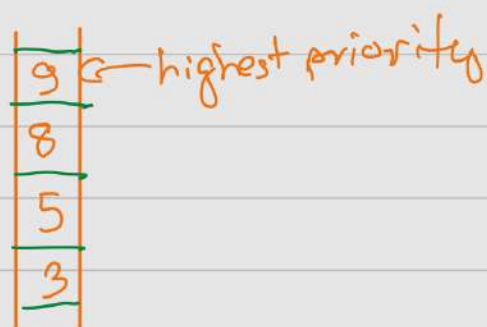
neigh valid  $\rightarrow$  obstacle  
vist  $>$  X

$dis[i][j] = \text{min distance of } (i,j) \text{ from start}$

$vis[i][j] = (i,j)$  has been visited / distance been updated.

# PRIORITY QUEUE

It is a special type of queue in which each element is associated with a priority value and elements with higher priority are served first.



## C++ Priority queue methods:

push(): inserts element in priority queue

pop(): removes the element with highest priority

top(): returns the element with highest priority

size(): size of priority queue

empty(): if priority queue is empty or not

By-default: bigger-element is given higher priority

It is implemented by heap which we will learn more about this later

" Used to work with highest priority element at



the moment "

Qn: Merge 2 sorted lists.

A  $\xrightarrow{\quad\quad\quad} O(m)$

1	1	2	4	5
---	---	---	---	---

B  $\xrightarrow{\quad\quad\quad} n \cdot O(n)$

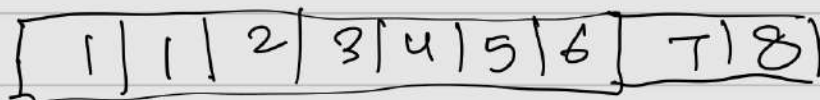
3	6	7	8
---	---	---	---

Output merge sorted array

trivial idea



$O((m+n) \log(m+n))$  Merge them into one array  
& then sort the completely merged array



$O(m+n)$

Qn: Merge  $k$  sorted lists



priority-queue



take all the 1<sup>st</sup> element

$(-1, 1)$

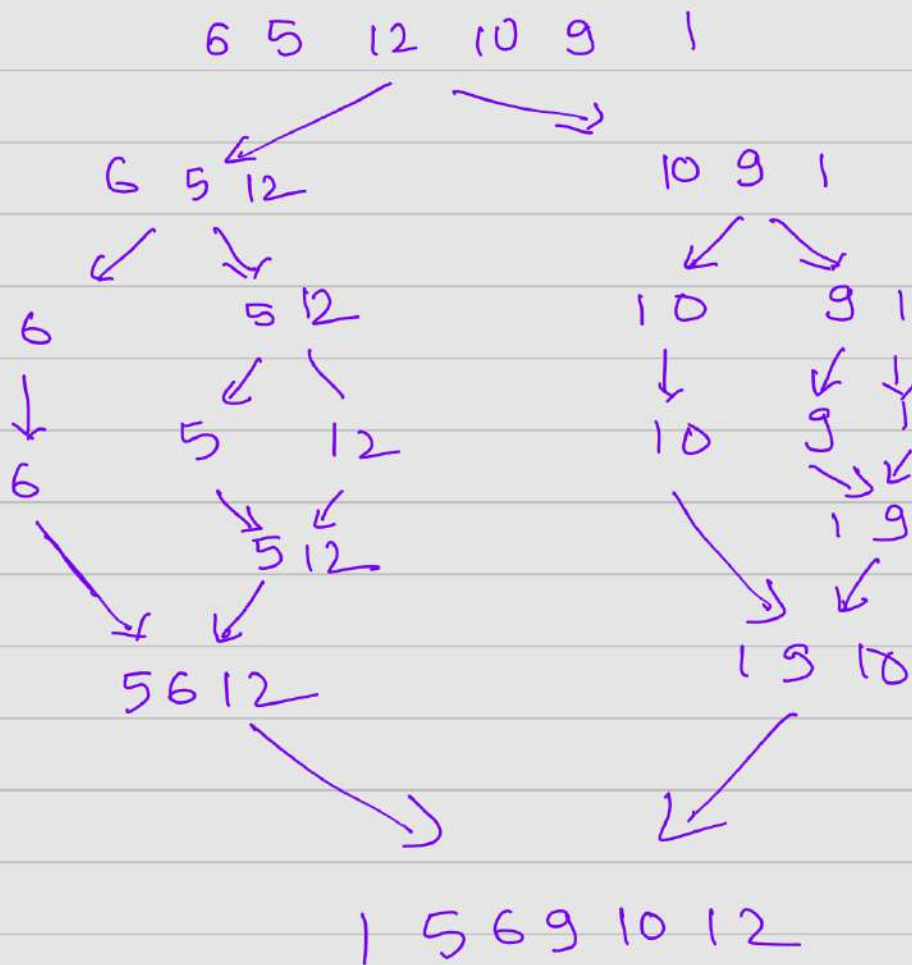




# Merge Sort

## Divide & Conquer Strategy

- Divide the two arrays in two halves ← Divide
- Recursively sort the two parts ← Conquer
- Merge them to form final array ← Combine



Pseudo code:

```
mergeSort(A, p, r) {  
    if p > r  
        return  
    q = (p + r) / 2
```

mergeSort(A, p, q) —  $T(n/2)$

mergeSort(A, q+1, r) —  $T(n/2)$

merge(A, p, q, r) } —  $O(n)$

$$T(n) = 2T\left(\frac{n}{2}\right) + cn$$

$$T(1) = 1$$

Time complexity :  $O(n \log n)$

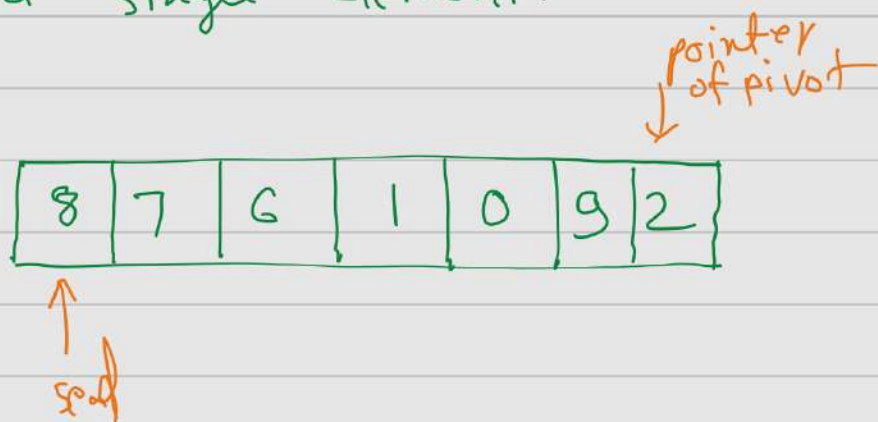
## Quick sort

• Divide & conquer approach

→ Choose pivot element. Partition the array st. all smaller elements belong to one side & other elements bigger than pivot on the other side.

→ Do this recursively for each side of the pivot. This continues until each subarray contains a single element.

partitioning of  
array in  
 $O(n)$



Quick Sort (A, left, right)

if (left < right)

{ pivot\_ind ← partition(A, left, right)

QuickSort(A, left, pivot\_ind - 1)

QuickSort(A, pivot\_ind + 1, right)

}

quicksort(arr, low, pi-1)



Sorting the elements on the left of pivot using recursion

quicksort(arr, pi+1, high)



Sorting the elements on the right of pivot using recursion

Please Read & Practice those two sortings. Write their implementation once.