# chapter 2- Sorting and Searching Algorithms

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#### Introduction

Objective: Understand and implement basic sorting and searching algorithms.

### Algorithms Covered:

- Searching Algorithms: Linear Search (Sequential Search), Binary Search
- Sorting Algorithms: Insertion Sort, Selection Sort, Bubble Sort, Pointer Sort

### Why Study Sorting & Searching?

- Common tasks for most computer systems.
- Sorting and searching are fundamental operations, impacting performance and efficiency.
- Practical applications in databases, file systems, and more.

#### > Activity:

• Student Task: Implement a simple sorting algorithm and a searching algorithm. Then, analyze their time complexities.

### **Simple Searching Algorithms**

- 1. Simple Searching algorithms
- Searching:- is a process of finding an element in a list of items or determining that the item is not in the list.
- ☐ Algorithm:
  - 1. Start.
  - 2. Set the list of numbers and the target value (key).
  - 3. Initialize a variable `index` to -1 (to store the index of the found element).
  - 4. Loop through the list starting from the first element:
    - a) Compare the current element with the target value.
    - b) If the current element matches the target:- Set `index` to the current position and exit the loop.
    - c) If the current element does not match, continue to the next element.
  - 5. After the loop:
    - a) If `index` is not -1, print the index where the element was found.
    - b) If `index` is still -1, print "Element not found".
  - 6. End
- ☐ Activity:
  - Write C++ code to Implement Linear Search in your IDE. Test with a list of integers.

#### Cont'd

#### Implementation: Assume the size of the list is n.

```
int LinearSearch(int list[], int key)
    index=-1;
    for(int i=0; i<n; i++)
      if(list[i]==key)
          index=i;
          break;
          return index;
```

# **Complexity Analysis:**

 Big-Oh of sequential searching → How many comparisons are made in the worst case ? n → O(n).

### B). Binary Searching

- Assume sorted data.
- Use Divide and conquer strategy (approach).

#### **Algorithm (Pseudo code):**

- 1. Start
- 2. Set the list of sorted numbers and the target value (key).
- 3. Initialize variables `top` (start index) and `bottom` (end index).
- 4. Loop until `top` is less than or equal to `bottom`:
  - a) Calculate the middle index:  $\dot$  middle = (top + bottom) / 2.
  - b) If the middle element is equal to the key, return `middle` as the index.
  - c) If the key is smaller than the middle element, set `bottom = middle 1` to search the left half.
  - d) If the key is larger than the middle element, set `top = middle + 1` to search the right half.
- 5. If the loop ends and the key is not found, return -1.
- 6. End
- ☐ Activity:
  - Write C++ code to Implement Binary Search in your IDE. Test with a list of integers.

# **Implementation:**

```
int BinarySearch(int list[], int key)
                                       if(found==0)
                                         index=-1;
  int found=0,index=0;
                                        else
  int top=n-1,bottom=0,middle;
                                         index=middle;
do{
                                       return index;
   middle=(top + bottom)/2;
  if(key==list[middle])
    found=1;
                                       Complexity Analysis:
  else{
    if(key<list[middle])</pre>
                                       Example: Find Big-Oh of
        top=middle-1;
                                       Binary search algorithm in
    else
                                       the worst case analysis.
       bottom=middle+1;
                                              \rightarrow O(log n)
} while(found==0 && top>=bottom);
```

# 2. Simple Sorting Algorithms

**Sorting:** is a process of reordering a list of items in either increasing or decreasing order.

- Ordering a list of items is fundamental problem of computer science.
- Sorting is the most important operation performed by computers.
- Sorting is the first step in more complex algorithms.

### Two basic properties of sorting algorithms:

**In-place:** It is possible to sort very large lists without the need to allocate additional working storage.

### 2. Simple Sorting Algorithms

**Stable:** If two elements that are equal, they will remain in the same relative position after sorting is completed.

#### Two classes of sorting algorithms:

O(n²): Includes the bubble, insertion, and selection sorting algorithms.

O(nlog n):Includes the heap, merge, and quick sorting algorithms.

Simple sorting algorithms include:

- i. Simple sorting
- ii. Bubble Sorting
- iii. Selection Sorting
- iv. Insertion Sorting
- v. Pointer Sorting

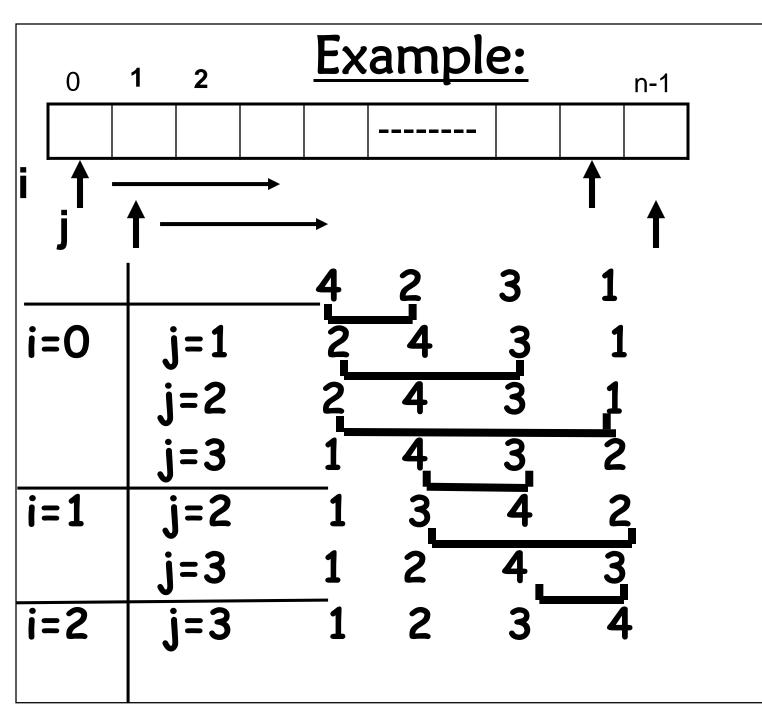
### I. Simple sorting

### **Algorithm:**

- In simple sort algorithm the first element is compared with the second, third and all subsequent elements.
- If any one of the other elements is less than the current first element then the first element is swapped with that element.
- Eventually, after the last element of the list is considered and swapped, then the first element has the smallest element in the list.
- The above steps are repeated with the second, third and all subsequent elements.

### **Implementation:**

```
Void SimpleSort(int list[])
 for(int i=0; i < = n-2; i++)
    for(int j=i+1; j < = n-1; j++)
        if(list[i] > list[j])
            int temp;
           temp=list[i];
            list[i] = list[j];
            list[j]=temp;
```



### Analysis: O(?)

```
1st pass----- (n-1) comparisons

2nd pass---- (n-2) comparisons

(n-1)th pass---- 1 comparison

T(n)=1+2+3+4+----+(n-2)+(n-1)

= (n*(n-1))/2

= n^2/2-n/2

= O(n^2)
```

#### **Complexity Analysis:**

- Analysis involves number of comparisons and swaps.
- How many comparisons?

$$1+2+3+...+(n-1)=O(n^2)$$

How many swaps?

$$1+2+3+...+(n-1) = O(n^2)$$

- **Example:** Suppose we have 32 unsorted data.
- a). How many comparisons are made by sequential search in the worst-case? → Number of comparisons =32.
- b). How many comparisons are made by binary search in the worst-case? (Assuming simple sorting).
  - → Number of comparisons = Number of comparisons for sorting + Number of comparisons for binary search

= 
$$(n*(n-1))/2 + \log n$$
  
=  $32/2(32-1) + \log 32$   
=  $16*31 + 5$ 

- c). How many comparisons are made by binary search in the worst-case if data is found to be already sorted?
  - $\rightarrow$  Number of comparisons =  $\log_2 32 = 5$ .

#### II. Bubble sort

### **Algorithm:**

- I. Compare each element (except the last one) with its neighbor to the right.
  - If they are out of order, swap them
  - This puts the largest element at the very end
  - The last element is now in the correct and final place
- II. Compare each element (except the last two) with its neighbor to the right.
  - If they are out of order, swap them
  - This puts the second largest element before last
  - The last two elements are now in their correct and final places

- III. Compare each element (except the last three) with its neighbor to the right.
- IV. Continue as above until you have no unsorted elements on the left.
  - Is the oldest, simplest, and slowest sort in use.
  - It works by comparing each item in a list with an item next to it, and swap them if required.
  - This causes the larger values to "bubble" to the end of the list while smaller values to "sink" towards the beginning of the list.
  - In general case, bubble sort has O(n²) level of complexity.

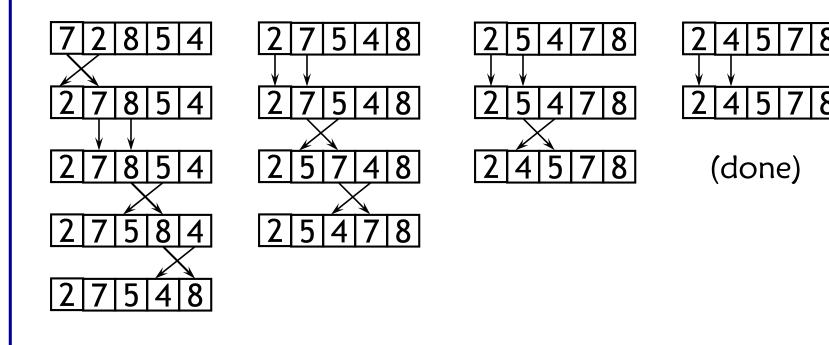
Advantage: Simplicity and ease of implementation.

Disadvantage: Horribly inefficient.

# **Example of Bubble sort**

		4	2	3	1
i=3	j=1	2	<b>-</b> 4 -	3	1
	j=2	2	3	4	1
	j=3	2	3	1	4
i=2	j=1	2	<b>-</b> 3	1	4
	j=2	2	1	3	4
i=1	j=1	1 	2	3	4

### Example of Bubble sort



### **Implementation:**

```
Void BubbleSort(int list[])
        int temp;
      for (int i=n-2; i>=0; i--) {
      for(int j=0; j<=i; j++)
         if (\operatorname{list}[j] > \operatorname{list}[j+1])
                temp=list[j];
                list[j])=list[j+1];
                list[j]=temp;
```

# **Complexity Analysis:**

- Analysis involves number of comparisons and swaps.
- How many comparisons?

$$1+2+3+...+(n-1)=O(n^2)$$

How many swaps?

$$1+2+3+...+(n-1)=O(n^2)$$

#### **III.** Selection Sort

### <u>Algorithm</u>

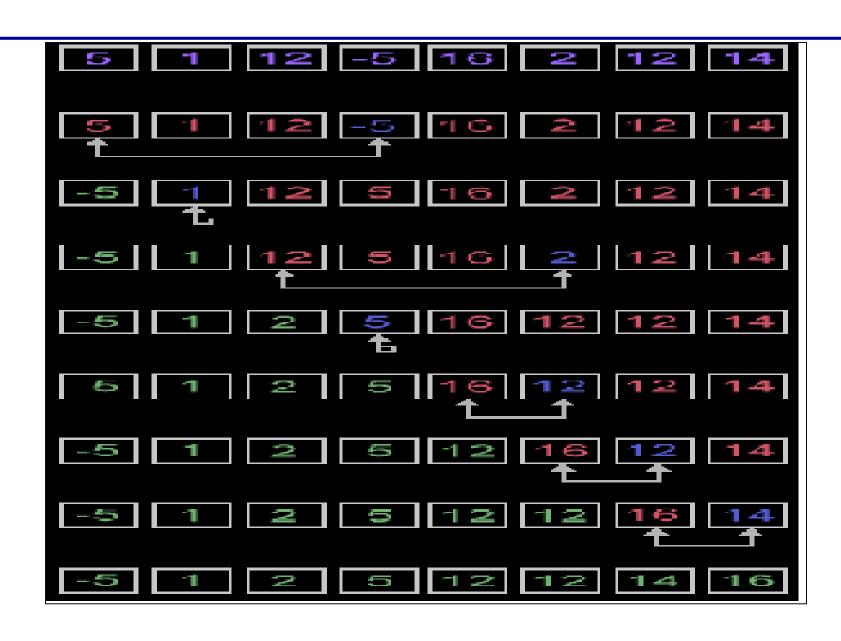
- The selection sort algorithm is in many ways similar to simple sort algorithms.
- The idea of algorithm is quite simple. Array is imaginary divided into two parts <u>sorted one</u> and <u>unsorted one</u>.
- At the beginning, <u>sorted part</u> is empty, while <u>unsorted one</u> contains whole array.
- At every step, algorithm finds minimal element in the unsorted part and adds it to the end of the sorted one.
- When <u>unsorted part</u> becomes empty, algorithm *stops*.

- Works by selecting the smallest unsorted item remaining in the list, and then swapping it with the item in the next position to be filled.
- Similar to the more efficient insertion sort.
- It yields a 60% performance improvement over the bubble sort.

Advantage: Simple and easy to implement.

Disadvantage: Inefficient for larger lists.

Exa	mple:	1			
		7	9	11	3
i=0	<b>j</b> =1	7	9	11	3
	<b>j</b> =2	7	9	,11	_3 7
	j=3	3	9	11	7
i=1	<b>j</b> =2	3	2	11	_7
	j=3	3	7	11	9
i=2	j=3	3	7	9	11



# **Implementation:**

```
void selectionSort(int list[]) {
   int minIndex, temp;
   for (int i = 0; i \le n - 2; i++) {
             minIndex = i;
       for (j = i + 1; j \le n-1; j++)
         if (list[j] < list[minIndex])</pre>
              minIndex = j;
        if (minIndex != i) {
            temp = list[i];
            list[i] = list[minIndex];
            list[minIndex] = temp;
```

# Complexity Analysis

- Selection sort stops, when unsorted part becomes empty.
- As we know, on every step number of unsorted elements decreased by one.
- Therefore, selection sort makes <u>n-1</u> steps (*n* is number of elements in array) of outer loop, before stop.
- Every step of outer loop requires finding minimum in unsorted part. Summing up, (n 1) + (n 2) + ... + 1, results in  $O(n^2)$  number of comparisons.
- Number of swaps may vary from zero (in case of sorted array) to <u>n-1</u> (in case array was sorted in reversed order), which results in <u>O(n)</u> number of swaps.
- Overall algorithm complexity is  $O(n^2)$ .
- Fact, that selection sort requires <u>n-1</u> number of swaps at most, makes it very efficient in situations, when write operation is significantly more expensive, than read operation.

#### IV. Insertion Sort

### **Algorithm:**

- Insertion sort algorithm somewhat resembles Selection Sort and Bubble sort.
- Array is imaginary divided into two parts sorted one and unsorted one.
- At the beginning, sorted part contains first element of the array and unsorted one contains the rest.
- At every step, algorithm takes first element in the unsorted part and inserts it to the right place of the sorted one.
- When unsorted part becomes empty, algorithm stops.

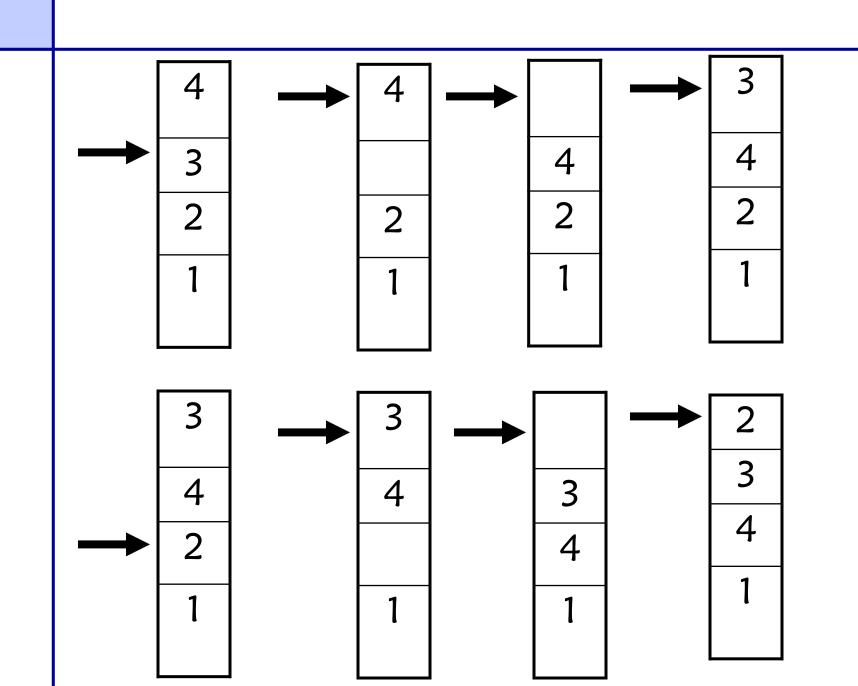
### **Using binary search**

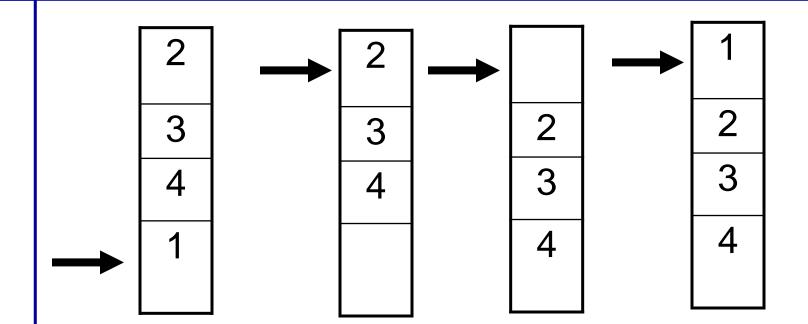
- It is reasonable to use <u>binary search</u> <u>algorithm</u> to find a proper place for insertion.
- This variant of the insertion sort is called <u>binary insertion sort</u>.
- After position for insertion is found, algorithm shifts the part of the array and inserts the element.

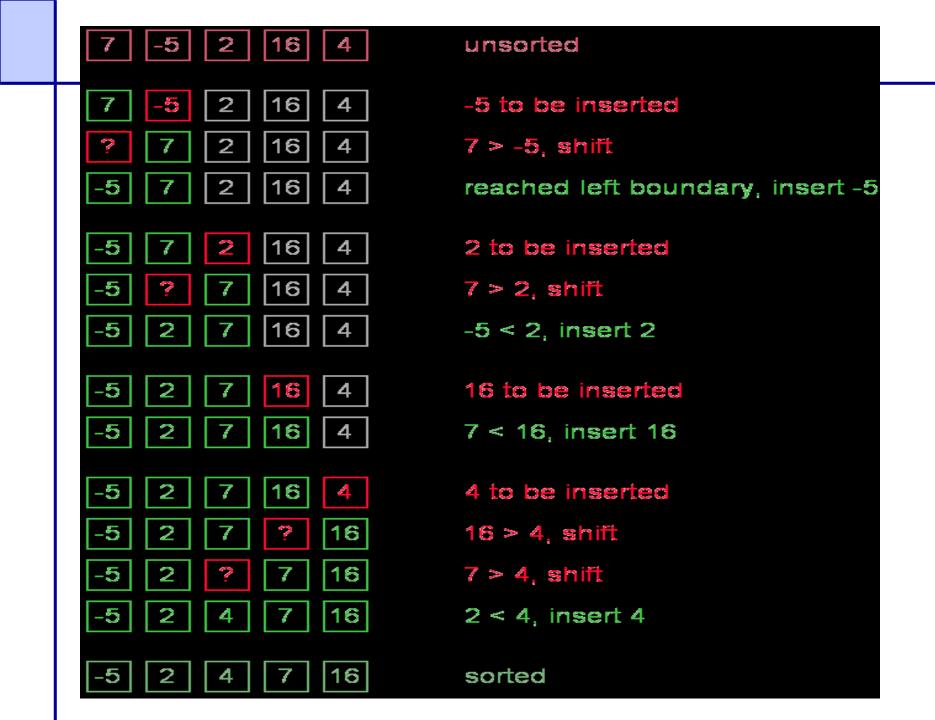
- Insertion sort works by inserting item into its proper place in the list.
- Insertion sort is simply like playing cards: To sort the cards in your hand, you extract a card, shift the remaining cards and then insert the extracted card in the correct place.
- This process is repeated until all the cards are in the correct sequence.
- Is over twice as fast as the bubble sort and is just as easy to implement as the selection sort.

Advantage: Relatively simple and easy to implement.

Disadvantage: Inefficient for large lists.







### C++ implementation

```
void InsertionSort(int list[])
    for (int i = 1; i \le n-1; i++) {
      for(int j = i; j >= 1; j--) {
         if(list[j-1] > list[j])
            int temp = list[j];
            list[j] = list[j-1];
            list[j-1] = temp;
          else
            break;
```

# **Complexity Analysis**

- The complexity of insertion sorting is <u>O(n)</u> at best case of an already sorted array and <u>O(n²)</u> at worst case, regardless of the method of insertion.
- Number of comparisons may vary depending on the insertion algorithm.
  - O(n<sup>2</sup>) for shifting or swapping methods.
  - O(nlogn) for binary insertion sort.

