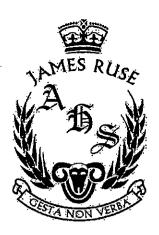
Class:	



TRIAL HIGHER SCHOOL CERTIFICATE EXAMINATION 2011

MATHEMATICS EXTENSION 2

Time Allowed – 3 Hours (Plus 5 minutes Reading Time)

- All questions may be attempted
- All questions are of equal value
- Department of Education approved calculators and templates are permitted
- · In every question, show all necessary working
- Marks may not be awarded for careless or badly arranged work
- · No grid paper is to be used unless provided with the examination paper

The answers to all questions are to be returned in separate stapled bundles clearly labeled Question 1, Question 2, etc. Each question must show your Candidate Number.

Question 1 (15 Marks)

Marks

Find: (a)

(i)
$$\int \frac{e^x}{\sqrt{e^{2x}-1}} dx$$

2

(ii)
$$\int \frac{1}{x^2 - 5x + 6} dx$$

2

(iii)
$$\int \frac{d\theta}{2 + \cos \theta}$$

3

Evaluate:
$$\int_{-1}^{1} \frac{x}{x^2 + 2x + 5} dx$$

4

(c) If
$$I = \int_0^{\frac{\pi}{2}} \frac{\cos x}{\cos x + 2\sin x} dx$$
 and $J = \int_0^{\frac{\pi}{2}} \frac{\sin x}{\cos x + 2\sin x} dx$,

(i) Show that
$$2I - J = \ln 2$$
.

1

(ii) Evaluate
$$I+2J$$
.

1

2

Question 2 (15 Marks) START A NEW PAGE

Plot neatly on an Argand diagram the points A, B and C corresponding (a) to the complex numbers w, w^2 and $w\overline{w}$ respectively where $w = \sqrt{3} + i$.

3

Let z = x + iy be a complex number satisfying the inequality (b)

4

$$z\overline{z} + (1-2i)z + (1+2i)\overline{z} \le 4$$
 where x and y are real.

Sketch the locus of z on an Argand diagram.

Solve the equation for w: (c) (i)

(ii)

2

$$w^2 = -11 - 60i$$
.

Write your answer in the form w = x + yi, where x and $y \in \mathbb{R}$

Hence, or otherwise, solve the equation:

3

$$z^2 - (1+4i)z - (1-17i) = 0$$

Five girls and three boys are seated at random around a circular table. (d) What is the probability that at least two boys are sitting next to each other? 3

(a) ABCD is a cyclic quadrilateral. Chords BE and DF bisect $\angle ABC$ and $\angle ADC$ respectively.

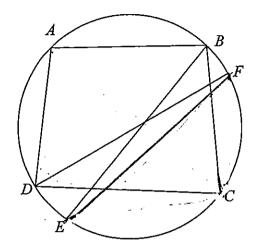


Diagram not to scale

Copy the diagram and prove that EF is a diameter of the circle.

3

- (b) Show whether the function f(x) = 2|x-1| |x| + 2|x+1| is even, odd or neither, giving reasons.
- 2
- (ii) Sketch the graph of the function f(x) = 2|x-1| |x| + 2|x+1|, clearly showing all intercepts with the coordinate axes and critical points. Label all branches with the relevant equations.
- 3

- (c) $P(x_1, y_1)$ is a point on the rectangular hyperbola xy = 9.
 - (i) Show that the Cartesian equation of the tangent at P is $y_1x + x_1y = 18$.
- 2
- (ii) Hence, or otherwise, derive the equation of the chord of contact from an external point $T(x_0, y_0)$ to the hyperbola xy = 9.
- 2
- (iii) Prove that the chord of contact is a focal chord when T is a point on the directrix.
- 3

Ouestion 4 (15 Marks) START A NEW PAGE

Marks

(a) (i) Find all stationary points for the curve $y^2 = x(3-x)^2$.

3

(ii) Sketch the curve $y^2 = x(3-x)^2$, showing all stationary points and the intercepts with the coordinate axes.

3

- (b) A particle of mass 2kg is projected vertically upwards with a velocity of $U \, \text{ms}^{-1}$ in a medium which exerts a resistive force of $\frac{v}{10}$ Newtons.
 - (i) Show that the maximum height H metres reached by the particle is given by:

3

$$H = 20 U + 4000 \ln \left(\frac{200}{200 + U} \right)$$
 (take $g = 10 \text{ ms}^{-2}$)

(ii) Find the time taken for the particle to reach the maximum height H.

3

(iii) If U = 400, show that the average speed during the ascent is:

3

$$200\left(\frac{2}{\ln 3}-1\right) \text{ ms}^{-1}$$
.

Question 5 (15 Marks) START A NEW PAGE

(a) A block of mass 5 kg is to be moved along a rough horizontal surface by a force (F Newtons) inclined at an angle of θ with the direction of motion where $0 \le \theta \le \frac{\pi}{2}$.

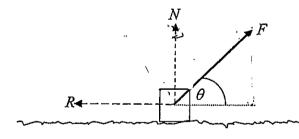


Diagram not to scale

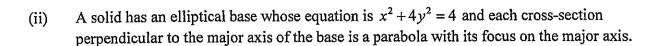
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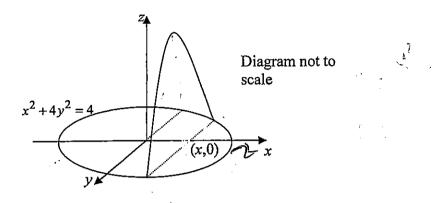
The motion is resisted by a frictional force (R Newtons) which is proportional to the normal reaction force (N Newtons) exerted on the block by the surface, such that R = 0.2 N.

- (i) Show that  $F = \frac{50}{5\cos\theta + \sin\theta}$  Newtons, when the block is about to move.
- (ii) Calculate the minimum value of F needed to overcome the frictional resistance between the block and the surface.

Question 5 continued over page

(b) (i) A parabola has the equation  $x^2 = 4ay$ . Show that the area bounded by this parabola 3 and the focal chord perpendicular to the axis is equal to  $\frac{8a^2}{3}$  units<sup>2</sup>.





Show that the area of the parabolic cross-section, x units from the origin, is given by the formula

$$A(x) = \frac{4-x^2}{6}$$

(β) Hence, find the volume of the resultant solid.

3

2

#### Question 6 (15 Marks) START A NEW PAGE

(a) The points  $P(a\cos\theta, b\sin\theta)$  and  $Q(a\cos\phi, b\sin\phi)$  lie on the ellipse

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1, \text{ where } \phi > \theta \text{ and } a > b.$$

The points  $P'(a\cos\theta, a\sin\theta)$  and  $Q'(a\cos\phi, a\sin\phi)$  lie on the auxiliary circle and subtend a right angle at the origin.

(i) Draw a neat sketch of the above information showing the relative positions of the points P, Q, P' and Q'.

(ii) Express the coordinates of Q in terms of  $\theta$ .

(iii) The tangents at P and Q meet in point R.

4

Find the coordinates of R in terms of  $\theta$ .

(iv) Show that R lies on the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 2$ 

Question 6 continued over page

(b) (i) If  $tan(x)tan(\theta - x) = k$  prove that:

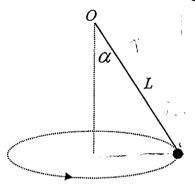
$$\frac{1+k}{1-k} = \frac{\cos(2x-\theta)}{\cos\theta}$$

(ii) Hence, or otherwise, solve the equation for all x.

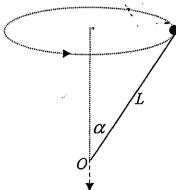
$$\tan x \tan \left(\frac{\pi}{3} - x\right) = 2 + \sqrt{3}$$

#### Question 7 (15 Marks) START A NEW PAGE

(a) A particle of mass m kg is fastened to one end of a light inextensible string of length L metres and the other end is attached to a fixed point O. The particle rotates with a uniform angular velocity  $\omega$  rad/s about a vertical line through O.



- (i) Show that if  $\alpha$  is the angle of inclination of the string to the downward vertical, then  $\alpha = \cos^{-1}\left(\frac{g}{L\omega^2}\right)$ .
- (ii) Explain why steady circular motion is only possible when  $\omega^2 > \frac{g}{L}$ .
- (iii) The point O is now made to descend with a uniform acceleration of f ms<sup>-2</sup>, whilst the particle continues to rotate with uniform angular velocity  $\omega$ .

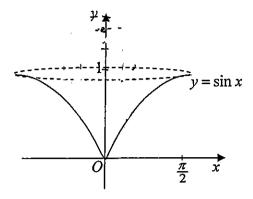


Find f so that the string makes an angle of  $\alpha$  with the upward vertical.

3

Question 7 continued over page

(b) The area between the curve  $y = \sin x$ , from x = 0 to  $x = \frac{\pi}{2}$ , the y-axis and the line y = 1 is rotated about the y-axis.



(i) Show that the volume of the solid formed can be found by using the formula

3

$$V = \pi \int_{0}^{\frac{\pi}{2}} x^2 \cos x \, dx$$

(ii) Hence, calculate the volume of the solid.

3

#### Question 8 (15 Marks) START A NEW PAGE

(a) The total number of different groups with 4 members which can be chosen from a group of n people is five times as many as the total number of different groups with 3 members which can be chosen from a group of n-2 people.

3

Find all possible values of n.

(b) Prove that  $\tan^{-1}(5) + \tan^{-1}(3) + \tan^{-1}(\frac{4}{7}) = \pi$ 

- (c) A curve, defined by the equation  $x^2 + 2xy + y^5 = 4$ , has a horizontal tangent at the point P(X, Y).

(i) Show that X is a root to the equation  $x^5 + x^2 + 4 = 0$ .

3

(ii) Show that the value of X is between -2 and -1:

1

(iii) With the use of a graph, or otherwise, show that X is the only real root to the equation  $x^5 + x^2 + 4 = 0$ .

4

### **End of Examination**

| TRIAL 2011  MATHEMATICS Extension 1; Question                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      | n8    |                                         |
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| Suggested Solutions                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                | Marks | Marker's Comments                       |
| a) ${}^{n}C_{4} = 5 {}^{n-2}C_{3}$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 | -     |                                         |
| $\frac{n!}{(n-4)!} = \frac{5(n-2)!}{(n-5)! \cdot 3!}$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              |       |                                         |
| $\frac{n(n-1)}{4}$ = .5                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            |       |                                         |
| n(n-1) = 20(n-1)<br>n = 20n = 80<br>$n^2 = 21n + 80 = 0$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | 1     | *************************************** |
| (n=16)(n=5)=0                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      |       |                                         |
| Mass State 116                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     | J     |                                         |
| 2) 0 < tan' 3 < tan' 5 < TT                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        |       | from ploops<br>from the =               |
| $tan(tan^{-1}3+tan^{-1}5) = 3+5^{-}=-4$ $1-15$ $7$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 | ,     | and mention of<br>restrictions D 2      |
| Bot as alvons about                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                |       | Lie Immos II                            |
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| 12m 3+ + 12m 5= + 12m (-4) + TT                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |       | ealier retriction                       |
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| =) Rifferentiate implicitly: 2 = +2y + 21 dy Dy do                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 | 0 1   |                                         |
| $\frac{2}{2}\left(\frac{2}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac{1}{2}x+\frac$ | 1     |                                         |
| 2×+ 54                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             | 1/2   |                                         |

Maths\Suggested Mk solns template\_V3\_all Ls.doo

| MATHEMATICS Extension 1: Question Suggested Solutions                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          | Marks | Marker's Comments                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              |
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| -17/2                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  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| \$ V =  <br>V =  im                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    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p   x 2 dy                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         | [     |                   |
| y = sin <sub>12</sub>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          | $= \frac{24}{2} = \frac{6}{9}$ $= \frac{1}{2} \frac{1}{2} \frac{1}{9} \frac{1}{2} 1$ | 1     |                   |
| (ii) V = 11 (V)                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        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| = T[x2sinx]                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            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| 2 ( \( \frac{1}{2} \) \( \frac{1} \) \( \frac{1} \) \( \frac{1}{2} \) \( \frac{1}{2} | 11.) AX T/2 (17.2 AX                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 | 1     |                   |
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| Ex to action                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | . 75 1 |                                |
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| MATHEMATICS: Question                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         | (2)    | ( <sub>7</sub> )               |
| Suggested Solutions                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | Marks  | Marker's Comments              |
| (a) $d$ $T$ (length = L)                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      |        | [47                            |
| mg,                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           |        | I mark each for the resolution |
| 2 ty =0'                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      | (      | of T.                          |
| The sum of | į      |                                |
| : THL = m/w 2 (4)                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             | \      | T= m L w2.                     |
| Substitute (4) into (1) $WLW^{2} \text{ for } d = Wg$ $Wd = \frac{g}{LW^{2}}$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 | l      | 6-1 X= 1-W2.                   |
| Lω2. (ii) 0 ≤ 6-7-2 ≤ 1                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       |        | to the time                    |
| $0 \le \frac{g}{Lw^2} \le 1 \Rightarrow g \le Lw^2$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | , \    | for body!  i. mo tion          |
| If g > Lw2 => bod)  <br>le circular motion 1s                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 |        | (m possible.                   |
| Also, i's wincreased bod (9) decreased                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 1      | d Increases                    |
| =) & is increased' 1.e When widto & == ?.                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     |        |                                |

| 7.JV     | MATHEMAT                                                   | TCS: Question         | teus  | 10 M (2)              |
|----------|------------------------------------------------------------|-----------------------|-------|-----------------------|
|          | Suggested Solutions                                        |                       | Marks | Marker's Comments     |
| Ciii')   | mf = h                                                     | length=L<br>rtically: |       | tesolve<br>the forces |
| Ts<br>T= | youtally: in a = mrw  = mrw  = mrw  2                      | L .                   |       | Correctly in rest.    |
| { but    | $T = m L w^{2} - 47 d = \frac{9}{Lw^{2}}$ Hitute (2) & (3) | _ 1                   |       | Subst. (2) & (3) into |
| m f      |                                                            | 2 x 1-102             | (     | Correct<br>Solution   |
| ₩,       | •                                                          |                       |       |                       |

| MATHEMATICS Extension 2: Question                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | 5                          |                                                                                                  |
|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------|--------------------------------------------------------------------------------------------------|
| Suggested Solutions                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 | Marks                      | Marker's Comments                                                                                |
| 26(a) q' P' P' (acoso, as.no)  1. P (acoso, b s.no)  -a 0 0 7 × Q' (acoso, as.no)  -b Now \$\phi > 0 > 0                                                                                                                                                                                                                                                                                                                                    \qua                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    | مرحه                       | tor each correct P'; P Q', Q with LP'OQ' = 17                                                    |
| $\begin{array}{cccccccccccccccccccccccccccccccccccc$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                |                            | ± For each ordinate                                                                              |
| E: x² + y² = 1  R P                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 | (E)                        | For getting  Ear of tangent at  My = - bws0  asiND                                               |
| ie - bx sina + ay cosa = celo  Solving * hunclteene ou sly  x sin 0 bx sina cosa + ay sin'a = ab sind(l  2) x cosa - bx sina cosa + ay cosa = ab cosa(l  400 0 ay > ab (cosa + sina)  y = b (cosa + sina) = bt  subst un (l) bx cosa + ab (cosa + sina) sina                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | (2 <i>a.</i> )             | For correct method that leads to result    For getting 4   7   8   7   7   7   7   7   7   7   7 |
| $\Rightarrow x = a(\cos a - \sin a) = a/2cc$ $\therefore R = (a(\cos a - \sin a), b(\cos a + \sin a))$ $(iv) \text{ Lifts } x^2 + y^2 = a((\cos a - \sin a))^2 + b((\cos a + \sin a))^2$ $= a^2 + b^2 = a^2 + a^2 + b^2 + b^2 + b^2 + b^2 = a^2 + b^2 + b^2 + b^2 + b^2 + b^2 + b^2 + b^$ | s( Φ+<br>(μΦ) <sup>2</sup> | For a subst. List to test  Too a subst. List  to test  Too a subst. List  correctly              |
| J:\Maths\Suggested Mk solns template_V3.doc =: \times^2 + \frac{12}{2} = 2.                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         | q.ed                       | <br>!.                                                                                           |

| MATHEMATICS Extension 2: Question Suggested Solutions                                                           | Marks                        | Marker's Comments   |
|-----------------------------------------------------------------------------------------------------------------|------------------------------|---------------------|
| A 1                                                                                                             | 1                            |                     |
| (b) LH5 : 1+k = 1 + tanz +an(0-x)                                                                               |                              |                     |
| 1-k [ - + conc + con(0-2)                                                                                       |                              | Ushar tour A = 5201 |
| (i) .                                                                                                           |                              | using tent = sind   |
| = cosx cos (0-x) + 5 wx 5 w (0-x)                                                                               | ١                            |                     |
| cosx cos(0-x) - sinx sin(0-x)                                                                                   | 1+1                          | •                   |
| 205x 205(0-x) = 4(xx xx(0-x)                                                                                    |                              |                     |
|                                                                                                                 | 1                            | Uring               |
| ≥ cos[x-(β-x)]                                                                                                  | (                            | cos(A±B)产           |
| COS[X+(G-X)]                                                                                                    | 1 1                          | COLACOSE T SINA     |
| · · · · · · · · · · · · · · · · · · ·                                                                           | 1 '                          |                     |
| = (os (2x-0)                                                                                                    |                              |                     |
| Cos O                                                                                                           |                              |                     |
| = AHS                                                                                                           |                              |                     |
|                                                                                                                 |                              | [ <del>**</del> */  |
|                                                                                                                 |                              |                     |
| آد دهی ک                                                                                                        |                              | •                   |
|                                                                                                                 |                              |                     |
| PPROACH 1: 1+k = 1+tanz(tano - tanz)                                                                            |                              |                     |
| I-k 1+tan0+cenx                                                                                                 | 1                            |                     |
| 1 - teenx ( teen 0 - teenx )                                                                                    |                              |                     |
| 1 4 teen 0 teense                                                                                               |                              |                     |
| = 1 + tanotane + tanetano - t                                                                                   | de NZ                        |                     |
| 1 + tuno teens - teans teams + t                                                                                | ~~ " <sup>2</sup> 1¢         |                     |
| 17 (2000)                                                                                                       | 22.                          |                     |
| = 1 + 2 tean 0 tank - tan x.                                                                                    | ١.                           |                     |
|                                                                                                                 |                              |                     |
| 1 + tcentu                                                                                                      |                              |                     |
|                                                                                                                 |                              |                     |
| = 1 + 2+cent +cent - (Sec21c-1)                                                                                 | -                            |                     |
| چ <u>په د</u> کېد                                                                                               |                              |                     |
| = cos x 2 - s.ec x + 2+ceno. si                                                                                 | <u>     </u>                 | <i> </i>            |
|                                                                                                                 | 23C                          |                     |
| = 2005x -1 + 25inx cosx. 5ind                                                                                   |                              |                     |
| coso                                                                                                            | İ                            |                     |
| = cos Zz + sinzz, sino                                                                                          | ,                            |                     |
| المادة على ا | [ ]                          |                     |
|                                                                                                                 | 1                            |                     |
| = co+2x cos0 + sin 2x sin0 =                                                                                    |                              | (2x-0) qual         |
| C050                                                                                                            | ت                            | 250                 |
| 4                                                                                                               | <u></u>                      |                     |
|                                                                                                                 | 3 + 13                       | 1 For subst.        |
| cos #/2 [- (2+13) -                                                                                             | 1-13                         | simplifying         |
| K= 2+/3                                                                                                         | 1                            |                     |
| $(2x-\frac{\pi}{3})=-(3+\sqrt{3})=-(3+\sqrt{3})$                                                                | <u>۔</u> (ولائ               | -13(134)= -13       |
| 1 1+13                                                                                                          | -                            | 130300 713          |
|                                                                                                                 | 7                            | 1 13+1 /            |
| 4 - 6 20 12                                                                                                     |                              | (1/2)               |
| Cos(2x-3) = -12                                                                                                 |                              |                     |
| • -                                                                                                             | 2 -70                        | ,                   |
| $\frac{1}{2x-\frac{\pi}{3}}=2m\pi\pm(\frac{5\pi}{3})$                                                           | 466                          | '                   |
|                                                                                                                 |                              | (=                  |
| >c= \ mt + 71/2 (12)                                                                                            | ۸ <del>+</del> 7) <u>ا ا</u> | 1 SOLUTIONS         |
| (4m.                                                                                                            | -1)亚                         | ·                   |

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7.

| MATHEMATICS Extension 1: Question                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   |       |                                                               |
|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------|---------------------------------------------------------------|
| Suggested Solutions                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 | Marks | Marker's Comments                                             |
| ) Vert. $N + F \sin \theta = mg$<br>$N + F \sin \theta = 5 \times 10$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               | 12    | must show                                                     |
| Horiz. $R - F \cos \theta = 0$ $0.2N = F \cos \theta$ $N = 5 F \cos \theta$ $0.2N = F \cos \theta$ $0.2N $                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             | 12 12 | Mass Store Where SD comes from 2m. This is is HOW' question.  |
| 5 enotsing #  ii) F is min when 5 cos 0 + sin 0 is max  5 cos 0 + sin 0 = : R sin (0+d)  = R sin 0 cos d + R sin dign 0  : R sin d = 1 , R cos d = 5                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                | /     | Rolly well done.                                              |
| $R = \sqrt{1 + 5} = \sqrt{26}$ $S_{c-0} + J_{1}C_{0} = \sqrt{26} S_{1}C_{0} + 2C_{1}$ $ S_{in}(0+2)  \leq 1$ $ S_{in}(0+$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    | /     | many forgot  has 57-(6+2)=1  -2m.                             |
| Altern. $F' = \frac{50}{(5en\theta+\sin\theta)} \left( -5.92\theta+cn\theta \right) \ge 0$ when $5 \sin\theta = \cos\theta  \therefore  \tan\theta = \frac{1}{5}.$ $\therefore \sin\theta = \frac{1}{56},  \cos\theta = \frac{5}{56}  \left( 0.66 = 90 \right)$ Justify min $F = \frac{1}{565} = \frac{1}{576} \times \frac$ | 12    | many forget to . Justify min/man -1 m. many front \$5059; -im |

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| MATHEMATICS Extension 2: Question, 56                                                                                                                                                                                                                                                                                                              |          |                                                                         |  |
|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------|-------------------------------------------------------------------------|--|
| Suggested Solutions                                                                                                                                                                                                                                                                                                                                | Marks    | Marker's Comments                                                       |  |
| i) $4ay = x^{2} - y = \frac{x^{2}}{4a}$<br>when $y = a$ $4a = x^{2} - x = \pm 2a$<br>2a $2a$ $2aA = (x + y + x + 2)$                                                                                                                                                                                                                               | l m      | Many forget                                                             |  |
| $A = \int_{0}^{2a} a_{-} y  dx = 2x \int_{0}^{2a} -\frac{x^{2}}{4a} dx  (\text{even furtion})$ $-\frac{1}{2a}$ $= 2 \cdot x \left[ ax - \frac{x^{3}}{12a} \right] = 2x \left[ \frac{2a^{2} - \frac{8a^{3}}{12a}}{12a} \right]$ $= \frac{4a^{2} - \frac{8a^{3}}{12a}}{12a}$                                                                         | l m      | even $-\frac{1}{2}m$ $2a$ $2\int \frac{x^{2}}{4a}dx$ $a$ the wrong area |  |
| $= 2 \times \left[2a^{2} - \frac{1}{3}a^{2}\right] = 2 + \frac{4}{3}a^{2} = \frac{8a^{2}}{3} \text{ unit}$ $= x = \pm 2\sqrt{ay}$ $A = 2\sqrt{2} \times dy \text{ (even)} = 2\sqrt{2\sqrt{ay}} dy$                                                                                                                                                 | Im<br>Im | max 12 m                                                                |  |
| $A = 4\sqrt{a} \left( y^{3/2} \cdot \frac{2}{3} \right) = \frac{2}{3}\sqrt{a} a^{3/2} = \frac{2}{3}a^{2}u^{-1}t^{2}$                                                                                                                                                                                                                               | 1 m      | many fudging  since answer given  show auestian:  must show a=1/2       |  |
| from (i) $A = \frac{8}{3}a^2 = \frac{8}{3}(\frac{4}{2})^2 = \frac{8}{3}\frac{4^2}{4}$                                                                                                                                                                                                                                                              | 1 m      | <u>-</u>                                                                |  |
| $A = \frac{2}{3}y^{2} \qquad \text{Out } x^{2} + 4y^{2} = 4$ $A = \frac{2}{3} \cdot \frac{4 - x^{2}}{4} = \frac{4 - 2x^{2}}{6}$                                                                                                                                                                                                                    | /加       | \\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\                                  |  |
| $ \begin{array}{ll} \tilde{i}(\hat{\beta}) & V = \lim_{\Delta x \to 0} \sum_{X = -1} A(x) \Delta X \\ &= \int_{-1}^{\infty} \frac{4 - x}{6} dx = 2 \int_{0}^{\infty} \frac{4 - x^{2}}{6} dx = \frac{1}{3} \left(4 \times - \frac{x^{3}}{3}\right)^{2} \\ &= \frac{1}{3} \left(8 - \frac{8}{3}\right) = \frac{16}{9} \text{ unit}^{3} \end{array} $ | 1+12     | linit statement in                                                      |  |
| #                                                                                                                                                                                                                                                                                                                                                  |          |                                                                         |  |

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| NIT TRIAL TO! MATHEMATICS Extension 1: Question Suggested Solutions                            | Merks | Marker's Comments                               |
|------------------------------------------------------------------------------------------------|-------|-------------------------------------------------|
| $(3-x)^2 = x(3-x)^2$                                                                           |       |                                                 |
| method 1:                                                                                      |       |                                                 |
| $y = \pm \sqrt{x(3-1)^2}$                                                                      |       | FORGOT ± -tm                                    |
| $y' = \frac{3}{2\sqrt{\chi}} - \frac{3}{2}\sqrt{\chi}$ (for 470)                               | 1     |                                                 |
| s.p $y' = 0$ when $0 = \frac{3}{2\sqrt{x}}(1-x)$ (x+0)                                         |       |                                                 |
| :. x=1 y=2                                                                                     | 1     | many topot y values                             |
| By symmetry S.P (1,2) or (1,-2)                                                                | 1     |                                                 |
| Method 2 implicit differentiation<br>$y^2 = 3c(3-x)^2 = 9x - 6x^2 + x^3$                       |       |                                                 |
| 1 0 10 × + 321 ×                                                                               | /     | •                                               |
| $\frac{3yy' = 4-12x(1-x)}{2y} = \frac{3(x-3)(x-1)}{\pm 2\sqrt{x}[3-x]}$                        |       | many forget ± -2m                               |
| :- x=3 or 1 but x + 3 or 0                                                                     | 1     | if x=3 is included                              |
| $\int_{0}^{\infty} x = 1 \text{ ord} y$ $\int_{0}^{\infty} f(1,2) = \int_{0}^{\infty} f(1,-2)$ | /     | ner 2 m.                                        |
| b) 3 (1,2)                                                                                     | 3     | O Stationary Pts  (1) Vertical tangent  at 11=0 |
| V.T. (1-2)                                                                                     |       | (3 slape, scale currature                       |

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| YANTAN ANI MATHEMATICS Extension L: Ques Suggested Solutions                                                                      | Marks     | Marker's Comments                                             |
|-----------------------------------------------------------------------------------------------------------------------------------|-----------|---------------------------------------------------------------|
| oi) mx = -mg-to 1+ lng 1 to                                                                                                       |           |                                                               |
| 2 x = -20 - x<br>x = -(10 + \frac{1}{10})                                                                                         | / m       |                                                               |
| $V \frac{dv}{dx} = -\left(\frac{v+2\sigma\sigma}{2\sigma}\right)$                                                                 |           |                                                               |
| $\int_{0}^{H} dx = \int_{0}^{\infty} \frac{-20V}{200+V} dV \qquad Af hank H, V=0$                                                 |           | many forget moral H, V=0                                      |
| $H = -20 \int_{1}^{1} \frac{200  dv}{200 + v} = 20 \int_{0}^{1} \frac{100  dv}{400 + v}$                                          | 7 10      | sta Quetion.                                                  |
| $H = 20 \left[ V - 200 \ln (200 + V) \right] = 20 \left[ n - 200 \ln \left( \frac{1}{2} \right) \right]$                          | 200 2 h   | must show<br>- In ( dooth ) = + In (20<br>200)                |
| H = 20 H + 4000 l - (200 )                                                                                                        | 1         | (200                                                          |
| $\frac{1}{1}$ $\frac{dV}{dt} = -\left(\frac{100+V}{20}\right)$                                                                    |           |                                                               |
| Jet = J-20dv hort H, V=0                                                                                                          | / m       | did well                                                      |
| T = {- 20 l= (200+v)}                                                                                                             | l m       |                                                               |
| T = -dv ln ( douth) = +20 ln ( douth) se.                                                                                         | l m       | many fogut and - E                                            |
| iii) Are Speed = = = T=                                                                                                           |           | "SHa" Q.                                                      |
| $T = 20 \ln \left( \frac{200 + 400}{200} \right) = 20 \ln 3$                                                                      | 之,<br>(聖) | must show detalls.  put show la (200 +400)                    |
| D = 4000 x 20+ 4000 l- (200 )= 3000 + 4000 l- 3                                                                                   | 1/m       | $= l_n\left(\frac{6n}{20}\right) = l_n \cdot 3 - \frac{1}{2}$ |
| And Speed = = = = = = = = = = = = = = = = = =                                                                                     | 2 m       | must show In 3 = - la?                                        |
| $= \frac{4001}{200} \left(2 + 1 - \frac{1}{2}\right) = 20 \left(\frac{2}{1 - 3} + \frac{1 - \frac{1}{2}}{1 + \frac{1}{2}}\right)$ | をかか       | must show factorization                                       |

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| MATHEMATICS Extension 2: Question. 3                                                                                                                                                                                                                                                                                                                        | ****                                                                                       |
|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------|
| Suggested Solutions                                                                                                                                                                                                                                                                                                                                         | Marks Marker's Comments                                                                    |
| 3(a)                                                                                                                                                                                                                                                                                                                                                        | Method 2  L V  2. L DAF+B+20=  (augle sum of A)  is 180°).  1e. LDAF= 90°  Conclusion-REAS |
| $2\alpha + 2\beta = 180$ (Opposite angles of cyclic act                                                                                                                                                                                                                                                                                                     | FD.  admilateral ABCD is l                                                                 |
| EDC = d° (Angles subtended on circustanting on the same as  S (EDF = d°+ fb = 70° (adjacent angle)  E. Dand Fexist on circumcuscle EDF  A night angle at the circumference subtend  i. FF is a dicembler (correspond                                                                                                                                        | le addition)  s a dicemeter                                                                |
| $= \frac{2 -1(x+1) - -x +2 -1(x-1) }{2 x+1 - x +2 x-1 }$ $= \frac{2 x+1 - x +2 x-1 }{2 x-1 }$ $= \frac{2 x+1 - x +2 x-1 }{2 x-1 }$                                                                                                                                                                                                                          | a  =  a  $ a  =  a $ $ b-a  =  -(a-b) $ $ b-a  =  a-b $ $ b-a  =  a-b $                    |
| $\frac{ x }{ x } = \frac{ x-1 }{ x } = \frac{ x-1 }{ x }$ $\frac{ x }{ x } = \frac{ x-1 }{ x } = \frac{ x-1 }{ x }$ $\frac{ x }{ x } = \frac{ x-1 }{ x } = \frac{ x-1 }{ x }$ $\frac{ x }{ x } = \frac{ x-1 }{ x } = \frac{ x-1 }{ x }$ $\frac{ x }{ x } = \frac{ x-1 }{ x } = \frac{ x-1 }{ x }$ $\frac{ x }{ x } = \frac{ x-1 }{ x } = \frac{ x-1 }{ x }$ | For Y=3x, -3x<br>  For Y=-2x+4<br>  For (0,4)<br>  \$\frac{1}{3}\) For (\(\frac{1}{4}\)3   |

| MATHEMATICS Extension 2: Question                                      | 3              |                               |
|------------------------------------------------------------------------|----------------|-------------------------------|
| Suggested Solutions                                                    | Marks          | Marker's Comments             |
| 3€) (i) ×4 = 9                                                         | -              |                               |
| y= 9 = 9x-1                                                            | -              |                               |
| :. u + 2 dy = 0                                                        | _              |                               |
|                                                                        | _              |                               |
| $1.e.  dy = -y \qquad dy = -q$ $\frac{dy}{dx} = \frac{y}{x}$           | - 1            |                               |
| ax x                                                                   | -   - \        | 15-141                        |
| is are dient of tangent at P(20,4,): my = -4, (as Equ. of Tangent at P | "一支/           | 1 1 DV 100-                   |
| Y-Y, = -Y( (x-x() *                                                    | -  `           | server selet of lands         |
| <b>&gt;</b> (                                                          | <b>-</b>       | 12                            |
| > \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \                                |                |                               |
| so yx + x,y = 2x,y, but x,y, = 9 us bt                                 | P(14,14        | lies on reg = 9               |
| i. 12 + x14 = 2 = 18                                                   | -   호 +        | 1 For explaining 2 why xiyi=9 |
| ii) Tangent at P(x1, x, 1 is x, x + x1 y = 18                          | <del>-  </del> | 19 0                          |
| " " Q(x2, 1/2) is y k + x-y = 18                                       | 고              | \frac{1}{k} \pi \pi           |
| ······································                                 | [] . [         | 0                             |
| Let PQ be the chord of contact now from                                | T(x0,1         | (s) Taxo, (s)                 |
| these tangents alsove pass through T(xo, y)                            | -              | 2010 49                       |
| 1. 4/x + x1/2 = 403(1 + x0)( = 18 - (1)                                | 7              |                               |
| and 12 + x2 + x2 = 4 x + x2 + 18 - (2)                                 | 느느             |                               |
|                                                                        | •              | [2]                           |
| So boints P and Q lie on the equation you                              | + 2604         | = LB                          |
| PQ uniquely determine the "chord of                                    |                | " } For Justify               |
| to uniquely determine the chord of                                     | e u. t ce      | ct linking                    |
| which is of the form you tray = 18/                                    | - 호            |                               |
| (iii) Y FOR 24 = 4 1. 62                                               | = q <i>-</i> ≥ | c=3                           |
|                                                                        | .              |                               |
| Directrices: >c4y=                                                     | ta = =         | .cv5 = ± 3/2 🔒                |
| P 5 Foci (±3/2)                                                        | <u>+</u>  3√2) | *                             |
|                                                                        | :              | Khamata da                    |
| Given T(26,4) i                                                        |                | DIVESTIC                      |
| ZY=9                                                                   | ·              | Ţ                             |
| Now Chard of                                                           | conta          | ect is you + xoy=             |
| Q \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \                                | . 1            | ,                             |
|                                                                        |                | ect with transvers            |
| +                                                                      |                | .(5)                          |
| 12/                                                                    | ) = LB         |                               |
| t 2 200                                                                | <del>-</del> - | B = ± 3/2 2                   |
|                                                                        | ]              | -3/5·                         |
| 1                                                                      | 疕              | <b>ż</b> /                    |
| but tects is a t                                                       | ضعت ن          | S = 5 3                       |
| when T(xo, y) is on a c                                                | livec          | tuix 3                        |

L

| Extension (2).                                             |                                 |
|------------------------------------------------------------|---------------------------------|
| MATHEMATICS: Question Suggested Solutions Marks Marker's C | omments                         |
| (d) (i) Number of Ways that                                | er (iii), rk,  H(Ir) ralent rt, |

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|                                                                                                                                                                                                                                                                                                                              | 2).     |                                                                                                                         |
|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------|-------------------------------------------------------------------------------------------------------------------------|
| Suggested Solutions                                                                                                                                                                                                                                                                                                          | Marks   | Marker's Comments                                                                                                       |
|                                                                                                                                                                                                                                                                                                                              | ).      | nark<br>for each<br>point.                                                                                              |
| (b) $72 =  Z  = x^2 + y^2$ Let $72 =  Z  = x^2 + y^2$ Let $72 =  Z  = x^2 + y^2$ (1-21)(x+1y) = x+1y - 2/x + 2y  (1+21)(x-1y) = x-1y + 21x + 2y $27 + (1-21)7 + (1+21)7 = 9$ Veduces to $x^2 + y^2 + 2x + 4 - y = 9$ Circle centrel (-1,-2) $x^2 + y^2 + 2x + 4 - y = 9$ Circle centrel (-1,-2) $x^2 + y^2 + 2x + 4 - y = 9$ | 2 ( 2 + | mark Substituting I d Simplifying  T.  mark completing the square mark entre, tadius f the circle diagram for the local |

| MATHEMATICS Extension 2: Question                                                                   |       |                                      |
|-----------------------------------------------------------------------------------------------------|-------|--------------------------------------|
| Suggested Solutions                                                                                 | Marks | Marker's Comments                    |
| (1): Let $\sqrt{-11-601} = a+ib$ .<br>(1) $-11-60i = (a^2-b^2)+i2ab$ .<br>Equate real and imaginary |       | 2]                                   |
| $\frac{a^2 - b^2 = -1(2ab = -60)}{(a^2 - b^2)^2 = (a^2 + b^2)^2 - 4a^2b^2}$                         |       | Correct<br>quadratic<br>expression   |
|                                                                                                     | (     | Solving a<br>quartic equa<br>Correct |
| $\frac{(11)  Z^{2} - (1+4i) \cdot Z - (1-17i) = 0}{Z = b \cdot 1 \sqrt{b^{2} - 4ac}}$               |       | solution<br>for W.                   |
| $\frac{Za}{Z} = (1+4i) \pm \sqrt{-11-60i}$                                                          | l     | hse<br>quadratic                     |
| $= \frac{1}{14i} \pm (5-6i)$ $= \frac{2}{12} = 3-1$                                                 |       | Apply (Ci)                           |
|                                                                                                     | 1     | formula:                             |
|                                                                                                     | 1     |                                      |
| <b>\</b>                                                                                            |       |                                      |
|                                                                                                     |       |                                      |

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| TRIAL 2011 MATHEMATICS Extension 2: Question                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | Marks             | Marker's Comments                               |
|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------|-------------------------------------------------|
| Suggested Solutions                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            | - <del>****</del> |                                                 |
| Let I = I e de Let wiel                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        |                   |                                                 |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                | 1                 |                                                 |
| - Cathania Carlotta C | i i               | 11011001000                                     |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                | 1                 |                                                 |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                | '                 |                                                 |
| was a second sec |                   |                                                 |
| - 14 14 14-11 + K From                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         | i '               |                                                 |
| +ables                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         |                   |                                                 |
| - 1 / 0 × + 1 0 2 × - 1   + k                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | ١,                |                                                 |
| The same of the sa | 1 1               |                                                 |
| $(e^{x} > 0)$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  |                   | ***************************************         |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                |                   |                                                 |
| il Let I = 1                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | <del>.</del> †    |                                                 |
| 1 ~ 2 Cv . 6   A . 8                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | J.                | 4 1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-        |
| 2-3 x-2 (x-2)(x-2)                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             | ı)                |                                                 |
| =                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              | .                 |                                                 |
| [x-3)(x-2) [A(x-2)+8(x-1)=                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     | .                 | /#####################################          |
| x=2→ B = -1                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    | 4-1               | #\$14###\$\$\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\     |
| =1/1 - $1$ $1$ $1$ $1$ $1$ $1$ $1$ $1$ $1$ $1$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 | `  '              | ***************************************         |
| $\left[\begin{array}{cccccccccccccccccccccccccccccccccccc$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     | .†                | he make deducted                                |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                | .                 | if us disoute                                   |
| $= \ln  x-3  - \ln  x-2  + C$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  |                   | voluce sages                                    |
| , , , , , , , , , , , , , , , , , , ,                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          | •                 |                                                 |
| = h   x-3 + c                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | -   }             |                                                 |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                | -                 | ***************************************         |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                | <del>~</del> [    | ***************************************         |
| ii) let I =   do   Let t= ten ?                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                | ો                 | ***************************************         |
| 12+ 650 W= 2 sec % de                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          | <b>₹</b>          | ***************************************         |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                | ^                 | 2472449744-444446624674444444444444444444444444 |
| = 1 2 dt = 2 dt = 40                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | :                 | ***************************************         |
| J0457/2+ L-E-) T++-                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            | •                 | ***************************************         |
| 2 Co 0 = 1 - E                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 | ^                 | **************************************          |
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| = 2 +ax 14 +ax 21 +c                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | . 1               | ***************************************         |
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| MATHEMATICS Extension'L: Question Suggested Solutions                                                                                                                                                                                                                                                                                                                                                   | n   (co | .t) .                                           |
|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------|-------------------------------------------------|
| Suggested Solutions                                                                                                                                                                                                                                                                                                                                                                                     | Marks   | Marker's Comments                               |
| b) $\begin{bmatrix} 2x & dx & = 1 \\ 2x + 2 & -2 & dx \end{bmatrix}$<br>$= \frac{1}{2} \left\{ \frac{2x + 2}{x^2 + 2x + 5} \right\}$<br>$= \frac{1}{2} \left\{ \frac{2x + 2}{x^2 + 2x + 5} \right\} \left\{ \frac{d\alpha}{(x+1)^2 + 4x} \right\}$<br>$= \frac{1}{2} \left[ \frac{1}{2} \frac{2x + 2}{x^2 + 2x + 5} \right] \left[ \frac{1}{2} \frac{1}{4} \frac{1}{4} \frac{1}{2} \frac{1}{2} \right]$ | 1,1     |                                                 |
| $ \begin{array}{cccccccccccccccccccccccccccccccccccc$                                                                                                                                                                                                                                                                                                                                                   | 1,1     |                                                 |
| $= \lim_{x \to \infty} \frac{2 \cos x - \sin x}{x + 2 \cos x}$ $= \lim_{x \to \infty} \frac{2 \cos x - \sin x}{x + 2 \cos x} = \lim_{x \to \infty} \frac{2 \cos x}{x}$ $= \lim_{x \to \infty} \frac{2 \cos x - \sin x}{x + 2 \cos x} = \lim_{x \to \infty} \frac{2 \cos x}{x}$                                                                                                                          |         |                                                 |
| i) T+2J=                                                                                                                                                                                                                                                                                                                                                                                                | 1       |                                                 |
| $\begin{array}{cccccccccccccccccccccccccccccccccccc$                                                                                                                                                                                                                                                                                                                                                    |         | Generally I know                                |
| 1 = T = 2 (T-42) = 5π-4π + 4h                                                                                                                                                                                                                                                                                                                                                                           |         | those is a single southern agents some segments |
| T-TT+4432 , J=T-432                                                                                                                                                                                                                                                                                                                                                                                     | - 1,1   |                                                 |

J:\Maths\Suggested Mk solns template\_V3\_all Ls.doc