ASSIGNMENT 4

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Download all python codes from

https://github.com/Y.Nagarano/Assignment4/tree/main/codes

and latex-tikz codes from

https://github.com/Y.Nagaranj/Assignment4/tree/main/Assignment4

1 Question No 2.19(Quad forms)

Find the zeroes of the quadratic polynomial x^2-3 and verify the relationship between the zeros and coefficients.

2 SOLUTION

1) The vector form of equation is

$$y = x^2 - 3 \tag{2.0.1}$$

$$\mathbf{x}^T \begin{pmatrix} 1 & 0 \\ 0 & 0 \end{pmatrix} \mathbf{x} + \begin{pmatrix} 0 & 0 \end{pmatrix} \mathbf{x} - 3 = 0 \qquad (2.0.2)$$

Thus

$$y = 0 \implies x^2 - 3 = 0$$
 (2.0.3)

$$x = \sqrt{3} \tag{2.0.4}$$

The roots are $\alpha = \sqrt{3}$ and $\beta = -\sqrt{3}$. Compare given quadratic equation $x^2 - 3 = 0$ with $ux^2 + vx + f = 0$, we get u=1, v=0, f=-3.

Sum of the roots

$$\alpha + \beta = \frac{-v}{u} = 0 \tag{2.0.5}$$

product of the roots

$$\alpha\beta = \frac{f}{u} = -3\tag{2.0.6}$$

where u,v,f are parameters.

For $\mathbf{x} = \begin{pmatrix} \sqrt{3} \\ 0 \end{pmatrix}$ substitute in (2.0.2)

$$\left(\sqrt{3} \quad 0\right) \begin{pmatrix} 1 & 0 \\ 0 & 0 \end{pmatrix} \begin{pmatrix} \sqrt{3} \\ 0 \end{pmatrix} - 3 = 0$$
 (2.0.7)

For
$$\mathbf{x} = \begin{pmatrix} -\sqrt{3} \\ 0 \end{pmatrix}$$
 substitute in (2.0.2)

$$\begin{pmatrix} -\sqrt{3} & 0 \end{pmatrix} \begin{pmatrix} 1 & 0 \\ 0 & 0 \end{pmatrix} \begin{pmatrix} -\sqrt{3} \\ 0 \end{pmatrix} - 3 = 0$$
 (2.0.8)

Hence, $+\sqrt{3}$ and $-\sqrt{3}$ are zeros.

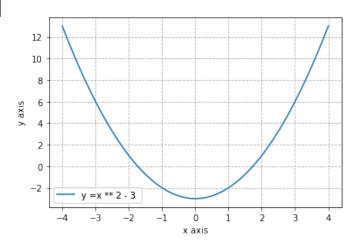


Fig. 2.1: roots of $x^2 - 3$.