

Ex 2.14. Solution. (Lecture 7 Slide 7).

$$f(x) = \sum_{i=0}^N a_i x^i$$

poly = 0.  
for (i=N; i ≥ 0; --i)  
poly = x \* poly + a[i]

a)  $x=3$   $f(x) = 4x^4 + 8x^3 + x + 2$   
 $N=4$ , we know  $x=3$ .

So $i=4$	$a[4]=4$	$\text{poly} = 3 * 0 + 4 = 4$
$i=3$	$a[3]=8$	$\text{poly} = 3 * 4 + 8 = 20$
$i=2$	$a[2]=0$ (no $x^2$ term in $f(x)$ )	$\text{poly} = 3 * 20 + 0 = 60$
$i=1$	$a[1]=1$	$\text{poly} = 3 * 60 + 1 = 181$
$i=0$	$a[0]=2$	$\text{poly} = 3 * 181 + 2 = \underline{\underline{545}}$

b)  $\sum_{i=0}^N a_i x^i = a_N x^N + a_{N-1} x^{N-1} + \dots + a_1 x + a_0$   
 $= \underbrace{x(x \dots x(x(a_N) + a_{N-1}) + a_{N-2}) \dots a_1)}_{N \text{ multiplications}} + a_0$

c)  $N$  multiplications. So  $O(N)$