JAMES RUSE AHS MATH. EXT | TRIAL, 2008

Question 1.		Marks
(a)	Find $\lim_{x\to 0} \frac{3x}{\tan 5x}$.	2
(b)	Find the obtuse angle between the lines $x - y - 1 = 0$ and $2x + y - 1 = 0$.	2
(c)	Find the general solution to $\sin \theta = \frac{\sqrt{3}}{2}$.	2
(d)	When the polynomial function $f(x)$ is divided by $x^2 - 16$, the remainder is $3x - 1$. What is the remainder when $f(x)$ is divided by $x - 4$?	2
(e)	Solve for x : $\frac{1-2x}{1+x} \ge 1$.	3
(f)	Find a primitive of $\frac{1}{\sqrt{x^2-9}}$.	1

Question 2. [START A NEW PAGE]

- (a) Given the function $g(x) = \sqrt{x+2}$ and that $g^{-1}(x)$ is the inverse function of g(x), find $g^{-1}(5)$.
- (b) (i) Show that: $\frac{2 \tan x}{1 + \tan^2 x} = \sin 2x$.
 - (ii) Hence, or otherwise, find $\int_{0}^{\frac{\pi}{4}} \frac{\tan x}{1 + \tan^{2} x} dx.$
- (c) Using the substitution $u = \sqrt{1+x}$, evaluate $\int_{0}^{3} \frac{5x^2 + 10x}{\sqrt{1+x}} dx.$
- (d) Sketch the graph of the curve: $y = 2\cos^{-1}(x) 1$, showing all essential information.

Question 3.	[START A NEW PAGE]	Marks
(a)	Find the exact value of $\tan\left(2\cos^{-1}\frac{12}{13}\right)$.	2
(b) .	Let point $P(4p,2p^2)$ be an arbitrary point on the parabola $x^2 = 8y$ with parameter p .	
	(i) Show that the equation of the tangent at P is $y = px - 2p^2$.	1
	 (ii) The tangent intersects the y-axis at C. The point Q divides CP, internally, in the ratio 1:3. Find the locus of all the Q points as parameter p varies. 	3
(c)	The velocity v ms ⁻¹ of a particle moving in a straight line at position x at time t seconds is given by: $v = x^3 - x$. Find the acceleration of the particle at any position.	2,
(d)	The numbers 1447, 1005 and 1231 all have something in common. Each is a four-digit number beginning with 1 that has exactly two identical different How many such four-digit numbers exist?	2 gits
(e)	Find $\int \cos^2\left(\frac{x}{2}\right) dx$.	2

Marks

2

3

(a) Find the term independent of x in the expansion of $\left(2x^2 - \frac{3}{x}\right)^9$.

(a) Considering the expansion: $(9+5x)^{29} = n + 1$

Question 5.

 $(9+5x)^{29} = p_0 + p_1x + p_2x^2 + ... + p_1x^k + ... + p_nx^n.$

2.

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(i) Use the Binomial theorem to write the expression for p_k .

(ii) Show that: $\frac{p_{k+1}}{p_k} = \frac{5(29-k)}{9(k+1)}$.

- (ii) Hence, or otherwise, find the largest coefficient in the expansion. 2 [you may leave your answer in the form: $\binom{29}{r} 3^a 5^b$].
- (b) An ice cube tray is filled with water which is at a temperature of 20° C and placed in a freezer that is at a constant temperature of -15° C.

 The cooling rate of the water is proportional to the difference between the temperature of the water W° C, so that W satisfies the rate equation: $\frac{dW}{dt} = -k(W+15), \text{ where } k \text{ is the rate constant of proportionality.}$
 - (i) Show that: $\frac{d}{dt}(We^{ht}) = -15ke^{ht}.$
 - (ii) Hence, show that: $W = 35e^{-kt} 15$.
 - (iii) After 5 minutes in the freezer, the temperature of the water cubes is $6^{\circ}C$.
 - Find the rate of cooling at this time (correct to 1 decimal place) 2
 - Find the time for the water cubes to reach $-10^{\circ}C$ (correct to the nearest minute).

(b) B C A

Two circles C_1 and C_2 intersect at C and D.

BC produced meets circle C_2 at E.

AB produced meets EF produced at G

Let $\angle DFE = \alpha$.

Copy or trace the diagram onto your writing booklet and prove that ADFG is a cyclic quadrilateral.

(c) A bag contains eleven balls, numbered 1, 2, 3, ... and 11.

If six balls are drawn simultaneously at random,

 C_2

- (i) How many ways can the sum of the numbers on the balls drawn be odd? 2
- (ii) What is the probability that the sum of the numbers on the balls drawn is odd?
- (d) When Farmer Browne retired he decided to invest \$2 000 in a fund which paid interest of 8% pa, compounded annually. From this fund he decided to donate a yearly prize of \$200 to be awarded to the Dux of Agriculture in Year 12. The prize money being withdrawn from this fund after the year's interest had been added.
 - (i) Show that the balance $\$B_n$ remaining after *n* prizes have been awarded will be: $B_n = 500(5-1\cdot08^n)$
 - (ii) Calculate the number of years that the \$200 prize can be awarded.

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Question 6

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- (a) A ball is projected from a point O on horizontal ground in a room of length 2R metres with an initial speed of U ms⁻¹ at an angle of projection of α. There is no air resistance and the acceleration due to gravity is g ms⁻².
 - (i) Assuming after t seconds the ball's horizontal distance x metres, is given by: $x = Ut \cos \alpha$, and the vertical component of motion is $\ddot{y} = -g$, show that the vertical displacement y of the ball is given by:

$$y = Ut\sin\alpha - \frac{1}{2}gt^2.$$

- (ii) Hence show that the range R metres for this ball is given by: $R = \frac{U^2 \sin 2\alpha}{g}.$
- (iii) Suppose that the room has a height of 3.5 metres and the angle of projection is fixed for $0 < \alpha < \frac{\pi}{2}$ but the speed of projection U varies.

 Prove that:
 - (a) the maximum range will occur when $U^2 = 7g \cos ec^2 \alpha$.
 - (β) the maximum range would be $14\cot\alpha$.
- (b) Given the polynomial function:

$$f_n(x) = 1 + \frac{x}{1!} + \frac{x(x+1)}{2!} + \dots + \frac{x(x+1)\dots(x+n-1)}{n!}$$
, for $n = 1, 2, 3, \dots$

where for n = 1: $f_1(x) = 1 + \frac{x}{1!} = x + 1$ which has a zero at -1.

- (i) Show that for n = 2: $f_2(x) = \frac{1}{2!}(x+1)(x+2)$ and state the zeros of $f_2(x)$.
- (ii) Hence **complete** the proof by mathematical induction that the zeros of the polynomial function $f_n(x)$ are -1, -2, -3, ... and -n for n = 1, 2, 3, ..., that is prove that: $f_n(x) = \frac{1}{n!}(x+1)(x+2)(x+3)...(x+n)$, for n = 1, 2, 3, ...

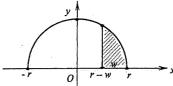
Question 7.

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(a) Given the semi-circle equation: $y = \sqrt{r^2 - x^2}$,



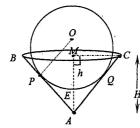
The shaded area of thickness w is rotated about the x-axis to form the volume of a 'cap'.

Show that the volume of the solid of revolution V is given by:

$$V=\frac{\pi}{3}(3r-w)w^2.$$

(b) An inverted cone ABC of height H units with a base radius of R units is filled with water.
A subgroup of radius x units is inserted into the inverted cone so as to touch

A sphere of radius r units is inserted into the inverted cone so as to touch the inner walls of the cone at P & Q to a depth of h units, as shown below.



Not to scale

$$MB = MC = R, MA = H, AC = L,$$

 $OP = r$ and $ME = h$.

- (i) Show that: $r = \frac{(H-h)R}{L-R}$, where $L = \sqrt{H^2 + R^2}$.
- (ii) Hence show that the volume of water V cubic units displaced by the sphere is given by:

$$V = \frac{\pi}{3(L-R)} [3RHh^2 - (L+2R)h^3].$$

- (iii) Hence, or otherwise find the radius of the sphere that displaced the maximum volume of water under the above conditions.
- (c) (i) Write down the binomial expansion of $(1-x)^{2n}$ in ascending powers of x.
 - (ii) Hence show that: $\binom{2n}{1} + 3\binom{2n}{3} + \dots + (2n-1)\binom{2n}{2n-1} = 2\binom{2n}{2} + 4\binom{2n}{4} + \dots + 2n\binom{2n}{2n}$

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MATHEMATICS Extension 1 : Question Suggested Solutions	Marks	Marker's Comments
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MATHEMATICS Extension 1 : Questi Suggested Solutions	Marks	Marker's Comments
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7) : + = 0 or + = 20 sing		
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MATHEMATICS Extension 1 : Question	on6	
Suggested Solutions	Marks	Marker's Comments
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p(a) was shown true in part (1)		
ssume P(n) is true for some integer K		
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$\frac{2}{k}(x) = \frac{1}{1} + \frac{x}{k} + \frac{2(x+1) + \dots + x(x+1) - (x+k-1)}{k!} = \frac{2}{k!}$		((2)
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MATHEMATICS Extension 1 : Questions Suggested Solutions	Marks	Marker's Comments
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= 11 2 43 - (4-w) (312 - (4-w))	,2)7	•
$= \prod_{i=1}^{n} \frac{2x^{3}}{3} - (f-\omega)(3x^{2} - x^{2} + 2x\omega - x^{2})$		
$= \prod_{i=1}^{n} \left[\frac{2r^{3} - (r - \omega)(2r^{2} + 2r\omega - \omega^{2})}{2r^{3} + 2r\omega - r\omega^{2} - 2r^{2}\omega - r\omega^{2}\omega -$	2rw2+w	3)]
$= \frac{\pi}{2} \left(\frac{3r}{2} - \omega^2 \right) = \frac{\pi}{2} \left(\frac{3r}{2} - \omega \right) \omega$		
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3(L-R) 3(L-R) 3(L-R)	····	
i) dy = T [GRHN - 3(L+2A) N2]	#	
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n(2RH - (L+2R)h) = 0		
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2h2 L-R TT [2AH - 4AH] =-	2 RH	A = RHL (L-R)(Lt

	MATHEMATICS Extension 1 : Question Suggested Solutions	Marks	Marker's Comments
$ \frac{2n}{2n} = \frac{2n}{2n} \times 2$			
By differentiating both sides with 2^{2n-1} $2n(1-x)^{2n-1} = -(2n) + 2(2n)x - 3(3n)x^{2n-1}$ $2n(1-x)^{2n-1} = -(2n) + 2(2n)x - 3(3n)x^{2n-1}$ $2n(1-x)^{2n-1} + 2(2n)x - 3(3n)x^{2n-1}$ $3n(1-x)^{2n-1} + 2(2n)x^{2n-1} + 2n(2n)x^{2n-1}$ $3n(2n)^{2n-1} + 2n(2n)^{2n-1} = 2n(2n)x^{2n-1}$ $3n(2n)^{2n-1} + 3n(3n)^{2n-1} = 2n(2n)x^{2n-1}$ $3n(2n)^{2n-1} + 3n(3n)^{2n-1} = 2n(2n)x^{2n-1}$ $3n(2n)^{2n-1} + 3n(3n)^{2n-1} = 2n(2n)x^{2n-1}$ $3n(2n)^{2n-1} + 3n(2n)^{2n-1} = 2n(2n)x^{2n-1} = 2n(2n)x^{2n-1}$ $3n(2n)^{2n-1} + 3n(2n)^{2n-1} = 2n(2n)x^{2n-1}$ $3n(2n)^{2n-1} + 3n(2n)x^{2n-1} $	2.42	. 20	
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$\frac{2n}{2n-1} = -\frac{2n}{2n} + \frac{2(\frac{2n}{2})x - 3(\frac{2n}{3})x^2 + \dots + 2n(\frac{2n}{2n})x^{2n-1}}{2n}$ $\frac{2n}{2n-1} = -\frac{2n}{2n} + \frac{2(\frac{2n}{2})x - 3(\frac{2n}{3})x^2 + \dots + 2n(\frac{2n}{2n})x^{2n-1}}{2n}$ $\frac{2n}{2n-1} + \frac{2n}{2n-1} + \frac{2n}{2n-1} = \frac{2n}{2n-1} = \frac{2n}{2n-1} + \frac{2n}{2n-1} = \frac{2n}{2n-1} = \frac{2n}{2n-1} = \frac{2n}{2n-1} + \frac{2n}{2n-1} = \frac{2n}{2n$	Dath Sides w		
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$\frac{2n}{2n} + 2(2n) - 3(2n) + \dots - (2n-1)(2n-1) + 2n (2n)$ $= -(2n) + 2(2n) + \dots + (2n-1)(2n-1) + 2n (2n)$ $= -(2n) + 3(2n) + \dots + (2n-1)(2n-1) = -(2n-1)(2n-1) + \dots + (2n-1)(2n-1) + \dots + (2n-1)(2n-1) = -(2n-1)(2n-1) + \dots + (2n-1)(2n-1) = -(2n-1)(2n-1) + \dots + (2n-1)(2n-1) $		1	
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