

**Envelope :**

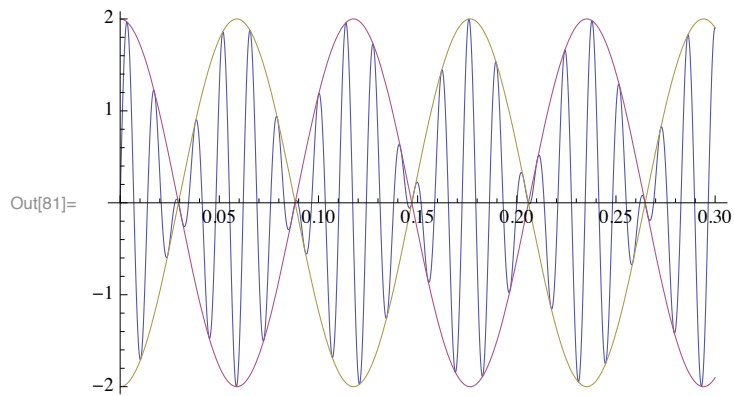
$$f(t) = \pm 2 \cos \left[ 2\pi \frac{(aq - pb)}{(p + q)} t \pm \pi \frac{(p - q)(2k + 1)}{2(p + q)} \right], \quad k = 0, 1, 2, 3, \dots$$

**Convergents [81 / 64]**

$$\text{Out}[100] = \left\{ 1, \frac{4}{3}, \frac{5}{4}, \frac{19}{15}, \frac{81}{64} \right\}$$

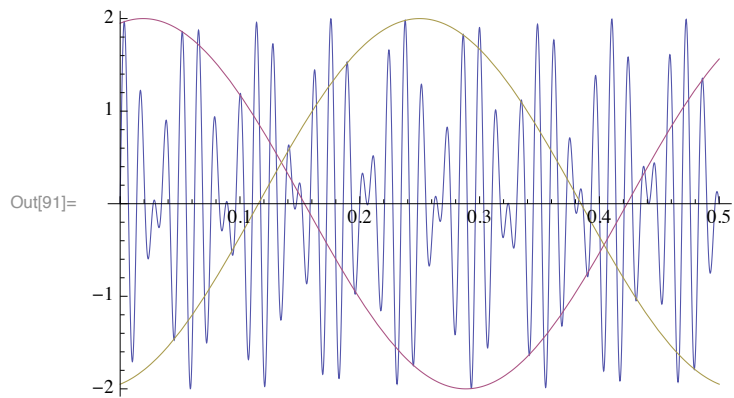
$$\frac{a}{b} = \frac{81}{64}, \quad \frac{p}{q} = \frac{1}{1}$$

**Plot[{Sin[2 π 64 t] + Sin[2 π 81 t], 2 Cos[2 π (17 / 2) t], -2 Cos[2 π (17 / 2) t]}, {t, 0, 0.3}]**



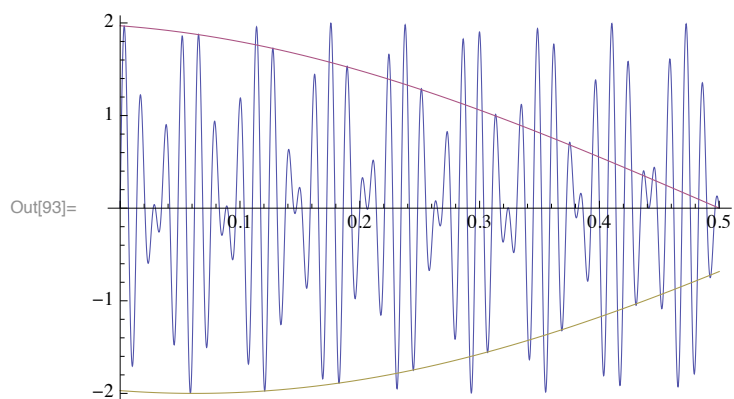
$$\frac{p}{q} = \frac{4}{3}$$

**In[91]:= Plot[{Sin[2 π 64 t] + Sin[2 π 81 t], 2 Cos[2 π (-13 / 7) t + π (1 / 14)], -2 Cos[2 π (-13 / 7) t - π (1 / 14)]}, {t, 0, 0.5}]**



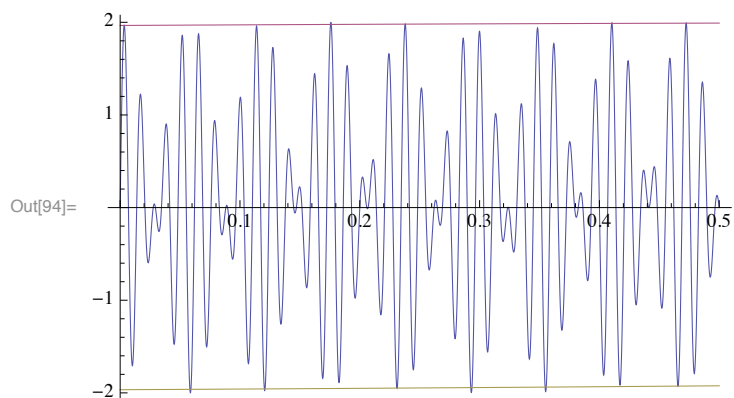
$$\frac{p}{q} = \frac{5}{4}$$

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In[93]:= Plot[{Sin[2 π 64 t] + Sin[2 π 81 t],  
2 Cos[π (8 / 9) t + π / 18], -2 Cos[π (8 / 9) t - π / 18]}, {t, 0, 0.5}]
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$$\frac{p}{q} = \frac{19}{15}$$

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In[94]:= Plot[{Sin[2 π 64 t] + Sin[2 π 81 t],  
2 Cos[2 π (-1 / 34) t + π (1 / 17)], -2 Cos[2 π (-1 / 34) t - π (1 / 17)]}, {t, 0, 0.5}]
```



$$\frac{p}{q} = \frac{81}{64}$$

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In[102]:= Plot[{Sin[2 π 64 t] + Sin[2 π 81 t], 2 Cos[π (17 / 290)], -2 Cos[-π (17 / 290)]}, {t, 0, 0.5}]
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