```
List[Round[(Range[17] 290 / 17), 2] - 1]
 {{17, 33, 51, 67, 85, 101, 119, 135, 153, 169, 187, 203, 221, 237, 255, 271, 289}}
List[Round[(Range[17] 290 / 17), 2] + 1]
 {{19, 35, 53, 69, 87, 103, 121, 137, 155, 171, 189, 205, 223, 239, 257, 273, 291}}
Plot [\sin[2\pi 81 x] + \sin[2\pi 64 x], \{x, -0.01, 1.01\},
   Epilog \rightarrow {PointSize[0.01], Point[{-1/290, 2 \sin[2 \pi 81 * -1/290]}],
             Point[{1/290, 2 \sin[2\pi81*1/290]}], Point[{17/290, 2 \sin[2\pi81*17/290]}],
             \texttt{Point}[\{19 \,/\, 290,\, 2\, \texttt{Sin}[2\,\pi\,81 \star 19 \,/\, 290]\}]\,,\, \texttt{Point}[\{35 \,/\, 290,\, 2\, \texttt{Sin}[2\,\pi\,81 \star 35 \,/\, 290]\}]\,,
             Point[{33/290, 2 sin[2 \pi 81 * 33/290]}], Point[{51/290, 2 sin[2 \pi 81 * 51/290]}], Point[{51/290, 2 sin[2 \pi 81 * 51/290]}]], Point[{51/290, 2 sin[2 \pi 81 * 51/290]}]]], Point[{51/290, 2 sin[2 \pi 81 * 51/290]}]]]]
             Point[{53 / 290, 2 Sin[2 \pi 81 * 53 / 290]}], Point[{67 / 290, 2 Sin[2 \pi 81 * 67 / 290]}],
             Point[\{69 / 290, 2 \sin[2 \pi 81 * 69 / 290]\}], Point[\{85 / 290, 2 \sin[2 \pi 81 * 85 / 290]\}], Point[\{69 / 290, 2 \sin[2 \pi 81 * 85 / 290]\}], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]\}], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]\}], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]\}], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]\}], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]\}], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]\}], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]\}], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]\}], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]\}], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]\}], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]\}], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]\}], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]\}], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]\}], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]\}], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]\}], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]\}], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]\}], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]\}], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]\}], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]\}], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]\}], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]\}], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]\}], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]\}], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]\}], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]\}], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]\}], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]\}], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]\}], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]\}], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]\}], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]\}], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]\}], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]\}], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]\}], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]]], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]]], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]]], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]]]], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]]]], Point[\{80 / 290, 2 \sin[2 \pi 81 * 85 / 290]]]]
             Point[{87 / 290, 2 Sin[2 \pi 81 * 87 / 290]}], Point[{101 / 290, 2 Sin[2 \pi 81 * 101 / 290]}],
             Point[\{121 / 290, 2 \sin[2\pi81 * 121 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]\}], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]]], Point[\{135 / 290, 2 \sin[2\pi81 * 135 / 290]]]
             Point[{137 / 290, 2 Sin[2 \pi 81 * 137 / 290]}], Point[{153 / 290, 2 Sin[2 \pi 81 * 153 / 290]}],
             Point[\{171/290, 2 \sin[2\pi 81 * 171/290]\}], Point[\{187/290, 2 \sin[2\pi 81 * 187/290]\}],
             Point[{189 / 290, 2 \sin[2 \pi 81 * 189 / 290]}], Point[{203 / 290, 2 \sin[2 \pi 81 * 203 / 290]}],
             Point[{205 / 290, 2 Sin[2 \pi 81 * 205 / 290]}], Point[{221 / 290, 2 Sin[2 \pi 81 * 221 / 290]}],
             Point[{273 / 290, 2 Sin[2 \pi 81 * 273 / 290]}], Point[{289 / 290, 2 Sin[2 \pi 81 * 289 / 290]}],
             Point[\{291/290, 2 \sin[2 \pi 81 * 291/290]\}]\}]
                                                                                                         0.6
List[Round[(Range[3] 70 / 3), 2] - 1]
 {{23, 45, 69}}
List[Round[(Range[3] 70 / 3), 2] + 1]
 {{25, 47, 71}}
```

```
Plot [\sin[2\pi 19x] + \sin[2\pi 16x], \{x, -0.02, 1.02\},
 Epilog \rightarrow {PointSize[0.01], Point[{-1/70, 2 \sin[2 \pi 19 * -1/70]}],
    Point[\{1/70, 2 \sin[2\pi 19 * 1/70]\}], Point[\{23/70, 2 \sin[2\pi 19 * 23/70]\}],
    \texttt{Point}[\{25 \,/\, 70,\, 2\, \texttt{Sin}[2\,\pi\,19 \,\star\, 25 \,/\, 70]\}]\,,\, \texttt{Point}[\{45 \,/\, 70,\, 2\, \texttt{Sin}[2\,\pi\,19 \,\star\, 45 \,/\, 70]\}]\,,
    Point[\{47 / 70, 2 \sin[2\pi 19 * 47 / 70]\}], Point[\{69 / 70, 2 \sin[2\pi 19 * 69 / 70]\}],
    Point[\{71 / 70, 2 \sin[2 \pi 19 * 71 / 70]\}]\}]
                                                           1.0
List[Round[(Range[5] 118 / 5), 2] - 1]
{{23, 47, 69, 93, 117}}
List[Round[(Range[5] 118 / 5), 2] + 1]
{{25, 49, 71, 95, 119}}
Plot[Sin[2 \pi 32 x] + Sin[2 \pi 27 x], {x, -0.02, 1.02},
 \texttt{Epilog} \rightarrow \{\texttt{PointSize[0.01], Point[\{-1 \,/\, 118,\, 2\, Sin[2\,\pi\,32\,\star\,-1 \,/\, 118]\}],}
    Point[\{1/118, 2 \sin[2\pi 32 * 1/118]\}], Point[\{23/118, 2 \sin[2\pi 32 * 23/118]\}],
    {\tt Point[\{25\,/\,118\,,\,2\,Sin[2\,\pi\,32\,\star\,25\,/\,118]\}]\,,\,Point[\{47\,/\,118\,,\,2\,Sin[2\,\pi\,32\,\star\,47\,/\,118]\}]\,,}
    Point[{49/118, 2 \sin[2 \pi 32 * 49/118]}], Point[{69/118, 2 \sin[2 \pi 32 * 69/118]}],
    Point[{71/118, 2 \sin[2 \pi 32 * 71/118]}], Point[{93/118, 2 \sin[2 \pi 32 * 93/118]}],
    Point[{95 / 118, 2 sin[2 \pi 32 * 95 / 118]}], Point[{117 / 118, 2 sin[2 \pi 32 * 117 / 118]}],
    Point[\{119 / 118, 2 \sin[2 \pi 32 * 119 / 118]\}]\}]
List[Round[(Range[19] 2 (51 + 32) / 19), 2] - 1]
\{\{7, 17, 25, 33, 43, 51, 61, 69, 77, 87, 95, 103, 113, 121, 131, 139, 147, 157, 165\}\}
List[Round[(Range[19] 166 / 19), 2] + 1]
{{9, 19, 27, 35, 45, 53, 63, 71, 79, 89, 97, 105, 115, 123, 133, 141, 149, 159, 167}}
```

```
Plot[Sin[2 \pi 51 x] + Sin[2 \pi 32 x], {x, -0.02, 1.02},
 Epilog \rightarrow {PointSize[0.01], Point[{-1/166, 2 Sin[2\pi51*-1/166]}],
   Point[\{1/166, 2 \sin[2\pi 51 * 1/166]\}], Point[\{7/166, 2 \sin[2\pi 51 * 7/166]\}],
   Point[{9 / 166, 2 Sin[2 \pi 51 * 9 / 166]}], Point[{17 / 166, 2 Sin[2 \pi 51 * 17 / 166]}],
   Point[{19 / 166, 2 Sin[2 \pi 51 * 19 / 166]}], Point[{25 / 166, 2 Sin[2 \pi 51 * 25 / 166]}],
   Point[{27 / 166, 2 Sin[2 \pi 51 * 27 / 166]}], Point[{33 / 166, 2 Sin[2 \pi 51 * 33 / 166]}],
   Point[{35 / 166, 2 Sin[2 \pi 51 * 35 / 166]}], Point[{43 / 166, 2 Sin[2 \pi 51 * 43 / 166]}],
   Point[{45 / 166, 2 Sin[2 \pi 51 * 45 / 166]}], Point[{51 / 166, 2 Sin[2 \pi 51 * 51 / 166]}],
   Point[{53 / 166, 2 Sin[2 \pi 51 * 53 / 166]}], Point[{61 / 166, 2 Sin[2 \pi 51 * 61 / 166]}],
   Point[{63 / 166, 2 Sin[2 \pi 51 * 63 / 166]}], Point[{69 / 166, 2 Sin[2 \pi 51 * 69 / 166]}],
   Point[{71/166, 2 Sin[2 \pi 51 * 71/166]}], Point[{77/166, 2 Sin[2 \pi 51 * 77/166]}],
   Point[{79/166, 2 Sin[2 \pi 51 * 79/166]}], Point[{87/166, 2 Sin[2 \pi 51 * 87/166]}],
   Point[{89 / 166, 2 Sin[2 \pi 51 * 89 / 166]}], Point[{95 / 166, 2 Sin[2 \pi 51 * 95 / 166]}],
   Point[\{97 / 166, 2 \sin[2 \pi 51 * 97 / 166]\}], Point[\{103 / 166, 2 \sin[2 \pi 51 * 103 / 166]\}],
   Point[\{105 / 166, 2 \sin[2\pi 51 * 105 / 166]\}], Point[\{113 / 166, 2 \sin[2\pi 51 * 113 / 166]\}],
   Point[{115 / 166, 2 Sin[2 \pi 51 * 115 / 166]}], Point[{121 / 166, 2 Sin[2 \pi 51 * 121 / 166]}],
   {\tt Point[\{123\ /\ 166,\ 2\ Sin[2\ \pi\ 51\ *\ 123\ /\ 166]\}],\ Point[\{131\ /\ 166,\ 2\ Sin[2\ \pi\ 51\ *\ 131\ /\ 166]\}],}
   Point[{133 / 166, 2 Sin[2 \pi 51 * 133 / 166]}], Point[{139 / 166, 2 Sin[2 \pi 51 * 139 / 166]}],
   Point[\{141/166, 2\sin[2\pi51*141/166]\}], Point[\{147/166, 2\sin[2\pi51*147/166]\}],
   Point[{149 / 166, 2 Sin[2 \pi 51 * 149 / 166]}], Point[{157 / 166, 2 Sin[2 \pi 51 * 157 / 166]}],
   Point[\{159 / 166, 2 \sin[2\pi 51 * 159 / 166]\}], Point[\{165 / 166, 2 \sin[2\pi 51 * 165 / 166]\}],
   Point[\{167 / 166, 2 \sin[2 \pi 51 * 167 / 166]\}]\}]
List[Round[(Range[17] 290 / 17), 2] - 1]
{{17, 33, 51, 67, 85, 101, 119, 135, 153, 169, 187, 203, 221, 237, 255, 271, 289}}
List[Round[(Range[17] 290 / 17), 2] + 1]
{{19, 35, 53, 69, 87, 103, 121, 137, 155, 171, 189, 205, 223, 239, 257, 273, 291}}
List[Round[(Range[17] 162 / 17)]]
\{\{10, 19, 29, 38, 48, 57, 67, 76, 86, 95, 105, 114, 124, 133, 143, 152, 162\}\}
List[Round[(Range[17] 128 / 17)]]
{{8, 15, 23, 30, 38, 45, 53, 60, 68, 75, 83, 90, 98, 105, 113, 120, 128}}
List[%% / %]
   5 19 29 19 24 19 67 19
                                        43
                                              19
                                                   105
                                                        19
                                                              62 19
                                                                       143
      34
                                             15
                                                    83
                                                         15 49
                                                                  15 113 15
List[%% + % + 1]
\{\{\{19, 35, 53, 69, 87, 103, 121, 137, 155, 171, 189, 205, 223, 239, 257, 273, 291\}\}\}
List[%% + % - 1]
\{\{\{17, 33, 51, 67, 85, 101, 119, 135, 153, 169, 187, 203, 221, 237, 255, 271, 289\}\}\}
```