Marks

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- (b) A 240 metre tall tower stands on a large flat plain. From a point on the plain East of the tower James measures the angle of elevation of the top of the tower as 30°. Bruce, who is South of the tower, measures the angle of elevation of the top of the tower as 45°.
  - (i) Draw a neat sketch showing the above information.
  - (ii) Show that James is  $240\sqrt{3}$  metres from the base of the tower and also find the distance of Bruce from the base of the tower.
  - (iii) Find the distance between James and Bruce.

Question 1 (12 Marks)

(c) Use the substitution  $u^2 = x \ (u > 0)$  to find the exact value of  $\int_{\frac{1}{4}}^{\frac{1}{4}} \frac{dx}{\sqrt{x - x^2}}$ .

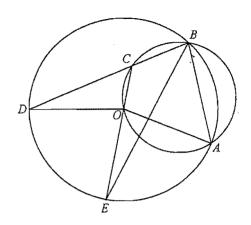
Question 2 START A NEW PAGE (12 Marks) Marks

- (a) (i) Prove that the tangent to the parabola  $x^2 = 4ay$  at the point  $P(2ap, ap^2)$  is given by  $px y ap^2 = 0$ .
  - (ii) The tangent at P meets the directrix at the point T. Find the co-ordinates of T.
  - (iii) If F is the focus of the parabola prove that PF is perpendicular to FT.
- (b) (i) Sketch the curve  $y = 1 + \sin x$  for  $0 \le x \le 2\pi$ .
  - (ii) Find the exact volume of the solid formed when the area bounded by the curve  $y = 1 + \sin x$  and the x-axis for  $0 \le x \le 2\pi$  is rotated one revolution about the x-axis.

Question 3 START A NEW PAGE (12 Marks)

Marks

a) A, B and D are three points on a circle with centre O. A smaller circle is drawn through the points O, A and B. The chord BD of the larger circle cuts the smaller circle at C and chord CO extended cuts the larger circle at E.



- (i) Copy the diagram onto your examination paper and explain why  $\angle CBA = \angle EOA$ .
- (ii) Prove that BE bisects  $\angle DBA$ .
- b) (i) The curve  $y = x^4$  is rotated one revolution about the y-axis to form a container for storing water. Calculate the volume of water that can be stored if the container is filled to a depth of h cm.
  - (ii) Water is poured into the above container at a rate of 60 ml/minute. Find the rate at which the depth is increasing when the depth is 16 cm.
- The equation of motion of a particle moving along a horizontal straight line is given by the formula  $x = 3\cos\left(\frac{1}{4}t\right) + \sin\left(\frac{1}{4}t\right)$ , where x metres is the displacement of the particle at time t seconds.
  - (i) Explain whether the particle is initially moving to the right or left, and whether it is speeding up or slowing down.
  - (ii) Find the time for the particle to first reach the origin. Give your answer correct to one decimal place.

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Question 4	START	'A NEW	PAGE	(12 Marks)

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Marks

- (a) (i) Prove that  $\sin^{-1} x + \cos^{-1} x = \frac{\pi}{2}$  for  $-1 \le x \le 1$ .
  - (ii) Find the acute angle between the curves  $y = \sin^{-1} x$  and  $y = \cos^{-1} x$  at the point where they intersect. Give your answer correct to the nearest degree.
- (b) Find the smallest positive solution, in radians, of the equation  $\cos 3\theta = \sin 2\theta$ .
- (c) (i) Write down the coefficient of  $x^k$  when the binomial product  $(5+3x)^{20}$  is expanded in ascending powers of x.
  - (ii) Which two adjacent terms in the above expansion have their coefficients in the ratio 2:3?

## **Question 5** START A NEW PAGE (12 Marks)

- (a) (i) If  $\theta = \tan^{-1} A + \tan^{-1} B$  show that  $\tan \theta = \frac{A + B}{1 AB}$ 
  - (ii) Hence solve the equation  $\tan^{-1} 3x + \tan^{-1} 2x = \frac{\pi}{4}$ .
- (b) Use Mathematical Induction to prove that for all positive integers  $n \ge 1$ ,

$$\frac{1}{1} + \frac{1}{1+2} + \frac{1}{1+2+3} + \dots + \frac{1}{1+2+3+\dots+n} = \frac{2n}{n+1}$$

- (c) At training, a coach decides to organise a practise game between two teams using 5 players for each team. The coach has 12 players to choose from, including the Ruse twins James and Bruce.
  - (i) How many different practice games could be organised if there are no restrictions on who plays on each team?
  - (ii) Find the probability that in a game chosen at random, the Ruse twins would not be playing against each other.

## Question 6 START A NEW PAGE (12 Marks)

- a)  $A_n = 1^2 + 5^2 + 9^2 + ... + (4n-3)^2$  and  $B_n = 3^2 + 7^2 + 11^2 + ...$ 
  - Write down the  $n^{th}$  term of the sequence  $B_n$ .
  - (ii) If  $S_{2n} = A_n B_n$ , show that  $S_{2n} = -8n^2$ .
  - ii) Hence evaluate  $101^2 103^2 + 105^2 107^2 + ... + 2009^2 2011^2$
- (b) The number (N) of ants in an ant colony at time t weeks is given by the formula  $N = 150\ 000 Be^{-kt}$ , where B and k are positive constants. The initial size of the colony when discovered was 2 000 and 5 weeks later the size had increased to 50 000.
  - Show that the instantaneous rate of increase in the size of the colony can be given by the equation  $\frac{dN}{dt} = k(150\ 000 N)$ .
  - (ii) Find the exact values of B and k.
  - (iii) Find the maximum size of the colony.
  - (iv) Find the size of the colony 20 weeks after its discovery. Give your answer correct to the nearest 1000 ants.

## Question 7 START A NEW PAGE (12 Marks)

- Write down an expression for the expansion of cos(A+B) and hence prove that  $cos^22\theta = 2cos^2\theta 1$ .
  - (ii) ABC is a triangle with sides a, b, c and a perimeter of length p. Prove that  $\cos\left(\frac{A}{2}\right) = \frac{1}{2}\sqrt{\frac{p(p-2a)}{bc}}$ .
- (b) An object is projected from the origin O with initial speed Um/s at an angle of elevation of  $\alpha$ . At the same instant another object is projected from a point A which is h units above the origin O. The second object is projected with initial speed Vm/s at an angle of elevation of  $\beta$ , where  $\beta < \alpha$ . Both objects move freely under gravity in the same plane.
  - (i) Given that the equations of motion for the object projected from the origin are:  $x = Ut \cos \alpha \quad \text{and} \quad y = Ut \sin \alpha \frac{1}{2}gt^2,$  write down the equations of motion for the object projected from the point A.
  - (ii) If the objects collide T seconds after they are projected, prove that  $T = \frac{h\cos\beta}{U\sin(\alpha-\beta)}$ .

## THIS IS THE END OF THE EXAMINATION PAPER

Marks

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Marks

3U TRIAL	MATHEMATICS Extension 1 : Questi		-2010
	Suggested Solutions	Marks	Marker's Comments
Solution:	$dx = \int_0^{\pi} \frac{\sin\left(\frac{x}{4}\right)}{\cos\left(\frac{x}{4}\right)} dx$		
	$=-4\int_0^{\pi} \left\{ \frac{-\frac{1}{4}\sin\left(\frac{x}{4}\right)}{\cos\left(\frac{x}{4}\right)} \right\} dx$		50% siccess vate
	$= -4 \left[ \ln \left( \cos \left( \frac{x}{4} \right) \right) \right]_{0}^{\pi}$ $= -4 \left\{ \ln \left( \cos \left( \frac{\pi}{4} \right) \right) - \ln (\cos (0)) \right\}$ $= -4 \left\{ \ln \left( \frac{1}{\sqrt{2}} \right) - \ln (1) \right\}$	-	
	$= -4 \ln \left( \frac{1}{\sqrt{2}} \right)$ $= -4 \ln \left( 2^{\frac{1}{2}} \right)$ $= 2 \ln 2$		
(Bruce) South	Tower (240 m)  (East) 30°  (James) 54.57		

		***************************************
2U TRIAL MATHEMATICS Extension 1: Question		2010
Suggested Solutions	Marks*	Marker's Comments
Solution: $\frac{240}{OJ} = \tan 30^{\circ}$	ىو	·
$OJ = \frac{240}{\tan 30^{\circ}}$ $= \frac{240}{\left(\frac{1}{\sqrt{3}}\right)}$		
$= 240\sqrt{3}$ Distance from base to James = $240\sqrt{3}$ metres	1	
Distance from base to Bruce = 240 metres (triangle is isosceles)	1	
(iii) Find the distance between James and Bruce. <b>Solution:</b> $BJ^{2} = (240\sqrt{3})^{2} + 240^{2}  (Pythagoras' Theorem)$ $= 240^{2}(3+1) \frac{1}{16}$		to Pythagirois
$= 240^{\circ}(3+1) \  \%  $ $= 240^{\circ}(4)$ $BJ = 240 \times 2$ $= 480$	2	12 Typhogerous  1 If nobettempt 2 to clarify Brue 2 James
Distance between James and Brûce = 400 m		
$\int_{\frac{1}{4}}^{\frac{1}{4}} \frac{dx}{\sqrt{x-x^2}} = \int_{\frac{1}{4}}^{\frac{1}{4}} \frac{2udu}{\sqrt{u^2-u^4}} \qquad u^2 = x \ (u > 0)$ $2udu = dx$	1	hands
$=\int_{\frac{\pi}{4}}^{\frac{\pi}{4}} \frac{2udu}{u\sqrt{1-u^2}} \qquad x = \frac{1}{4} \Rightarrow u^2 = \frac{1}{4}$ $=\int_{\frac{\pi}{4}}^{\frac{\pi}{4}} \frac{2du}{u}$	(	
$= \int_{\frac{1}{2}}^{\frac{1}{2}} \frac{2du}{\sqrt{1-u^2}} \qquad u = \frac{1}{2}  (u > 0)$ $= 2\left[\sin^{-1}u\right]_{\frac{1}{2}}^{\frac{1}{2}} \qquad x = \frac{1}{2} \Rightarrow u^2 = \frac{1}{2}$	1	
$=2\left(\sin^{-1}\left(\frac{1}{\sqrt{2}}\right)-\sin^{-1}\left(\frac{1}{2}\right)\right) \qquad u=\frac{1}{\sqrt{2}}  (u>0)$	(	•
$=2\left(\frac{\pi}{4}-\frac{\pi}{6}\right)$	,	
$\int_{\frac{1}{4}}^{\frac{1}{4}} \frac{dx}{\sqrt{x-x^2}} = \frac{\pi}{6}$	(	

TRIAL 2010 MATHEMATICS Extension 1: Question	on 2	
Suggested Solutions	Marks	Marker's Comments
(a) (b) 4= #2		ALL ROLL & COMMENTS
dy = 20 dsc 20		
when x = sup	١.	
dy = P	1	
Eqn. of tangent is: y-ap2=p(x-2ap2		
px-y-op=0	1	
(11) Directrix has an eqn. 4=-a(1)	<del>                                     </del>	
Eqn. of tangent from (i) is:poc-y-ap=0	(2)	No penalty
Sub (1) in (2)		for not mentioning
px+a-ap2=0		no hout marks
$p = ap^2 - a$ $x = a(p^2 - 1), p \neq 0$		awarded
County on P		·
··· Co-ords. of T are (a(p2),-a)	1	
(1) F(0,a), P(2ap,ap2), T(a(p21),-a)		
$m(EP) = \frac{3aP}{a(P_2 I)}$		
= a(631)		
zap		
2p		
m(ET) = a-a 0-a(p=1)		
-a(p2-1)		
$= \frac{b_2 - 1}{-5b}$	,	
For perpendicular lines m(FP) x m(FT) =-1		
w(Eb) x w (EL) = b=1 x -30		
~-/	1	
PF_L FT		
		<u> </u>

(b) V=T \(\frac{\pi}{2\pi}\) (1+5mx)^2dx	2.	t mark deducted for any arrow heads I mark shape I mark for scale needed to show To style + 2TT on x exis.
$= \pi \int_{0}^{2\pi} (1+2\sin x + \sin^{2} x) dx$ $= \pi \int_{0}^{2\pi} (1+2\sin x + \frac{1-\cos 2x}{2}) dx$ $= \frac{\pi}{2} \int_{0}^{2\pi} (3+4\sin x - \cos 2x) dx$ $= \frac{\pi}{2} \left[ 3x - 4\cos x - \frac{1}{2}\sin 2x \right]_{0}^{2\pi}$ $= \frac{\pi}{2} \left[ 6\pi + 3\cos 2\pi - \frac{1}{2}\sin 4\pi \right] - (0+3\cos 0 - \frac{1}{2}\sin 0)$ $= \frac{\pi}{2} \left[ (6\pi + 3) - (0+3) \right]$	1	Marks were awarded if the area was taken between and III and III.  DR between III and III.
V = 3Th <sup>2</sup> Vol. = 3Th <sup>2</sup> If the area rotated was Irmited to between and SII  V = The (1+5 inx) <sup>2</sup> doc  V = II (9Th+8) u <sup>3</sup> J.Maths/Suggested Mk solns template_V2_no Ls.doc		

MATHEMATICS Extension 1 : Question......

Suggested Solutions Marks

Marker's Comments

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MATHEMATICS Extension 1 : Quest		
Suggested Solutions	Marks	Marker's Comments
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	3/2	If they use the auxillary and mathod then Tork & done corr
when t=0 = 4 ===============================	112	velocity - 1/2 mK acceleration - 1/2 mK
since voc particle is nown to the right since vocat aso, particle is slowing down	1/2	[auxillary argle Jiocos (\$
) particle at origin when $x=2$ $0=363\left(\frac{\pi}{4}\right)+3i\sqrt{\frac{\pi}{4}}$	. V2	
365(A) = -SiN(A)	^	* using Abardary angle
ta(4) = -3 ta(-3) there Kisan	1/2	Ink-correct expressions link for solving correctly and agiting
E = 4KT + 4+cn(-3)	1 3 2	£=7.65
when k=0, t= 47 + + +0 (-3)		* If the auxillary angle nethod was
time taken is 7 loseands (14)	1 /2	2 mks fac solving coop
	~ ~	* If they got to-to
		* If they got t= f
	~	
	~	
	~	
	». «	

MATHEMATICS Extension 1 : Questi Suggested Solutions	on2	
Suggested Solutions	Marks	Marker's Comments
(e)jupy diagram neathy  CBA = EOA (exterior angle of cyclic  qual occan regula the inter  opposite angle)  (ii) let EBA = >c	У <sub>2</sub> « У <sub>2</sub>	lose the mark it to drawn badly.  no reason = no marks
<u> </u>	1/2 1/2	
= 27 - X = X = X = X = SA (5+1 X)	\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\	
-: BE 612275 < DBA	Yz Yz Ya	If they wrote the initial statement wrong or around the x-axis \$1 or
Valure is 75 hth cm  The state of the state	1/2 1/2 1/2 1/2	15TT -> 1/2 mks 15TT and a sentence with units -> 2mks

TRIAL 2010 Ext MATHEMATICS OF 4		
Suggested Solutions  [KIGL 2010 Ext 1 MATHEMATICS: Question4.	Marks	Marker's Comments
$\frac{d}{dx} \sin(x) = \frac{1}{\sqrt{1-x^2}} - 1 < x < 1$ $\frac{d}{dx} \cos(x) = \frac{1}{\sqrt{1-x^2}} - 1 < x < 1$ $\frac{d}{dx} \left[ \sin'(x) + \cos'(x) \right] = 0$ $\sin'(x) + \cos'(x) = \text{constant}$ when $x = 0$ $\sin'(0) + \cos'(0) = 0 + \frac{\pi}{2} = \frac{\pi}{2}$ $\sin(x) + \cos'(x) = \frac{\pi}{2}, -1 = x \le 1$ $\sin'(x) + \cos'(x) = \frac{\pi}{2}, -1 = x \le 1$	1	many students did Bx  VI-SC  only get 1 m
$Sin'x = con'x$ $Sin'x + con'x = \overline{z}$ $2 Sin'x = \overline{z}$ $Sin'x = \overline{z}$	1	many students  did not prove  and state only  x=50 get 1m
$\frac{d}{dx} \sin\left(\frac{1}{\sqrt{x}}\right) = \sqrt{x}$ $\frac{d}{dx} \cos\left(\frac{1}{\sqrt{x}}\right) = \sqrt{x}$ $\tan \theta = \left \frac{m_1 - m_2}{1 + m_1 \times m_2}\right  = 2\sqrt{x}$	1 12	
$\theta = 71  (\text{Neapost dograe})$ $cos (20+6) = 2 \sin \theta \cos \theta$ $im \cos \theta (40 \sin^2 \theta + 2 \sin \theta - 1) = 0$ $cos \theta = 0  \text{as } \sin \theta = -1 \pm \sqrt{5}$ $\theta = 1  \text{as } 0.314 - \dots  G = 0.314$ Heroury\staffhomes\WOH\Admin_M Fao\Assessment info\Suggested Mk solns template_V2.doo	,	forgot to remote the forgot to the standard f

MATHEMATICS: Question	4	
Suggested Solutions	Marks	Marker's Comments
$(a)$ $(a)$ $3\theta = 5$ $(a)$ $(a)$		
3m co 30 = co (= -20)		
$30 = 2n \pi t \left( \frac{\pi}{2} - 16 \right)  n \in \mathbb{Z}$	/	forget nez zm
0 = = = = = = = = = = = = = = = = = = =	/	
$\theta = \frac{\pi}{10}$ is the smallest possible sola.	/	14th
~ Sin(王-30)= Sin(20)		
20 = nit + (7) " [ = -36]	1	
nevan 0 = n II nodd 6 = II - n II	/	
G=I smallest possible solo	1	
c(i) weff of x = (20) 3 15 20-k	/	. , ,
$ (77) \frac{2}{3} = \begin{pmatrix} 20 \\ 16 \end{pmatrix} 3^{k} $ $ (77) \begin{pmatrix} 20 \\ (k+1) \end{pmatrix} 3 $ $ 5$	/	many students did 3 and
$\frac{2}{3} = \frac{5}{3} \frac{(k+1)}{(20-k)}$	1	can't solve for k to be itsper
	士	max/m.
terms involving x and x or sixth and xeventh term	1 2	many students lost & if they
or sixth and stocker		wite To Ty when
or $\binom{20}{k-1} \frac{3^{k-1}}{5} \cdot \frac{5^{1-k}}{5} = \frac{2}{3}$		they define $\frac{T_6}{T_7} = \frac{2}{3}$
$\frac{\left(\frac{K-1}{3}\right)}{\left(\frac{2^{\circ}}{k}\right)}\frac{3^{H}\cdot 5^{LD-H}}{3^{H}\cdot 5^{LD-H}} = \frac{2}{3}$	,	$k = \frac{189}{19} \approx K = \frac{17}{19}$
$\frac{K}{2J-K} \cdot \frac{J}{3} = \frac{2}{3}$	/	as a result of =
k- 6		get In.
sixth and sever K term (or term in volv. x r and x b)	1	

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		5	•
	MATHEMATICS Extension 1 : Questi Suggested Solutions	Marks,	Marker's Comments
(a) (i)	If $\theta = \tan^{-1} A + \tan^{-1} B$ show that $\tan \theta = \frac{A + B}{1 - AB}$ . Solution: $\theta = \tan^{-1} A + \tan^{-1} B$	0"	•
· · · · · · · · · · · ·	$\theta = \alpha + \beta$ where $\alpha = \tan^{-1} A$ and $\beta = \tan^{-1} B$ $\tan(\alpha + \beta) = \frac{\tan \alpha + \tan \beta}{1 - \tan \alpha \tan \beta}$		Mustshow
#	$= \frac{A+B}{1-AB}$		
(ii)	Hence solve the equation $\tan^{-1} 3x + \tan^{-1} 2x = \frac{\pi}{4}$ .	3	,
	Solution: $\tan\left(\frac{\pi}{4}\right) = \frac{3x + 2x}{1 - (3x)(2x)}$		P substitution
	$1 = \frac{5x}{1 - 6x^2}$		
	$1-6x^{2} = 5x$ $6x^{2} + 5x - 1 = 0$ $(6x-1)(x+1) = 0$		quadratic equation + factorisation
	$x = \frac{1}{6} \text{ or } -1$		2 so Introns
	but $\tan^{-1} 3x$ and $\tan^{-1} 2x$ are both acute (since their sum	$<\frac{\pi}{2}$ ), the	
(b)	$\therefore x = \frac{1}{6}$		1 rejecting x=-1
Let P	(n) be the proposition that:	4	
	$\frac{1}{1} + \frac{1}{1+2} + \frac{1}{1+2+3} + \dots + \frac{1}{1+2+3+\dots+n} = \frac{2n}{n+1}$		1) Test for n=1
Test when	for all positive integers $n$ $n = 1$ , $LHS = \frac{1}{1}$ , $RHS = \frac{2(1)}{1+1} = 1$	21,	
∴ LH	IS = RHS		
: P(	1) 15		
	true		

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MATHEMATICS Extension 1 : Question	<u>.</u> 5	
Suggested Solutions	Marks p	Marker's Comments
Assume $P(k)$ is true for $n = k$ , $k \in \mathbb{Z}^+$ i.e. $\frac{1}{1} + \frac{1}{1+2} + \frac{1}{1+2+3} + \dots + \frac{1}{1+2+3+\dots+k} = \frac{2k}{k+1}$	عو	2 assumption including REZ+
To prove true for $n = k + 1$ i.e. $\frac{1}{1} + \frac{1}{1+2} + \frac{1}{1+2+3} + \dots + \frac{1}{1+2+3+\dots+k} + \frac{1}{1+2+3+\dots+k+1}$	-	$ \begin{array}{c} \text{(1)} & \text{required to} \\ \text{prove} & \text{prove} \\ \frac{2(k+1)}{(k+1)+1} & \text{statement} \\ \frac{2k+2}{k+2} & \text{table} \end{array} $
Now LHS = $\frac{1}{1} + \frac{1}{1+2} + \frac{1}{1+2+3} + + \frac{1}{1+2+3++k} + \frac{1}{1+2+3}$ = $\frac{2k}{k+1} + \frac{1}{1+2+3++k+(k+1)}$ (by assumption) = $\frac{2k}{k+1} + \frac{1}{\frac{1}{2}(k+1)(k+2)}$ = $\frac{2k}{k+1} + \frac{2}{(k+1)(k+2)}$ = $\frac{2k(k+2)+2}{(k+1)(k+2)}$ = $\frac{2(k^2+2k+1)}{(k+1)(k+2)}$ = $\frac{2(k+1)^2}{(k+1)(k+2)}$ = $\frac{2(k+1)^2}{(k+2)}$ = $\frac{2(k+1)}{(k+2)}$ = $\frac{2k+2}{k+2}$ = $\frac{2k+2}{k+2}$	1 + + k +	(k+1)  (1) substition of assumption including "by assumption" (1) showing AP sum completion

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MATHEMATICS Extension 1 : Quest	3.6	Manhanta Carrai
Suggested Solutions	Marks *	Marker's Comments
)(i) $3u = 3^{2} + 1^{2} + 1^{2}$ Now $3 = 3 + (n-1) + 2 + 4n-1$		
ntermot B. is (4n-1)		回
52, = A, -B, - E (41-2) = E (241-2) = E (241-2)	3)* -(41	() <sup>*</sup> J
= -8E (2r-1) =	7	12 For "5 2n = -16n+
	ِيُّا ِدِدِ رِيَّا حِدِ	16 8-16n
======================================		<u>[a</u>
$\sum_{n=1}^{\infty} \frac{1^{2}-3}{n^{2}} + \frac{5}{n^{2}} + \frac{1}{n^{2}} + \frac{1}{n^{2}$	~ (un-	) m pairs (1)
= -8[(+3+5++ (2x-1)]	~ (1 <del>7</del> )	
= -Bx n [ 1 + 2n-1] = -Bu	(2)	for using A.se.
1) A - 5-6	rec.	4n-3 = 101 => n = ;
	***	4n-3 = 2009 => n= 4n-1 = 2011 -
aassaanaan ka Soo Soo Soo aanaa ka k	~ 1 ~ 1 ~ 2	For n = 503 For n = 26-1 = 2
	1	FAT -8x 5032+.8x
\$ Suc = -2x204 + -2x20 + - 1 - 2x4020	***	-
= -2[204 + 212 + 220 + 2017 + 4020] 		4-18 51+(n-1)2
= -8 × 478 \ 51 + 1005 = -2019 B		
aan ka maan ka maa ka maa Ka maa ka maa ma		

MATHEMATICS Extension 1 : Questi	on•	1 1 1 0
Suggested Solutions	Marks	Marker's Comments
) (i) N = 150 000 - Be-Kt -(*)		
momontonio continuo manta anti anti anti anti anti anti anti	200	Be-kt)
LHS: IN =+ KBE RHS = KC150 000 - (15)	9 3005 -	
at - kBe-kc		For Exce
1 2H = K(150000-H)		
at q. cd.		
энтэдтэлтбалган хүрэх хэргэд (с <mark>ан «Майлага» тэргээн даган Моман хүргэж тайган үүлт тайга хүргэж төөгэх</mark> хайгааса		
W - KBE-Pt		
THE PARTY OF THE P	<u>_Q</u>	
out/as Be = 150000-N (*) transpose		
10 2H = K(150 000 −H)		
ZX		
) Data t=0 N= 2000 t=5	1=50	DOO -5
7 P	a) _ /=/	4 900 (R& OOO **
and the Assertation and the second	3 =-1	48000e-5k
9	+100	= 25   EXCH
See See A service and the serv	148	27
NO N = 150 000 - 148 000 e		·
-5k=	如等	[2
	*7	371/
2- K=-Llu(25)	1/// +	上外(話/レ
	11/	1 ln (37)
"TE I N' E		N'= KBe-Kt > 0
i) For possible wax N, dN =0	1	M. = KISE . SO
The state of the s	<b>^</b>	N" = - KBe-Kt <0
i.e K(150 000 - H) = 0		
' N = 150 000	. ]	1
4.00	OR,	use Box prayhood
TEST AND - KBERTOO	d	N 140 000 150 000 1000
onan unmanont <u>anung</u> unungan unman saman menangan menangan unungunungan menggunan dan menggunan menandan s	"  \{	
27	^ }	型 0 0
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The second secon		OR 14 150
mannanamananananananananananananananana		OK -
N = 150 800 - 148 800 2		2000
- L - 00 e-kt -> 5+	<u></u> +	2000 €
11 = /ED 880		9'
1 max ((lms)) H = 150 000 ants	v.	
roona muunkilaankasamirtakaraannaan famis muurismaanaanaanaanaanaanaan, oo araanaanaan ma	~	
anningan an a	m	1
(Y) t = 20 H = ?	z ln 25	120
- + M = K20 PM F	2 ln 25	T
N=150 800 - 148 000 C		
N = 150  sep - 148  sop 2 $N = 150  sep - 148  sop 2$	en 37	
-150 880 - 148 880 C	25	
and the state of t	m	
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= (50 000 - 30 547 · 1364 · · · · Calc dis		1,
= 119 152.86 Cale dis	pucacy	'
		1 or Equit.
." No of ants 119 000 (neasest 188	37	li or Eduin.

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fil cos (A+B) = cos A cos B - sin Asin B

COMMENTS

 $\cos 2\theta = \cos^2 \theta - \sin^2 \theta$ = 0000-(1-000) = 20000-1

 $\cos A = \frac{b^2 + c^2 - a^2}{a^2}$  (Cosine Rule)

 $\frac{1}{2} 2 \cos^2(\frac{4}{2}) - 1 = \frac{b^2 + c^2 - a^2}{2bc}$  (Using i)

· · · 2 cm (1)= b+c2-a2+1

 $\frac{1}{2}\cos(4x) = \frac{b^2+c^2-a^2+2bc}{2}$ 

 $co^{2}(2) = (b+c)^{2} - a^{2}$  $= \frac{(p-a)^2 - a^2}{4 \log a} \qquad (p=a+b+c)$ 

= (p-a+a)(p-a-a) (hiff a) 4bc sun-

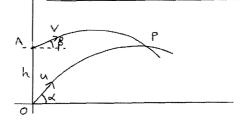
 $co^{2} = p(p-2a)$  $\cos(\frac{4}{2}) = \pm \sqrt{\frac{p(p-2a)}{p}}$ 

But A is angle of triangle. A < 180°, A/2 < 90° 1, co(12) > 0

 $\frac{1}{2} \left( \frac{p}{2} \right) = \frac{1}{2} \left| \frac{p(p-2a)}{a} \right|$ 

There were many untidy algebraic pathways used in this part.

Too many people lost the last mark for not explaining the sign.



- i) For second particle  $y = V + \cos \beta$   $y = V + \sin \beta - g + h$
- ii) at time t=T, the x and y values for each particle coincide.

i.e.  $VT\cos\beta = UT\cos\alpha \left(x \text{ value}\right)$   $V = U\cos\alpha \left(x\right)$ 

VTsin  $\beta - gT^2 + h = UTsind - gT^2 (y value)$ 

h = hT sind - VTsinB

Sub from \* h = UTsind - UTcood sin B

-, h = UT sud cos B-UT cooding .: h=uT(sindcop-coodsinp)

- '. h = UT sm (x-B)

 $T = \frac{h \cos \beta}{u \sin (\alpha - \beta)} (\alpha + \beta)$ 

Ouestion sand write down Many people wasted time by deriving these equation

Rather untidily, many people carried 't through the calculation when T is the correct value.

a few people got lost in equations of paths:

Students must take care to distinguish U & V.