

ASSIGNMENT 4

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Download all python codes from

<https://github.com/Y.Nagarani/Assignment4/tree/main/Assignment4>

and latex-tikz codes from

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∴ Vertex **c** is given by

$$\begin{pmatrix} 0 & -1 \\ 1 & 0 \\ 0 & 0 \end{pmatrix} \mathbf{c} = \begin{pmatrix} 3 \\ 0 \\ 0 \end{pmatrix} \quad (2.0.7)$$

$$\Rightarrow \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix} \mathbf{c} = \begin{pmatrix} 3 \\ 0 \end{pmatrix} \quad (2.0.8)$$

$$\Rightarrow \mathbf{c} = \begin{pmatrix} 0 \\ -3 \end{pmatrix} \quad (2.0.9)$$

Now,

1 QUESTION No 2.19(QUAD FORMS)

Find the zero's of the polynomial $x^2 - 3$ and verify the relationship between the zero's and the coefficients

2 SOLUTION

Given

$$y = x^2 - 3 \quad (2.0.1)$$

$$x^2 - y - 3 = 0 \quad (2.0.2)$$

compare with standard form of equation

$$ax^2 + bxy + cy^2 + 2dx + 2ey + f = 0 \quad (2.0.3)$$

$$a = 1, b = 0, c = 0, d = 0, e = \frac{-1}{2}, f = -3$$

Here,

$$\mathbf{V} = \begin{pmatrix} 1 & 0 \\ 0 & 0 \end{pmatrix}, \mathbf{u} = \begin{pmatrix} 0 \\ \frac{-1}{2} \end{pmatrix}, f = -3 \quad (2.0.4)$$

Using eigenvalue decomposition,

$$\mathbf{D} = \begin{pmatrix} 0 & 0 \\ 0 & 1 \end{pmatrix}, \mathbf{P} = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} \quad (2.0.5)$$

Now,

$$\begin{pmatrix} \mathbf{u}^T + \eta \mathbf{p}_1^T \\ \mathbf{V} \end{pmatrix} \mathbf{c} = \begin{pmatrix} -f \\ \eta \mathbf{p}_1 - \mathbf{u} \end{pmatrix} \quad (2.0.6)$$

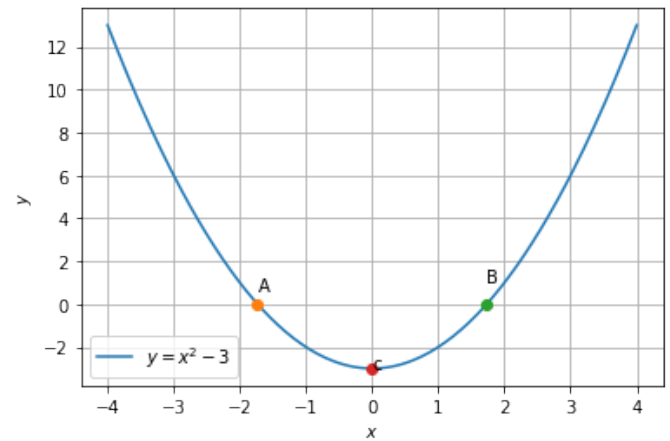


Fig. 2.1: $y = x^2 - 3$

$$\mathbf{p}_1^T \mathbf{c} = \begin{pmatrix} 0 & 1 \end{pmatrix} \begin{pmatrix} 0 \\ -3 \end{pmatrix} \quad (2.0.10)$$

$$= -3 \quad (2.0.11)$$

$$\mathbf{p}_2^T \mathbf{V} \mathbf{p}_2 = \begin{pmatrix} 1 & 0 \end{pmatrix} \begin{pmatrix} 1 & 0 \\ 0 & 0 \end{pmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix} \quad (2.0.12)$$

$$= 1 \quad (2.0.13)$$

∴

$$(\mathbf{p}_1^T \mathbf{c})(\mathbf{p}_2^T \mathbf{V} \mathbf{p}_2) = -3 < 0 \quad (2.0.14)$$

Hence, the given equation has real roots.