

# Construction of an FA from an RE

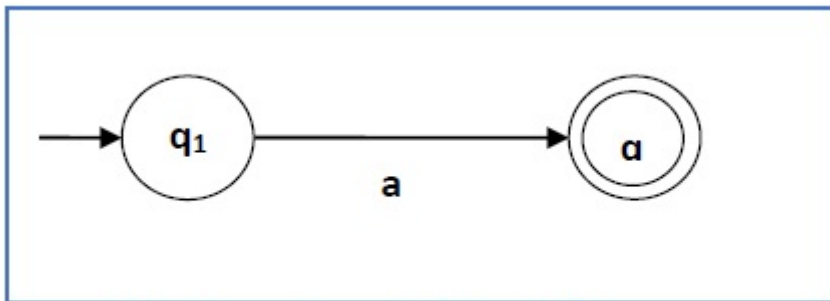
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We can use Thompson's Construction to find out a Finite Automaton from a Regular Expression. We will reduce the regular expression into smallest regular expressions and converting these to NFA and finally to DFA.

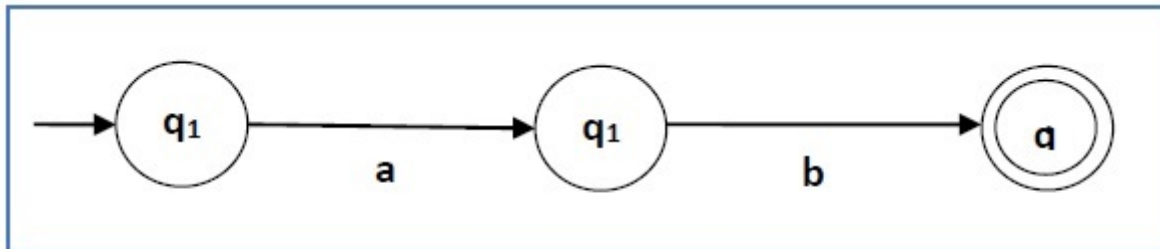
Some basic RE expressions are the following –

**Case 1** – For a regular expression ‘a’, we can construct the following FA –



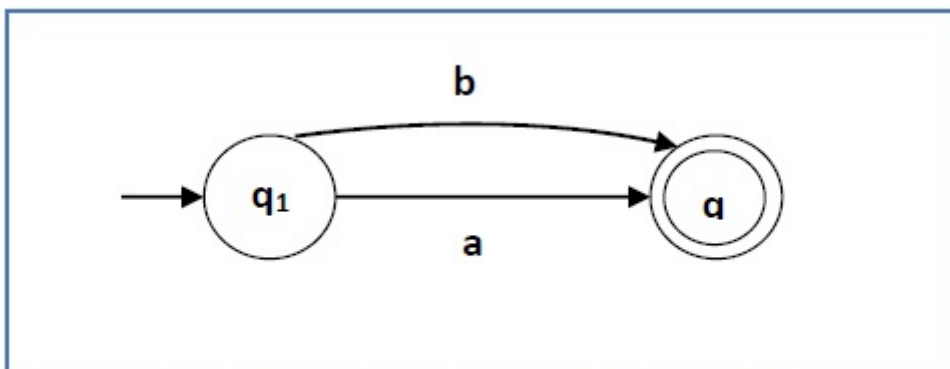
**Finite automata for RE = a**

**Case 2** – For a regular expression ‘ab’, we can construct the following FA –



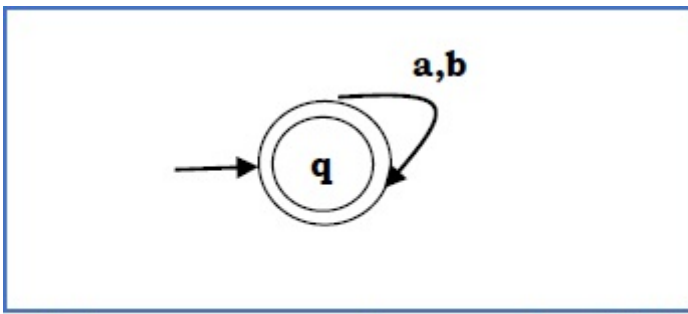
**Finite automata for RE = ab**

**Case 3** – For a regular expression  $a + b$ , we can construct the following FA –



**Finite automata for RE= (a+b)**

**Case 4** – For a regular expression  $a + b^*$ , we can construct the following FA –



**Finite automata for RE =  $(a+b)^*$**

## Method

**Step 1** Construct an NFA with Null moves from the given regular expression.

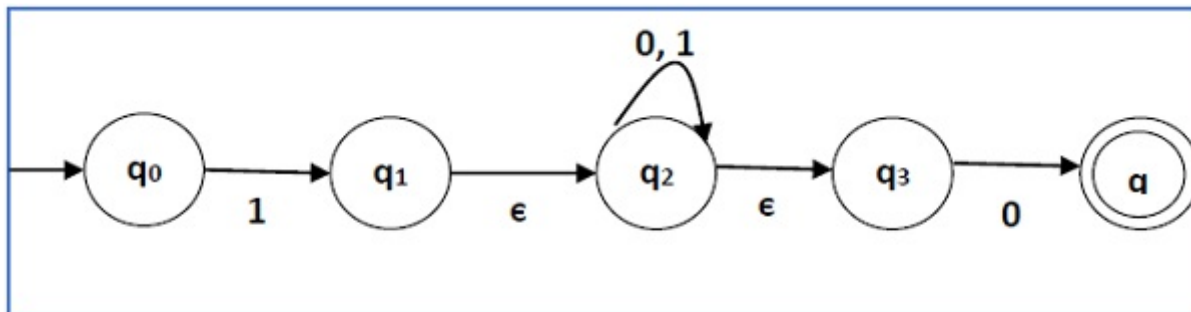
**Step 2** Remove Null transition from the NFA and convert it into its equivalent DFA.

## Problem

Convert the following RA into its equivalent DFA –  $1\ 0 + 1^* 0$

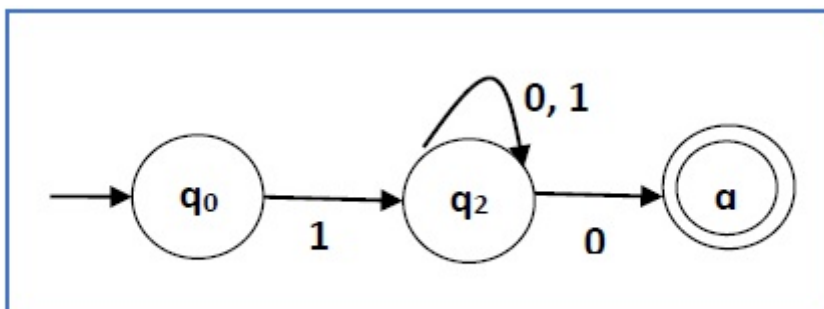
## Solution

We will concatenate three expressions "1", " $0 + 1^*$ " and "0"



**NFA with NULL transition for RA:  $1(0+1)^*0$**

Now we will remove the  $\epsilon$  transitions. After we remove the  $\epsilon$  transitions from the NFA, we get the following –



**NFA without NULL transition for RA:  $1(0+1)^*0$**

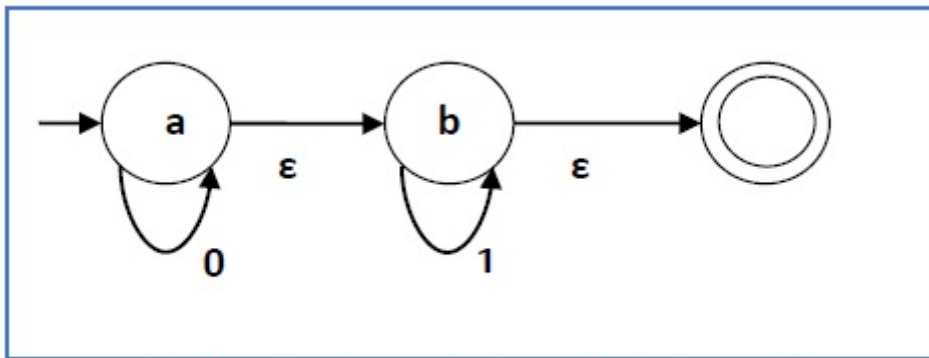
It is an NFA corresponding to the RE –  $1\ 0 + 1^* 0$ . If you want to convert it into a DFA, simply apply the method of converting NFA to DFA discussed in Chapter 1.

## Finite Automata with Null Moves $NFA - \epsilon$

A Finite Automaton with null moves  $FA - \epsilon$  does transit not only after giving input from the alphabet set but also without any input symbol. This transition without input is called a **null move**.

An NFA- $\epsilon$  is represented formally by a 5-tuple  $(Q, \Sigma, \delta, q_0, F)$ , consisting of

- $Q$  – a finite set of states
- $\Sigma$  – a finite set of input symbols
- $\delta$  – a transition function  $\delta : Q \times \Sigma \cup \epsilon \rightarrow 2^Q$
- $q_0$  – an initial state  $q_0 \in Q$
- $F$  – a set of final state/states of  $Q$   $F \subseteq Q$ .



**Finite automata with Null Moves**

The above  $FA - \epsilon$  accepts a string set –  $\{0, 1, 01\}$

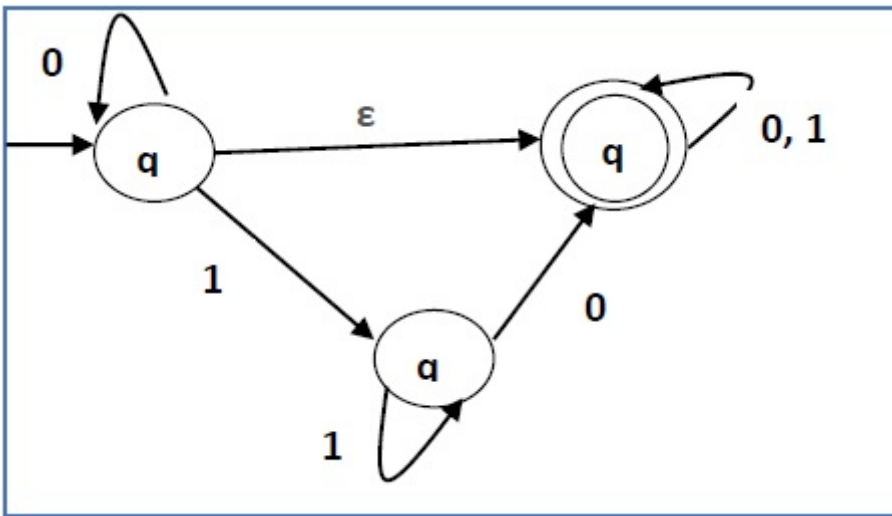
## Removal of Null Moves from Finite Automata

If in an NDFA, there is  $\epsilon$ -move between vertex  $X$  to vertex  $Y$ , we can remove it using the following steps –

- Find all the outgoing edges from  $Y$ .
- Copy all these edges starting from  $X$  without changing the edge labels.
- If  $X$  is an initial state, make  $Y$  also an initial state.
- If  $Y$  is a final state, make  $X$  also a final state.

### Problem

Convert the following NFA- $\epsilon$  to NFA without Null move.



### ***Solution***

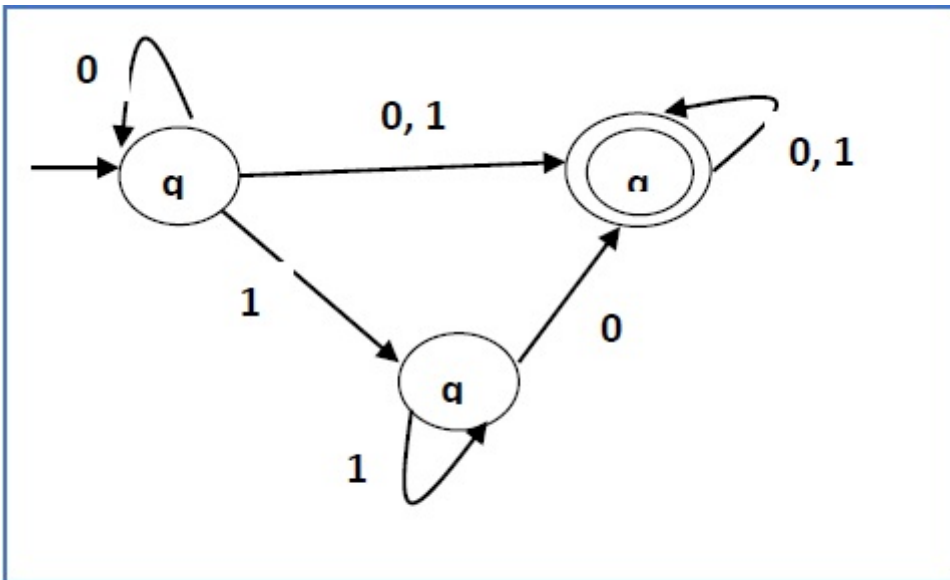
#### **Step 1 –**

Here the  $\epsilon$  transition is between  $q_1$  and  $q_2$ , so let  $q_1$  is  $X$  and  $q_f$  is  $Y$ .

Here the outgoing edges from  $q_f$  is to  $q_f$  for inputs 0 and 1.

#### **Step 2 –**

Now we will Copy all these edges from  $q_1$  without changing the edges from  $q_f$  and get the following FA –

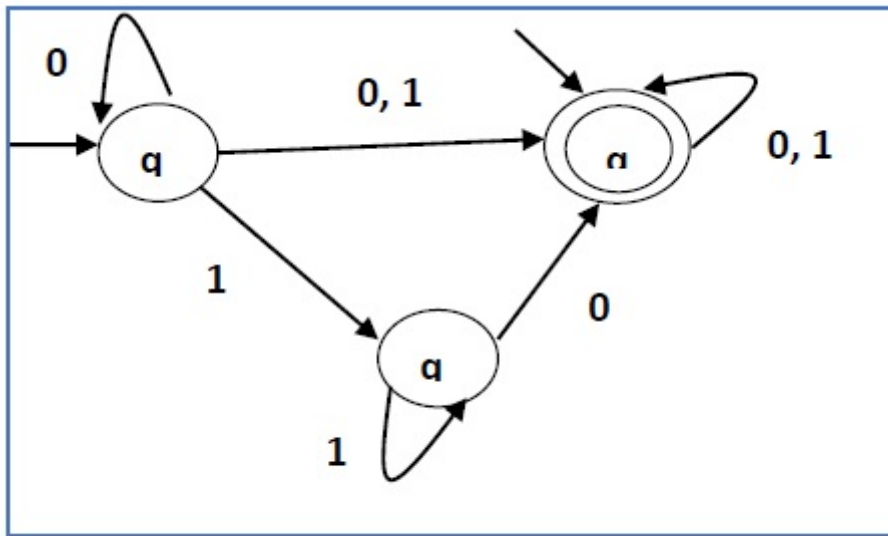


**NFA after step 2**

#### **Step 3 –**

Here  $q_1$  is an initial state, so we make  $q_f$  also an initial state.

So the FA becomes –

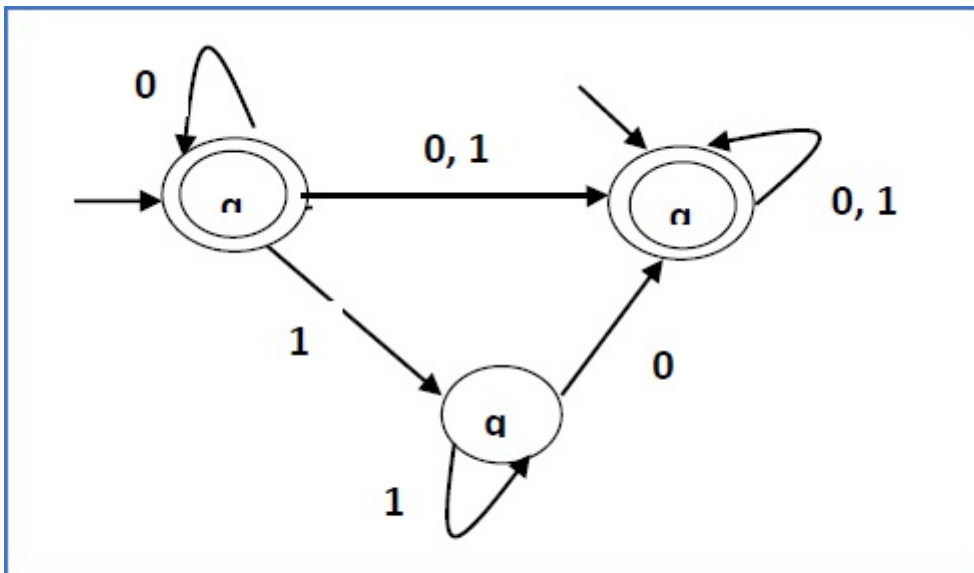


**NFA after Step 3**

Step 4 –

Here  $q_f$  is a final state, so we make  $q_1$  also a final state.

So the FA becomes –



**Final NFA without NULL moves**